

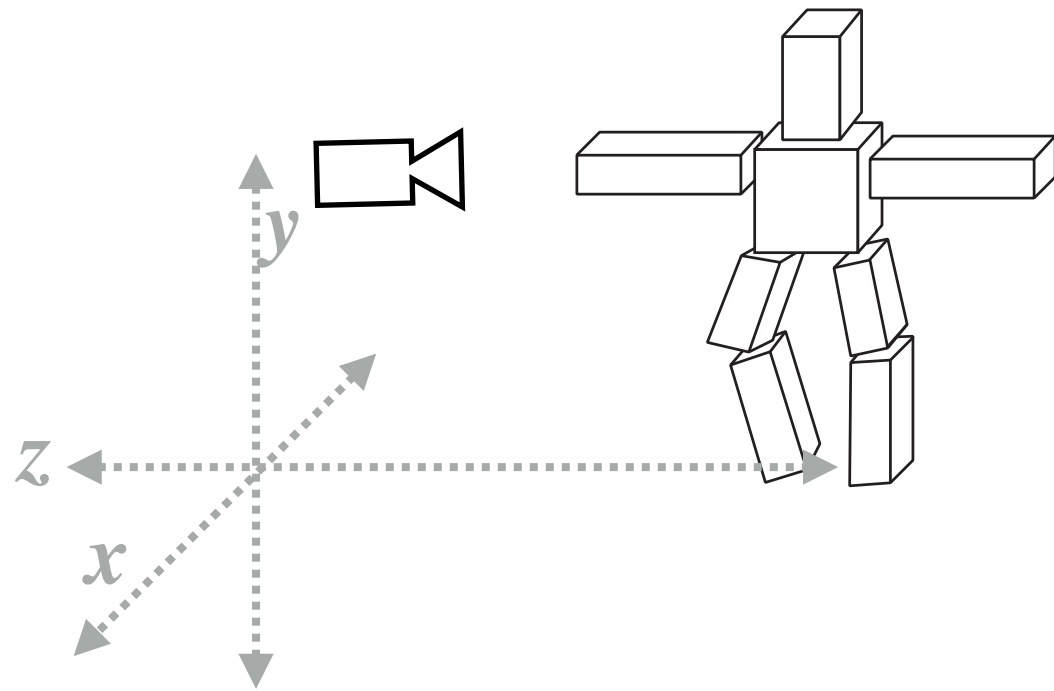
**Lecture 6:**

# **The Rasterization Pipeline**

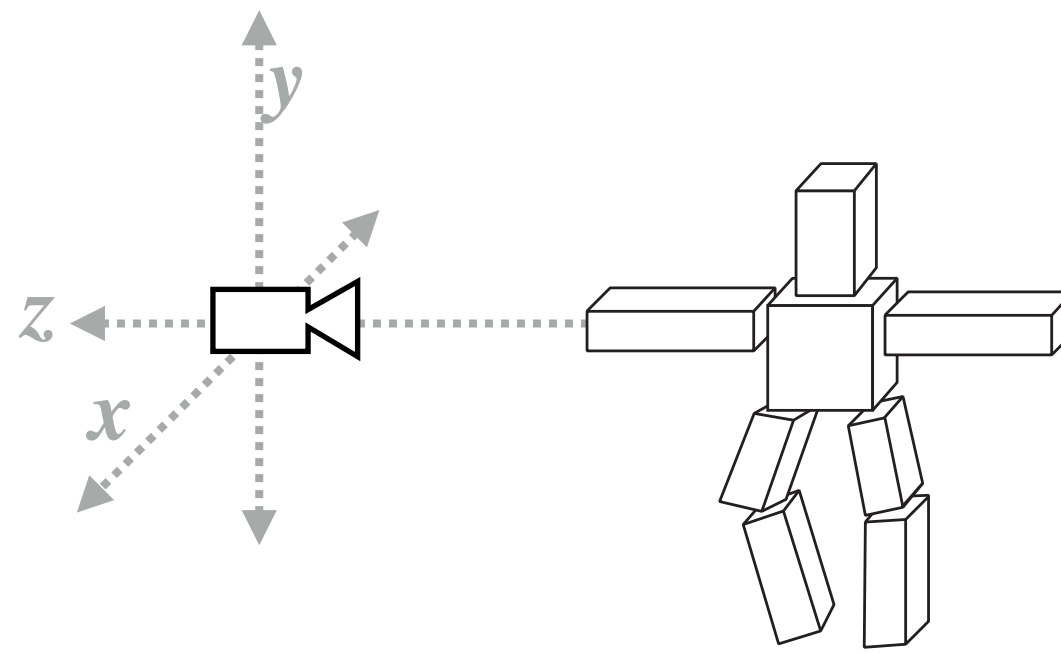
---

**Computer Graphics and Imaging**  
**UC Berkeley CS184/284A**

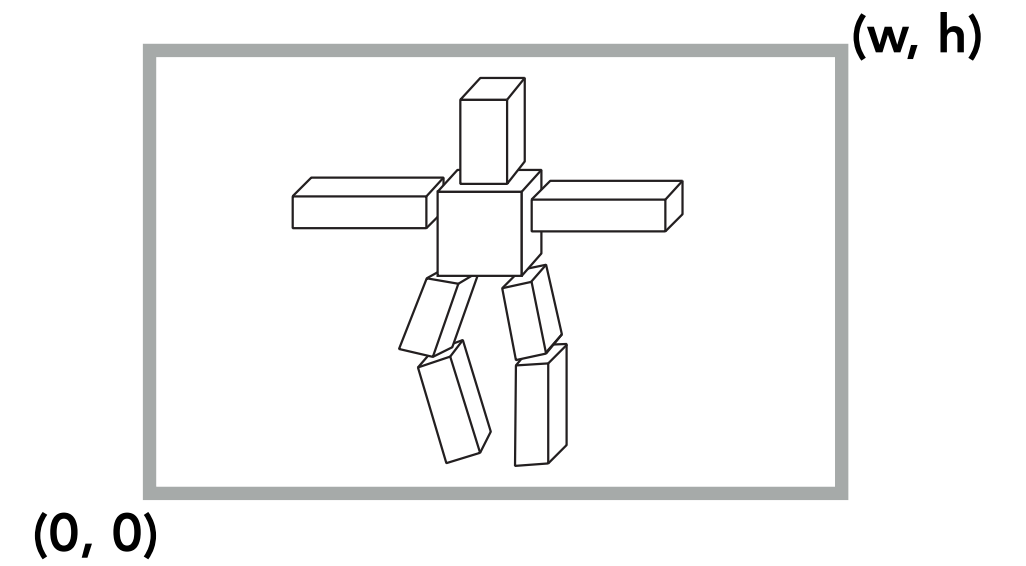
# What We've Covered So Far



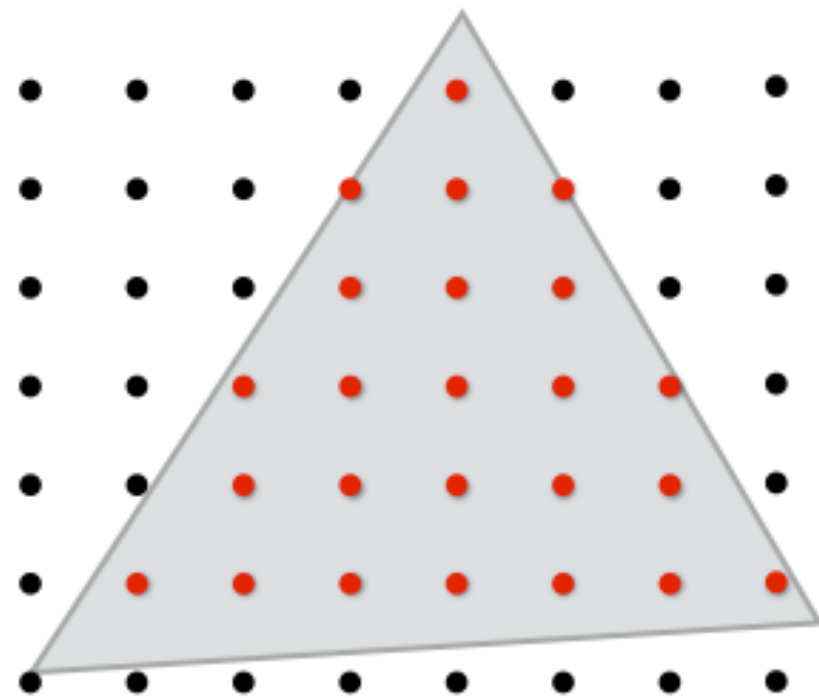
Position objects and the camera in the world



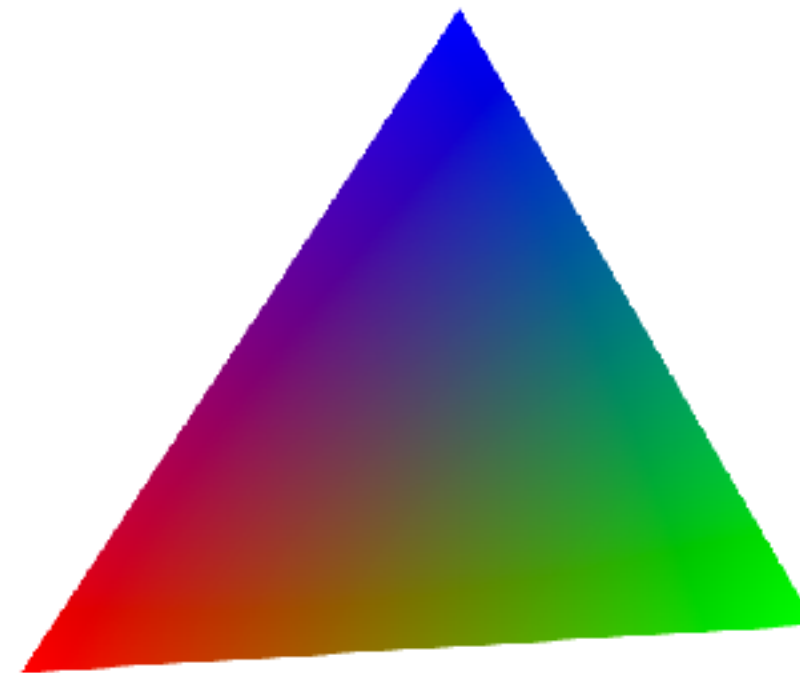
Compute position of objects relative to the camera



Project objects onto the screen



Sample triangle coverage

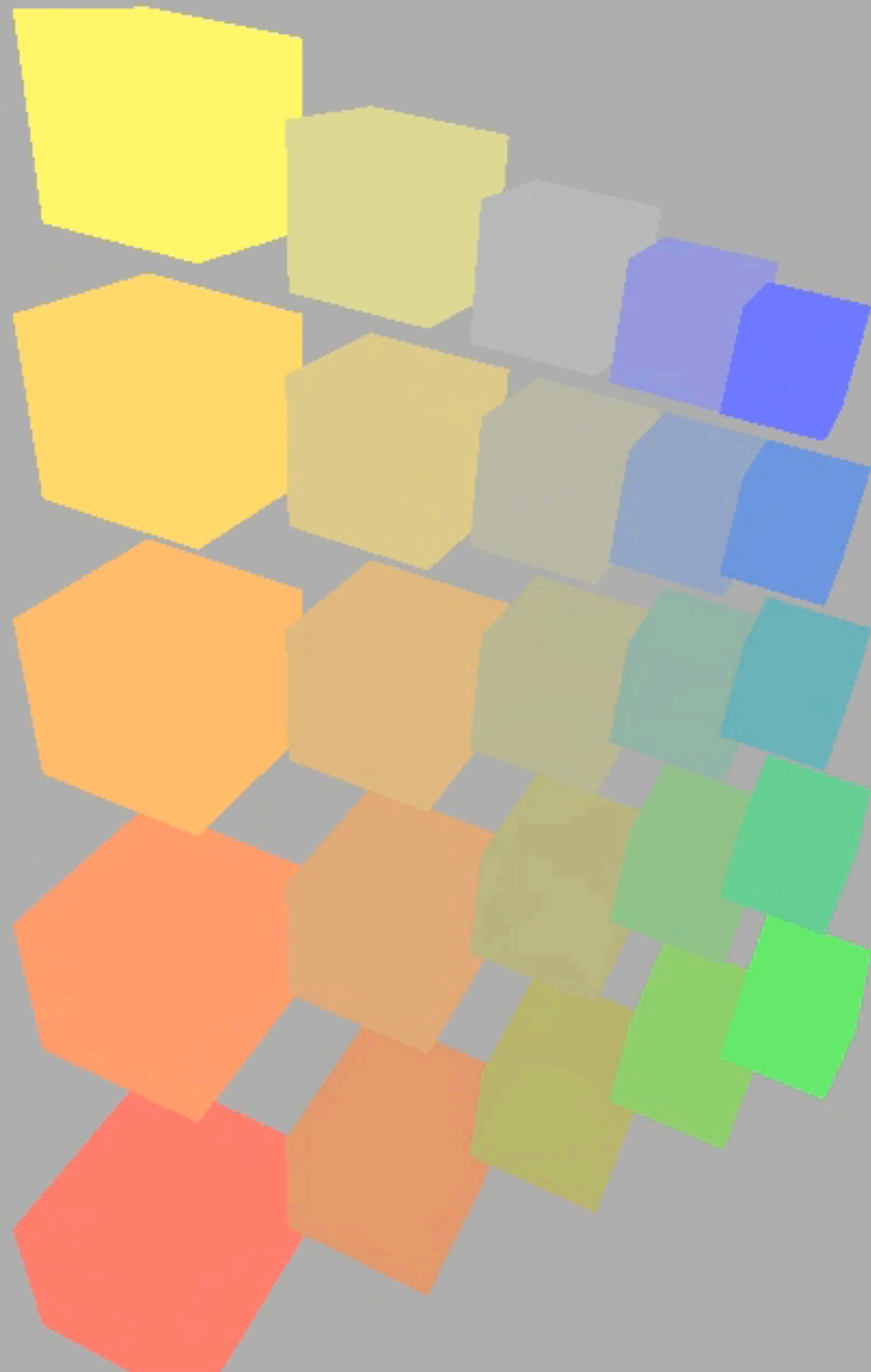


Interpolate triangle attributes

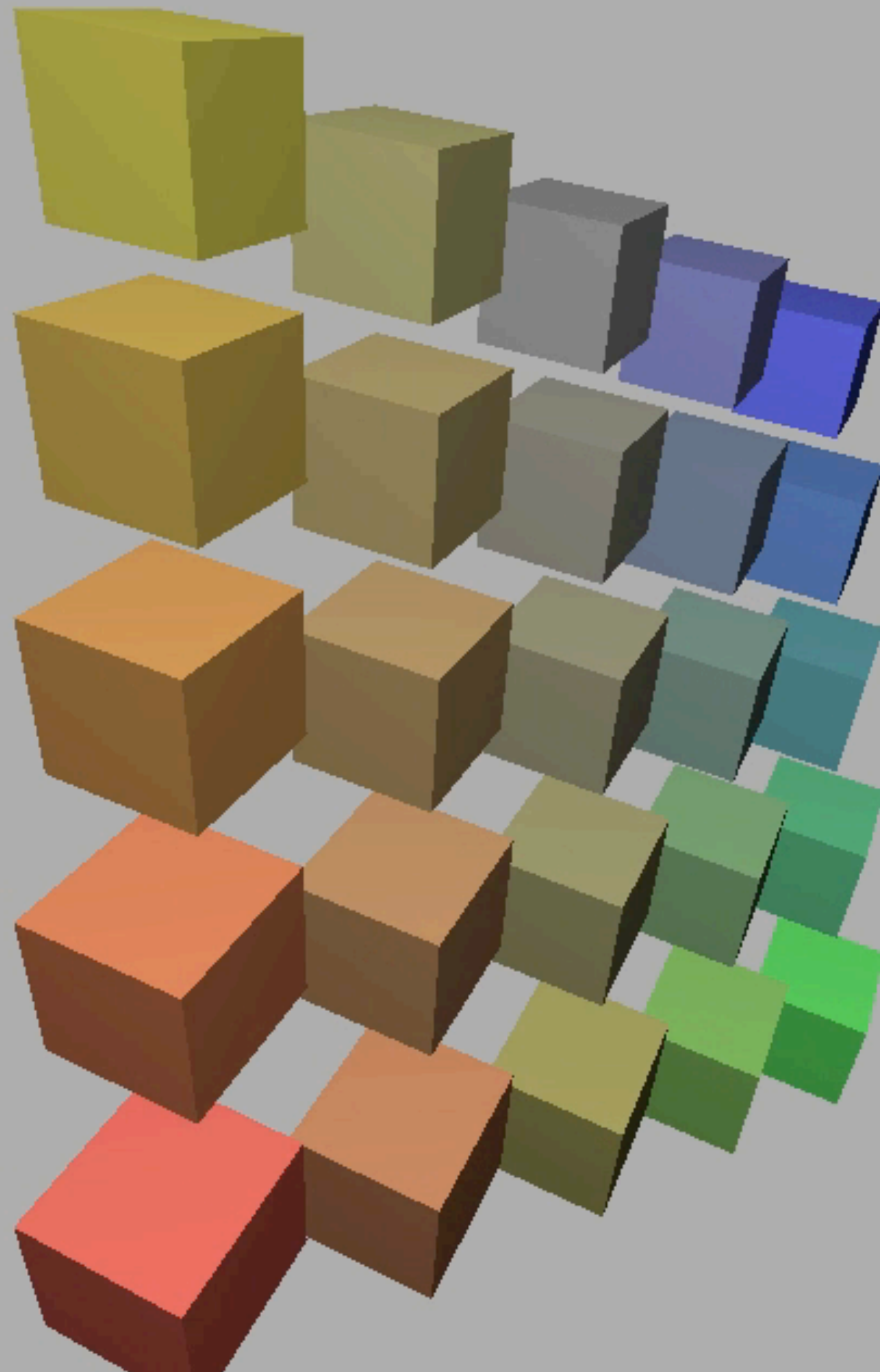


Sample texture maps

# Rotating Cubes in Perspective



# Rotating Cubes in Perspective





# What Else Are We Missing?



**Credit: Bertrand Benoit. "Sweet Feast," 2009. [Blender /VRay]**



# What Else Are We Missing?



**Credit: Giuseppe Albergo. "Colibri" [Blender]**



# What Else Are We Missing?

## Surface representations

- Objects in the real world exhibit highly complex geometric details



## Lighting and materials

- Appearance is a result of how light sources reflect off complex materials



## Camera models

- Real lenses create images with focusing and other optical effects



# Course Roadmap

## Rasterization Pipeline

### Core Concepts

- Sampling
- Antialiasing
- Transforms

Intro

Rasterization

Transforms & Projection

Texture Mapping

Today: Visibility, Shading, Overall Pipeline

## Geometric Modeling



## Lighting & Materials



## Cameras & Imaging



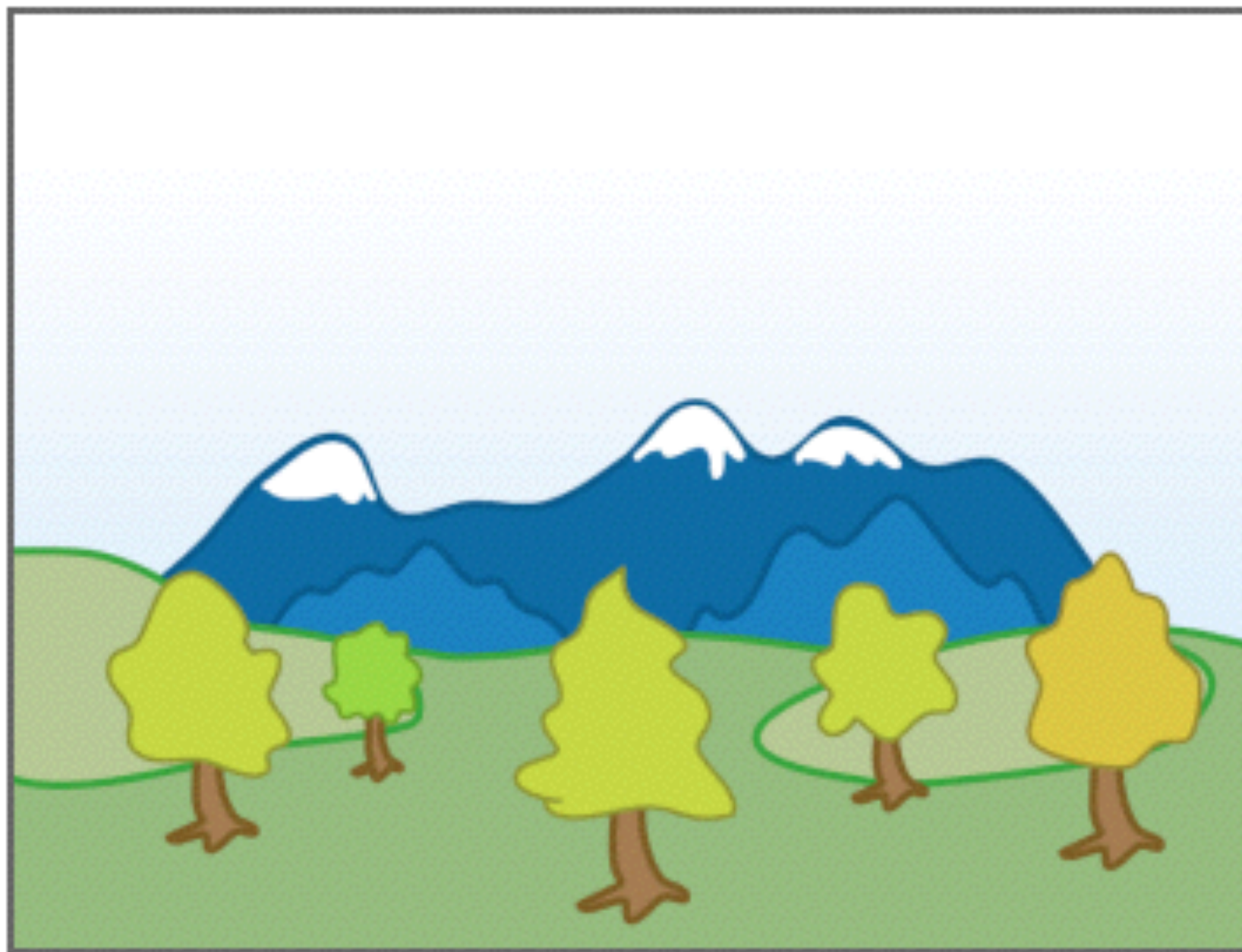


**Visibility**

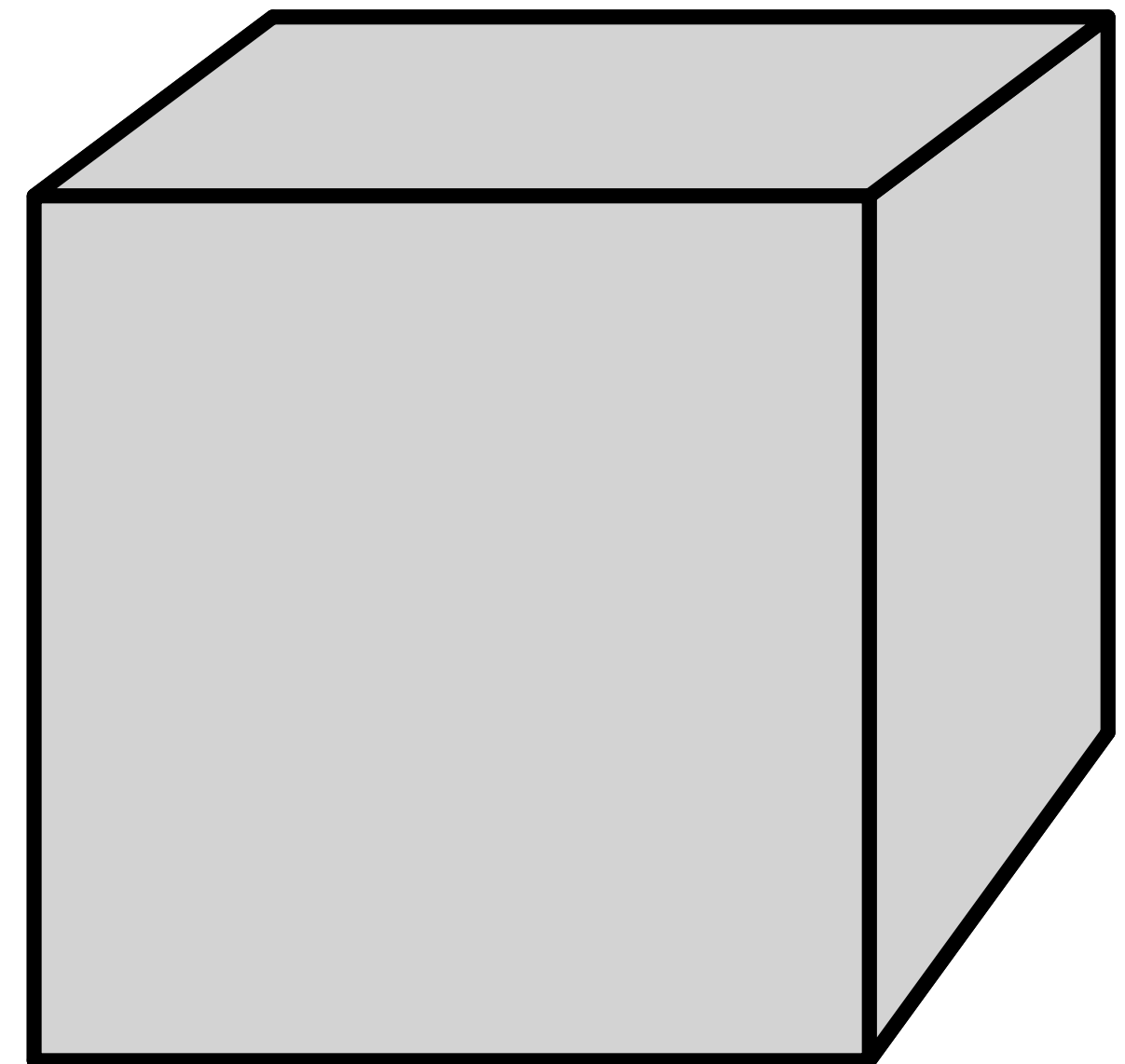
# Painter's Algorithm

Inspired by how painters paint

Paint from back to front, overwrite in the framebuffer



[Wikipedia]

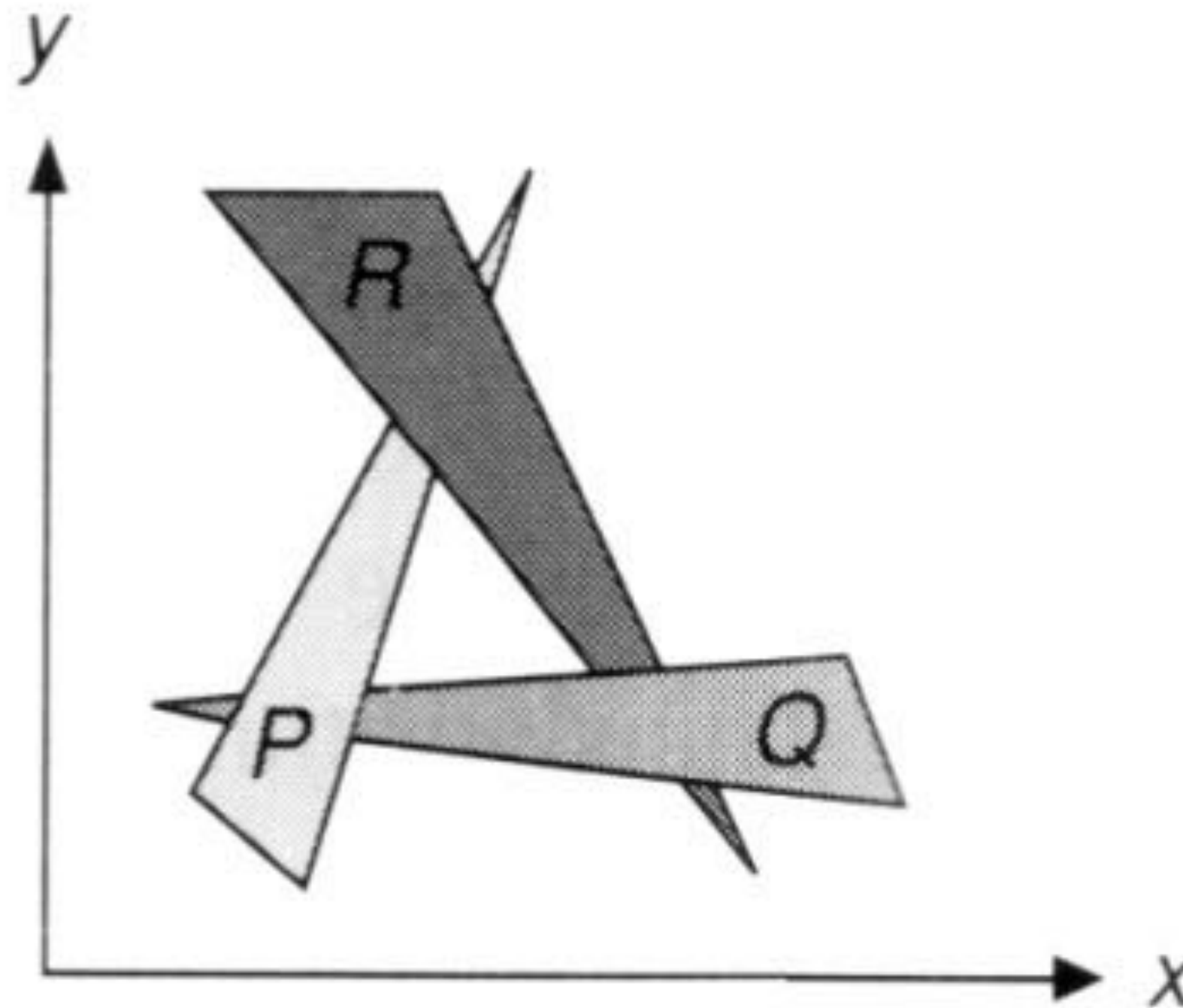




# Painter's Algorithm

Requires sorting in depth ( $O(n \log n)$  for  $n$  triangles)

Can have unresolvable depth order



[Foley et al.]

# Z-Buffer

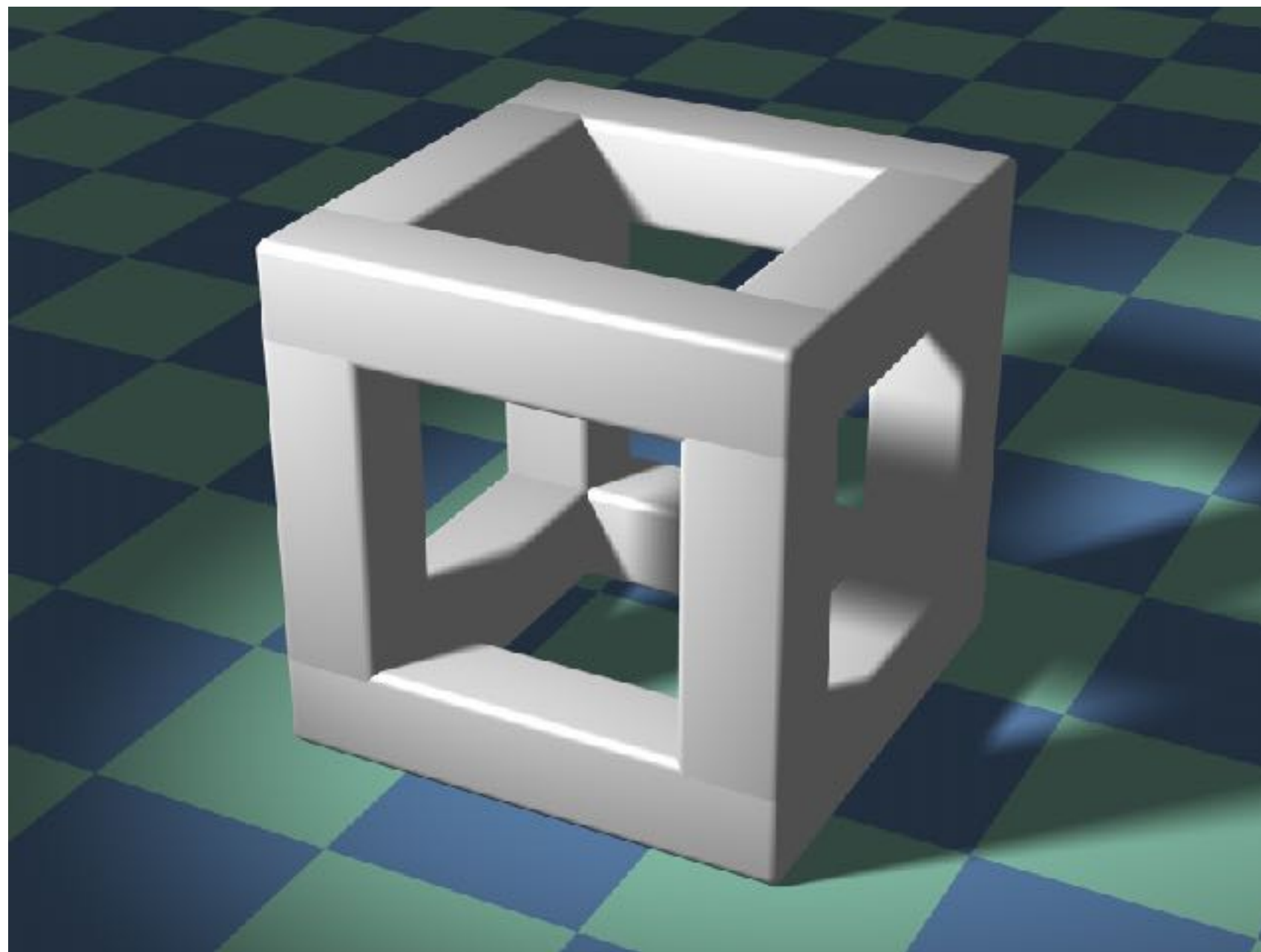
This is the hidden-surface-removal algorithm that eventually won.

Idea:

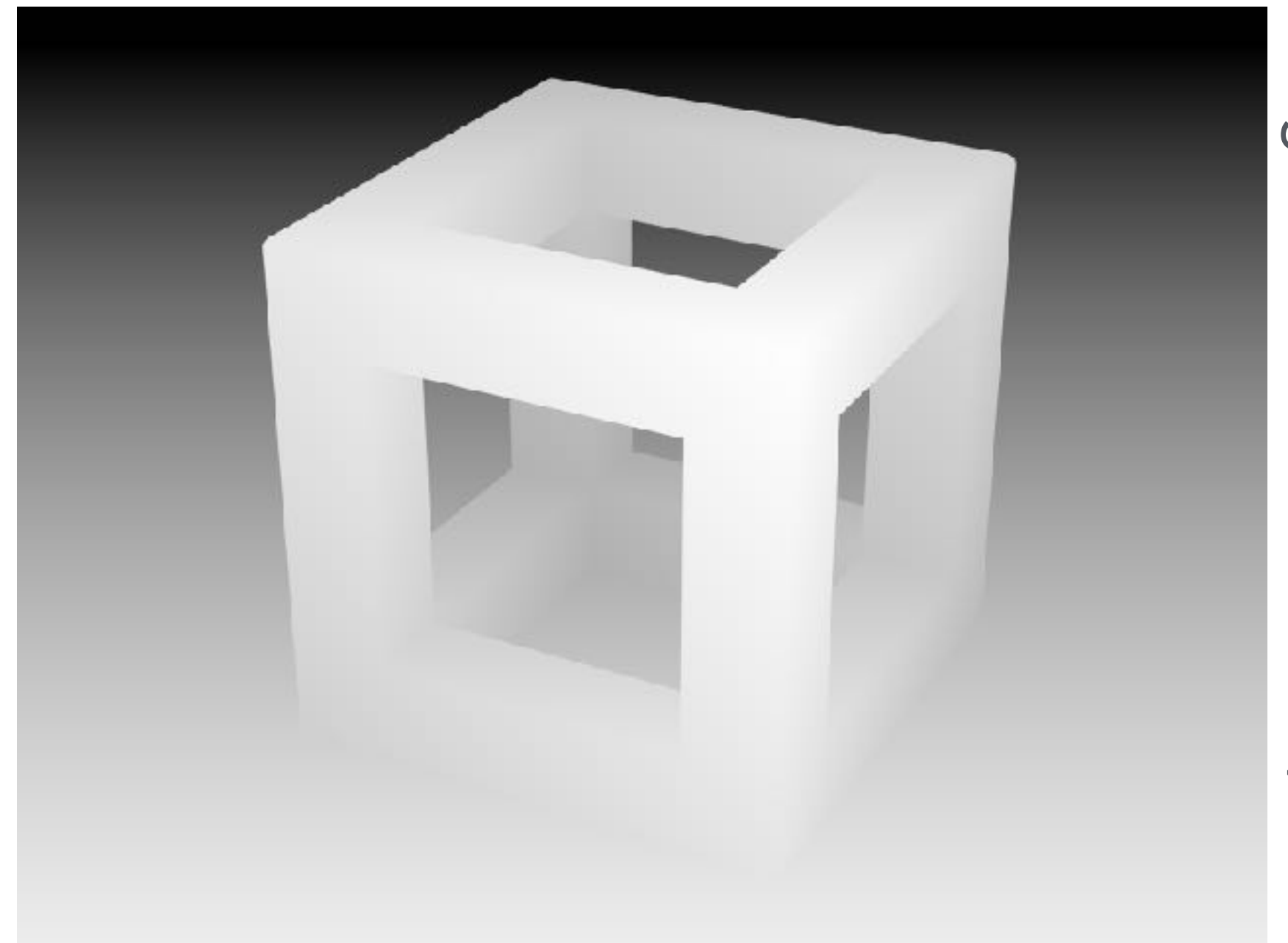
- Store current min. z-value for each sample position
- Needs an additional buffer for depth values
  - framebuffer stores RGB color values
  - depth buffer (z-buffer) stores depth (16 to 32 bits)



# Z-Buffer Example



**Rendering**



**Depth buffer**

Image credit: Dominic Alves, flickr.

# Z-Buffer Algorithm

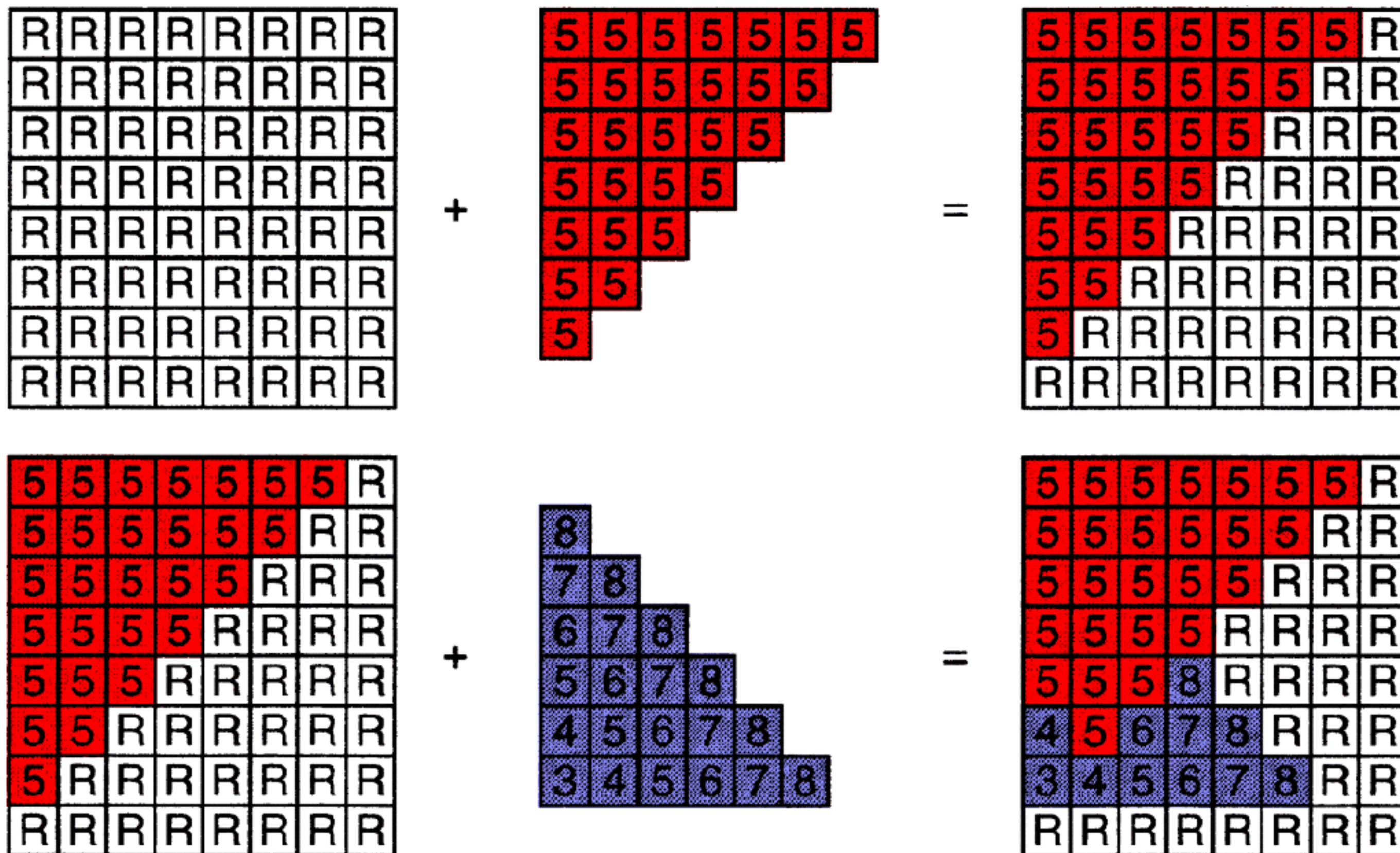
Initialize depth buffer to  $\infty$

During rasterization:

```
for (each triangle T)
  for (each sample (x,y,z) in T)
    if (z < zbuffer[x,y])           // closest sample so far
      framebuffer[x,y] = rgb;       // update color
      zbuffer[x,y] = z;             // update z
    else
      ; // do nothing, this sample is not closest
```



# Z-Buffer Algorithm



# Z-Buffer Complexity

## Complexity

- $O(n)$  for  $n$  triangles
- How can we sort  $n$  triangles in linear time?

## Most important visibility algorithm

- Implemented in hardware for all GPUs
- Used by OpenGL



# **Simple Shading**

## **(Blinn-Phong Reflection Model)**

# **Simple Shading vs Realistic Lighting & Materials**

## **What we will cover today**

- **A local shading model: simple, per-pixel, fast**
- **Based on perceptual observations, not physics**

## **What we will cover later in the course**

- **Physics-based lighting and material representations**
- **Global light transport simulation**



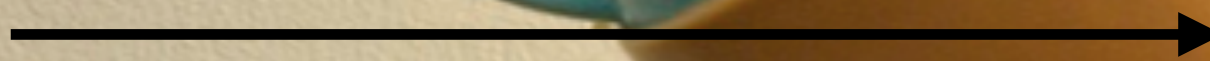
# Perceptual Observations



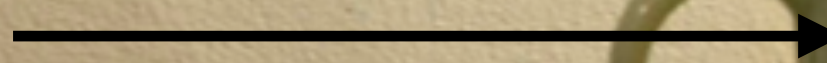
Specular highlights



Diffuse reflection



Ambient lighting



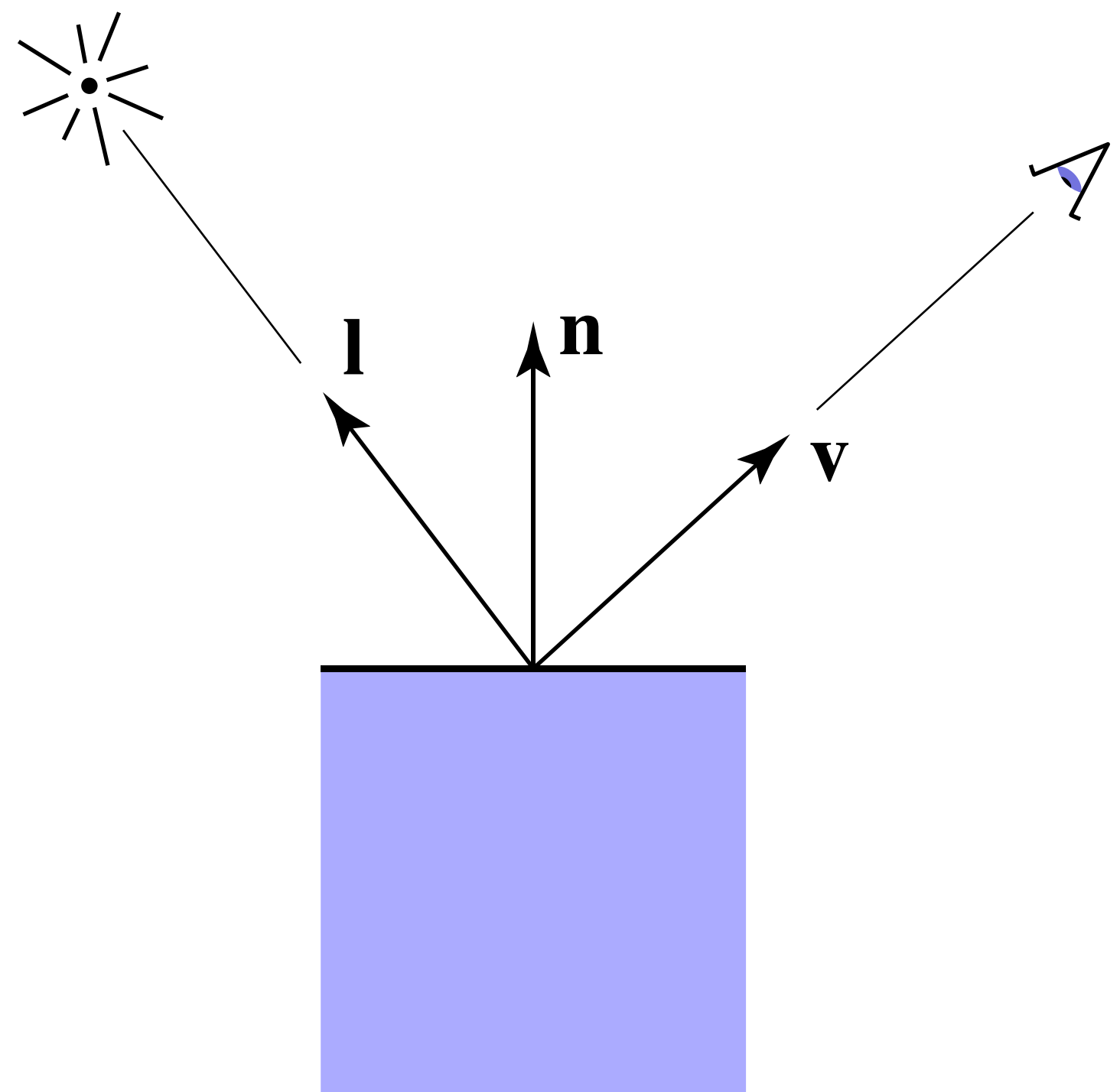


# Local Shading

Compute light reflected toward camera

Inputs:

- Viewer direction,  $v$
- Surface normal,  $n$
- Light direction,  $l$   
(for each of many lights)
- Surface parameters  
(color, shininess, ...)

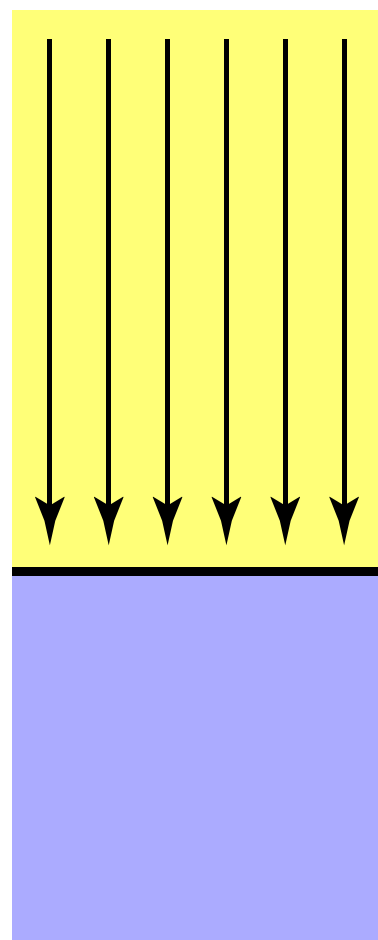


# Diffuse Reflection

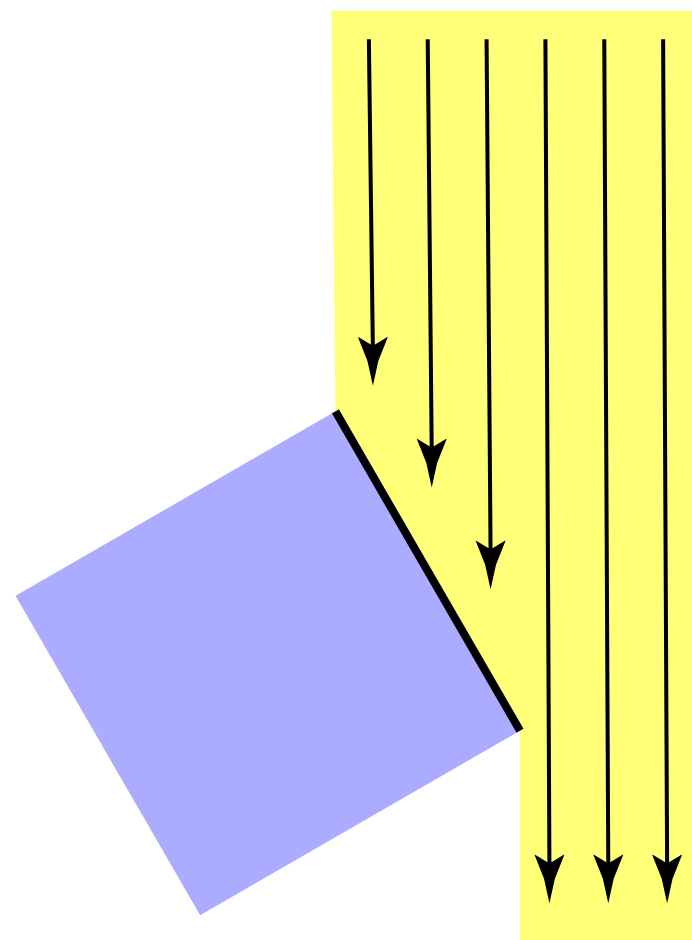
Light is scattered uniformly in all directions

- Surface color is the same for all viewing directions

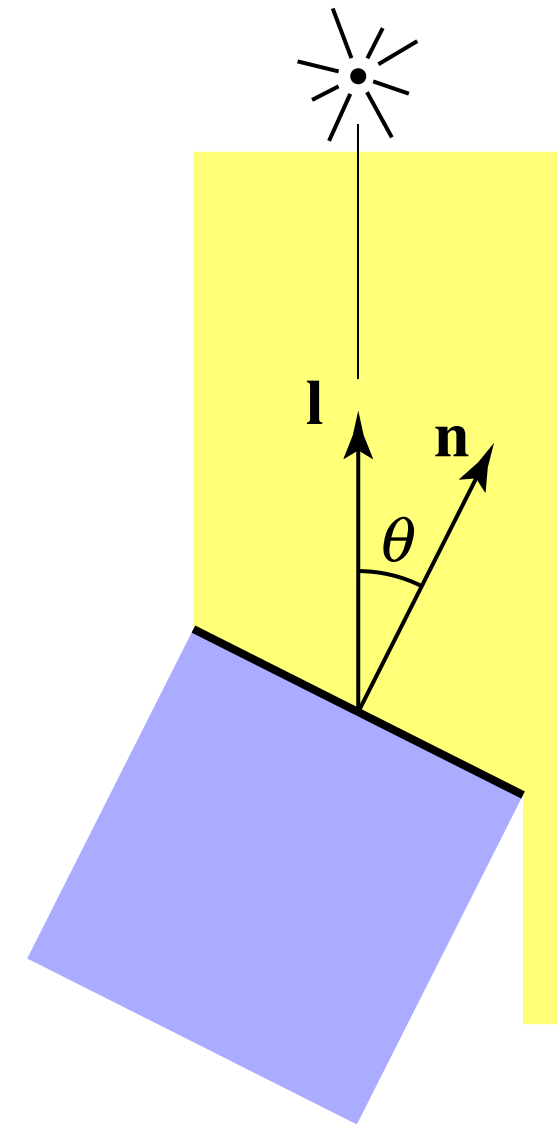
Lambert's cosine law



Top face of cube  
receives a certain  
amount of light

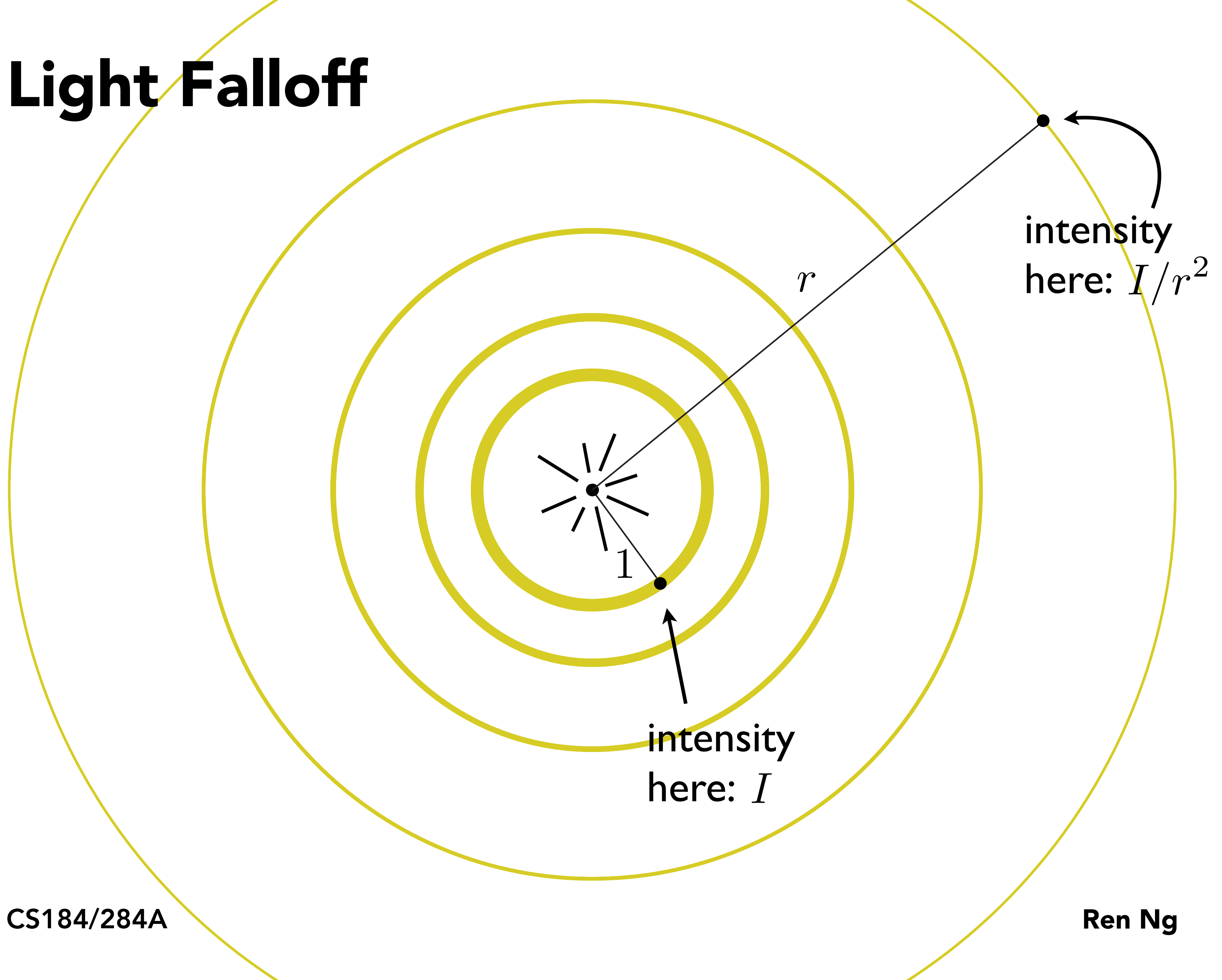


Top face of  
60° rotated cube  
intercepts half the light



In general, light per unit  
area is proportional to  
 $\cos \theta = \mathbf{l} \cdot \mathbf{n}$

# Light Falloff





# Perceptual Observations

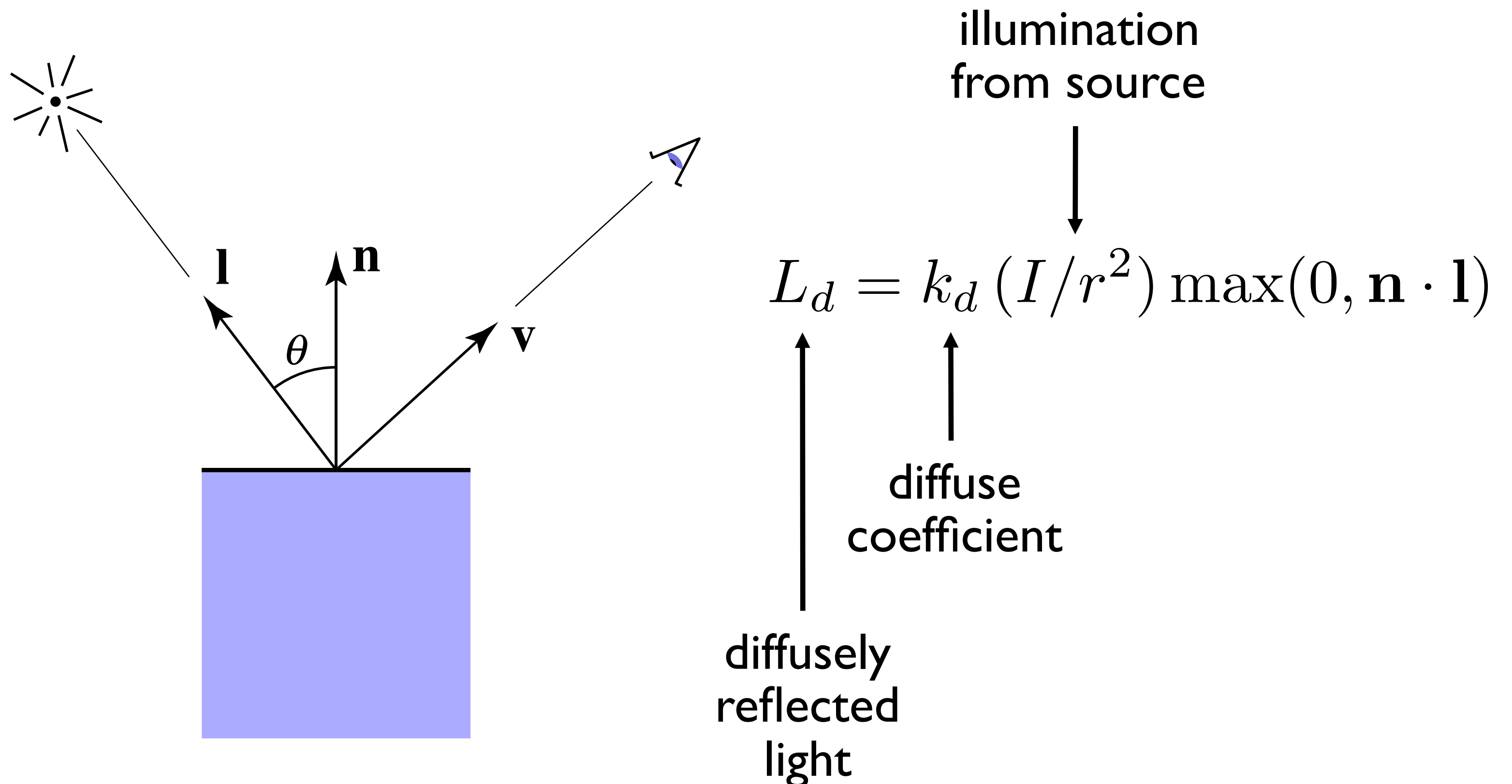


Photo credit: Jessica Andrews, flickr



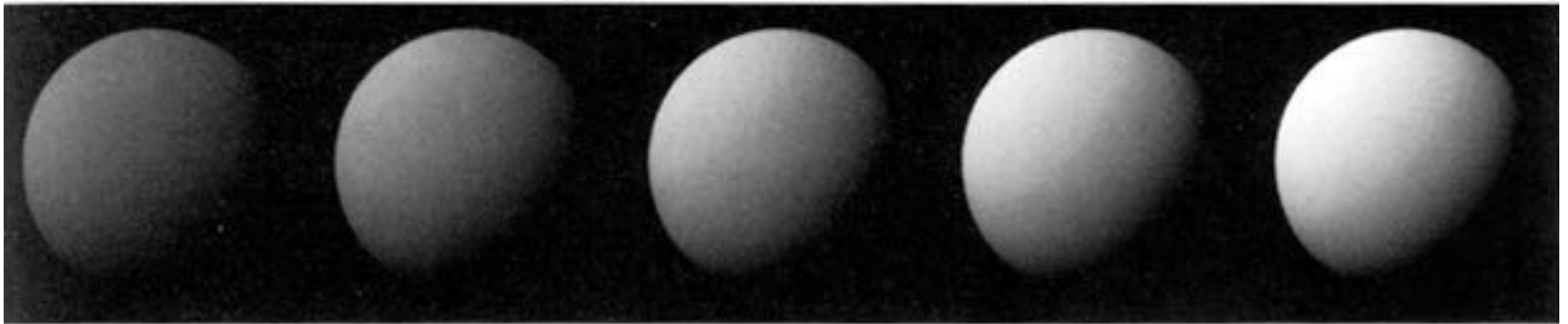
# Lambertian (Diffuse) Shading

Shading independent of view direction



# Lambertian (Diffuse) Shading

Produces matte appearance



$k_d \longrightarrow$

[Foley et al.]



# Perceptual Observations



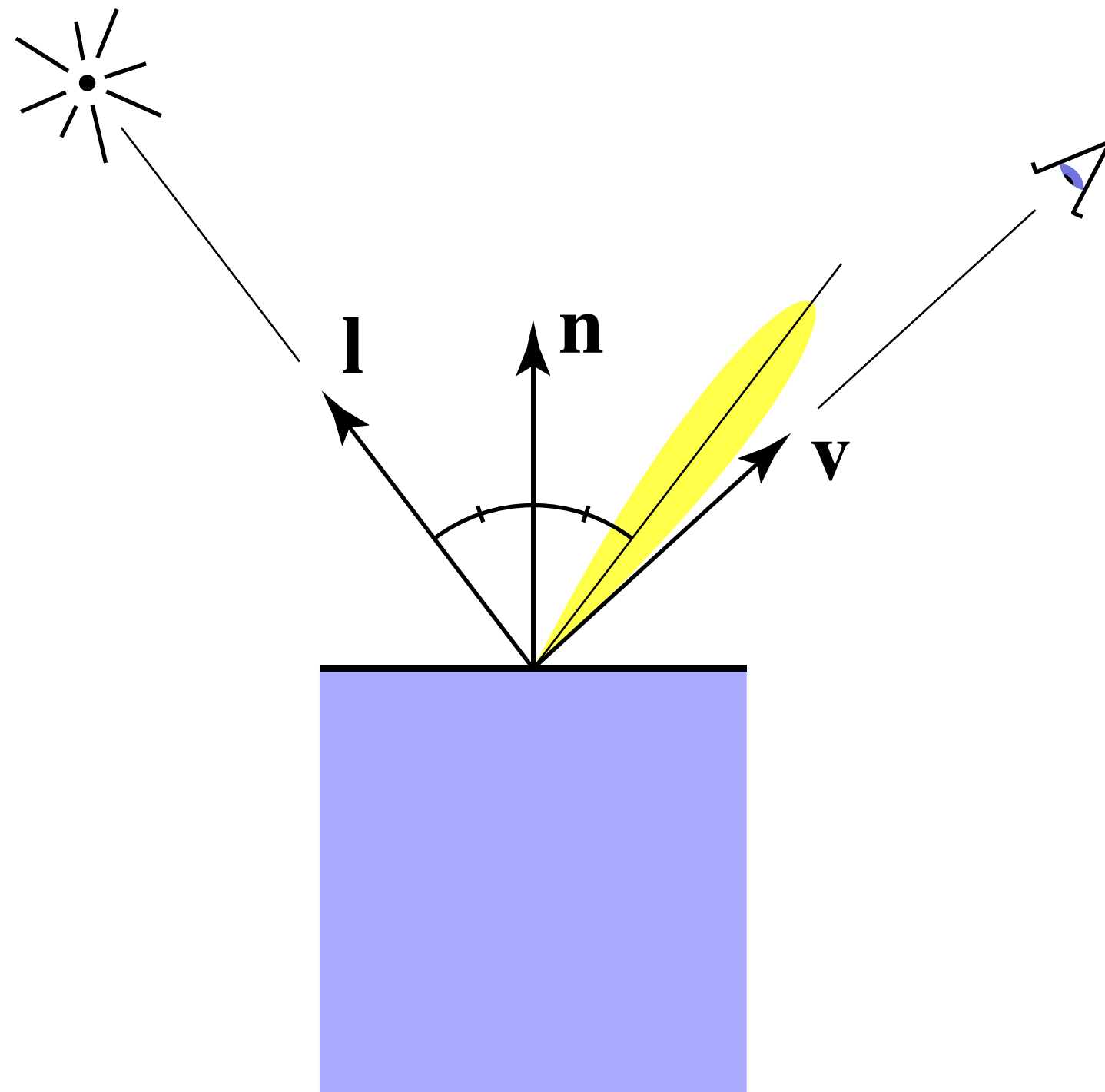
Photo credit: Jessica Andrews, flickr



# Specular Shading (Blinn-Phong)

Intensity depends on view direction

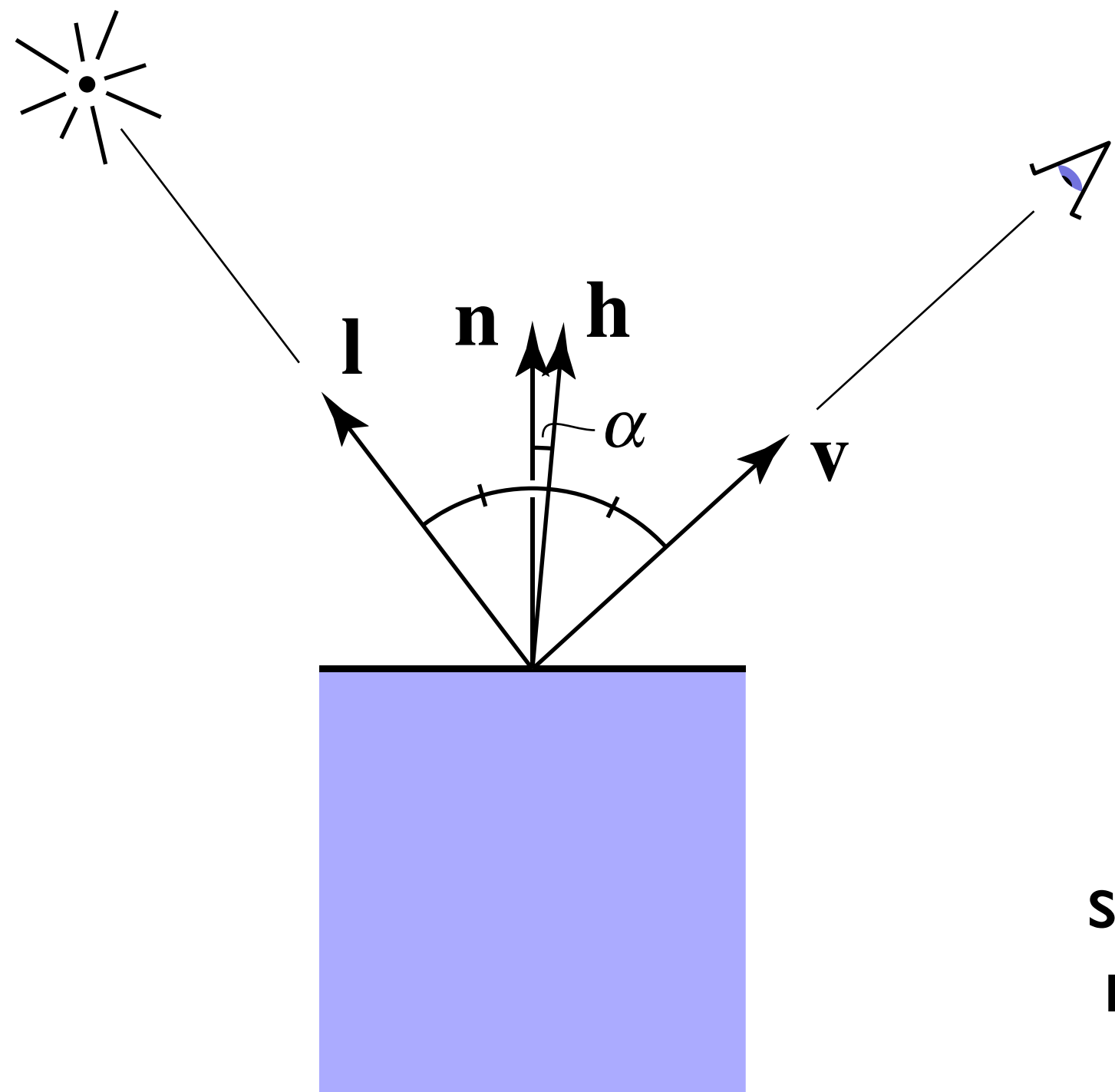
- Bright near mirror reflection direction



# Specular Shading (Blinn-Phong)

Close to mirror direction  $\Leftrightarrow$  half vector near normal

- Measure “near” by dot product of unit vectors



$$\mathbf{h} = \text{bisector}(\mathbf{v}, \mathbf{l})$$

$$= \frac{\mathbf{v} + \mathbf{l}}{\|\mathbf{v} + \mathbf{l}\|}$$

$$L_s = k_s (I/r^2) \max(0, \cos \alpha)^p$$

$$= k_s (I/r^2) \max(0, \mathbf{n} \cdot \mathbf{h})^p$$

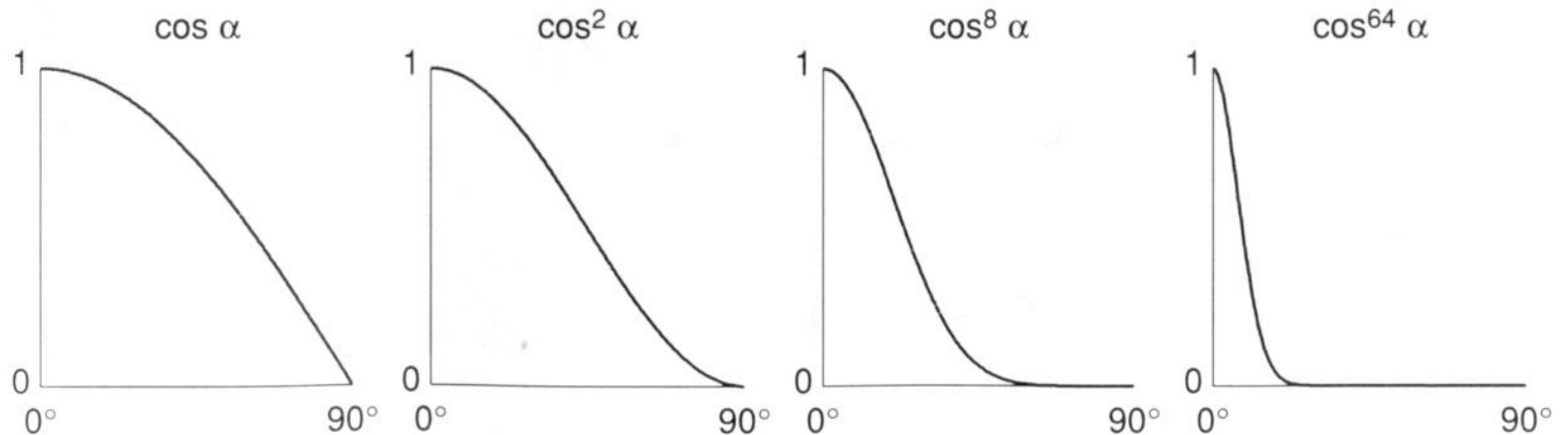
↑  
specularly  
reflected  
light

↑  
specular  
coefficient



# Cosine Power Plots

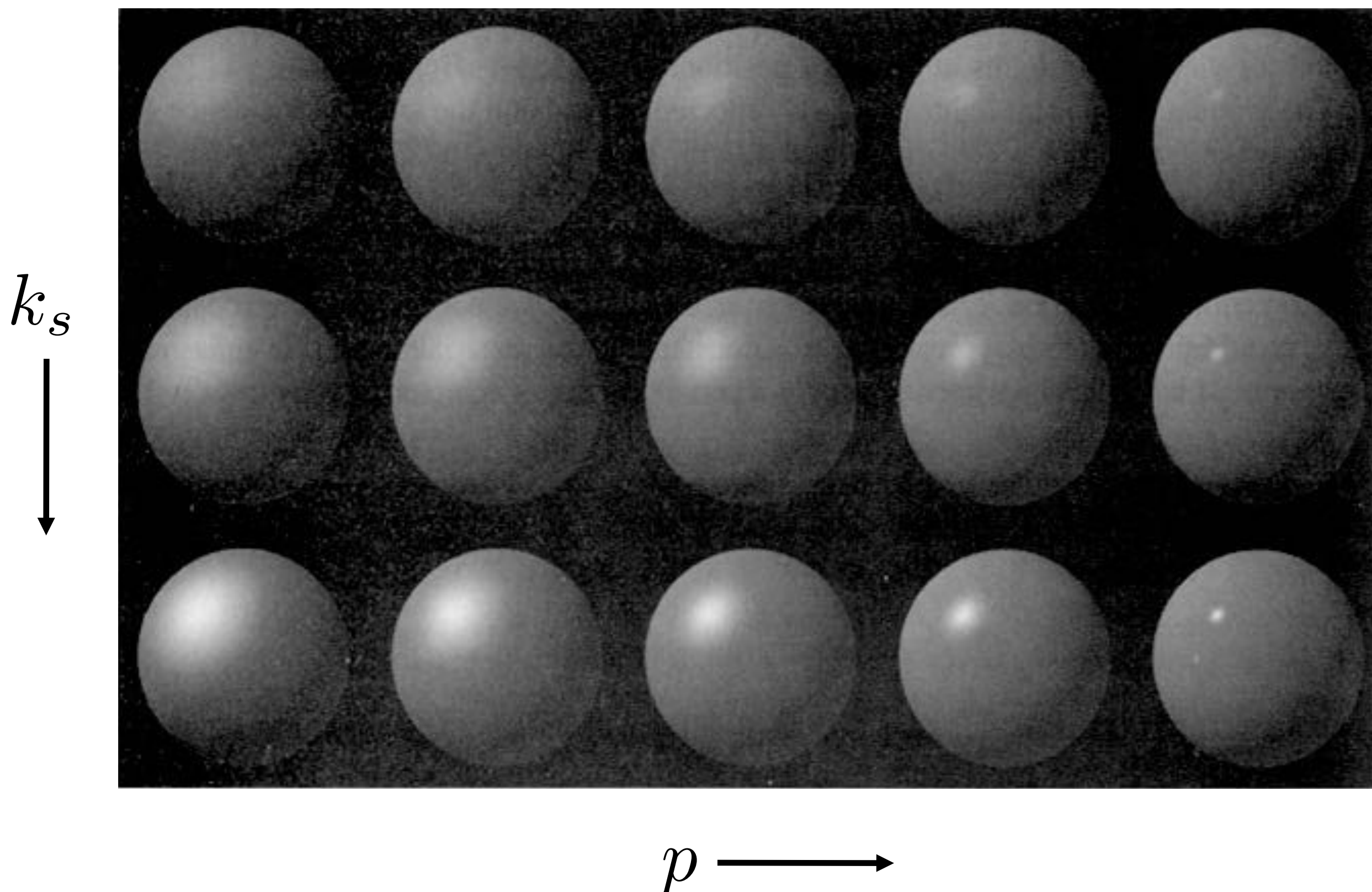
Increasing  $p$  narrows the reflection lobe



[Foley et al.]

# Specular Shading (Blinn-Phong)

$$L_s = k_s (I/r^2) \max(0, \mathbf{n} \cdot \mathbf{h})^p$$



[Foley et al.]



# Perceptual Observations



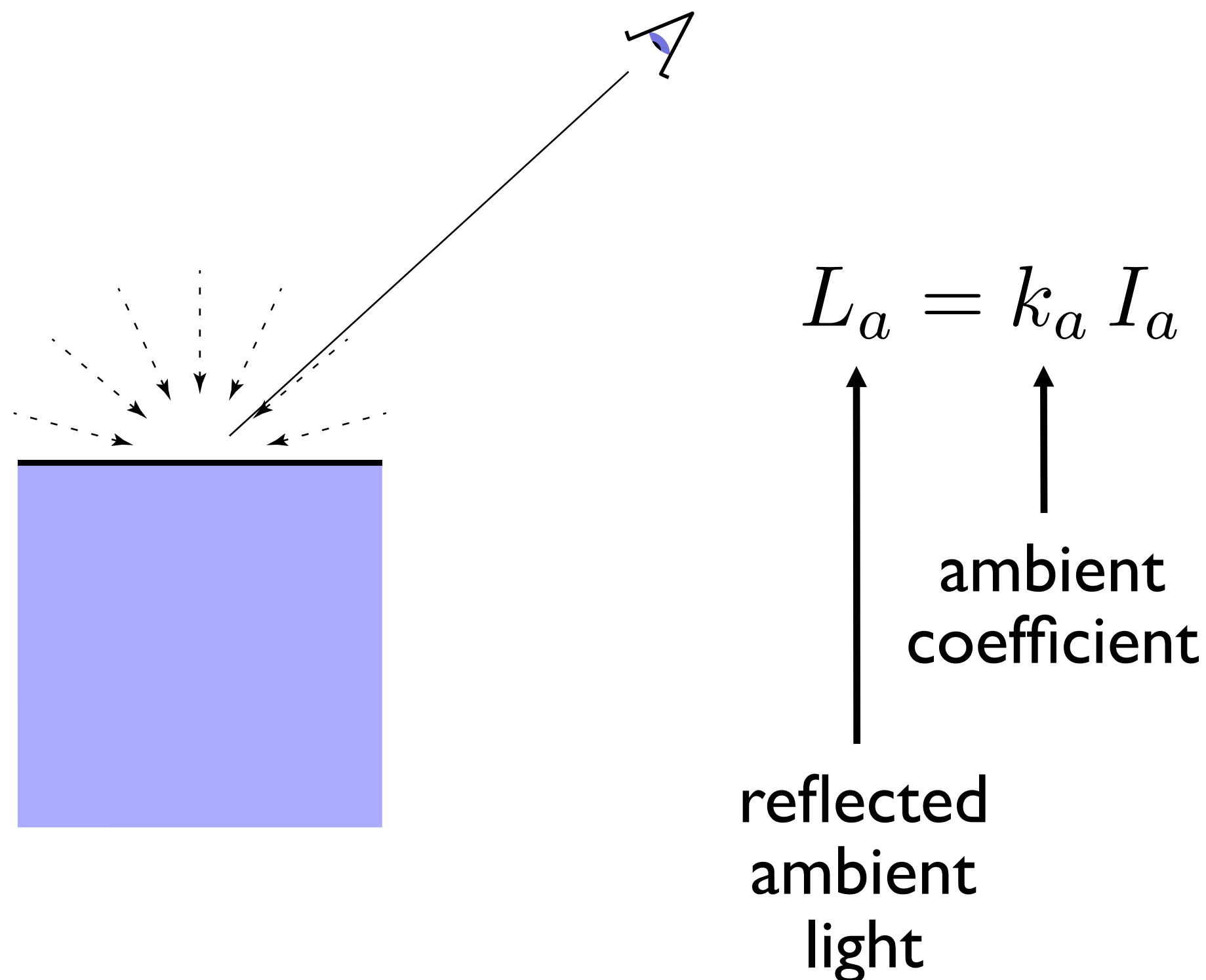
Photo credit: Jessica Andrews, flickr



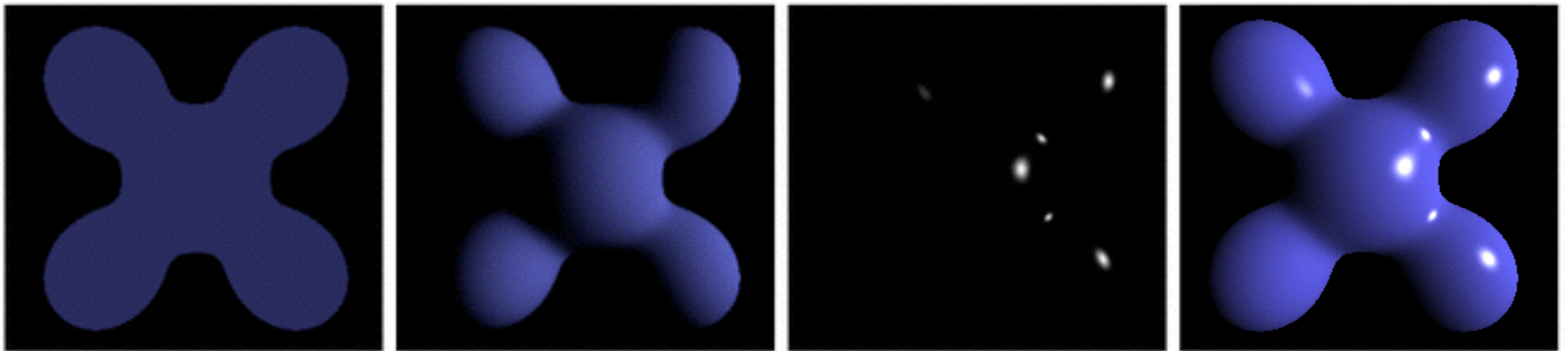
# Ambient Shading

Shading that does not depend on anything

- Add constant color to account for disregarded illumination and fill in black shadows



# Blinn-Phong Reflection Model



Ambient + Diffuse + Specular = Phong Reflection

$$\begin{aligned} L &= L_a + L_d + L_s \\ &= k_a I_a + k_d (I/r^2) \max(0, \mathbf{n} \cdot \mathbf{l}) + k_s (I/r^2) \max(0, \mathbf{n} \cdot \mathbf{h})^p \end{aligned}$$

# Blinn-Phong Reflection Model

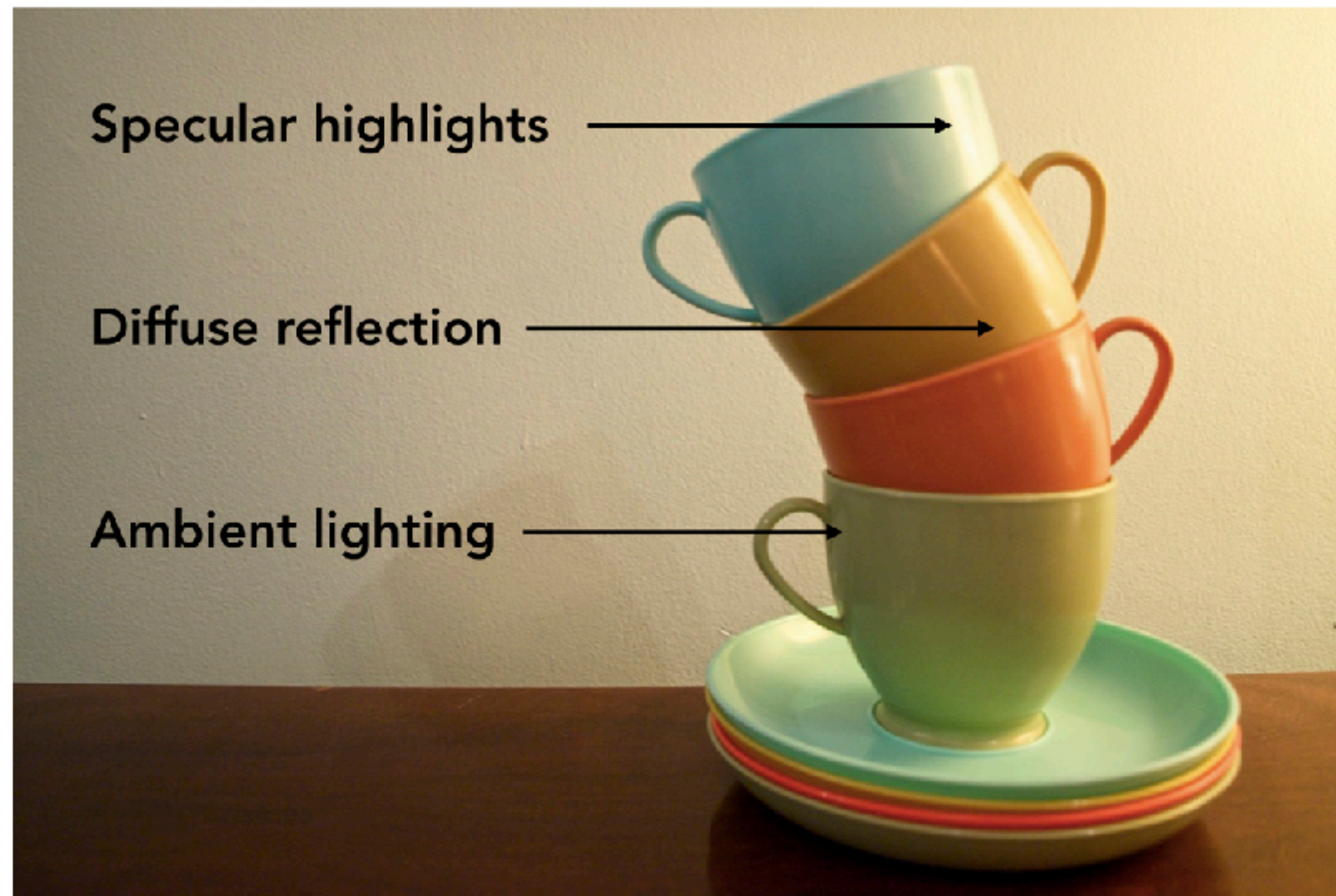


Photo credit: Jessica Andrews, flickr

$$\begin{aligned} L &= L_a + L_d + L_s \\ &= k_a I_a + k_d (I/r^2) \max(0, \mathbf{n} \cdot \mathbf{l}) + k_s (I/r^2) \max(0, \mathbf{n} \cdot \mathbf{h})^p \end{aligned}$$



# **Shading Triangle Meshes**

# Shading Frequency: Triangle, Vertex or Pixel

Shade each triangle (flat shading)

- Triangle face is flat — one normal vector
- Not good for smooth surfaces



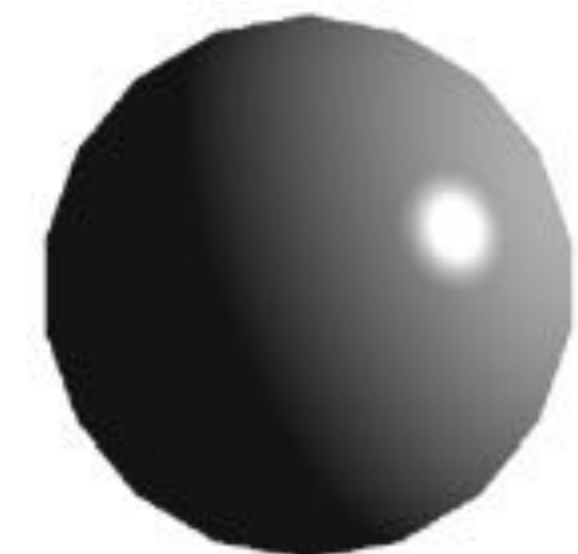
Shade each vertex ("Gouraud" shading)

- Interpolate colors from vertices across triangle
- Each vertex has a normal vector

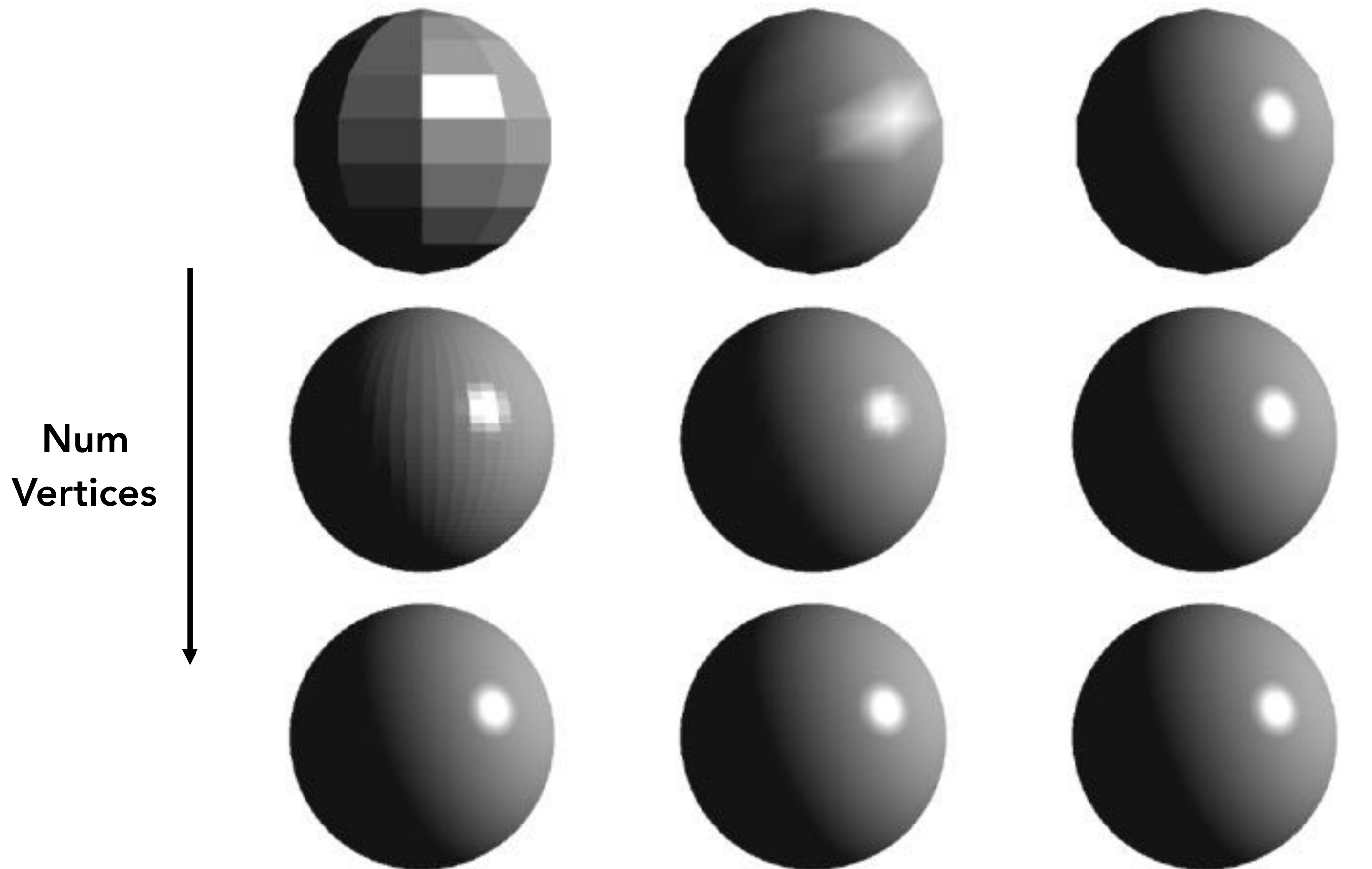


Shade each pixel ("Phong" shading)

- Interpolate normal vectors across each triangle
- Compute full shading model at each pixel



# Shading Frequency: Face, Vertex or Pixel



Shading freq. :  
Shading type :

Face  
Flat

Vertex  
Gouraud

Pixel  
Phong (\*)



# Defining Per-Vertex Normal Vectors

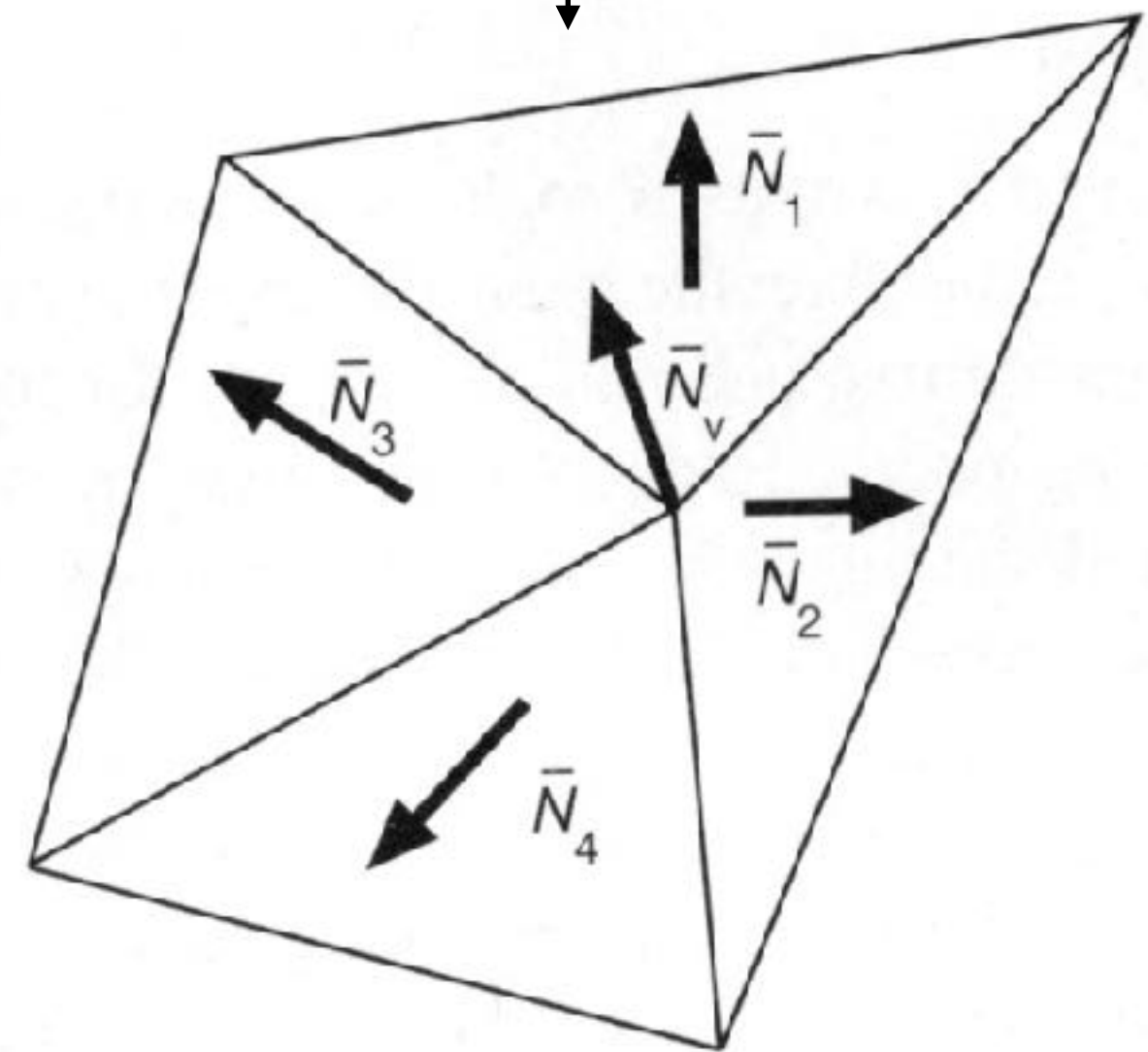
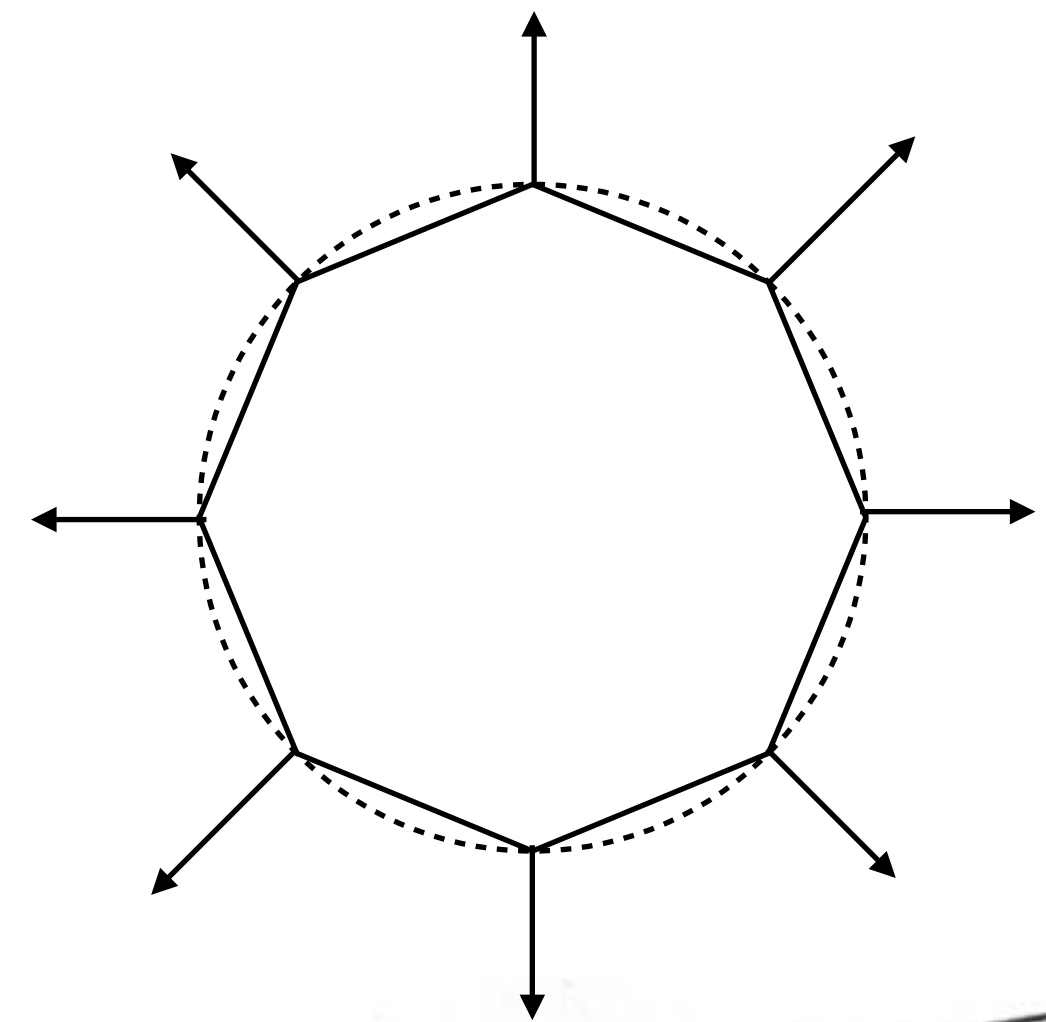
Best to get vertex normals from the underlying geometry

- e.g. consider a sphere

Otherwise have to infer vertex normals from triangle faces

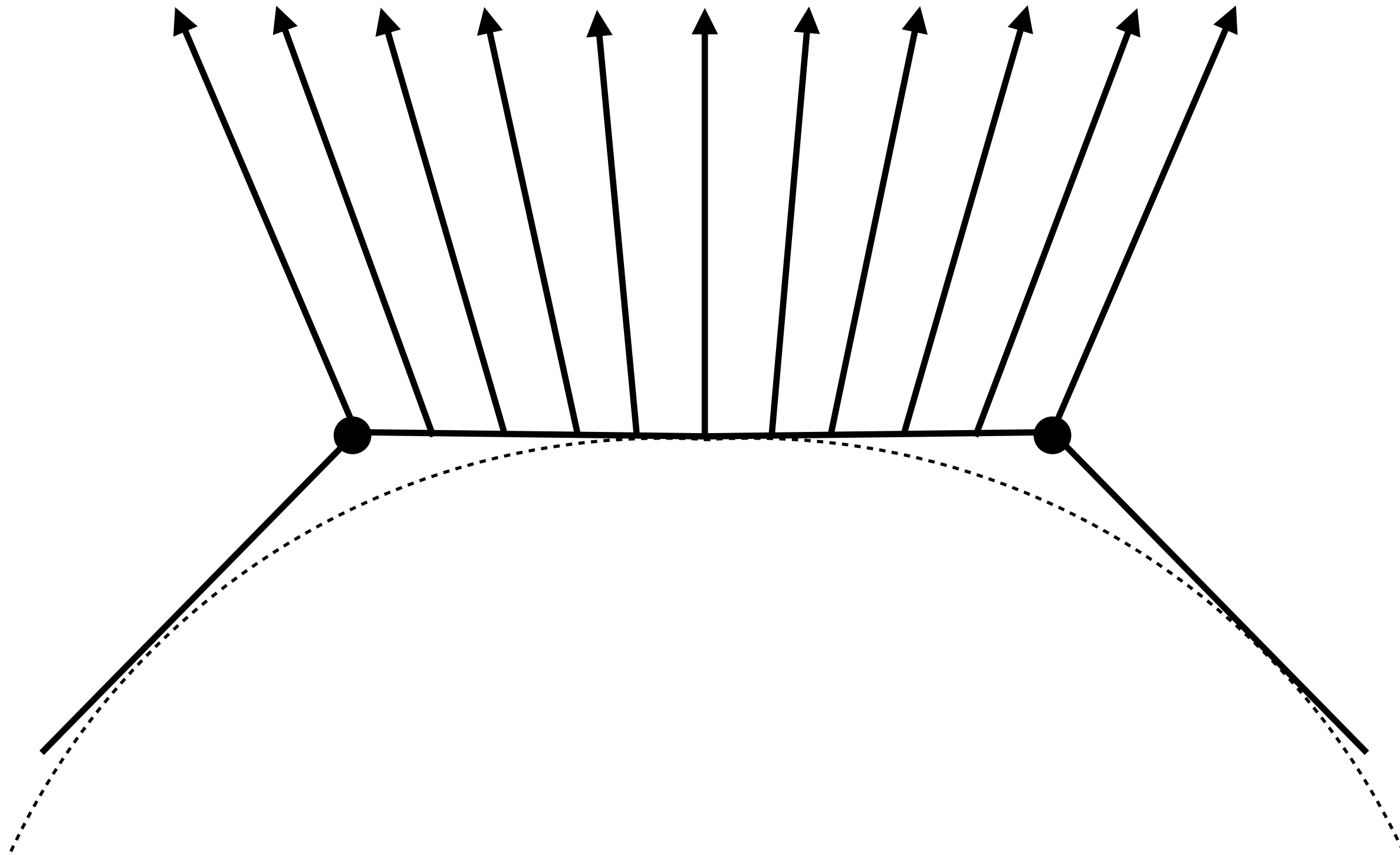
- Simple scheme: average surrounding face normals

$$N_v = \frac{\sum_i N_i}{\|\sum_i N_i\|}$$



# Defining Per-Pixel Normal Vectors

Barycentric interpolation of vertex normals

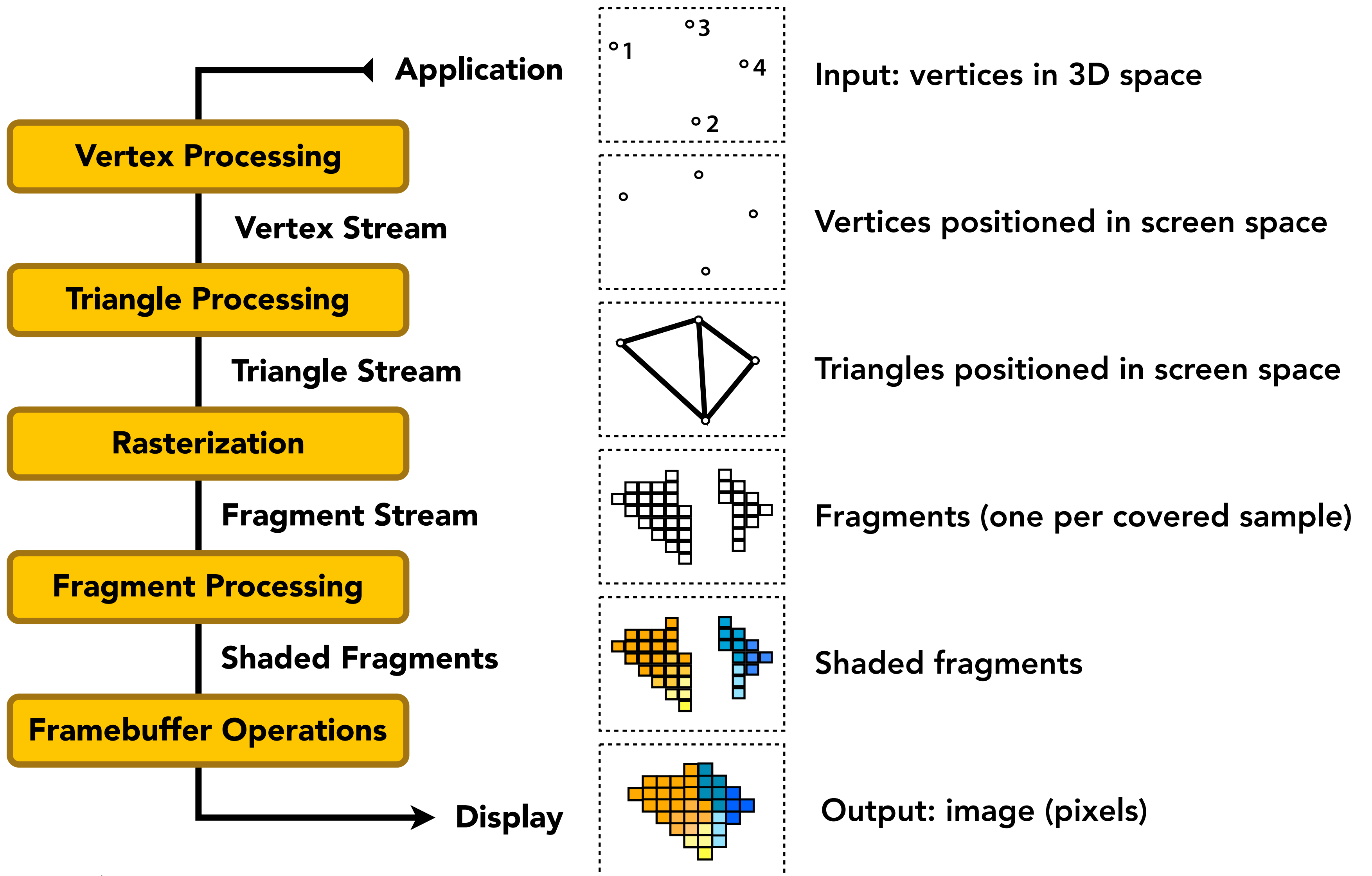


Problem: length of vectors?

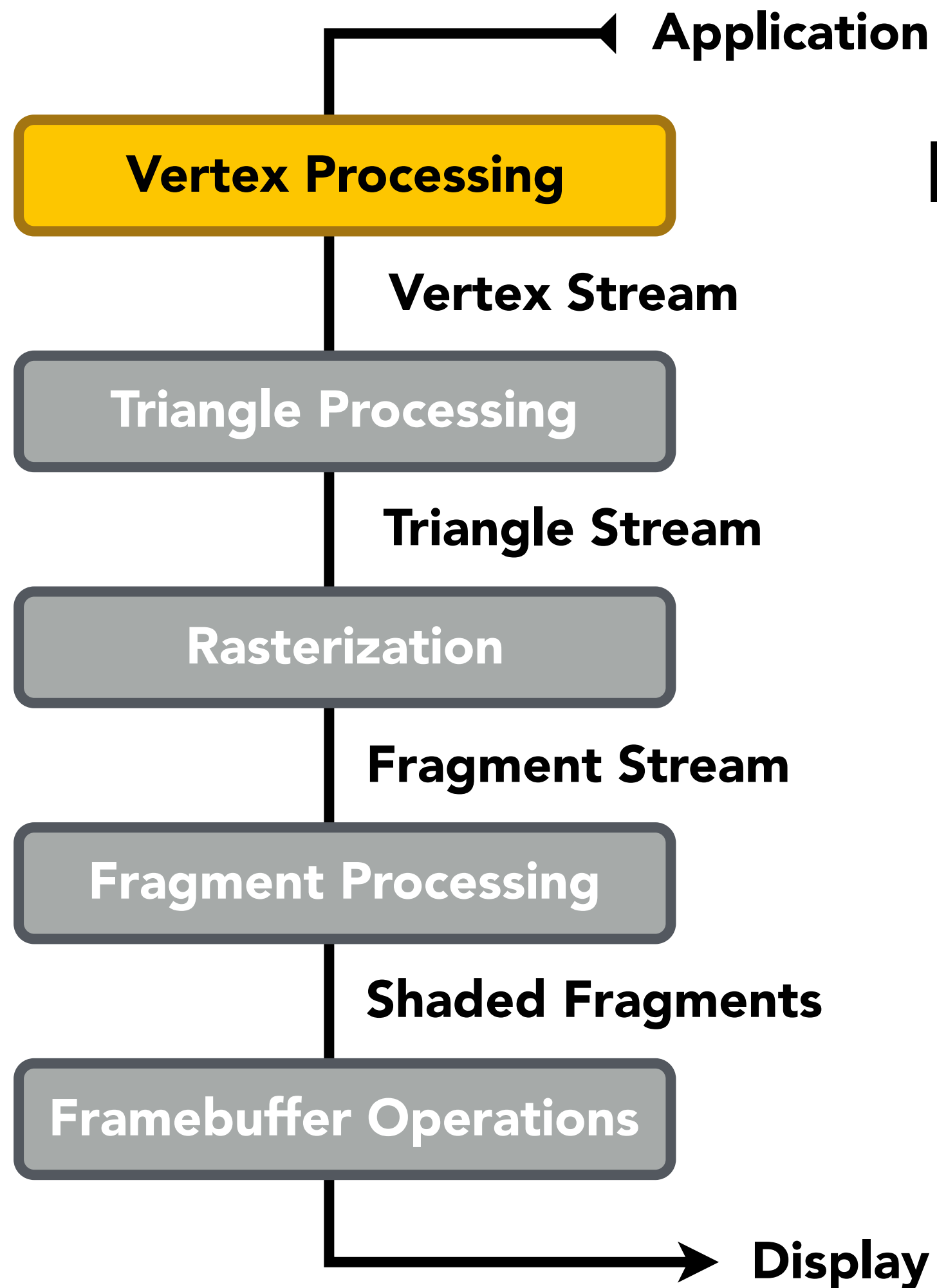
# **Rasterization Pipeline**



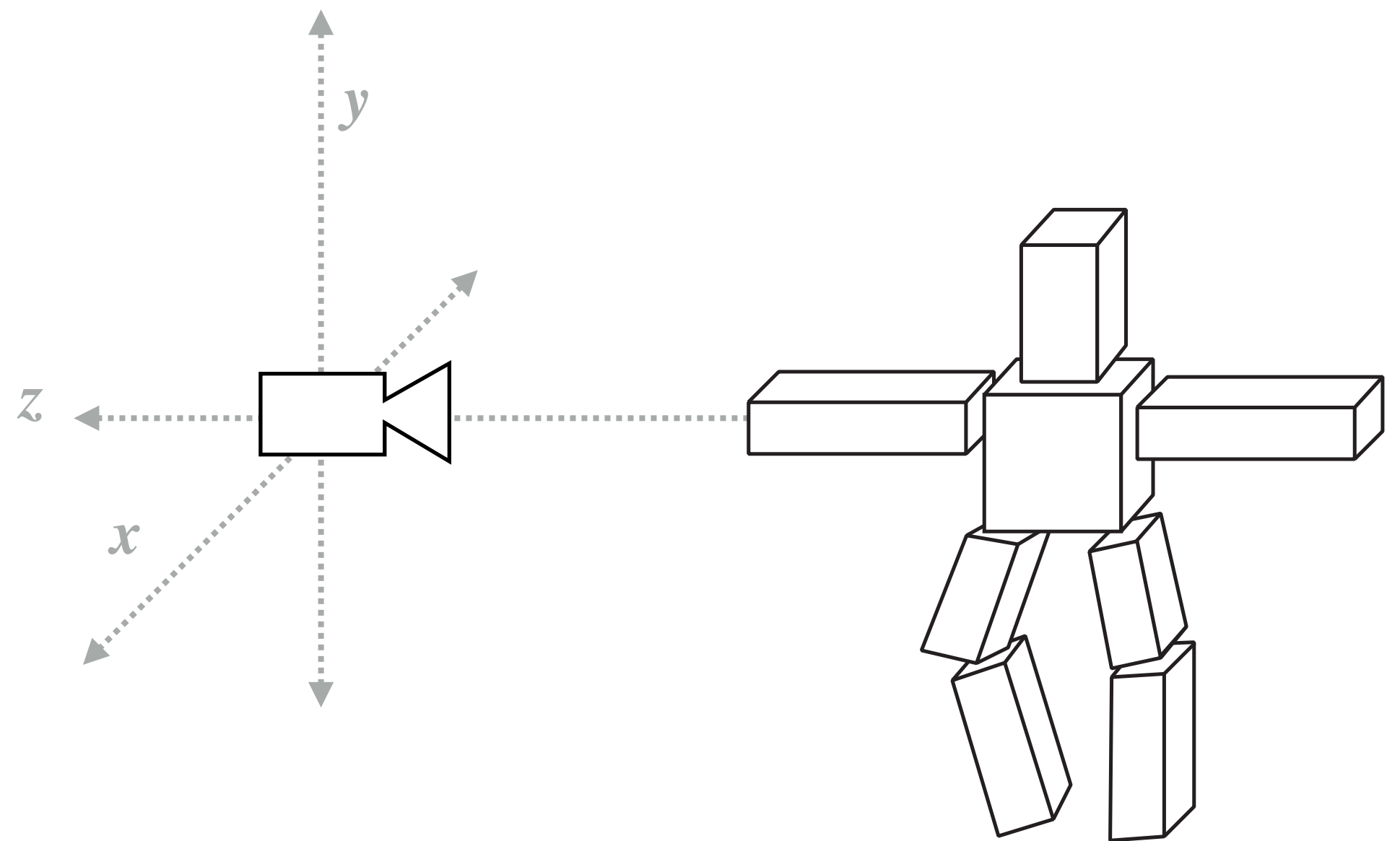
# Rasterization Pipeline



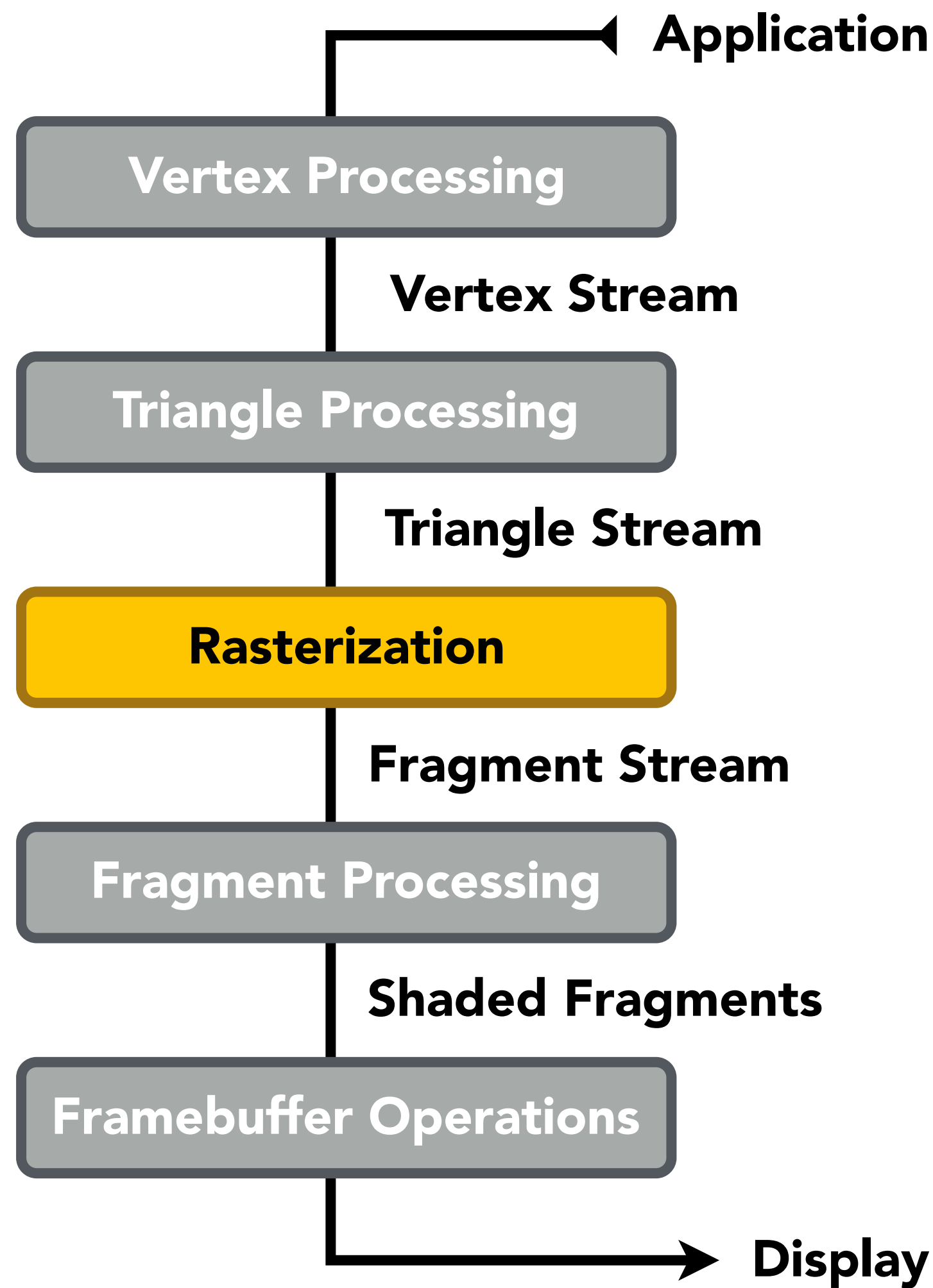
# Rasterization Pipeline



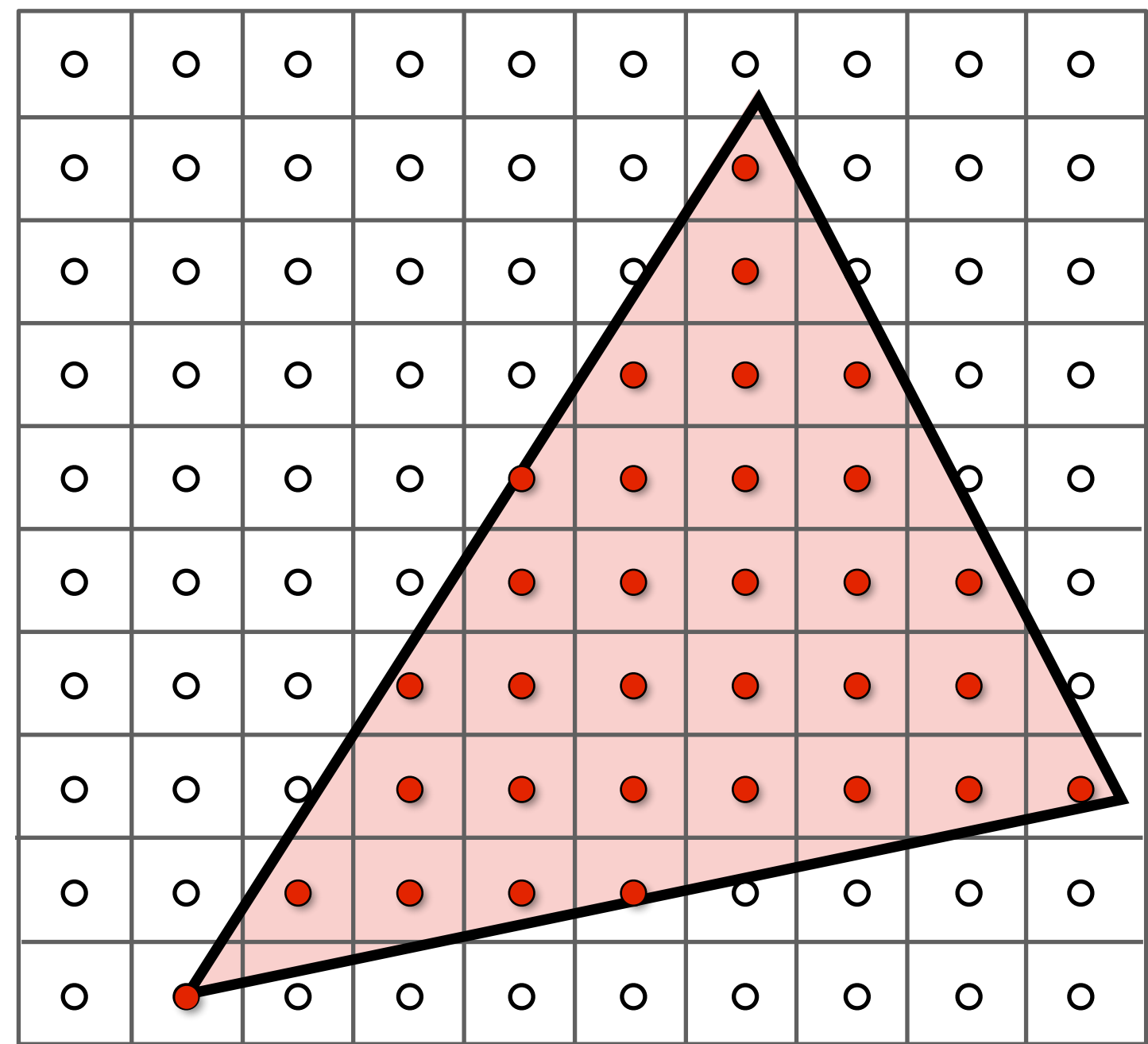
## Modeling & viewing transforms



# Rasterization Pipeline

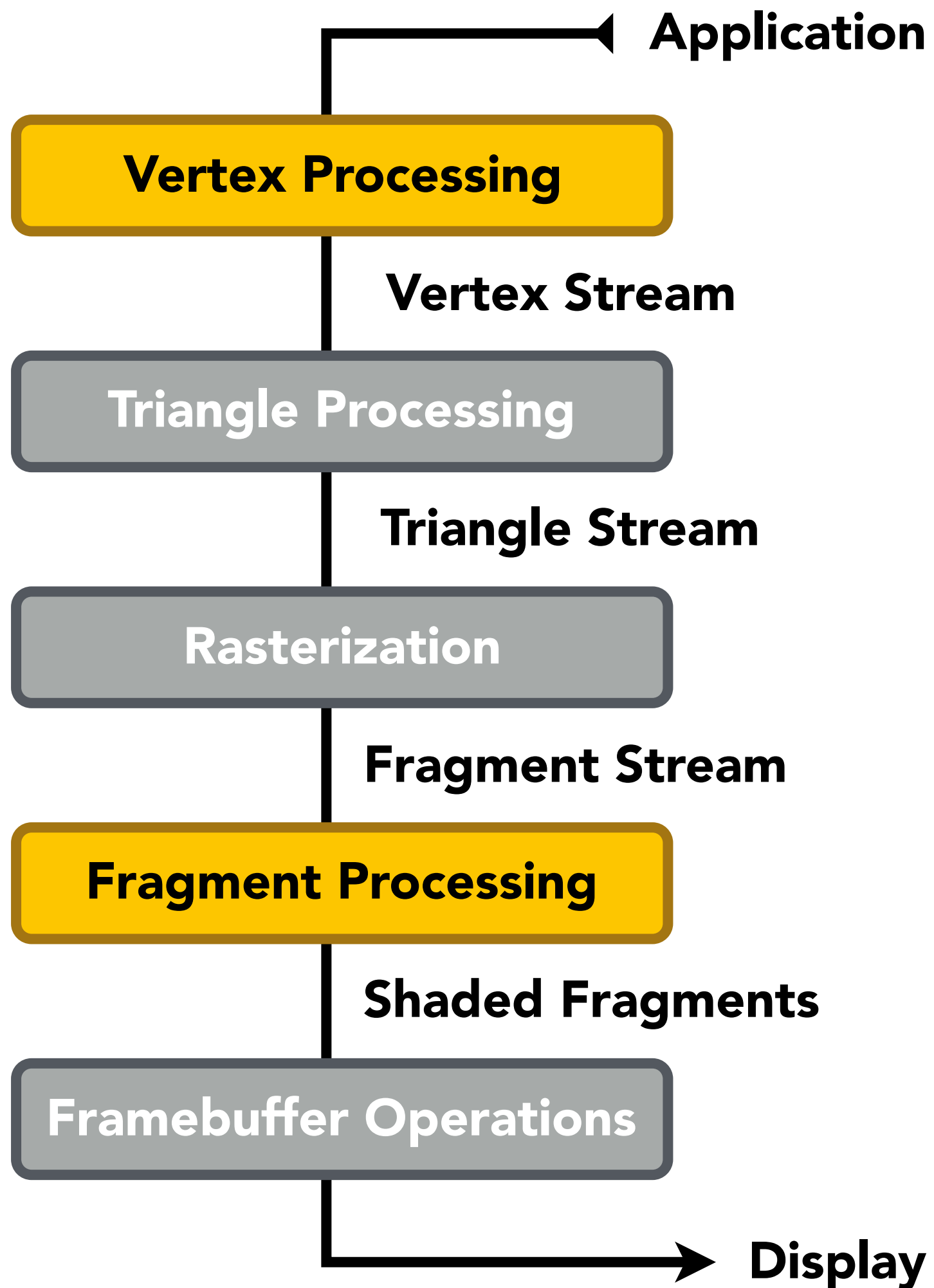


## Sampling triangle coverage

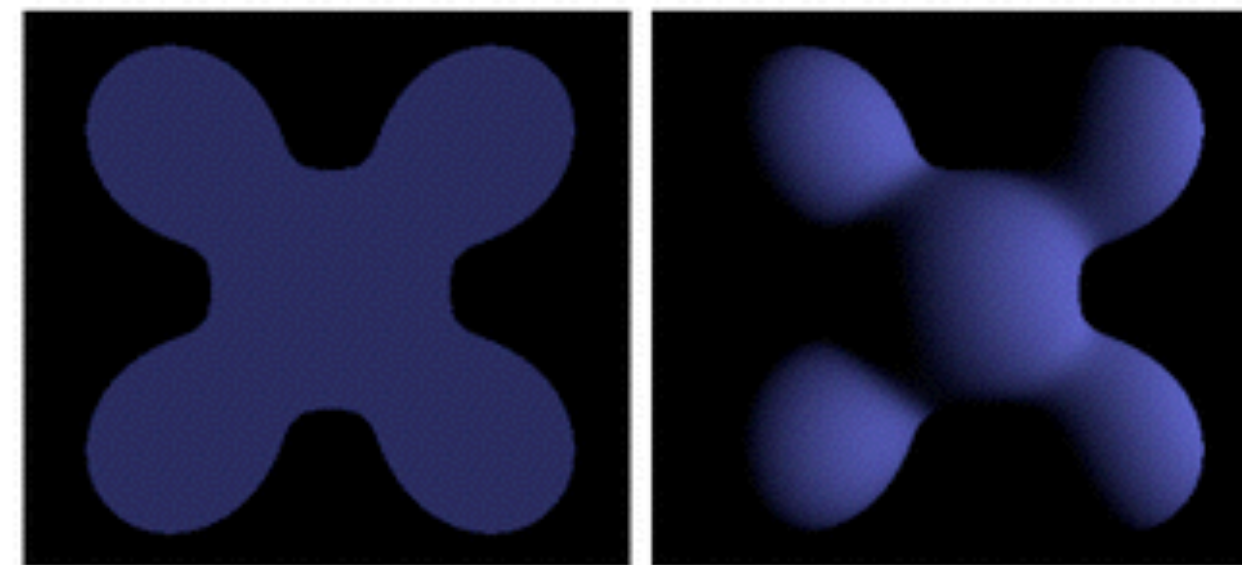




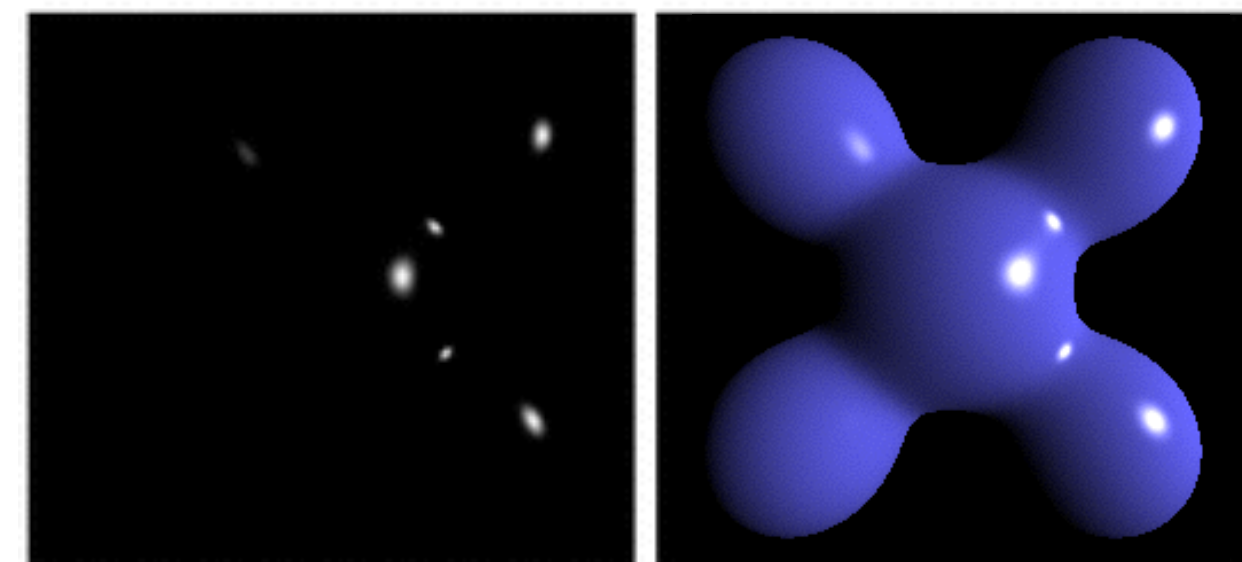
# Rasterization Pipeline



## Evaluating shading functions

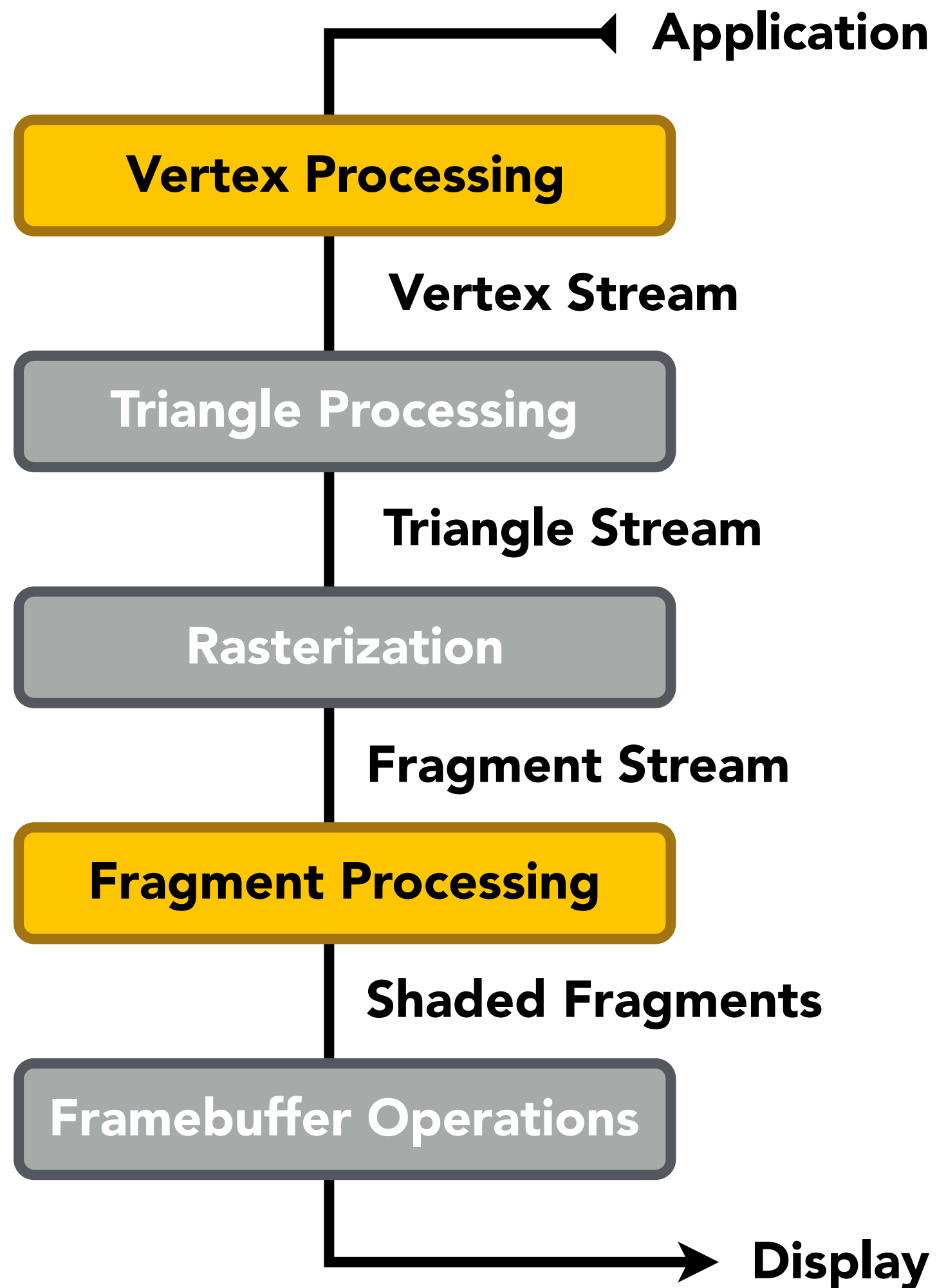


Ambient + Diffuse



+ Specular = Phong Reflection

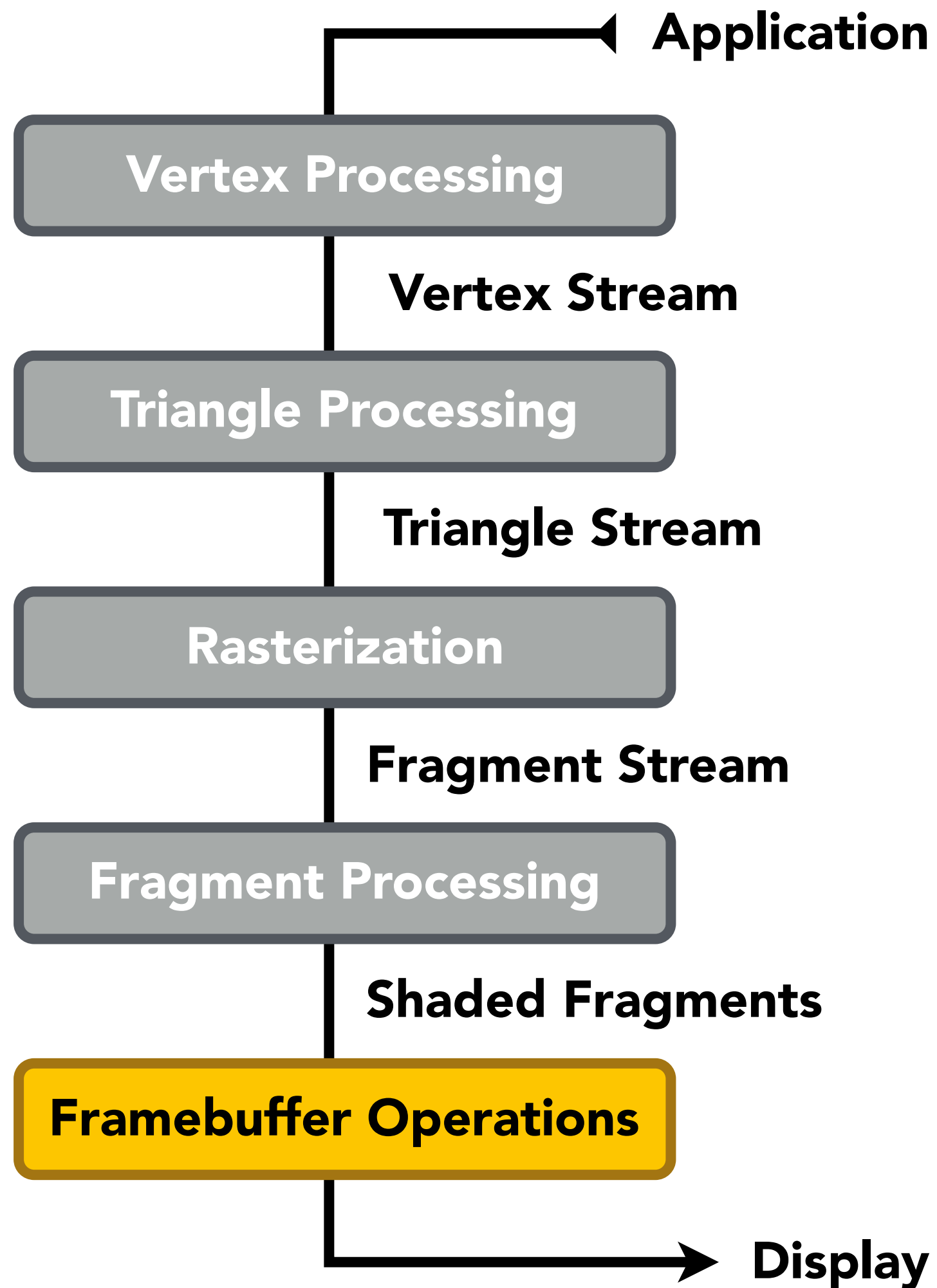
# Rasterization Pipeline



Texture mapping



# Rasterization Pipeline



## Z-Buffer Visibility Tests





# Shader Programs

- Program vertex and fragment processing stages
- Describe operation on a single vertex (or fragment)

## Example GLSL fragment shader program

```
uniform sampler2D myTexture;
uniform vec3 lightDir;
varying vec2 uv;
varying vec3 norm;

void diffuseShader()
{
    vec3 kd;
    kd = texture2d(myTexture, uv);
    kd *= clamp(dot(-lightDir, norm), 0.0, 1.0);
    gl_FragColor = vec4(kd, 1.0);
}
```

- Shader function executes once per fragment.
- Outputs color of surface at the current fragment's screen sample position.
- This shader performs a texture lookup to obtain the surface's material color at this point, then performs a diffuse lighting calculation.

# Shader Programs

- Program vertex and fragment processing stages
- Describe operation on a single vertex (or fragment)

## Example GLSL fragment shader program

```
uniform sampler2D myTexture;    // program parameter
uniform vec3 lightDir;         // program parameter
varying vec2 uv;               // per fragment value (interp. by rasterizer)
varying vec3 norm;             // per fragment value (interp. by rasterizer)

void diffuseShader()
{
    vec3 kd;
    kd = texture2D(myTexture, uv);    // material color from texture
    kd *= clamp(dot(-lightDir, norm), 0.0, 1.0); // Lambertian shading model
    gl_FragColor = vec4(kd, 1.0);     // output fragment color
}
```



# Goal: Highly Complex 3D Scenes in Realtime

- 100's of thousands to millions of triangles in a scene
- Complex vertex and fragment shader computations
- High resolution (2-4 megapixel + supersampling)
- 30-60 frames per second (even higher for VR)



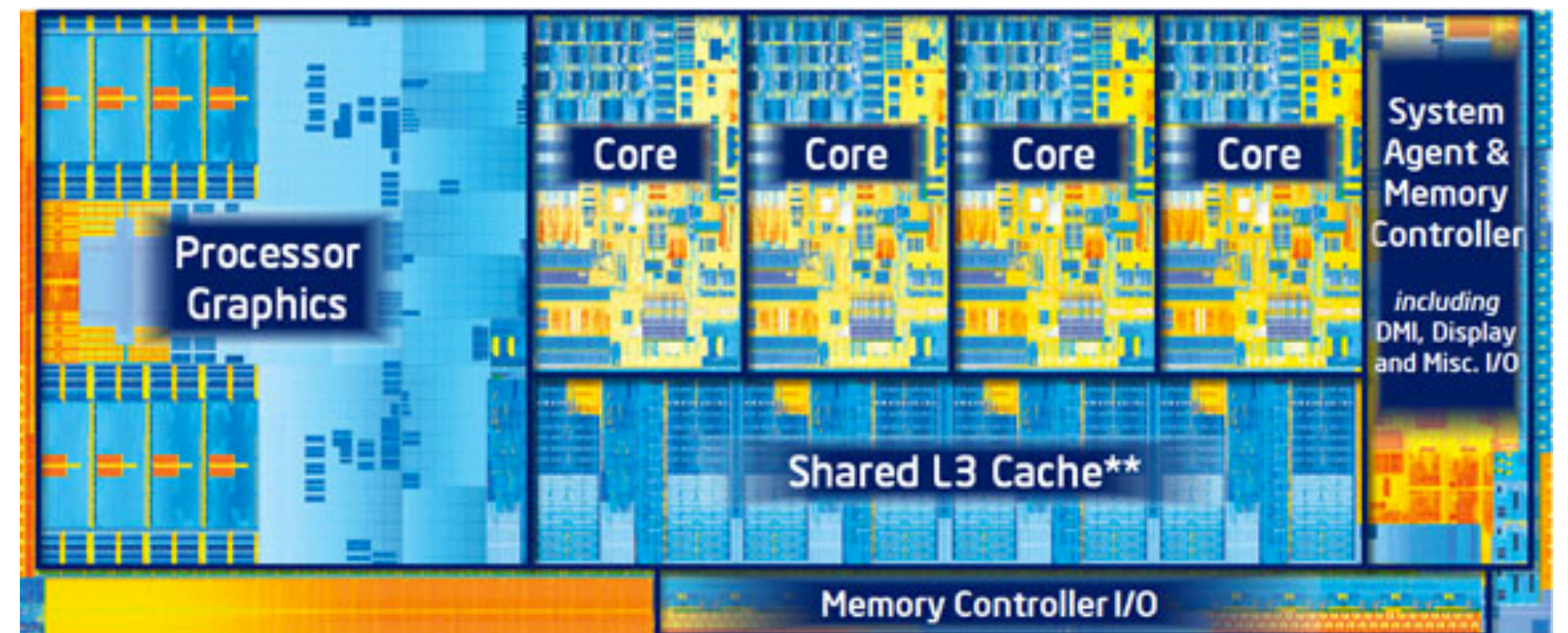


# Graphics Pipeline Implementation: GPUs

Specialized processors for executing graphics pipeline computations

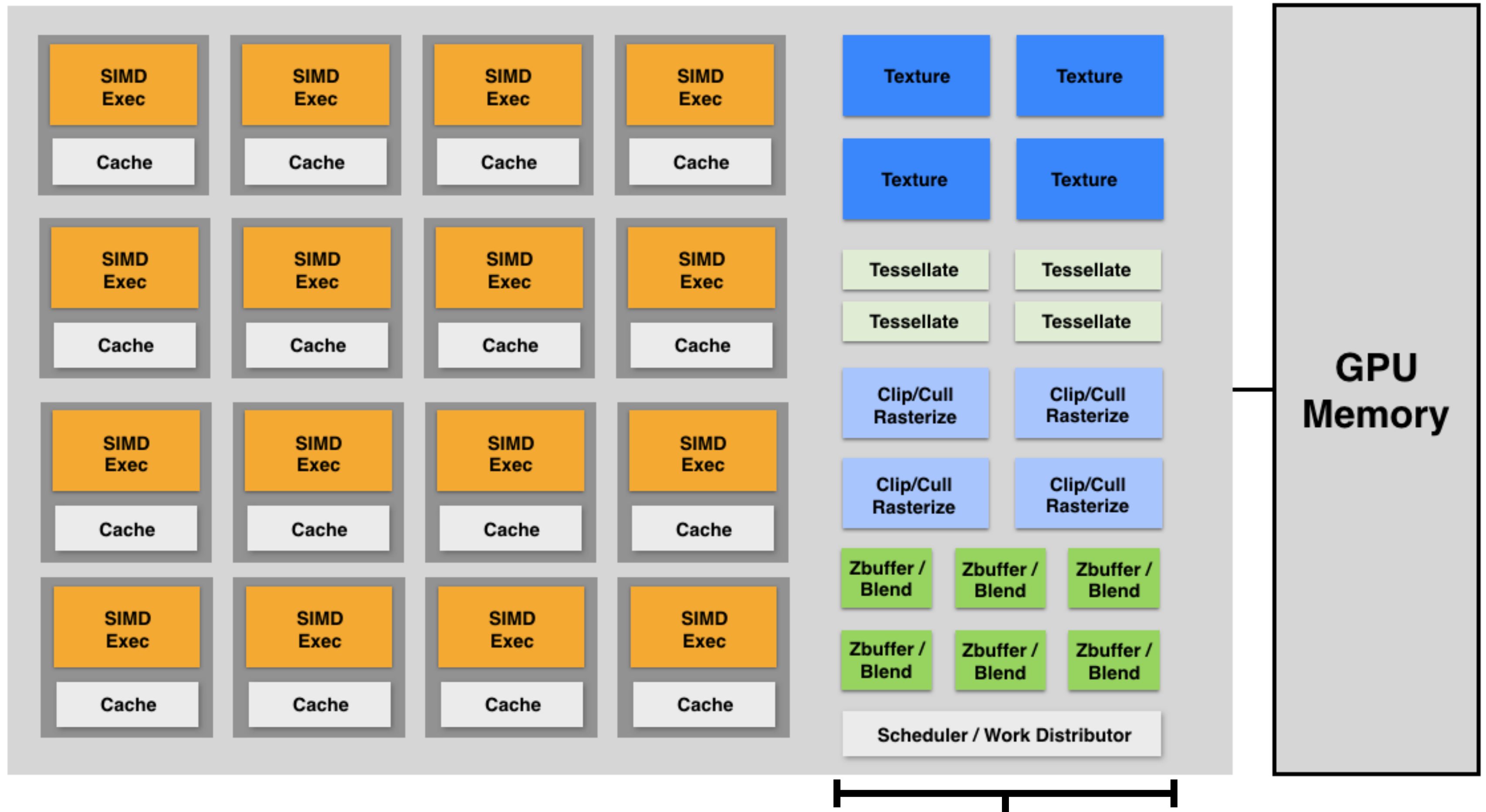


**Discrete GPU Card  
(NVIDIA GeForce Titan X)**



**Integrated GPU:  
(Part of Intel CPU die)**

# GPU: Heterogeneous, Multi-Core Processor



Modern GPUs offer ~2-4 Tera-FLOPs of performance for executing vertex and fragment shader programs

Tera-Op's of fixed-function compute capability over here

# Things to Remember

## Visibility

- Painter's algorithm and Z-Buffer algorithm

## Simple Shading Model

- Key geometry: lighting, viewing & normal vectors
- Ambient, diffuse & specular reflection functions
- Shading frequency: triangle, vertex or fragment

## Graphics Rasterization Pipeline

- Where do transforms, rasterization, shading, texturing and visibility computations occur?
- GPU = parallel processor implementing graphics pipeline



# Acknowledgments

Thanks to Steve Marschner, Mark Pauly and Kayvon Fatahalian for presentation resources.