Lecture 24/25:

Intro to Virtual Reality

Computer Graphics and Imaging UC Berkeley CS184/284A

Ivan Sutherland's Virtual Reality Research in 1968

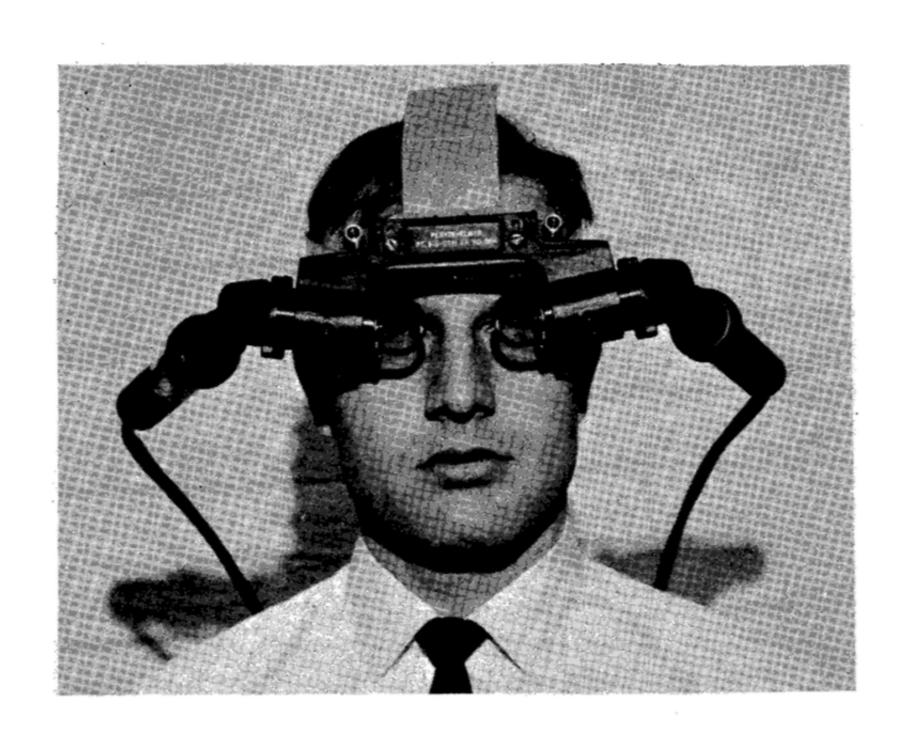


FIGURE 2—The head-mounted display optics with miniature CRT's



FIGURE 4—The ultrasonic head position sensor in use

VR Head-Mounted Displays (HMDs)



Also Valve Index, HP Reverb, etc...

Virtual Reality (VR) vs Augmented Reality (AR)

VR = virtual reality

 User is completely immersed in virtual world (sees only light emitted by display)

AR = augmented reality

 Display is an overlay that augments user's normal view of the real world (e.g., Terminator)





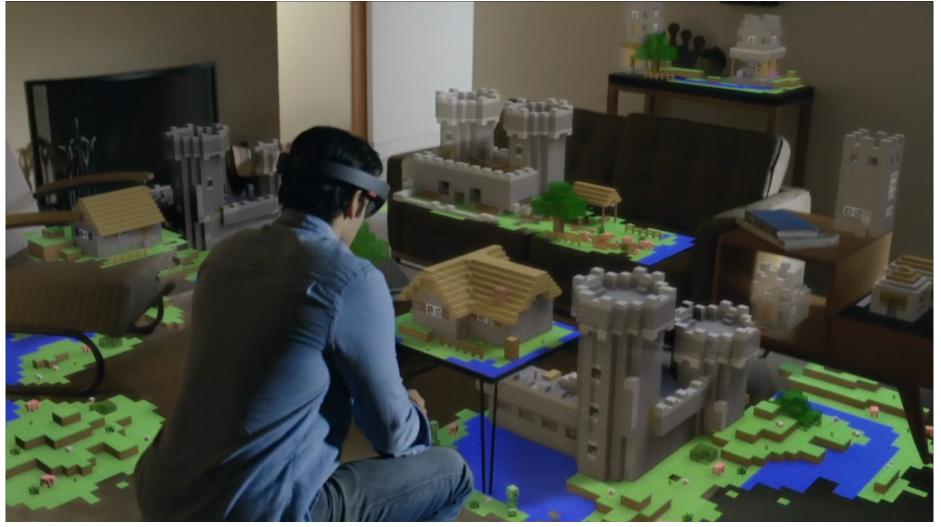
Image credit: Terminator 2 (naturally)

AR Headsets

Microsoft Hololens Magic Leap









Also Snap Spectacles

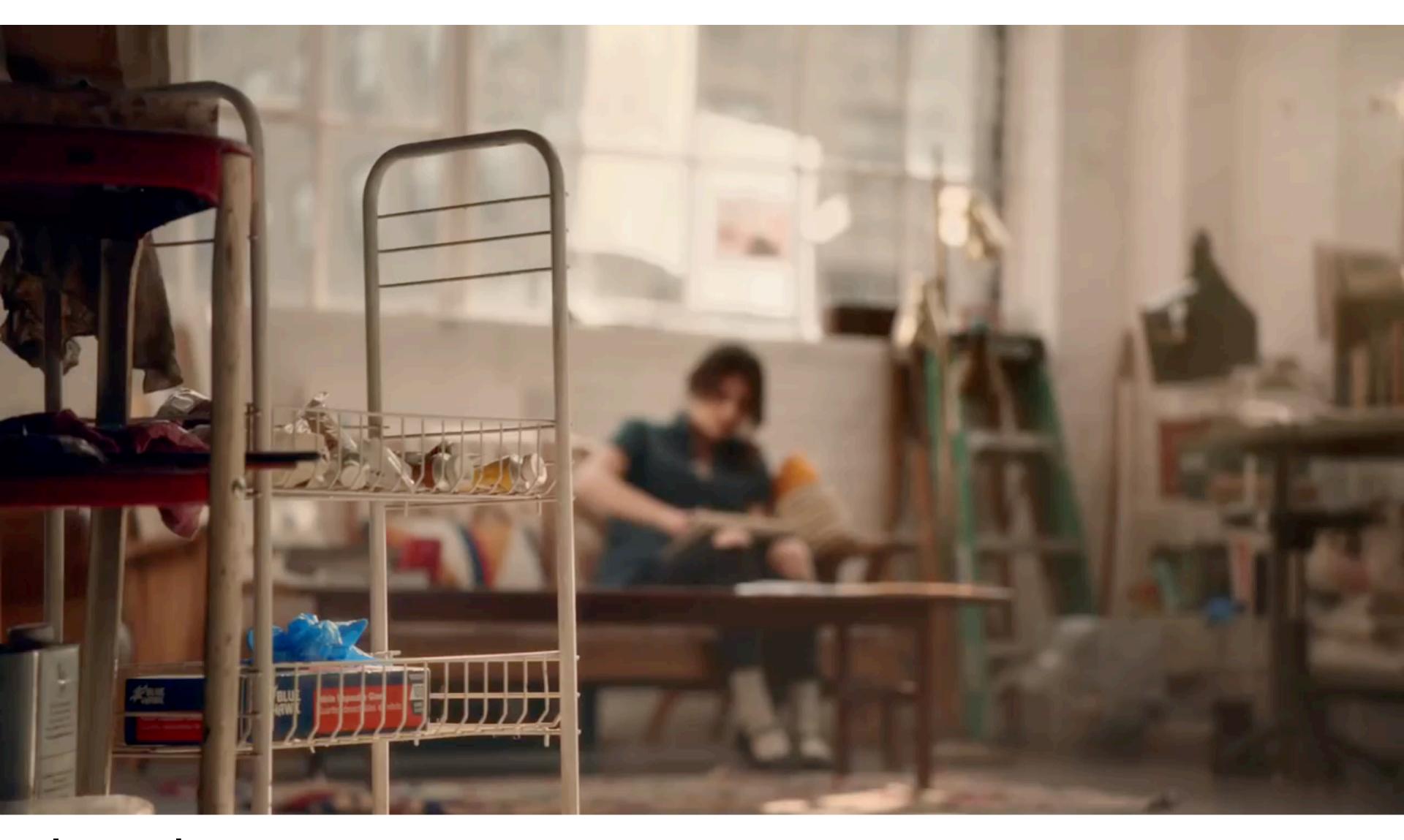
VR Applications

VR Gaming



Star Wars Squadrons (EA)

VR Painting



Tilt Brush

VR Video



VR Video



VR Teleconference / Video Chat



http://vrchat.com/

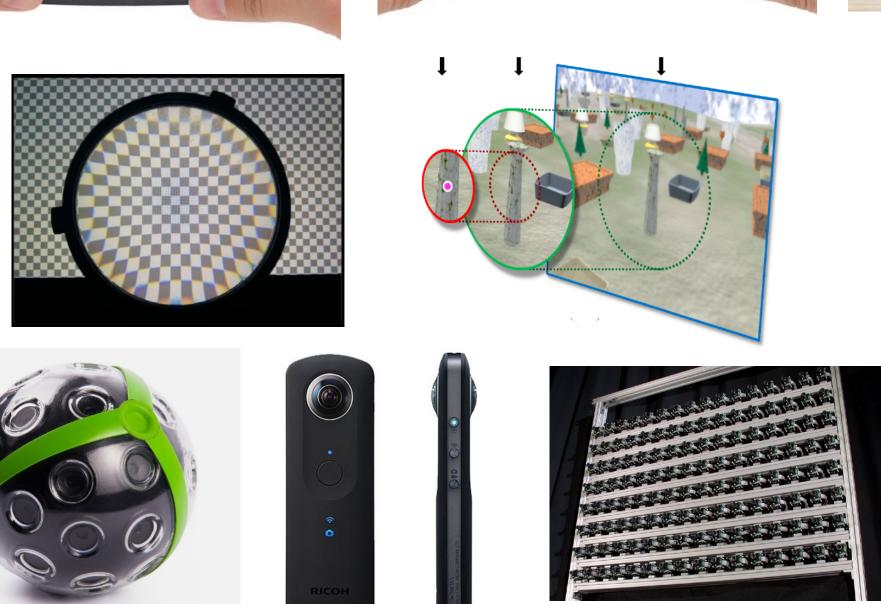
Overview of VR Topics

VR Displays



VR Rendering





VR Displays

Field of View

Regular 2D panel displays have windowed FOV

 User orients themselves to the physical window of the display

VR/AR displays provide 360 degree FOV

- Displays attached to head
- Head orientation is tracked physically
- Rendered view synchronized to head orientation in realtime (much more on this later)

3D Visual Cues

Panel displays give 3D cues from monocular rendering

- Occlusion, perspective, shading, focus blur, ...
 - Uses z-buffer, 4x4 matrices, lighting calculation, lens calculations...

VR/AR displays add further 3D cues

- Stereo: different perspective view in left/right eyes
 - Physically send different images into each eye
- Parallax (user-motion): different views as user moves
 - Uses head-tracking technology coupled to perspective rendering

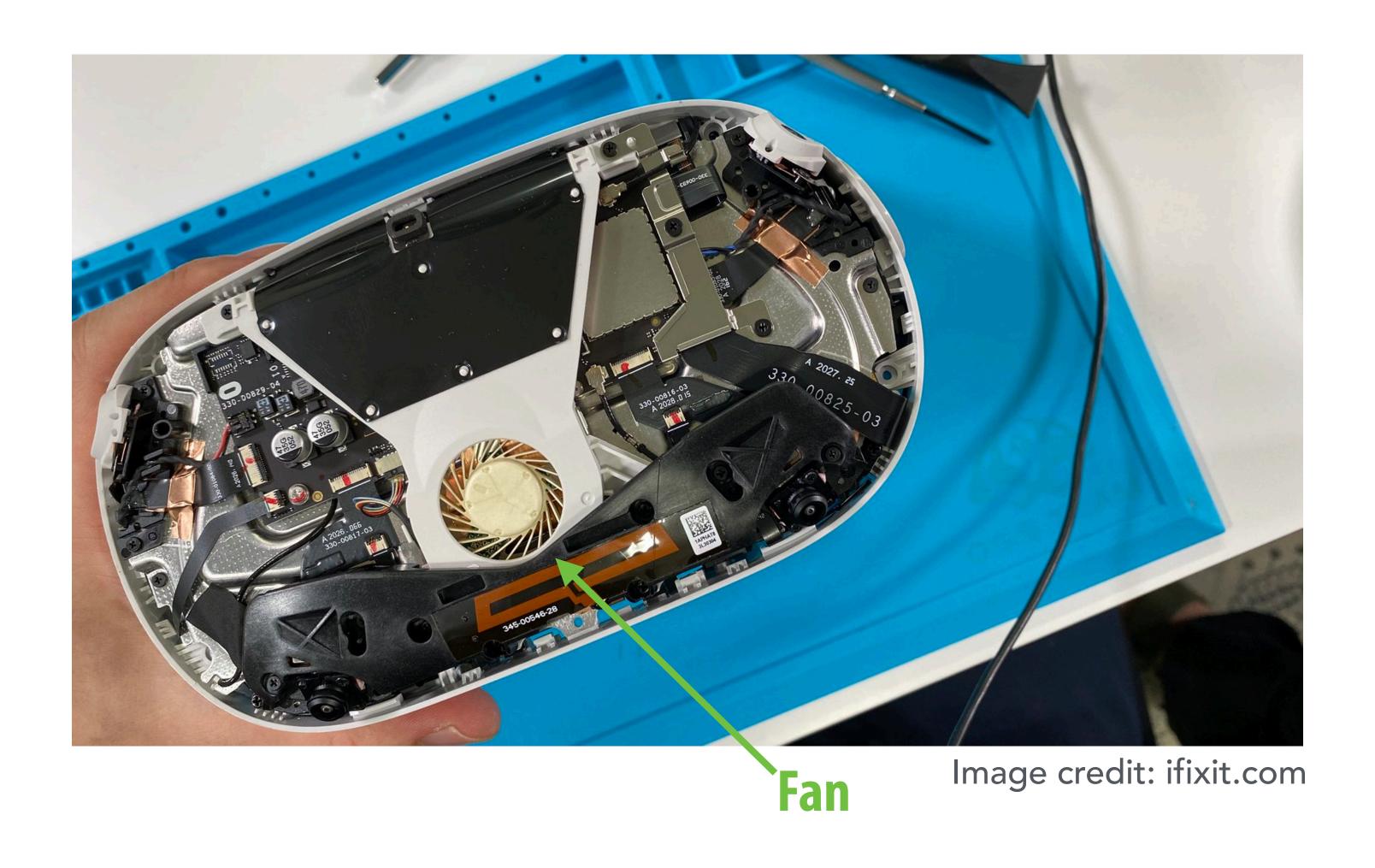
VR Headset Components

Oculus Quest 2 Headset (2020)









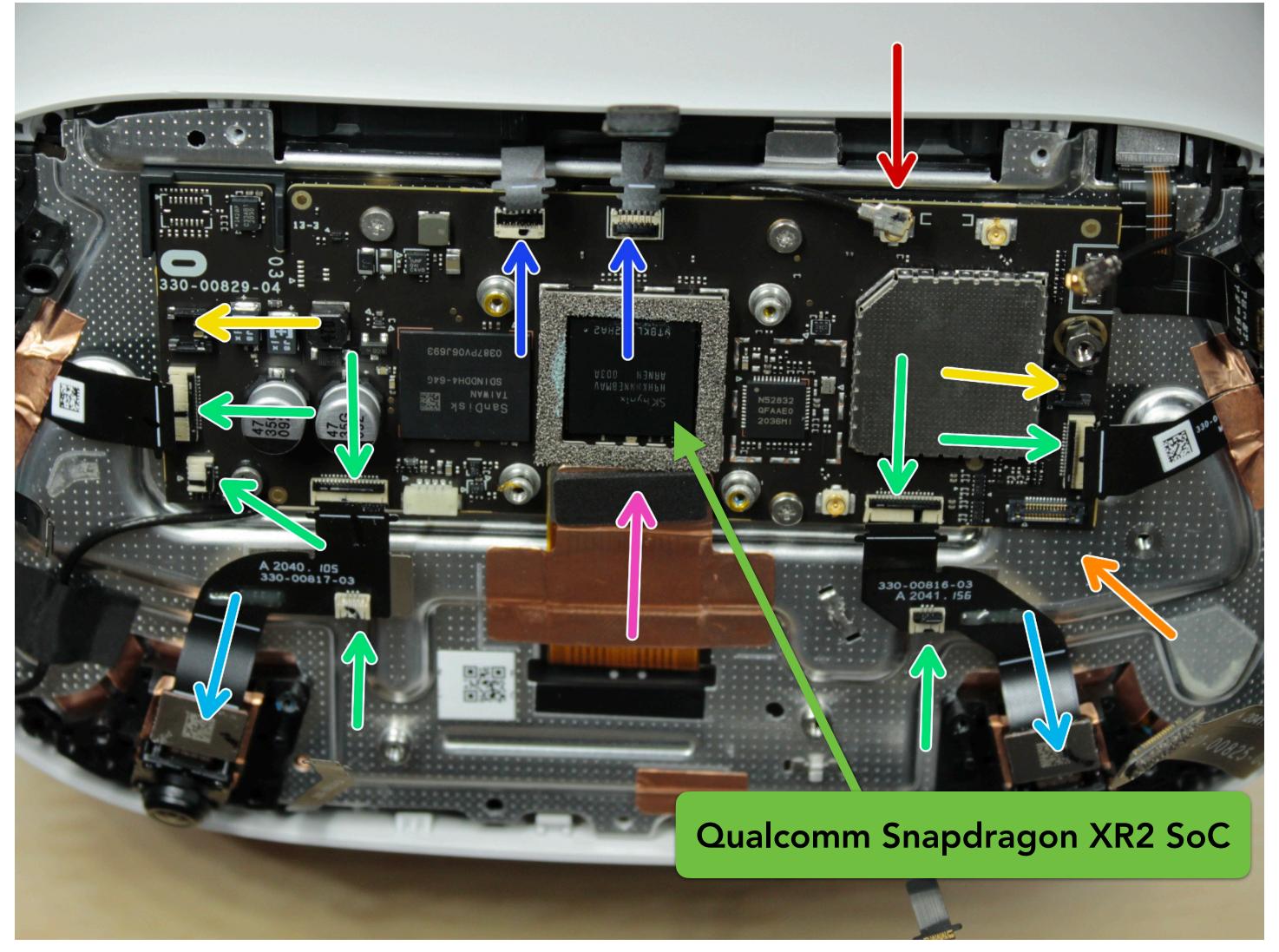


Image credit: ifixit.com

Oculus Quest 2 Headset (Snapdragon SoC)

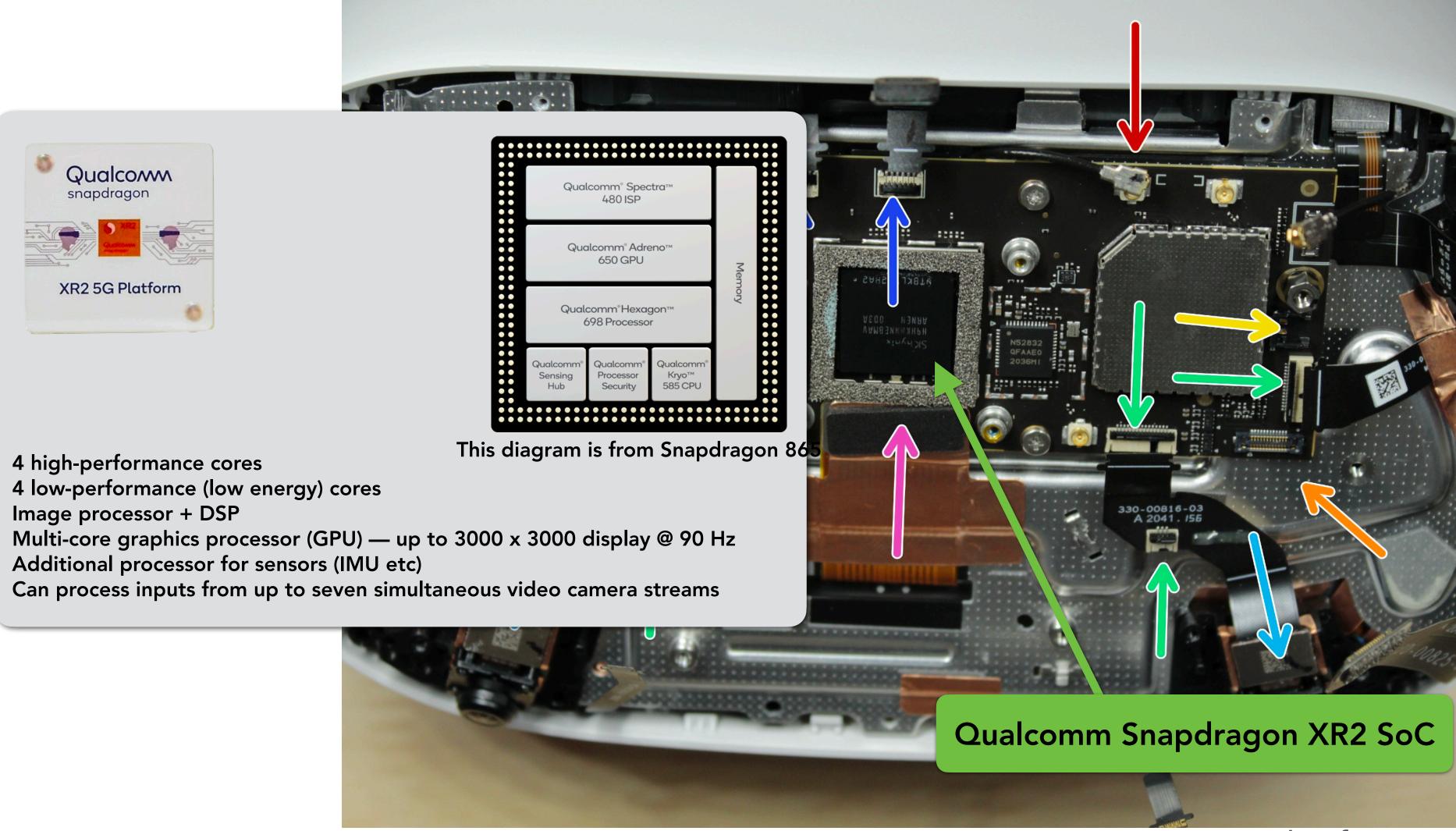
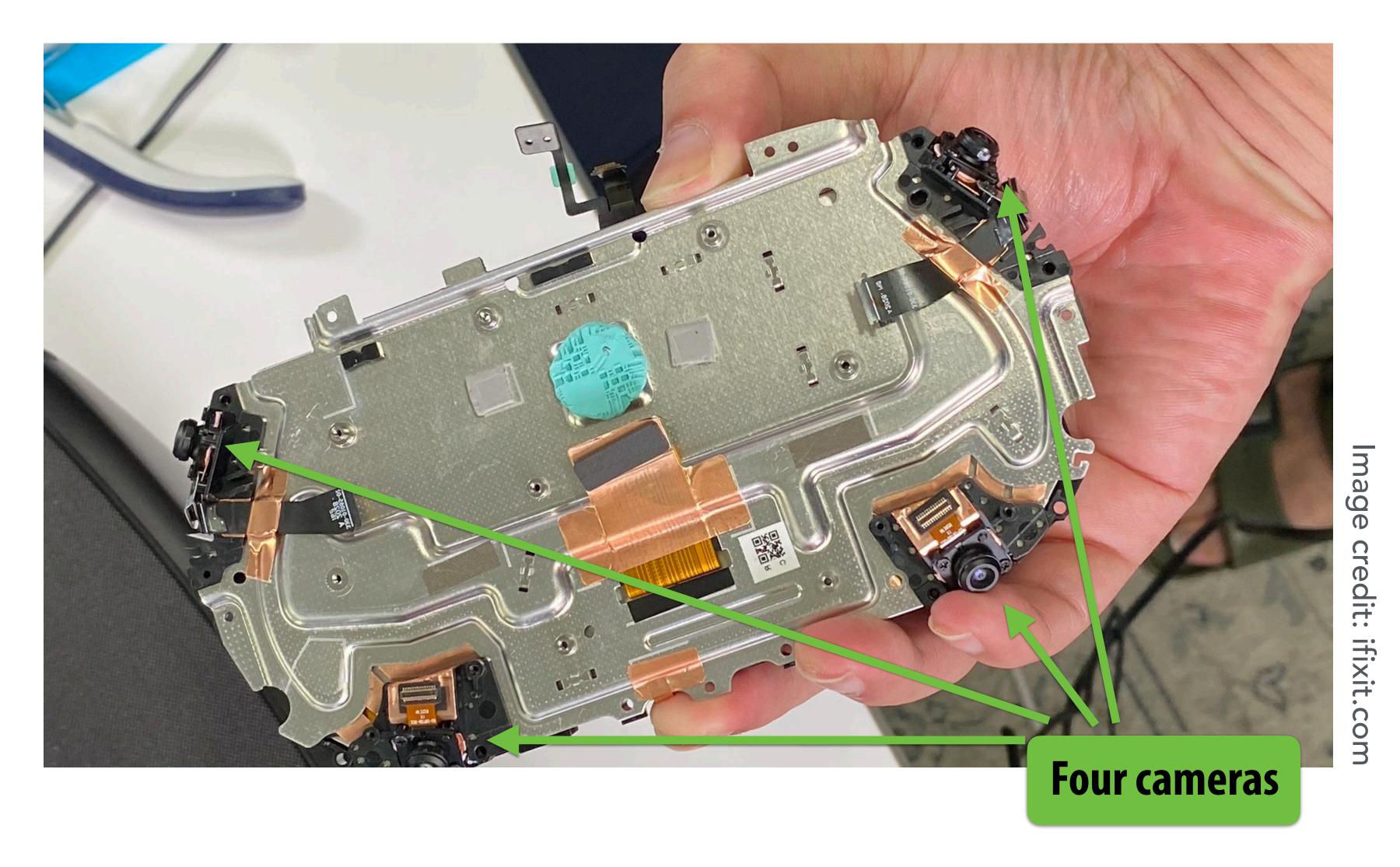


Image credit: ifixit.com



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Oculus Quest 2 Headset (Lens Assembly)



Image credit: ifixit.com

Oculus Quest 2 Display + Lens Assembly

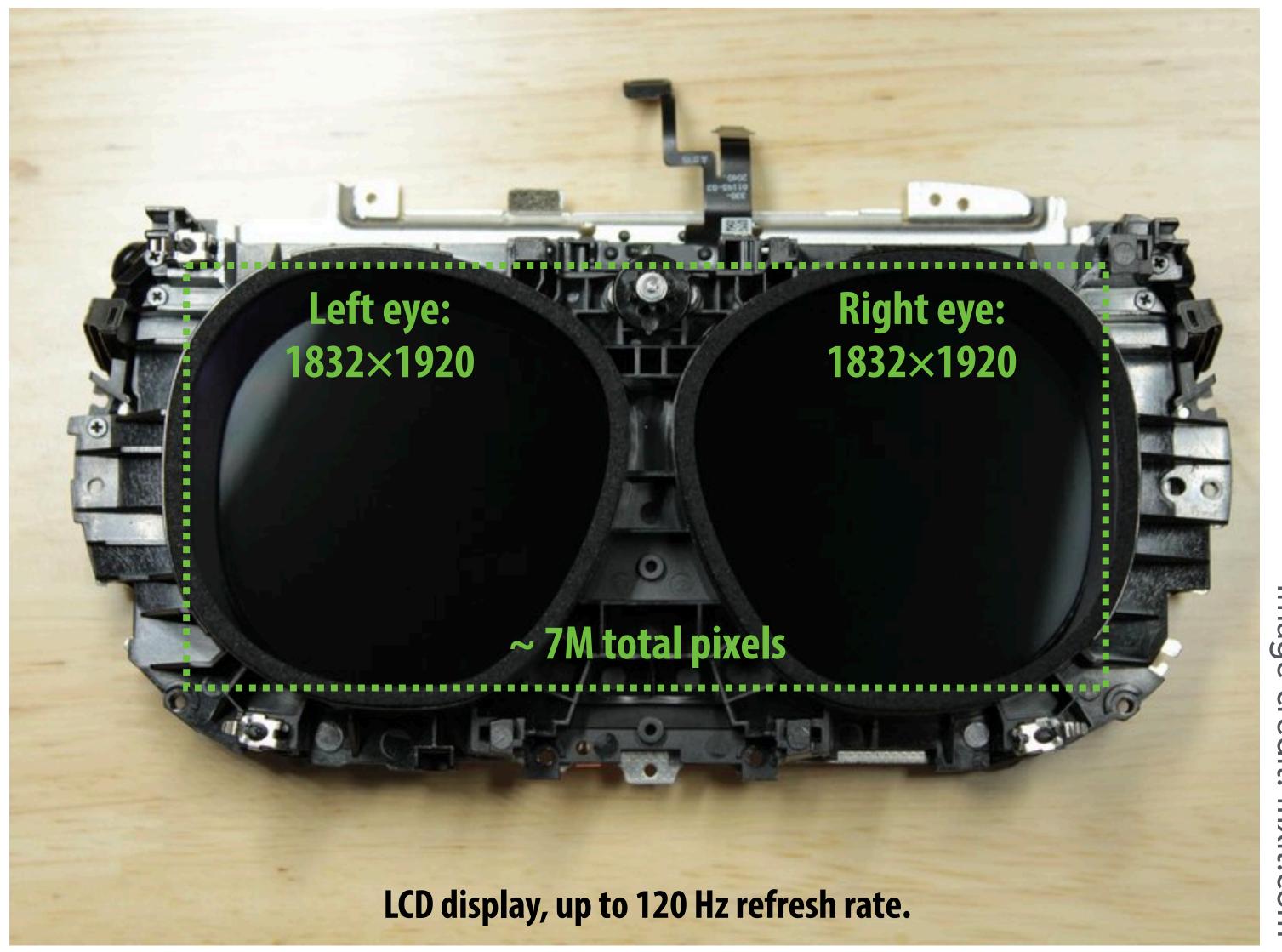


Image credit: ifixit.com

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Image credit: ifixit.com

https://www.ifixit.com/Teardown/Oculus+Rift+CV1+Teardown/60612



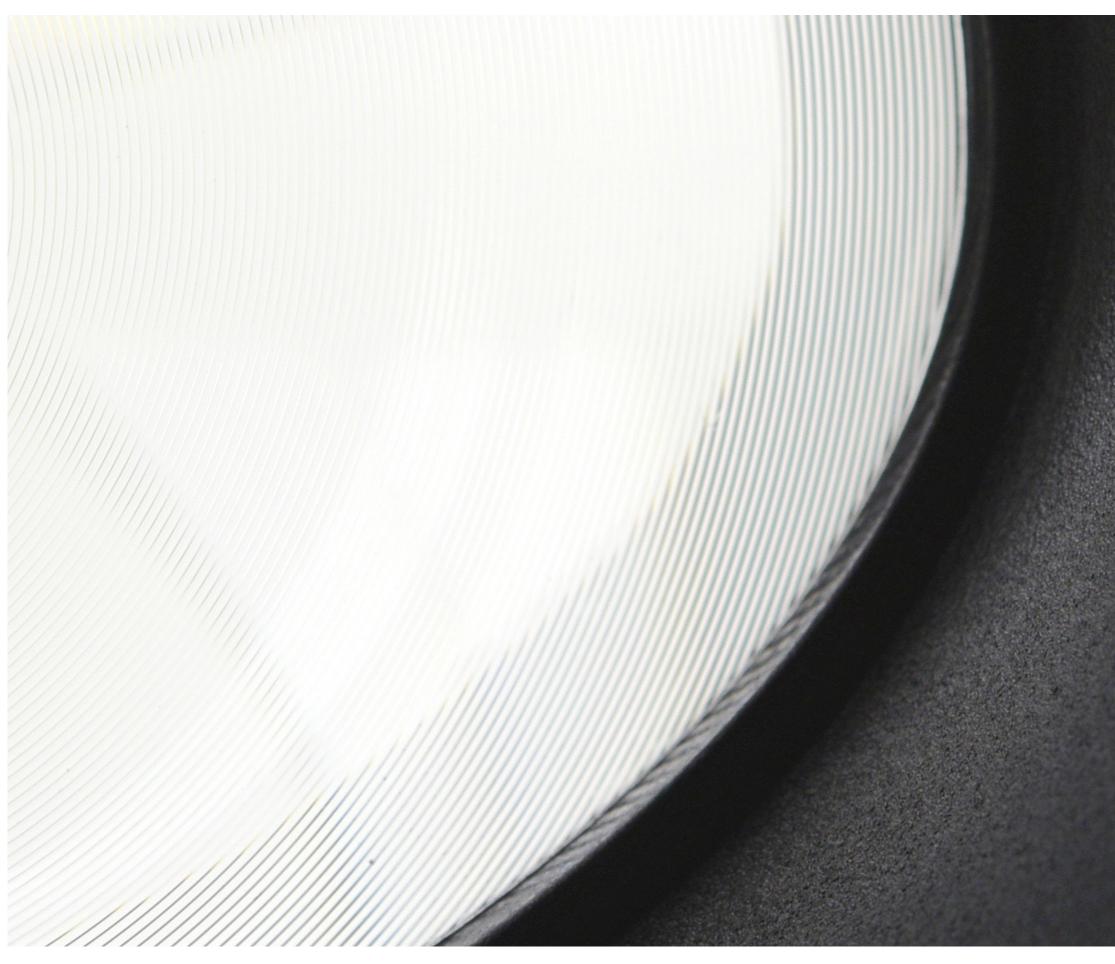




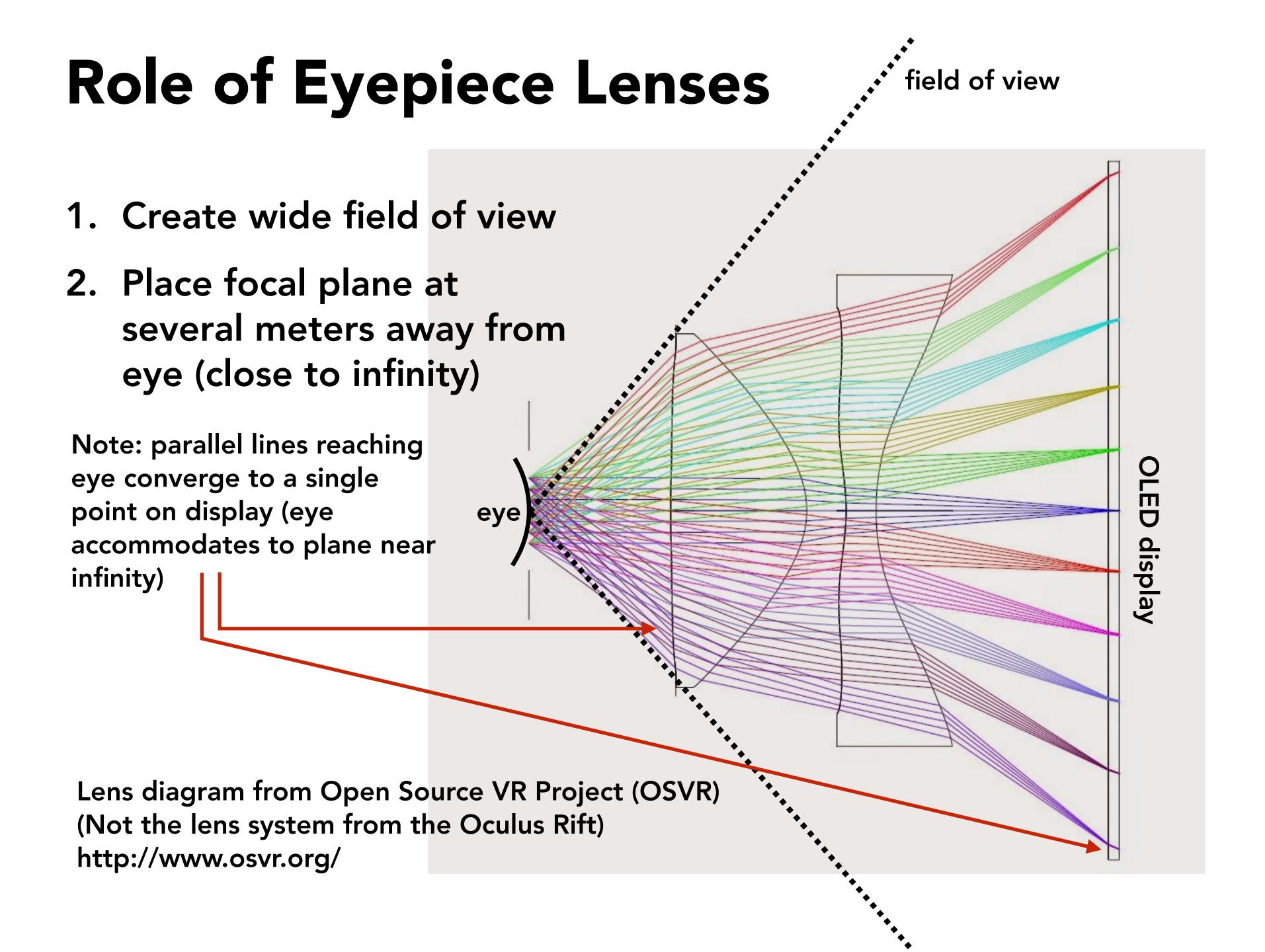


Oculus Rift Lenses



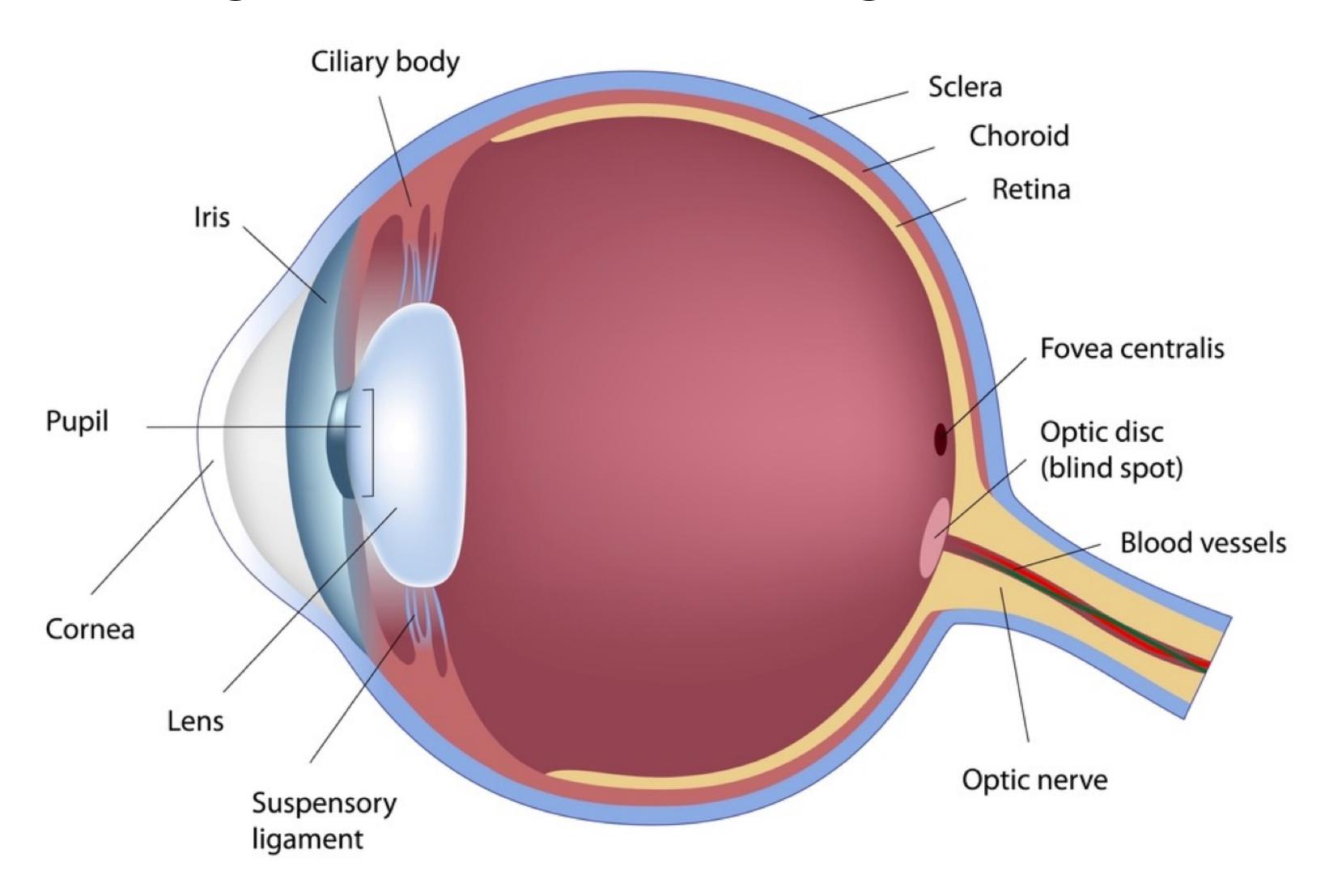


Fresnel eyepiece lens



Display Requirements Derive From Human Perception

Anatomy of The Human Eye



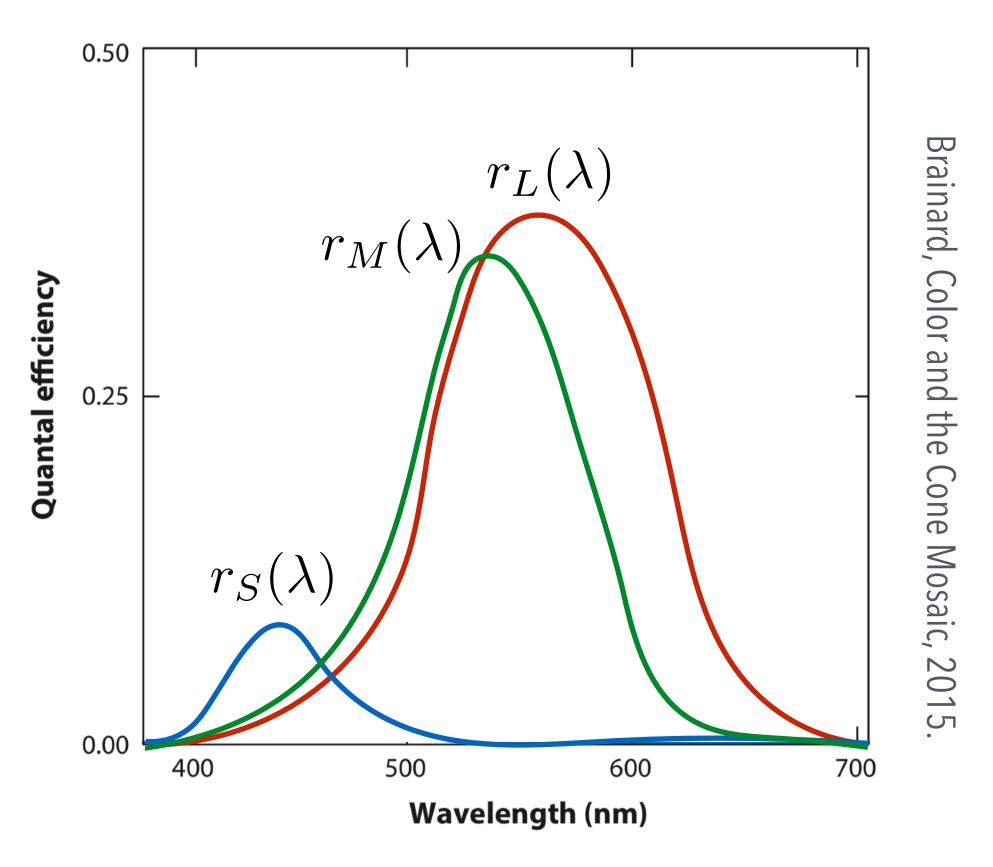
Display Requirements Derive From Human Perception

Example 1: Color

Recall: Spectral Response of Human Cone Cells

Instead of one detector as before, now we have three detectors (S, M, L cone cells), each with a different spectral response curve

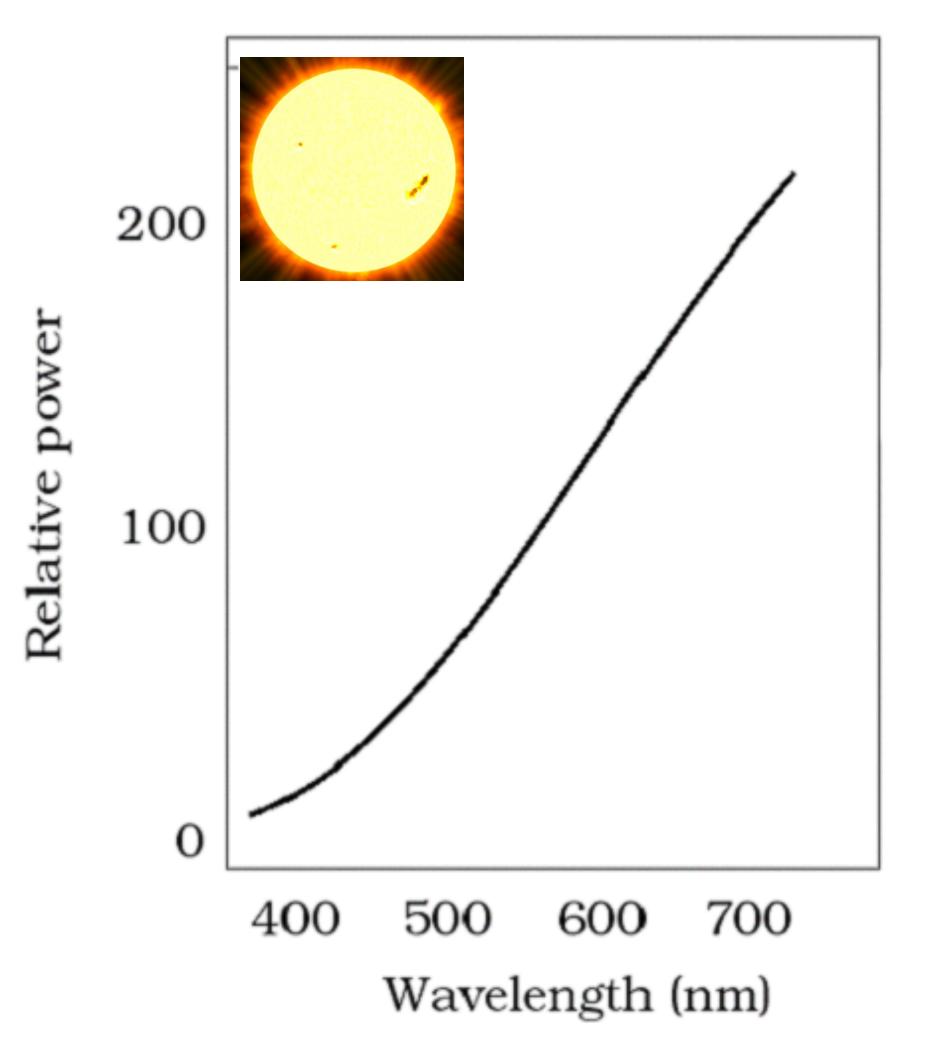
$$S = \int r_S(\lambda) s(\lambda) d\lambda$$
 $M = \int r_M(\lambda) s(\lambda) d\lambda$
 $L = \int r_L(\lambda) s(\lambda) d\lambda$

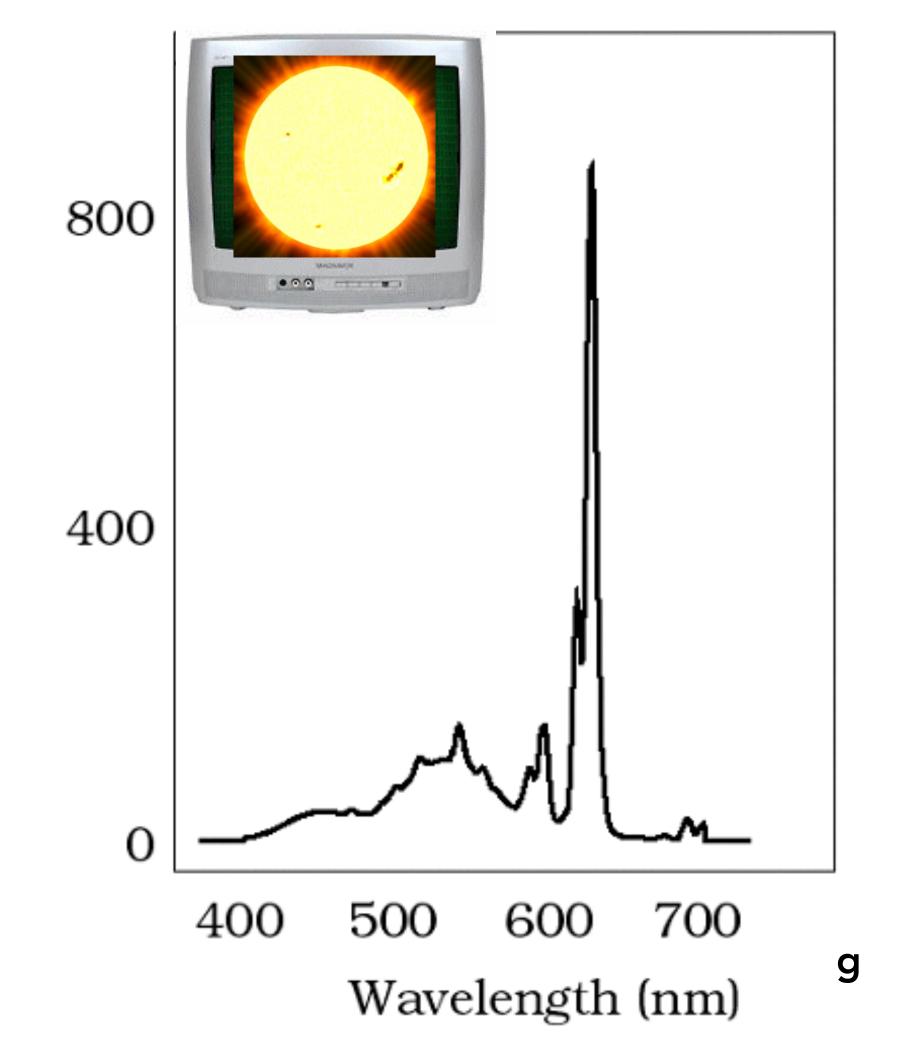


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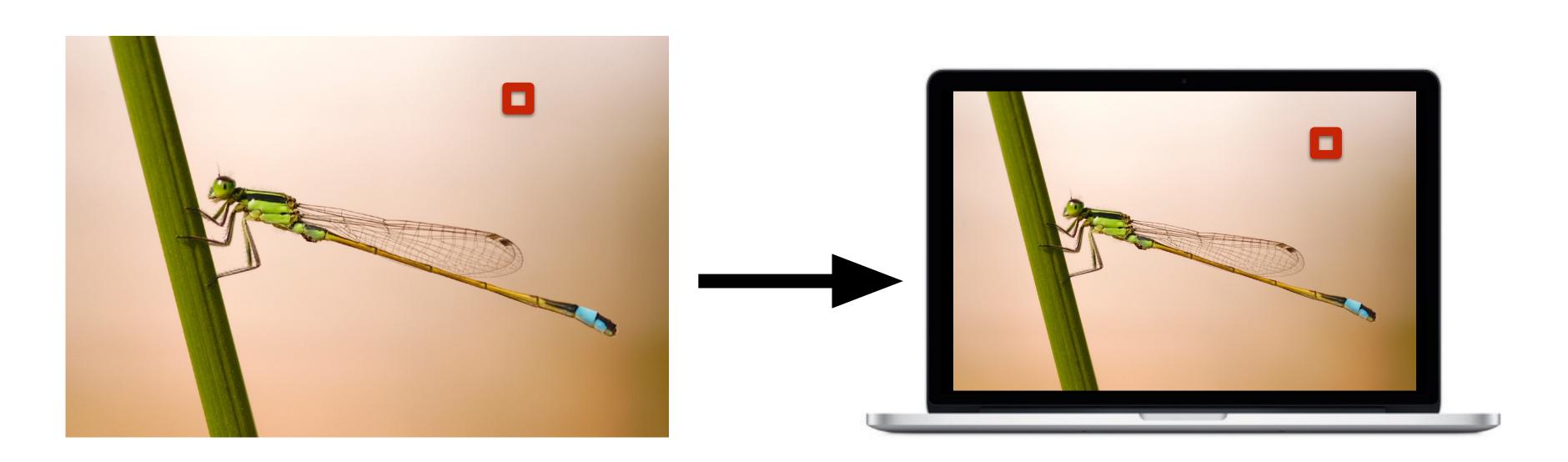
Recall: Metamerism

Color matching is an important illusion that is understood quantitatively





Recall: Color Reproduction



Target real spectrum $s(\lambda)$

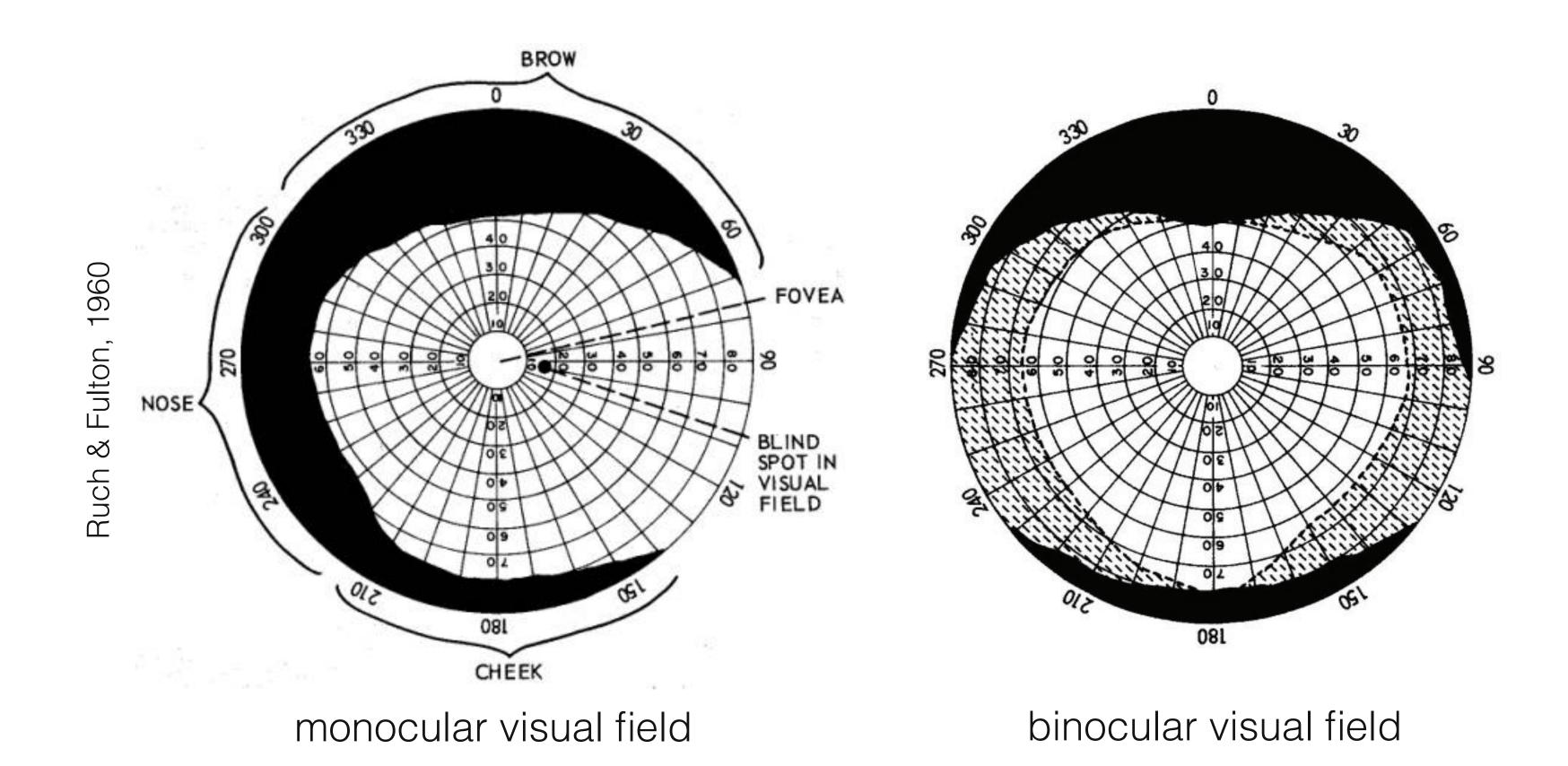
Display outputs spectrum $R s_R(\lambda) + G s_G(\lambda) + B s_B(\lambda)$

Goal: at each pixel, choose R, G, B values for display so that the output color matches the appearance of the target color in the real world.

Display Requirements Derive From Human Perception

Example 2: Field of View & Resolution

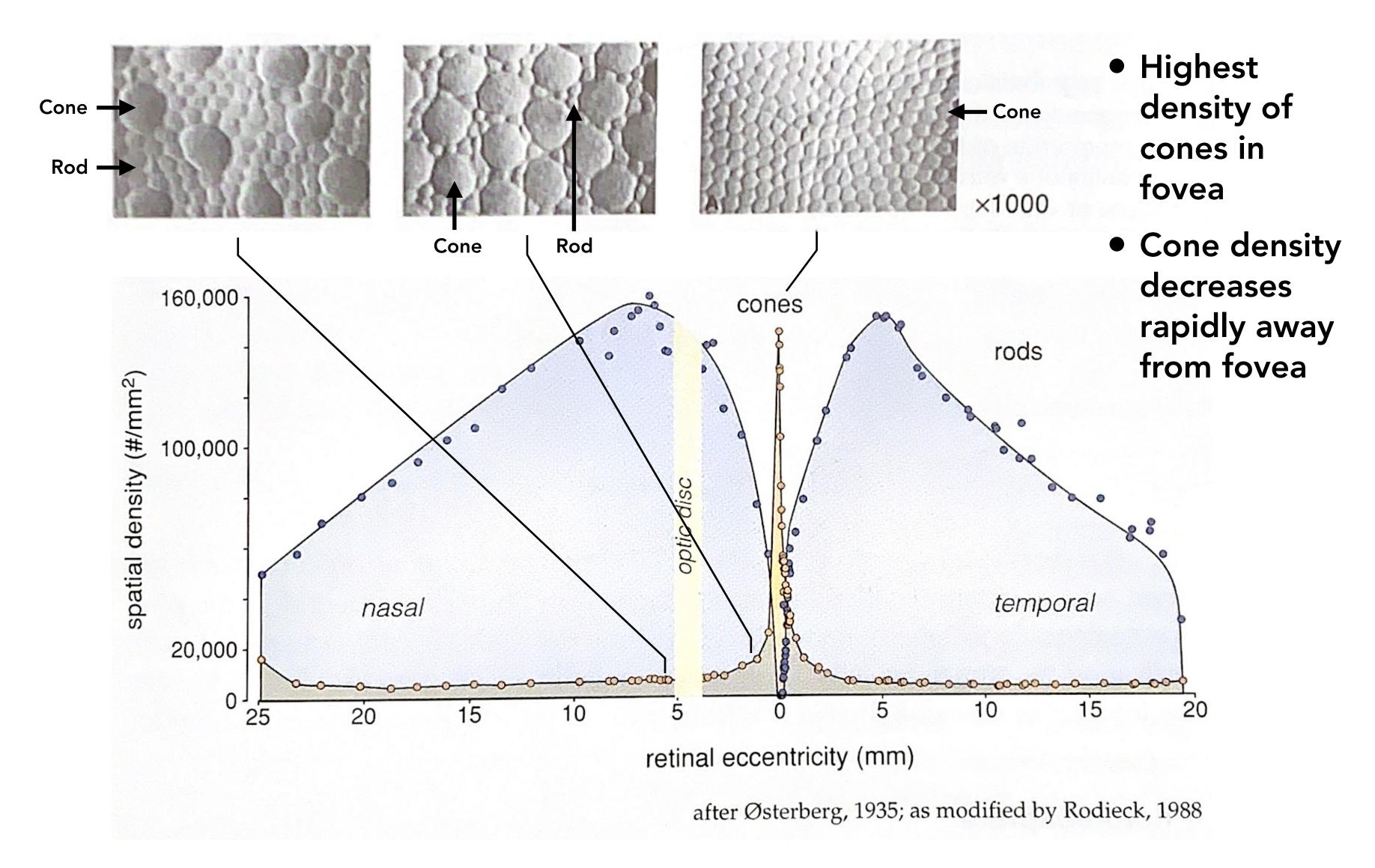
Human Visual Field of View



Human: ~160° view of field per eye (~200° overall) (Note: does not account for eye's ability to rotate in socket)

Slide credit: Gordon Wetzstein

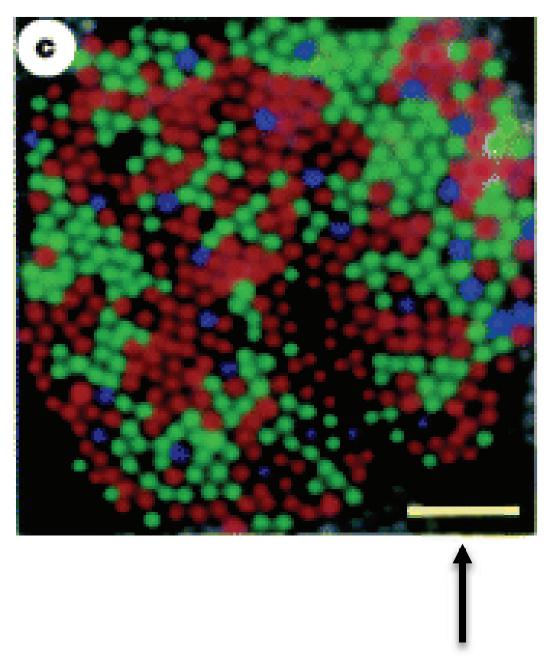
Recall: Photoreceptor Size and Distribution Across Retina



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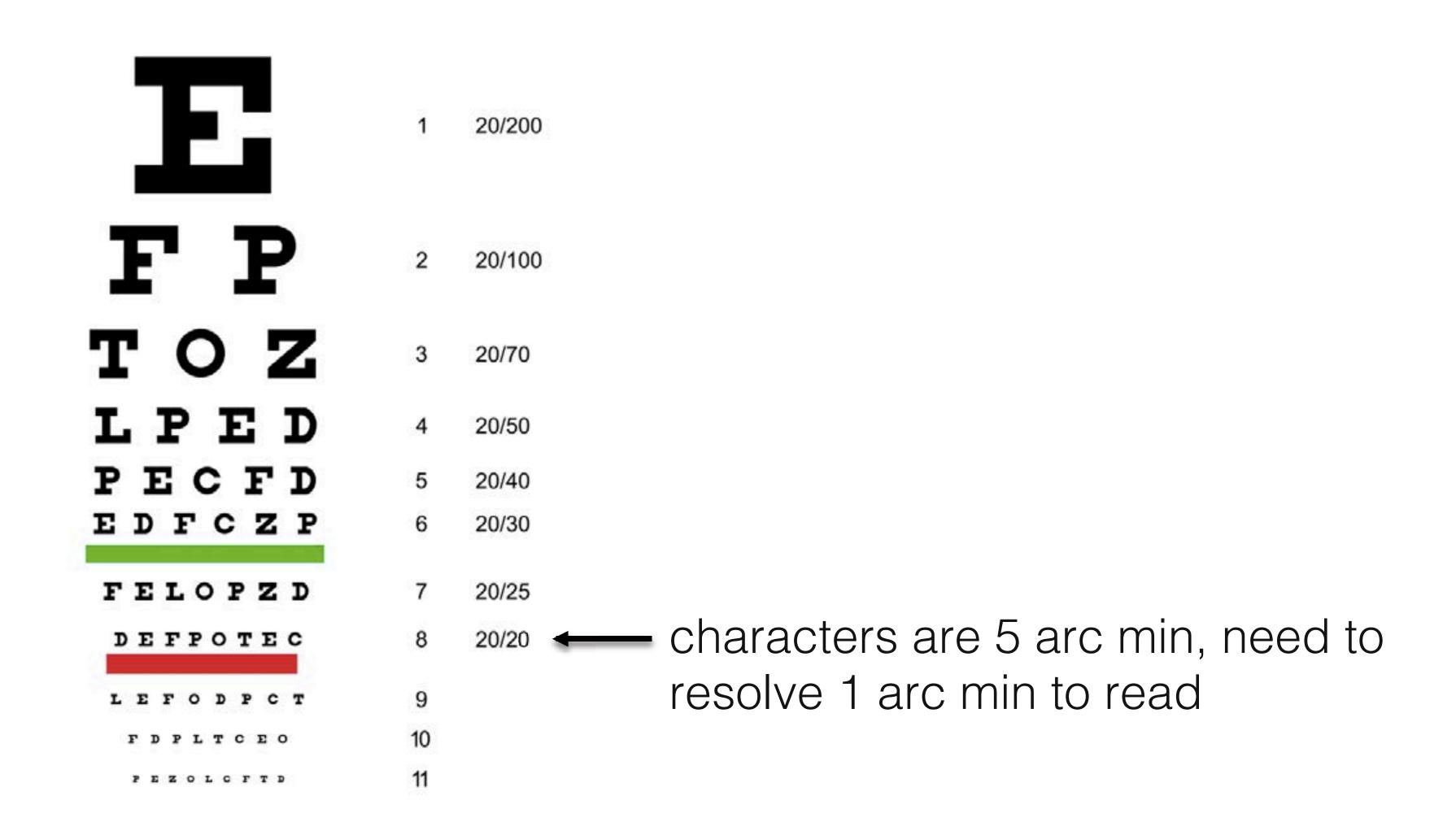
Visual Acuity

each photorecepter1 arc min (1/60 of a degree)



5 arcmin visual angle

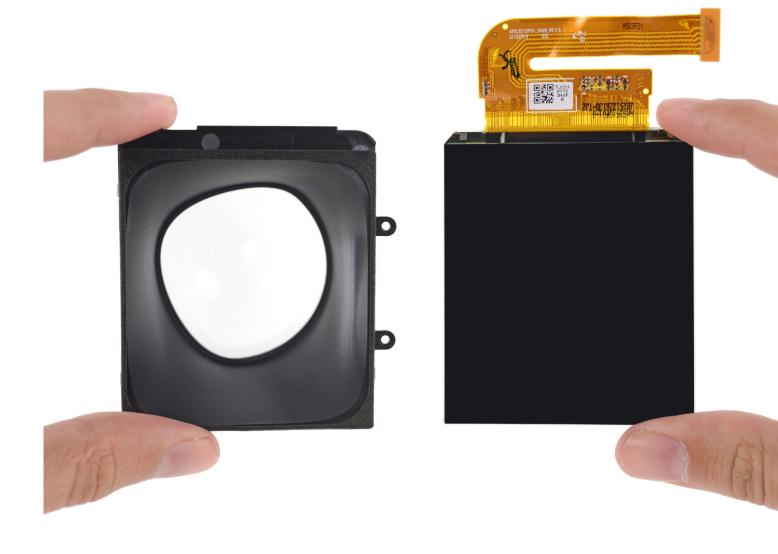
Visual Acuity



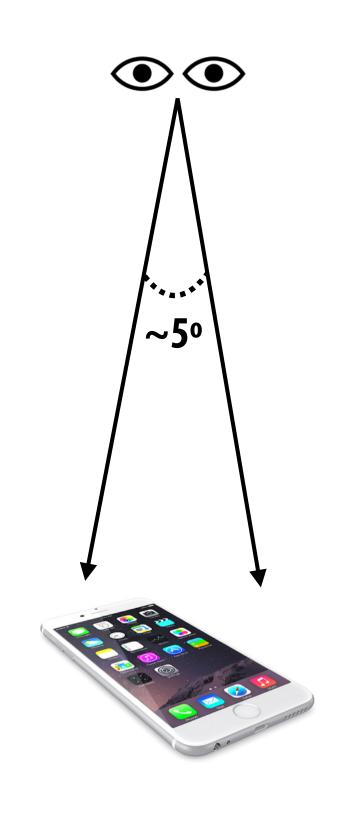
Current VR Headset Field of View and Resolution

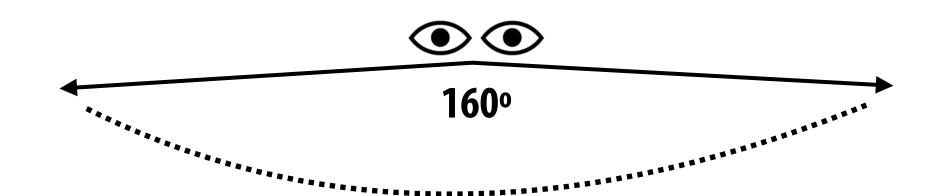
Example: HTC Vive Pro 2

- Field of view: approximately 100° per eye
 - Resolution: 2448 x 2448
 (6MP) pixel display
- About 24 pixels per degree (as opposed to ~60 samples for 20/20 vision)
- [Note: VR headsets exist up to 2880x2720 (7.8MP) now]



A VR Display at Human Visual Acuity





Human: ~160° view of field per eye (~200° overall) (Note: does not account for eye's ability to rotate in socket)

Future "retina" VR display:

~ 8K x 8K display per eye (50 ppd)

= 128 MPixel

iPhone 6: 4.7 in "retina" display: 1.3 MPixel 326 ppi → ~60 ppd Strongly suggests need for eye tracking and foveated rendering (eye can only perceive detail in 5° region about gaze point)

Display Requirements Derive From Human Perception

Example 3: Binocular Stereo and Eye Focus ("Accommodation")

Two Eyes: Two Views



Charles Wheatstone stereoscope, 1838

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Recall: Current VR HMD Optical Design



Image credit: ifixit.com

https://www.ifixit.com/Teardown/Oculus+Rift+CV1+Teardown/60612

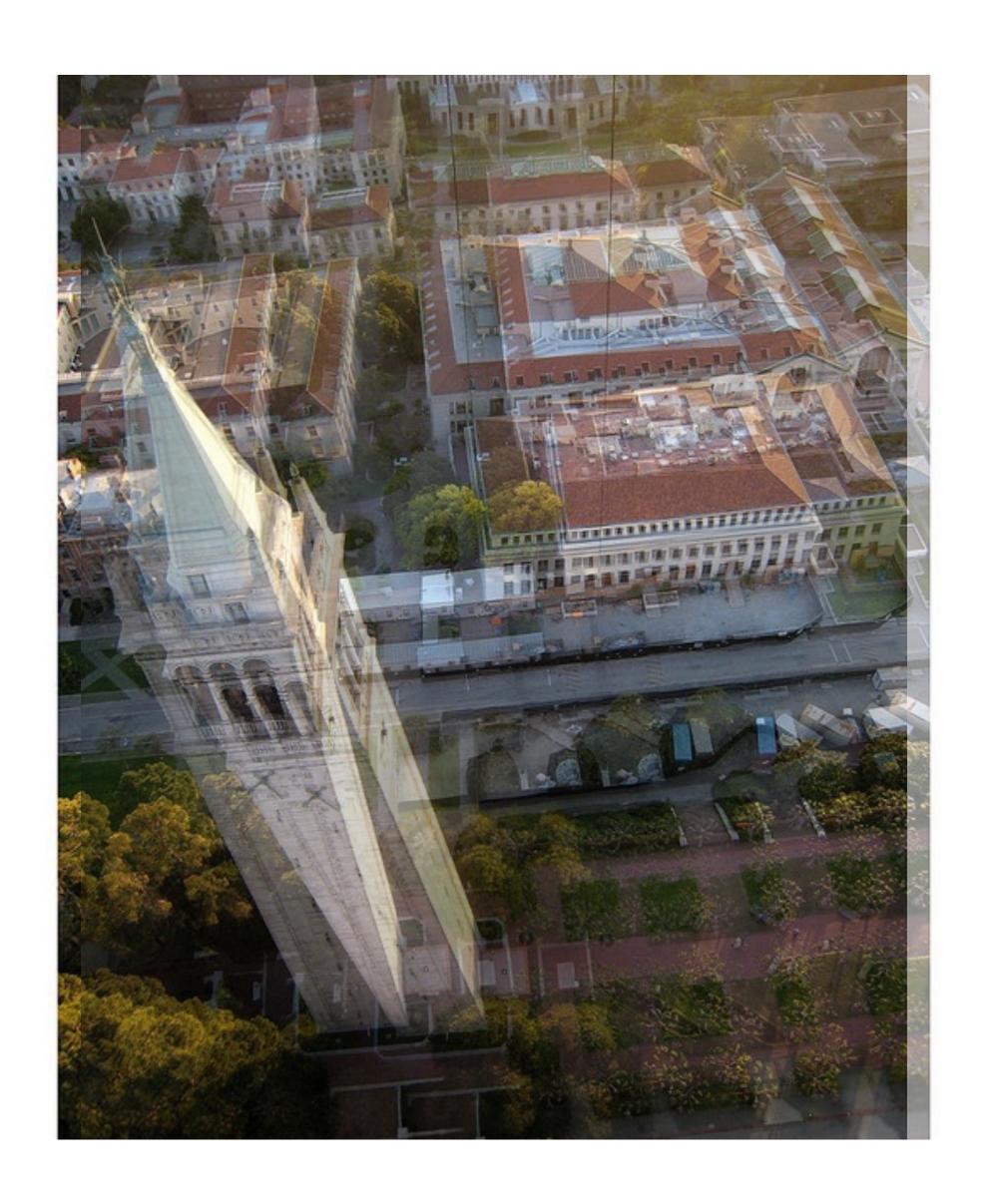
Stereo Vergence

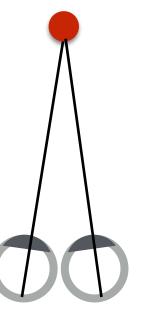


Left-eye perspective

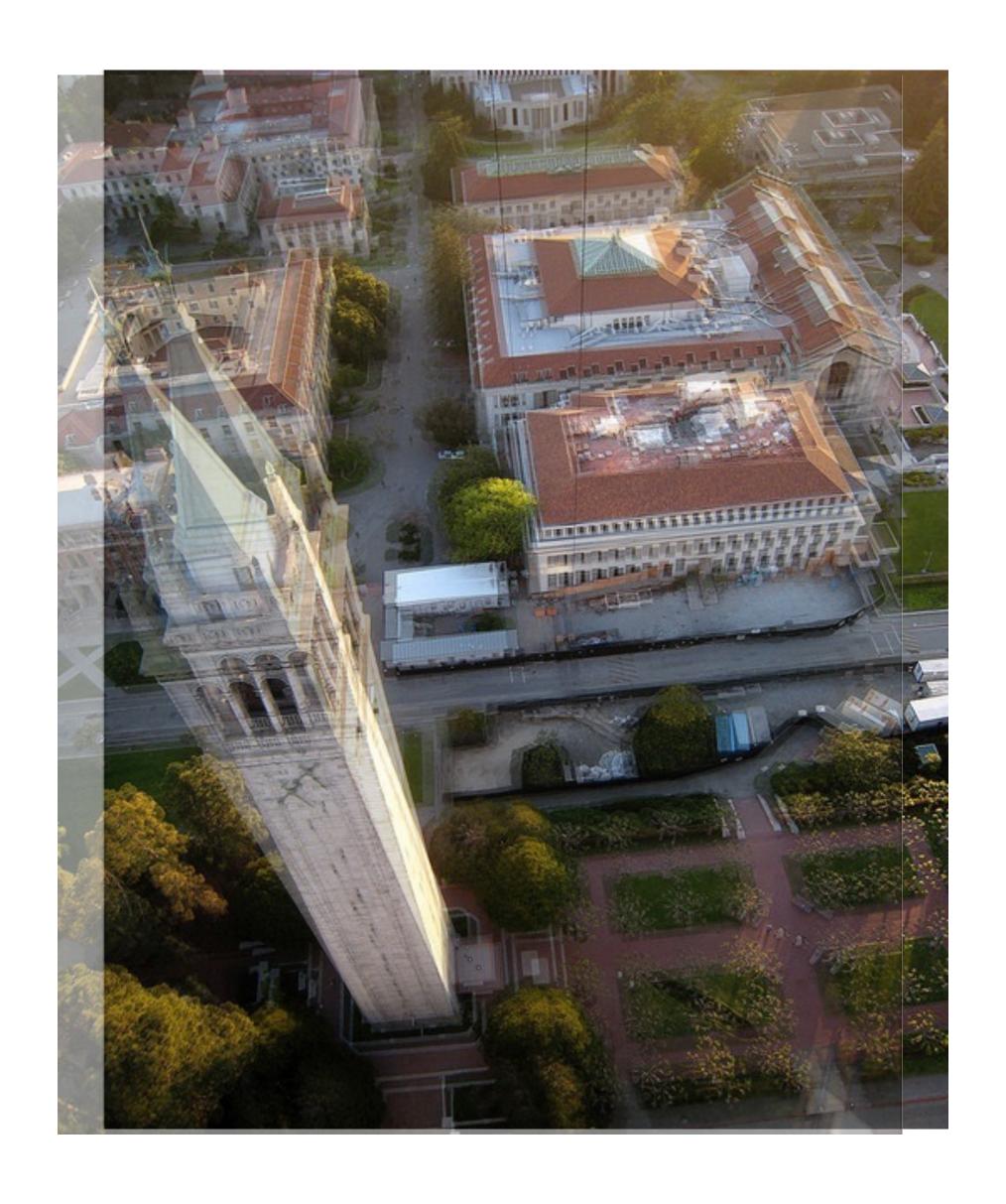
Right-eye perspective

Stereo Vergence





Stereo Vergence



Stereo

- Passive (no tracking of eyes)
- Present each eye with perspective view corresponding to that eye's location relative to the other eye
- Eyes will con(verge) by rotating physically in sockets in order to bring closer and further objects into physical alignment on retina

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Human Eye Muscles and Optical Controls

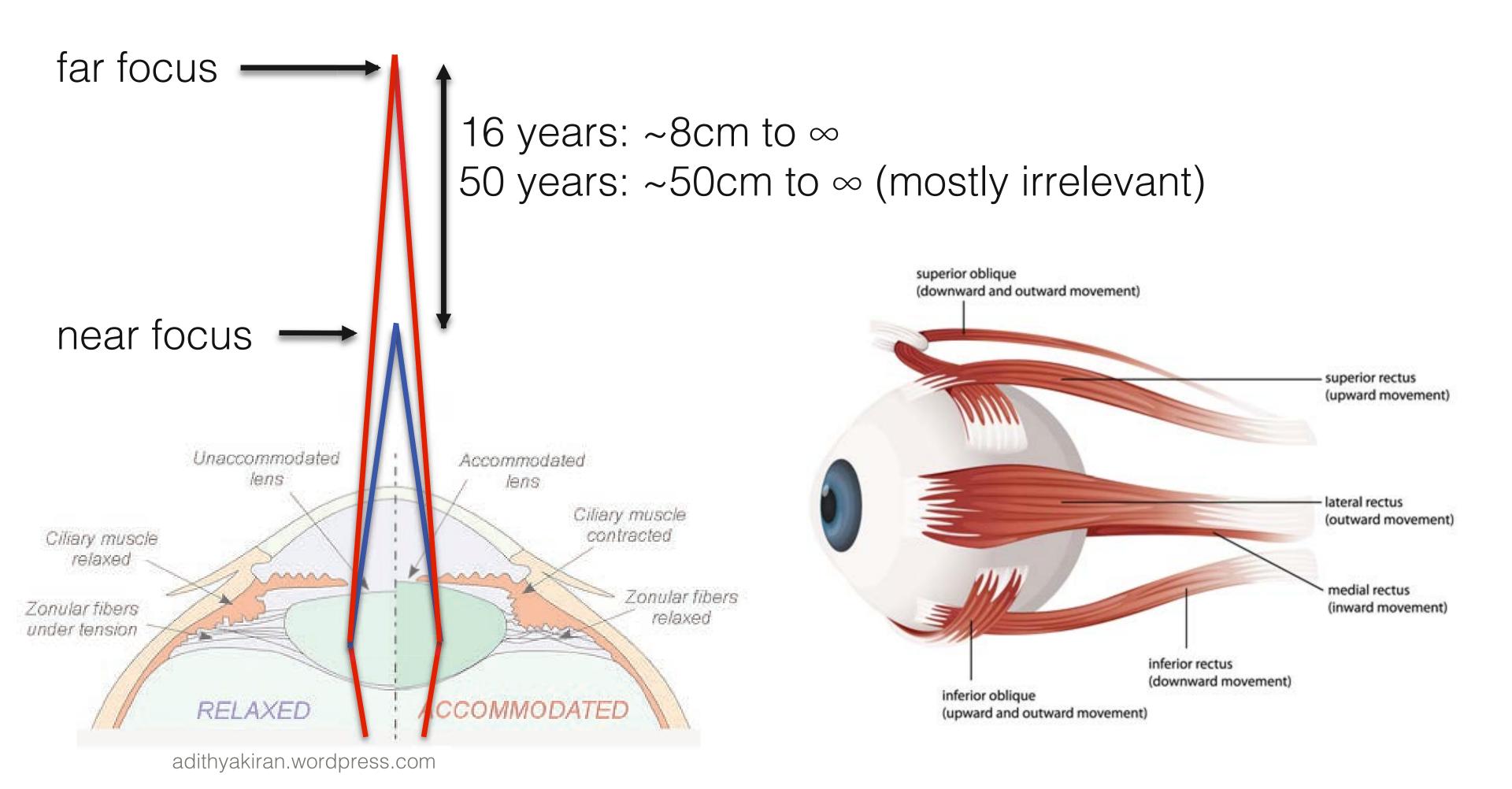
Stereopsis (Binocular) Focus Cues (Monocular) Oculomotor Cue extraocular muscles ciliary muscles relaxed contracted Accommodation Vergence Visual Cue

Retinal Blur

Slide credit: Gordon Wetzstein

Binocular Disparity

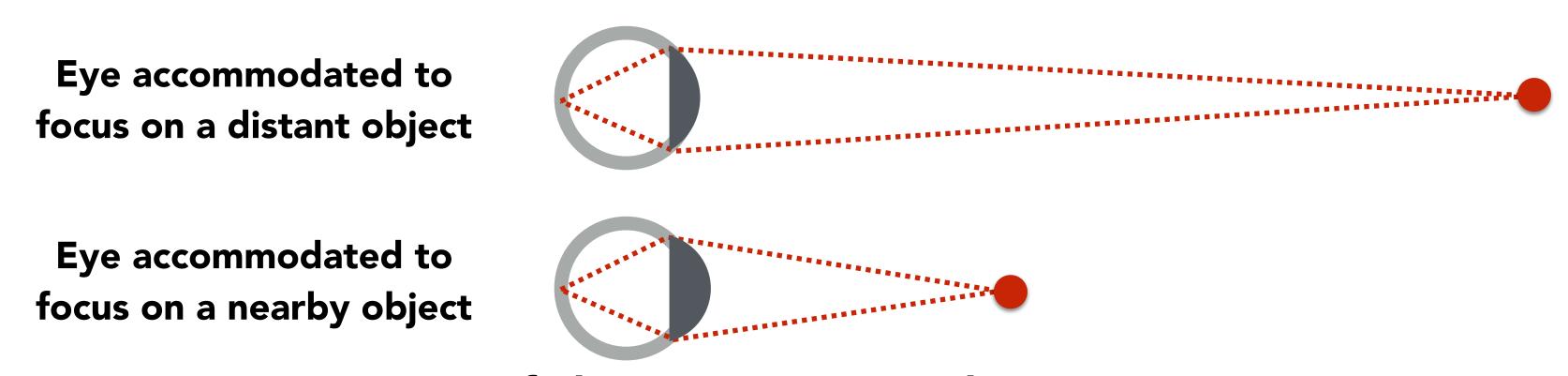
Human Eye Muscles and Optical Controls



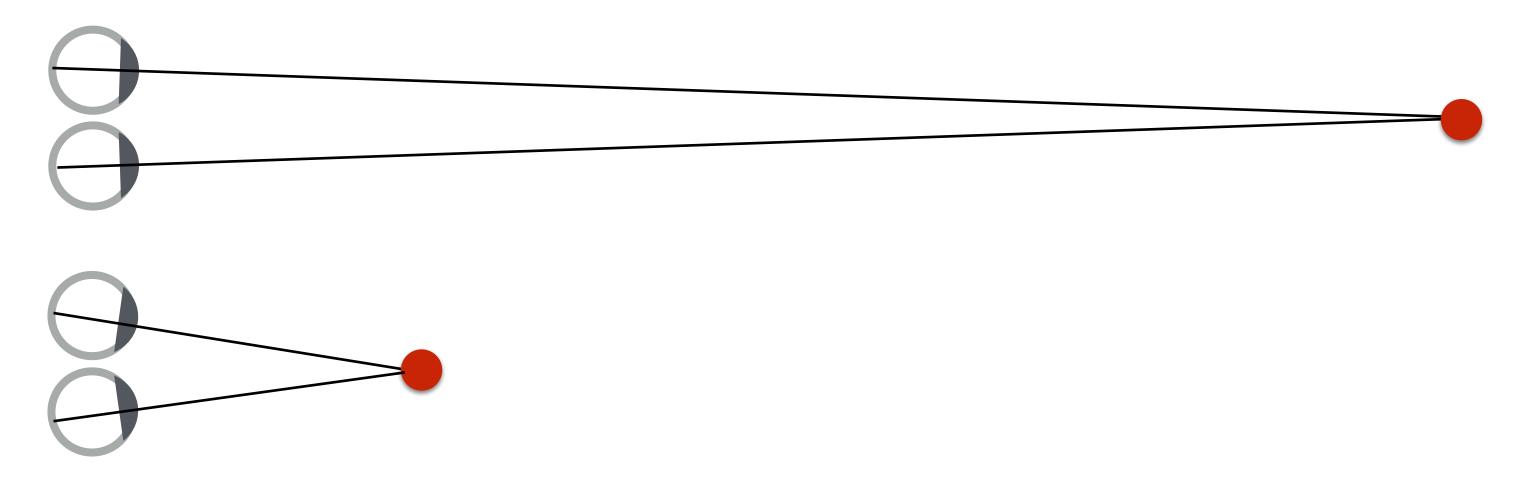
Slide credit: Gordon Wetzstein

Accommodation and Vergence

Accommodation: changing the optical power of the eye (lens) to focus at different distances



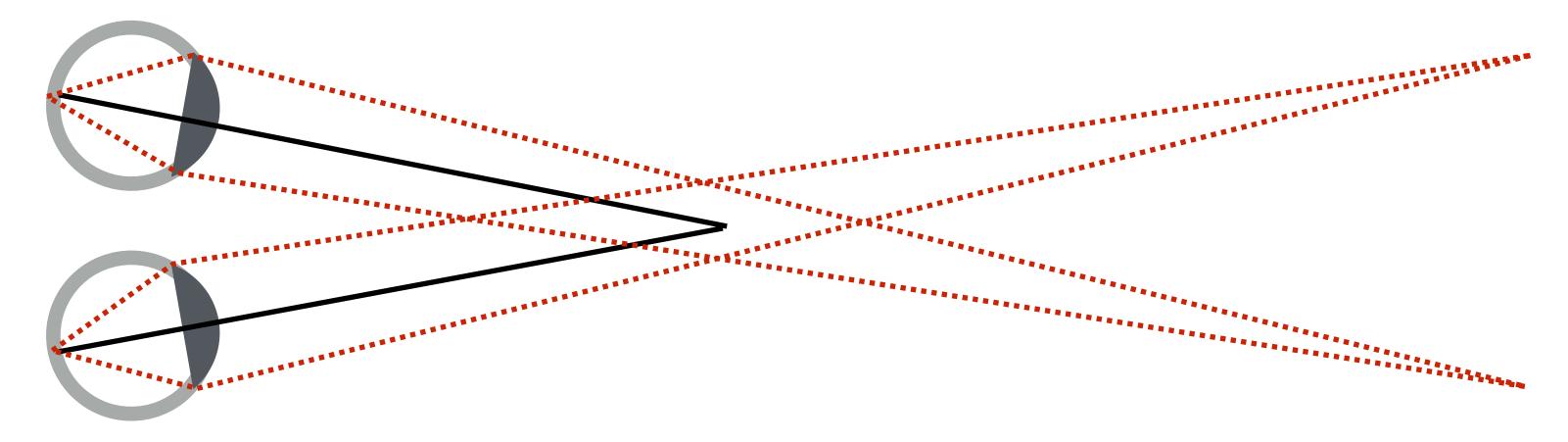
Vergence: rotation of the eye in its socket to ensure projection of object is centered on the retina



Accommodation – Vergence Conflict

Given design of current VR displays, consider what happens when objects are up-close to eye in virtual scene

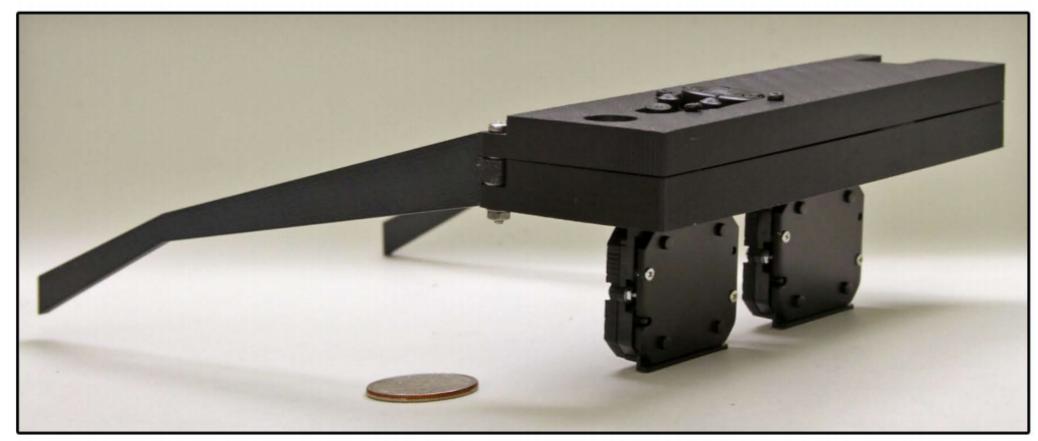
- Eyes must remain accommodated to far distance (otherwise image on screen won't be in focus)
- But eyes must converge in attempt to fuse stereoscopic images of object up close
- Brain receives conflicting depth clues... (discomfort, fatigue, nausea)

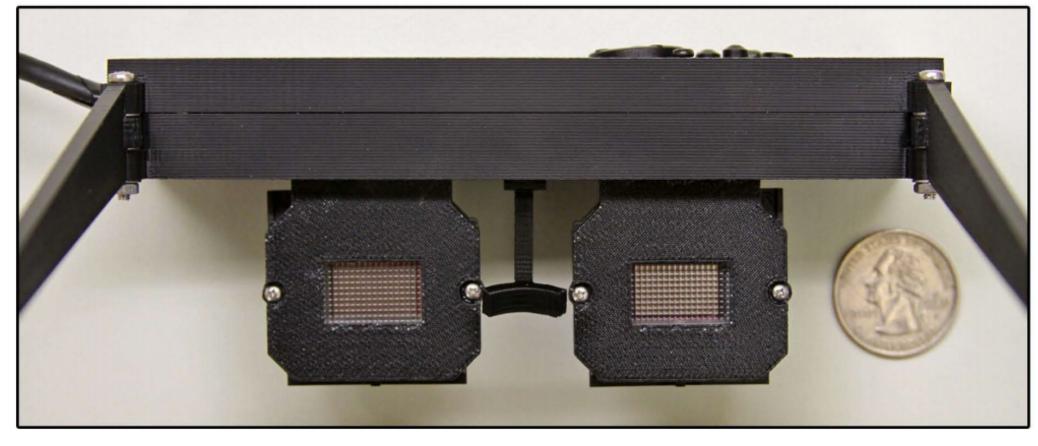


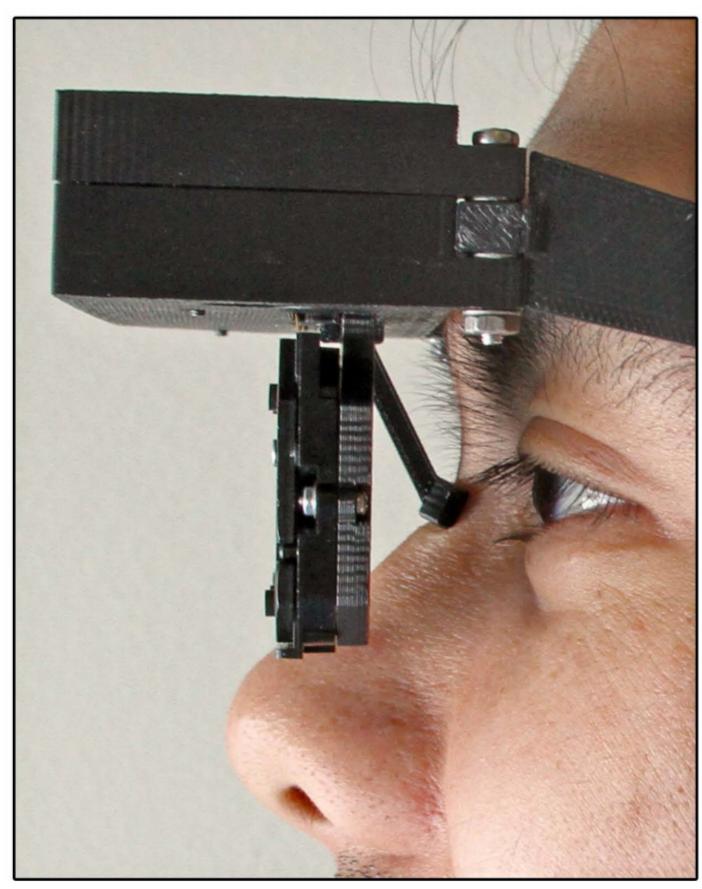
This problem stems from nature of display design. If you could just make a display that emits the light field that would be produced by a virtual scene, then you could avoid the accommodation - vergence conflict...

Aside: Research on Near-Eye Light Field Displays

Goal: recreate light field in front of eye







Lanman and Luebke, SIGGRAPH Asia 2013.

Display Requirements Derive From Human Perception

Example #4: Motion Parallax from Eye Motion

Google Cardboard: Tracking Using Headset Camera

Tracking uses gyro / rearfacing camera to estimate user's viewpoint

- 2D rotation tracking generally works well
- 3D positional tracking a challenge in general environments



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Environment-Supported Vision-Based Tracking?



Early VR test room at Valve, with markers positioned throughout environment

Oculus Rift IR LED Tracking System





Oculus Rift + IR LED sensor

Oculus Rift IR LED Tracking Hardware



Photo taken with IR-sensitive camera

https://www.ifixit.com/Teardown/Oculus+Rift+Constellation+Teardown/61128

Oculus Rift LED Tracking System (DK2)



Photo taken with IR-sensitive camera (IR LEDs not visible in real life)

Image credit: ifixit.com

Oculus Rift IR Camera IR filter (blocks visible spectrum) Camera lens **CMOS** sensor Note: silicon is sensitive to visible and IR wavelengths

https://www.ifixit.com/Teardown/Oculus+Rift+Constellation+Teardown/61128

Recall: Passive Optical Motion Capture







Retroflective markers attached to subject

IR illumination and cameras

- Markers on subject
- Positions by triangulation from multiple cameras
- 8+ cameras, 240 Hz, occlusions are difficult

Slide credit: Steve Marschner

Active Optical Motion Capture

- Each LED marker emits unique blinking pattern (ID)
- Reduce marker ambiguities / unintended swapping
- Have some lag to acquire marker IDs

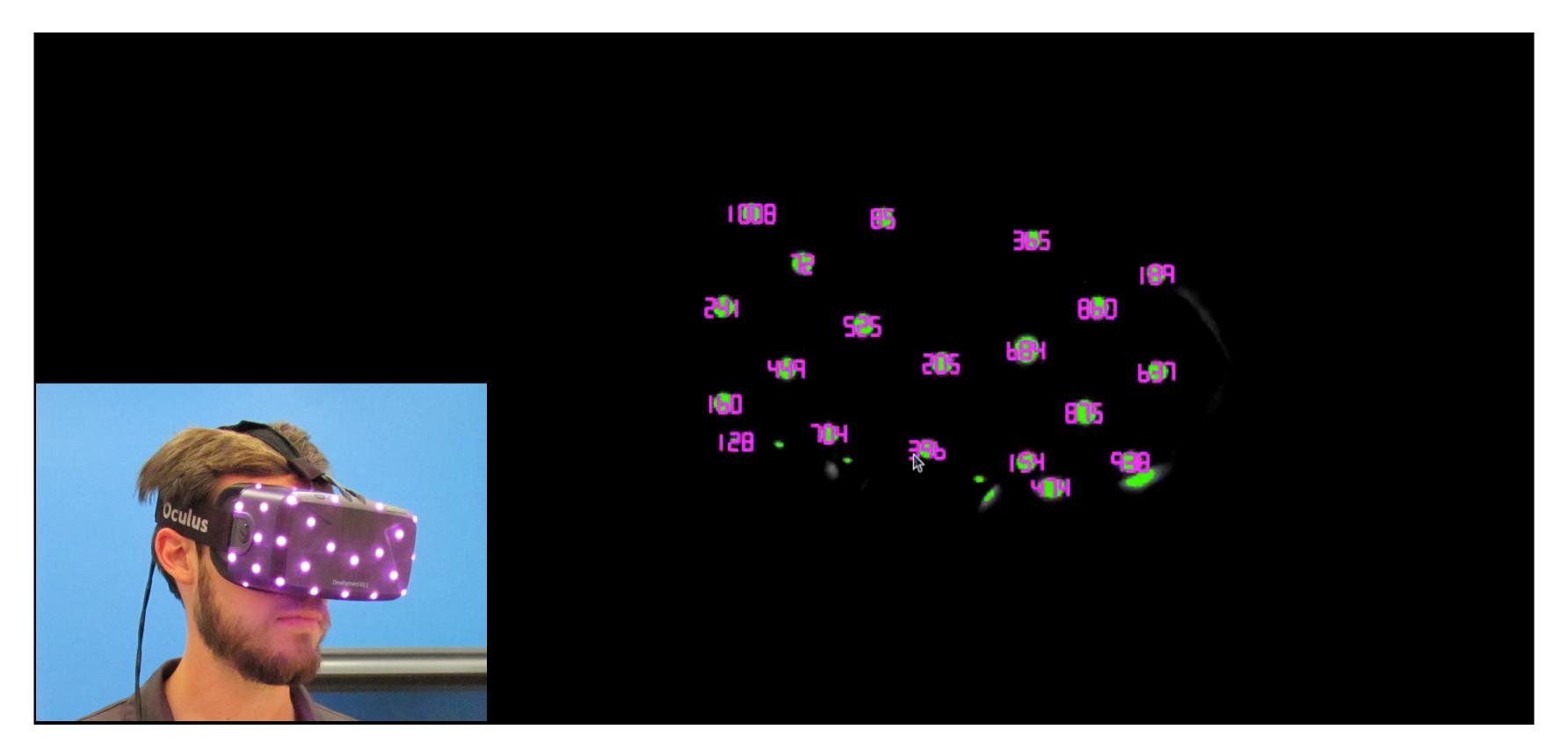


Phoenix Technology



Phase Space

Oculus Rift Uses Active Marker Motion Capture



Credit: Oliver Kreylos, https://www.youtube.com/watch?v=07Dt9Im34OI

- Motion capture: unknown shape, multiple cameras
- VR head tracking: known shape, single camera

6 DOF Head Pose Estimation

Head pose: 6 degrees of freedom (unknowns)

• 3D position and 3D rotation of headset (e.g. can represent as 4x4 matrix)

Inputs:

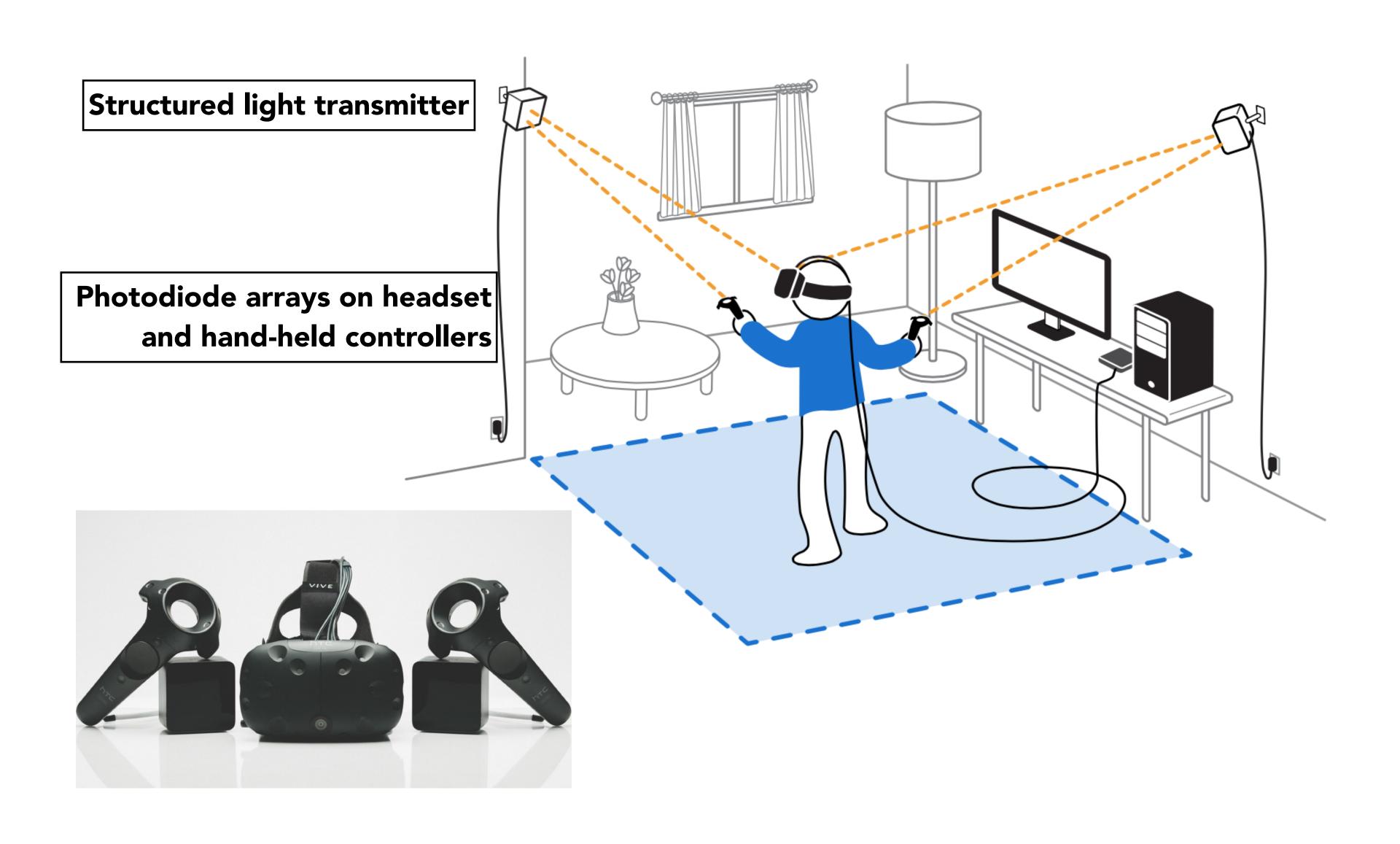
- Fixed: relative 3D position of markers on headset (e.g. can represent each marker offset as 4x4 matrix)
- Fixed: camera viewpoint (ignoring distortion, also a 4x4 projective mapping of 3D scene to 2D image)
- Each frame: 2D position of each headset marker in image

Pose calculation:

- Write down equations mapping each marker to image pixel location as a function of 6 degrees of freedom
- Solve for 6 degrees of freedom (e.g. least squares)

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HTC Vive Tracking System ("Lighthouse")

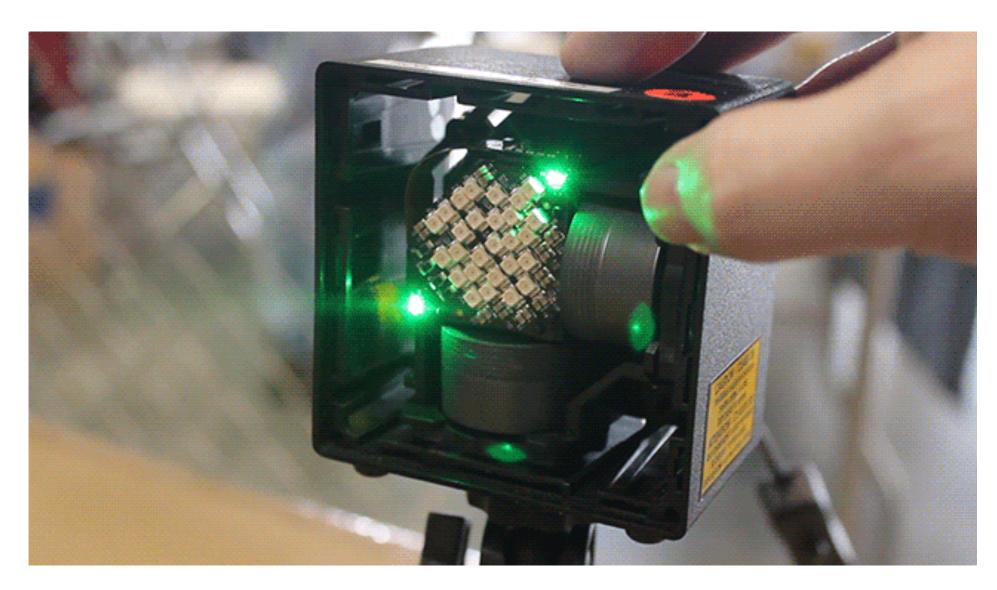


Vive Headset & Controllers Have Array of IR Photodiodes



(Prototype) Headset and controller are covered with IR photodiodes

HTC Vive Structured Light Emitter ("Lighthouse")





Light emitter contains array of LEDs (white) and two spinning wheels with lasers

Sequence of LED flash and laser sweeps provide structured lighting throughout room

Credit: Gizmodo: http://gizmodo.com/this-is-how-valve-s-amazing-lighthouse-tracking-technol-1705356768

HTC Vive Tracking System

For each frame, lighthouse does the following:

- LED pulse, followed by horizontal laser sweep
- LED pulse, followed by vertical laser sweep

Each photodiode on headset measures time offset between pulse and laser arrival

- Determines the x and y offset in the lighthouse's field of view
- In effect, obtain an image containing the 2D location of each photodiode in the world
 - (Can think of the lighthouse as a virtual "camera")

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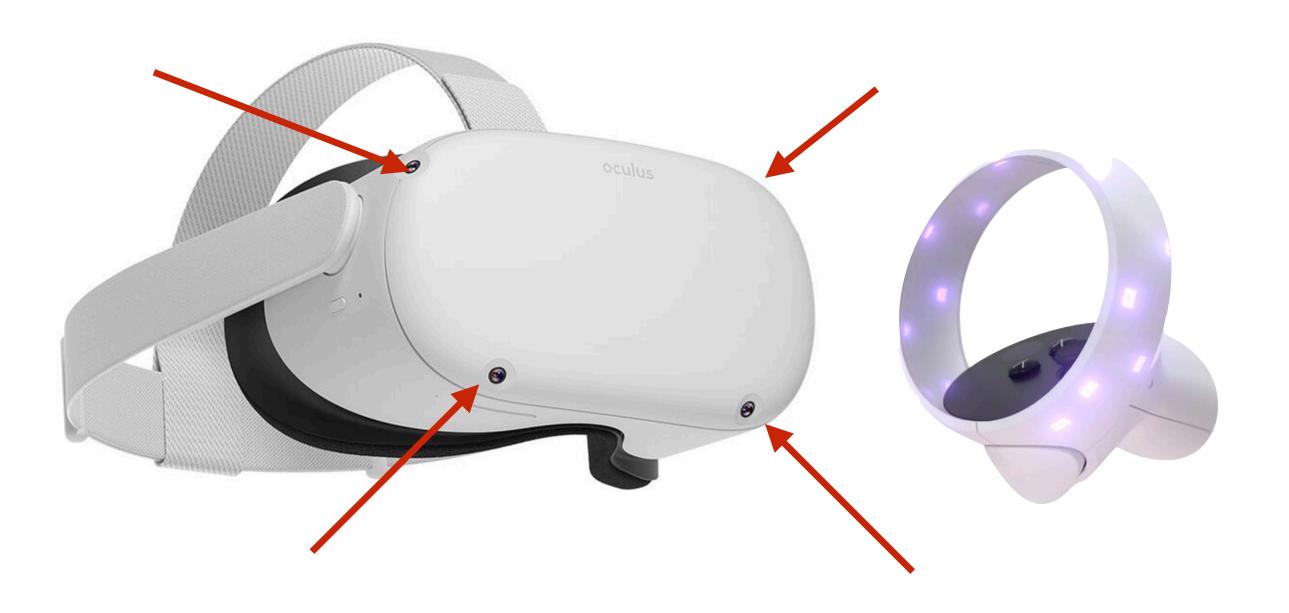
HTC Vive Tracking System ("Lighthouse")

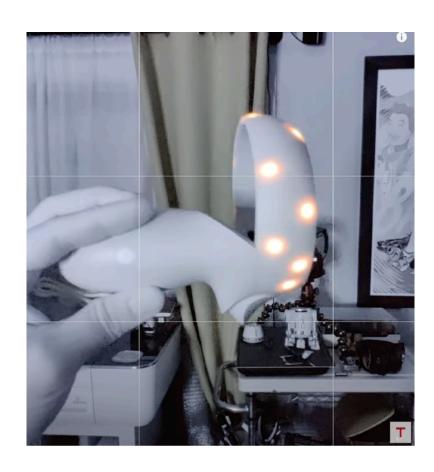


Credit: rvdm88 / youtube. https://www.youtube.com/watch?v=J54dotTt7k0

Many Modern Systems Use "Inside Out" Tracking

- Wide-angle cameras look outward from headset
- Use computer vision (SLAM) to estimate 3D structure of world and position/orientation of camera in the world
- These cameras also track the position/orientation of the controllers
 - Quest 2 controllers have 15 infrared LEDs to aid tracking





View of controller through infrared camera (credit Adam Savage's Testbed)

CS184/284A Slide credit: Kayvon Fatahalian

Ren Ng

Tracking Summary

Looked at a few tracking methods

- Camera on headset + computer vision + gyro
- External camera + marker array on headset
- External structured light + sensor array on headset
- "Inside out" tracking

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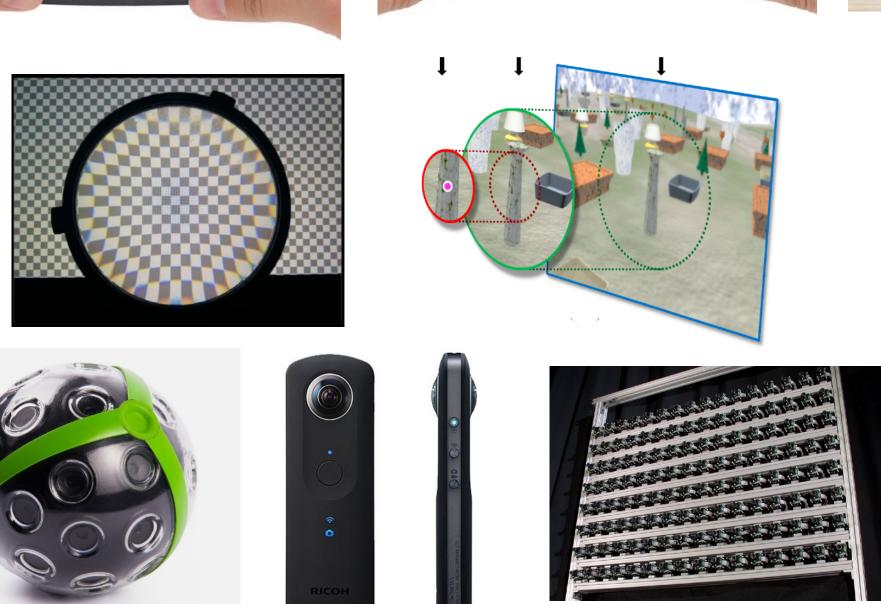
Overview of VR Topics

VR Displays



VR Rendering

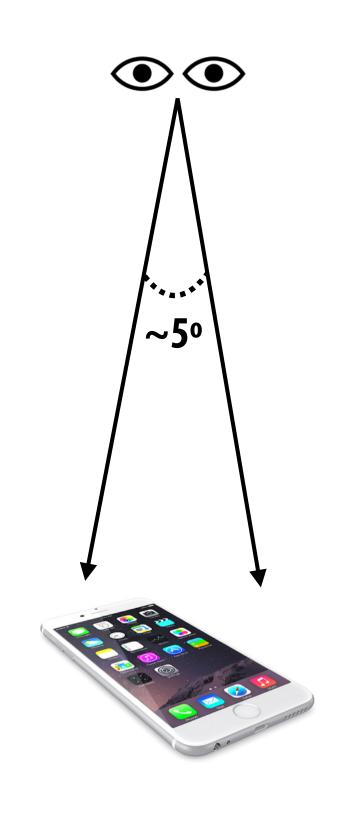


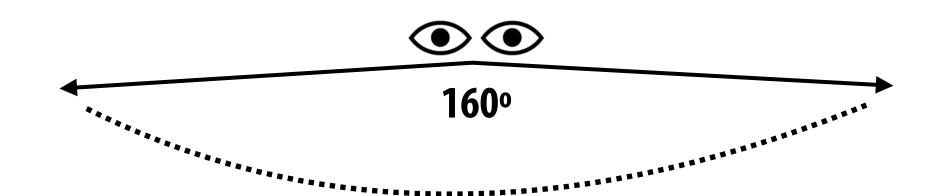


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Rendering Latency in VR

A VR Display at Human Visual Acuity





Human: ~160° view of field per eye (~200° overall) (Note: does not account for eye's ability to rotate in socket)

Future "retina" VR display:

~ 8K x 8K display per eye (50 ppd)

= 128 MPixel

iPhone 6: 4.7 in "retina" display: 1.3 MPixel 326 ppi → ~60 ppd Strongly suggests need for eye tracking and foveated rendering (eye can only perceive detail in 5° region about gaze point)

Latency Requirements in VR Are Challenging

The goal of a VR graphics system is to achieve "presence", tricking the brain into thinking what it is seeing is real

Achieving presence requires an exceptionally low-latency system

- What you see must change when you move your head!
- End-to-end latency: time from moving your head to the time new photons hit your eyes
 - Measure user's head movement
 - Update scene/camera position
 - Render new image
 - Transfer image to headset, then transfer to display in headset
 - Actually emit light from display (photons hit user's eyes)
- Latency goal of VR: 10-25 ms
 - Requires exceptionally low-latency head tracking
 - Requires exceptionally low-latency rendering and display

Thought Experiment: Effect of Latency

Consider 2,000 x 2,000 display spanning 100° field of view

20 pixels per degree

Assume:

- You move your head 90° in 1 second (only modest speed)
- End-to-end latency of system is a slow 33 ms (1/30 sec)

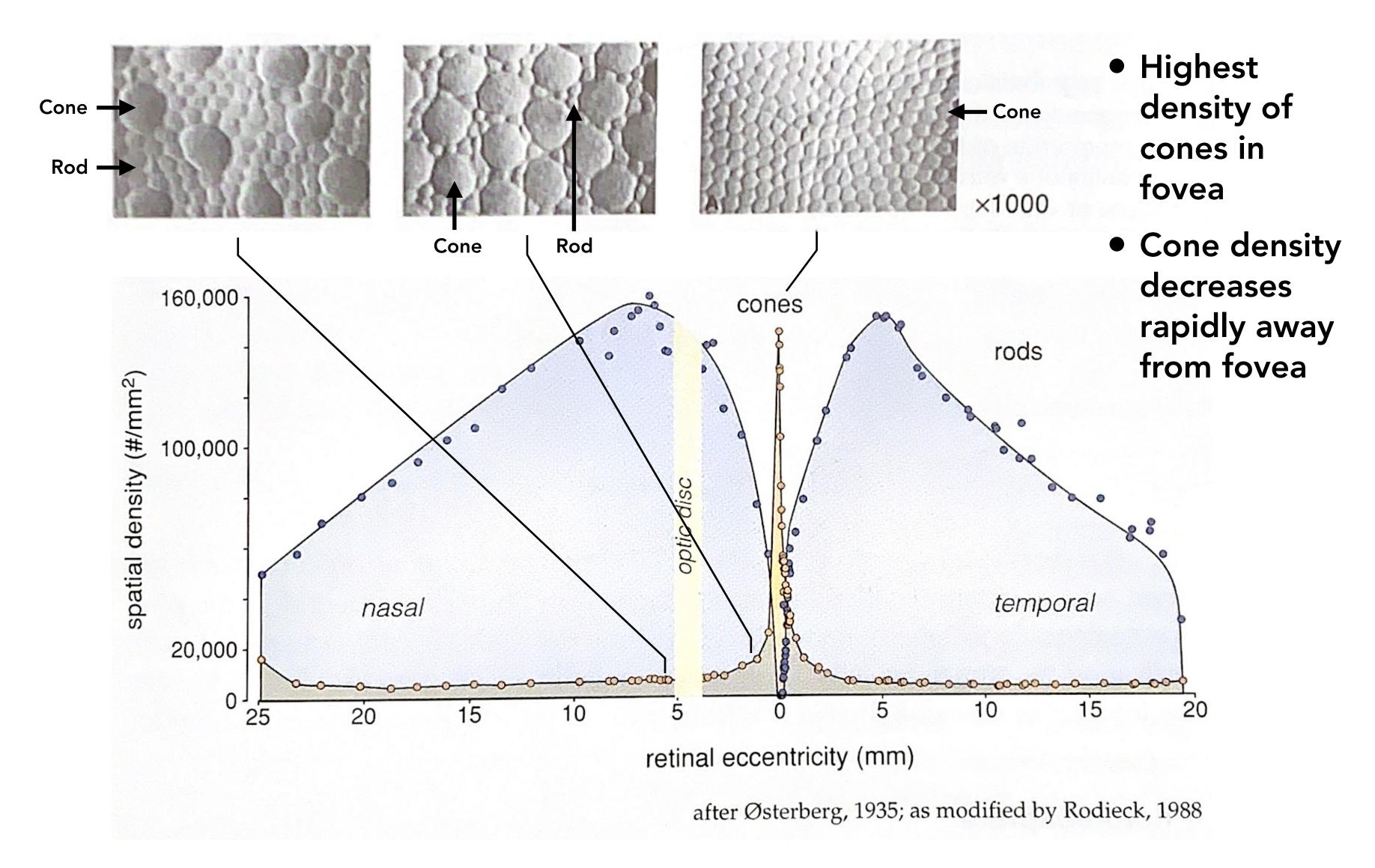
Result:

 Displayed pixels are off by 3.0° ~ 60 pixels from where they would be in an ideal system with 0 latency

Example credit: Michael Abrash

Rendering Challenge: Low Latency and High Resolution Require High Rendering Speed

Recall: Photoreceptor Size and Distribution Across Retina



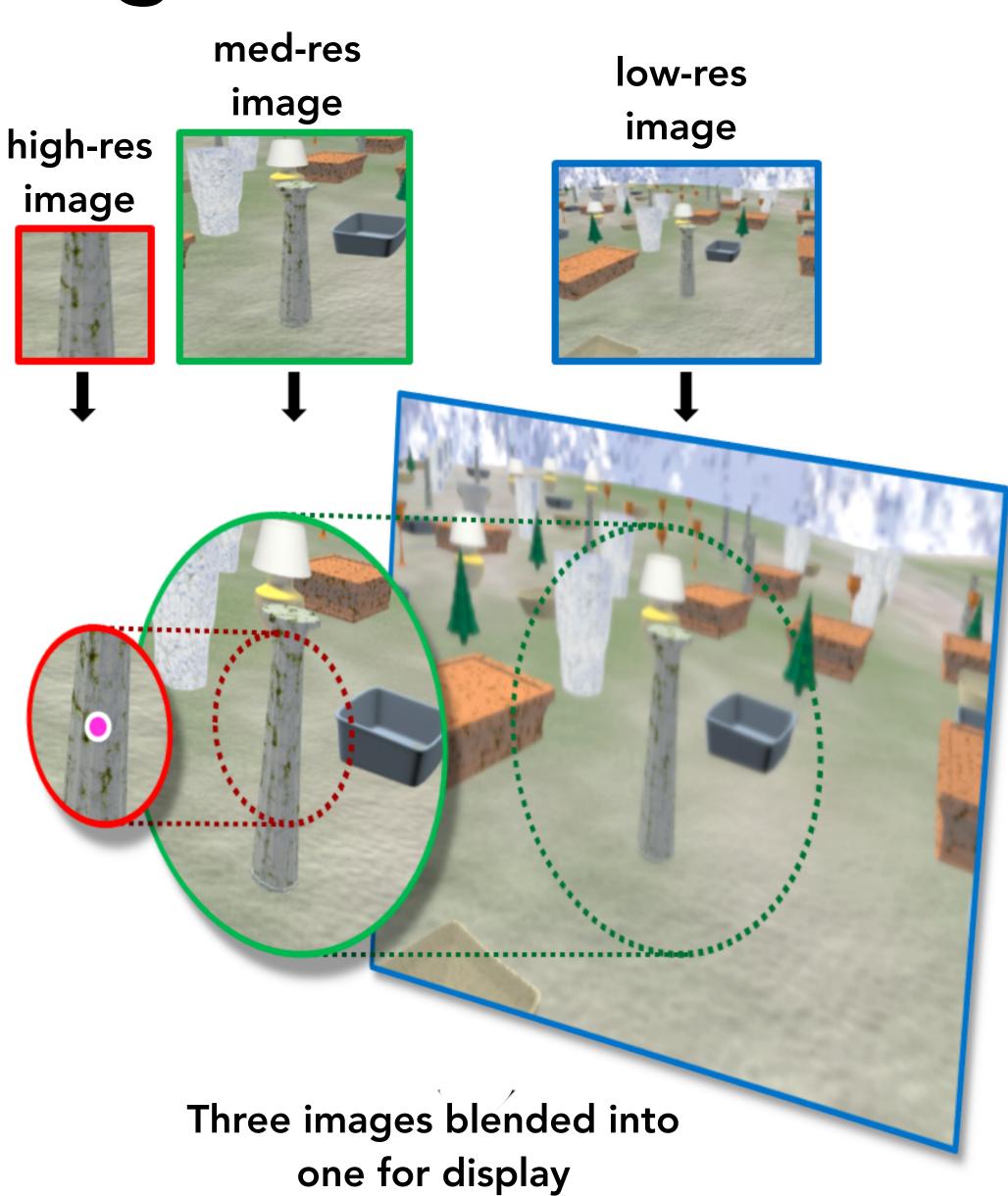
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Foveated Rendering

Idea: track user's gaze, render with increasingly lower resolution farther away from gaze point

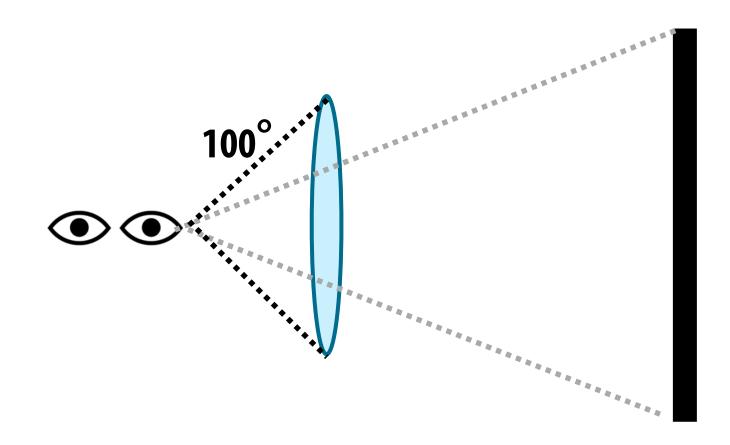
VR headset with eye tracker: HTC Vive Pro Eye



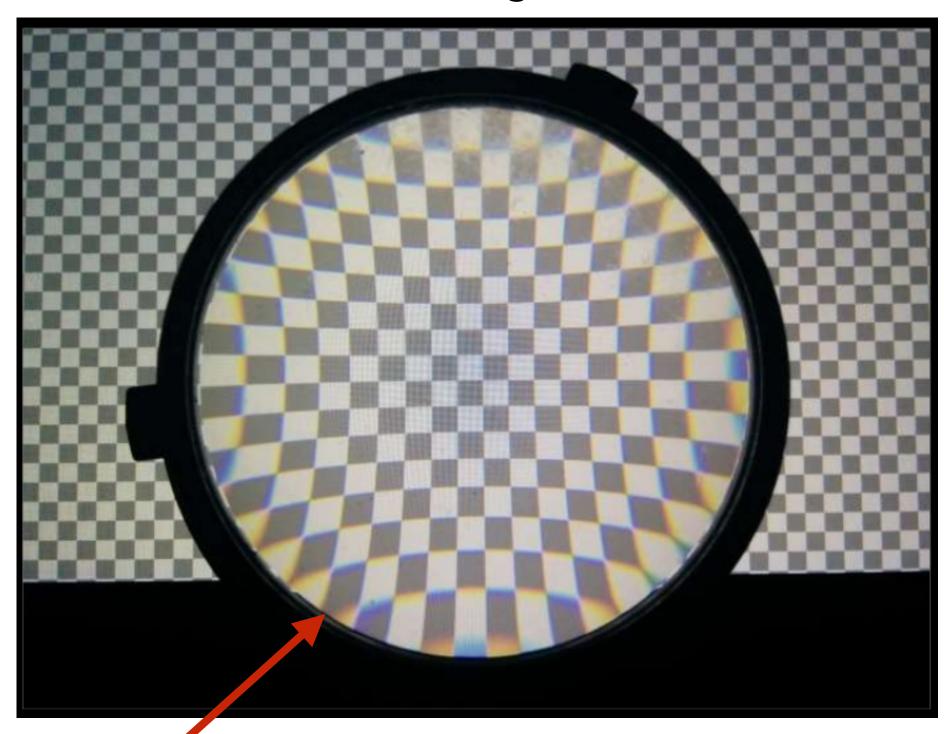


Rendering Challenge: Optical Distortion in VR Headset Viewing

Requirement: Wide Field of View



View of checkerboard through Oculus Rift (DK2) lens

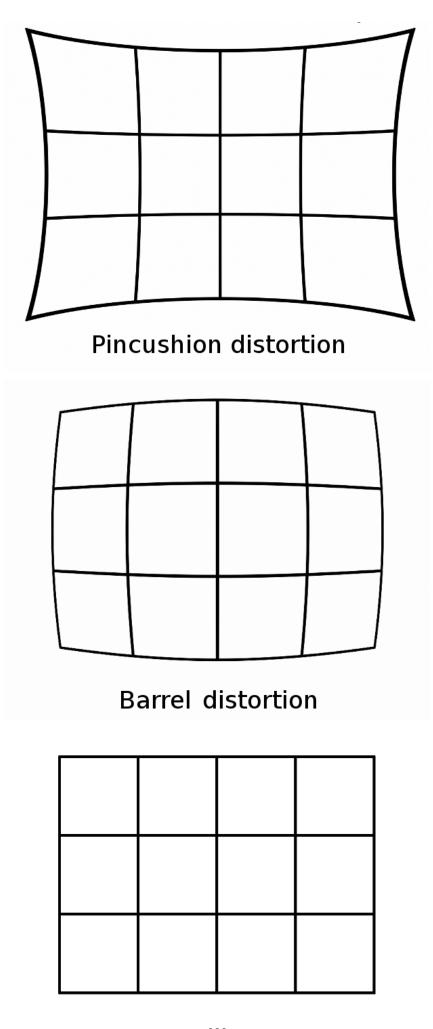


Lens introduces distortion

- Pincushion distortion
- Chromatic aberration (different wavelengths of light refract by different amount)

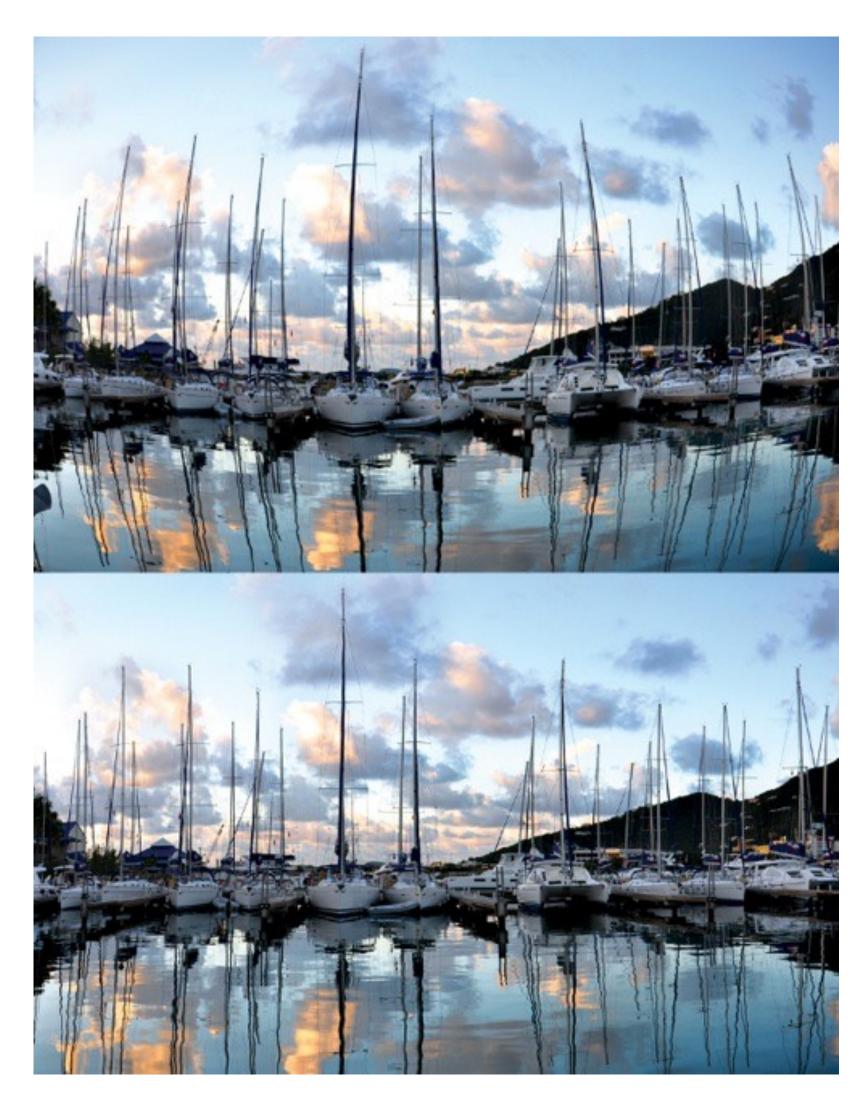
Icon credit: Eyes designed by SuperAtic LABS from the thenounproject.com Image credit: Cass Everitt

Software Correction of Lens Distortion in Photography



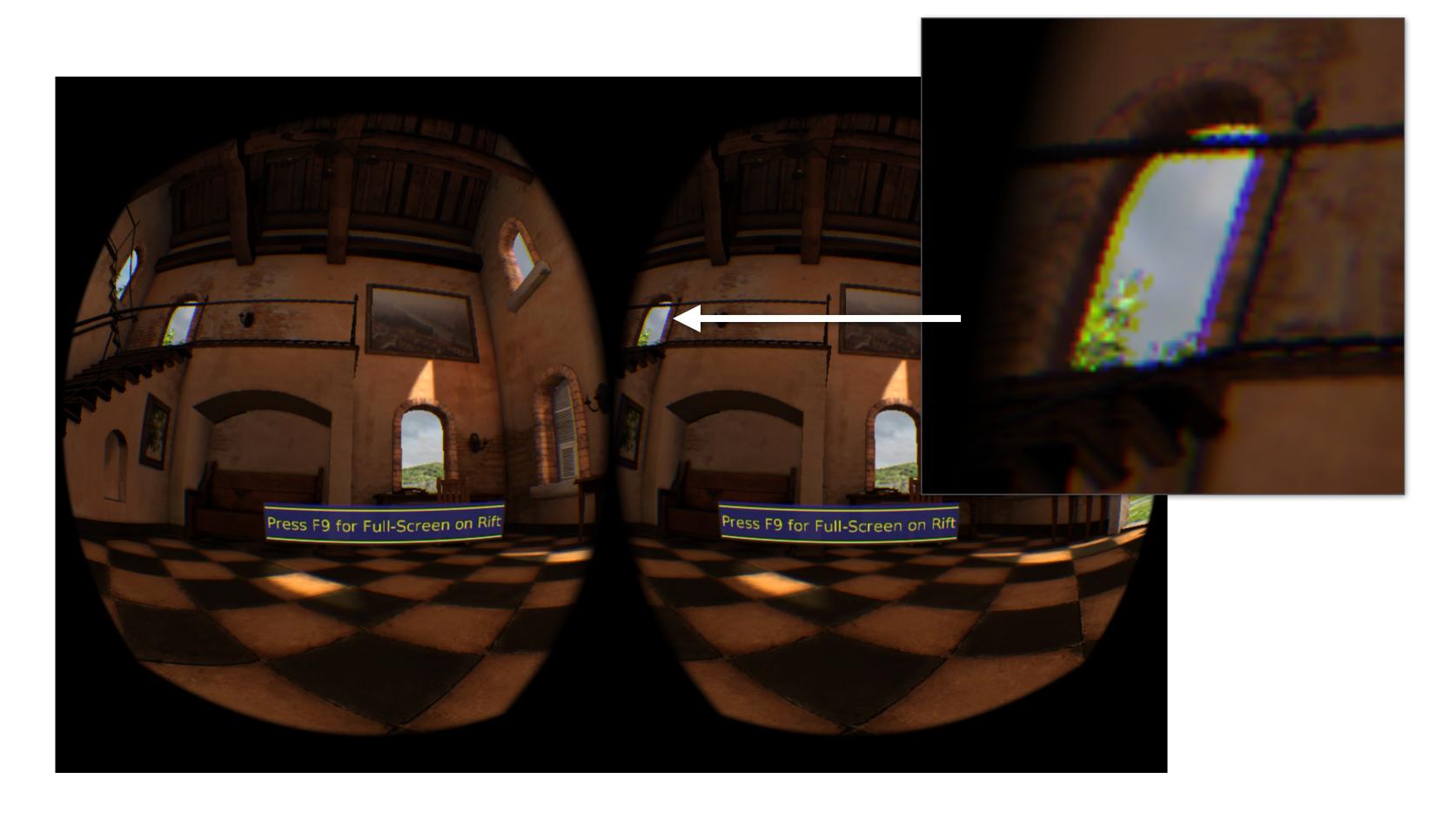


m43photo.blogspot.com



Credit: The Photoshop Creative Team http://blog.photoshopcreative.co.uk

Software Compensation of Lens Distortion in VR Rendering



Step 1: Render scene using traditional graphics pipeline at full resolution for each eye

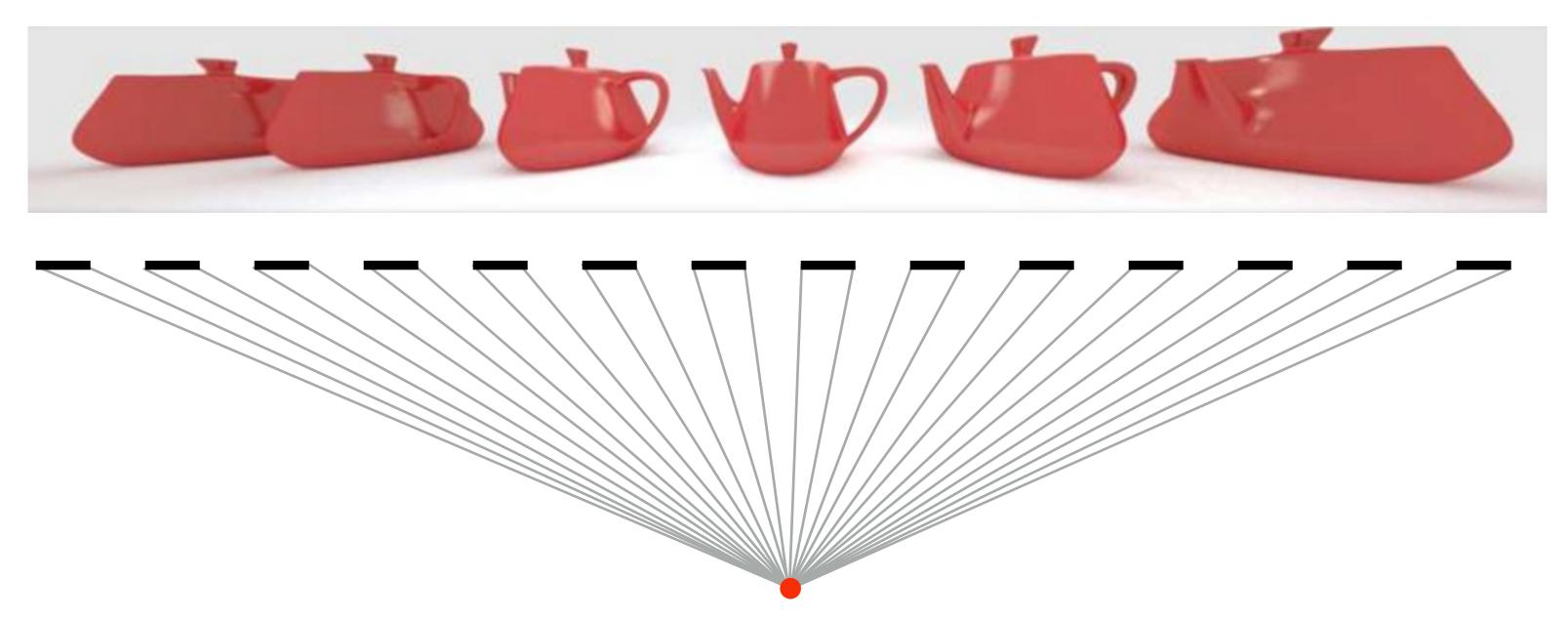
Step 2: Warp images in manner that scene appears correct after physical lens distortion (Can use separate distortions to R, G, B to approximately correct chromatic aberration)

Image credit: Oculus VR developer guide

Related Challenge: Rendering via Planar Projection

Recall: rasterization-based graphics is based on perspective projection to plane

- Distorts image under high FOV, as needed in VR rendering
- Recall: VR rendering spans wide FOV



Pixels span larger angle in center of image (lowest angular resolution in center)

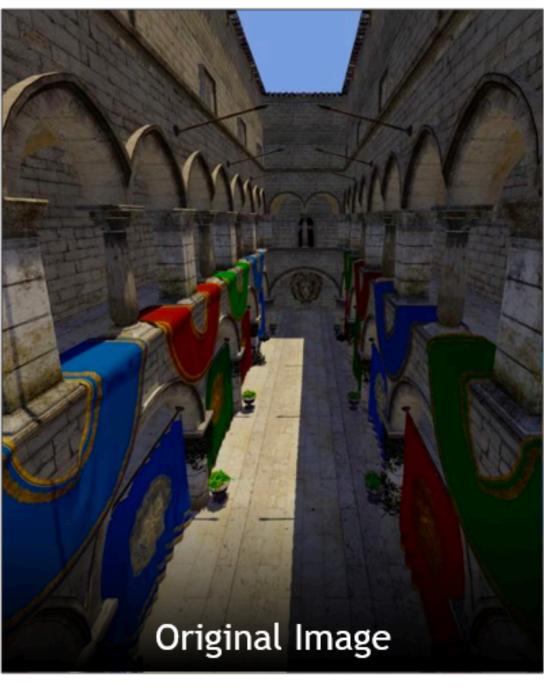
Potential solution space: curved displays, ray casting to achieve uniform angular resolution, rendering with piecewise linear projection plane (different plane per tile of screen)

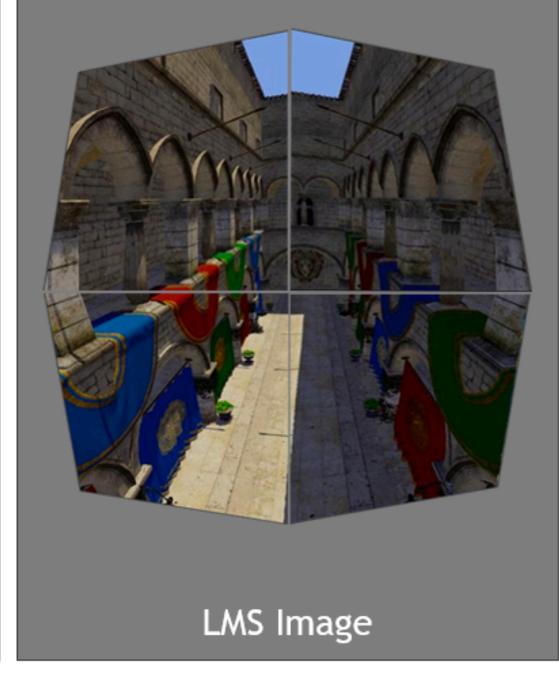
Image credit: Cass Everitt

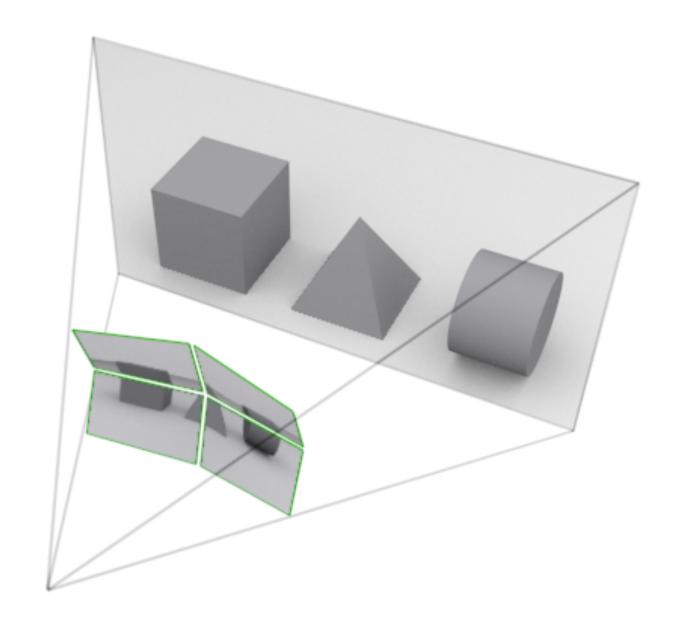
A Recent Implementation: Lens Matched Shading

Render scene with four viewports, each has different projection matrix

"Compresses" scene in the periphery (fewer samples), while not affecting scene near center of field of view





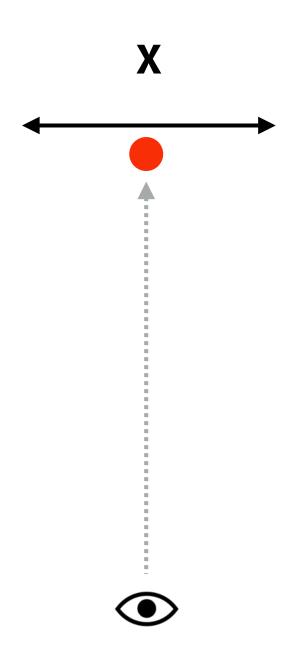


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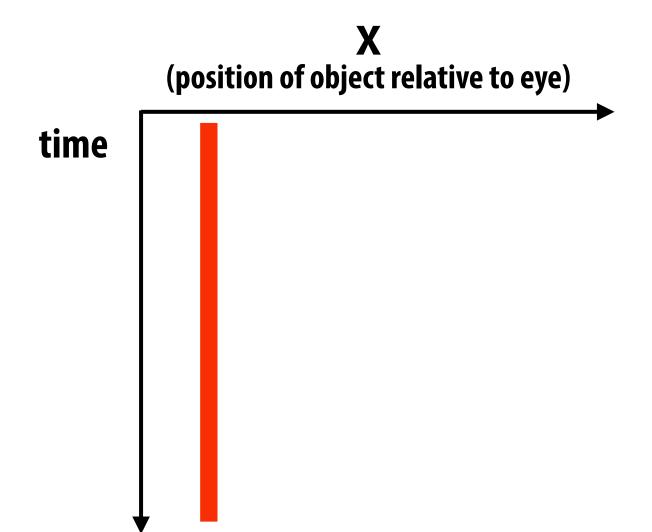
Slide credit: Kayvon Fatahalian

Rendering Challenge: Eye Motion And Finite Rendering Rate

Consider Finite VR Display Refresh Rate

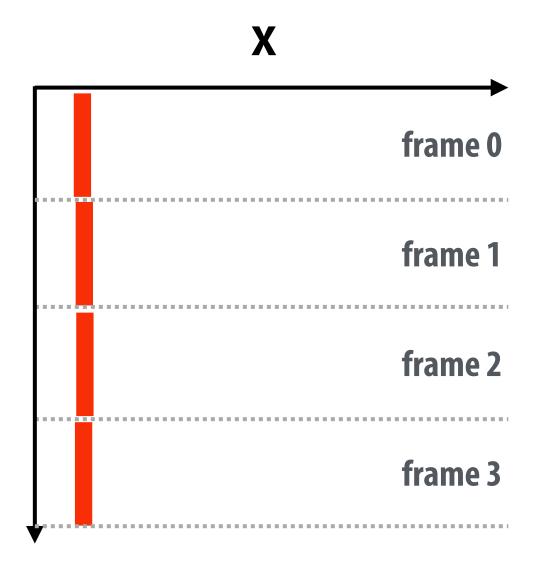


Reality (continuous)



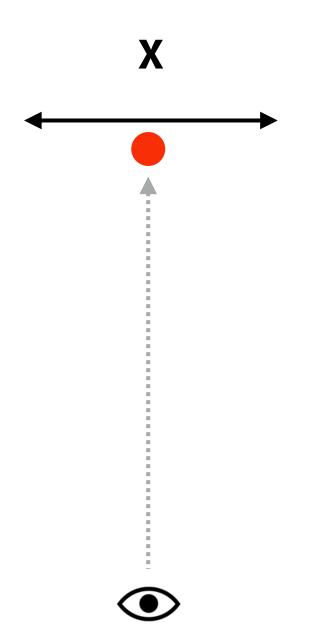
- Red object fixed;
- Eye gaze fixed

VR (discrete display refresh)

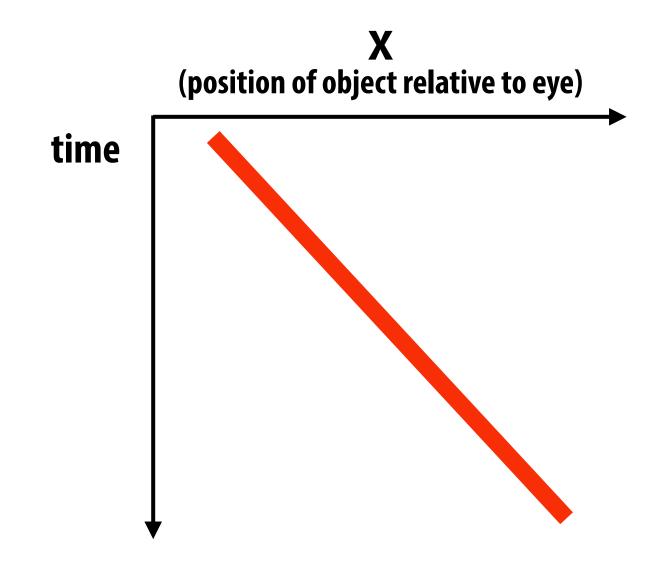


 Light from display (light updates every frame)

Case 2: Object Moving Relative to Eye

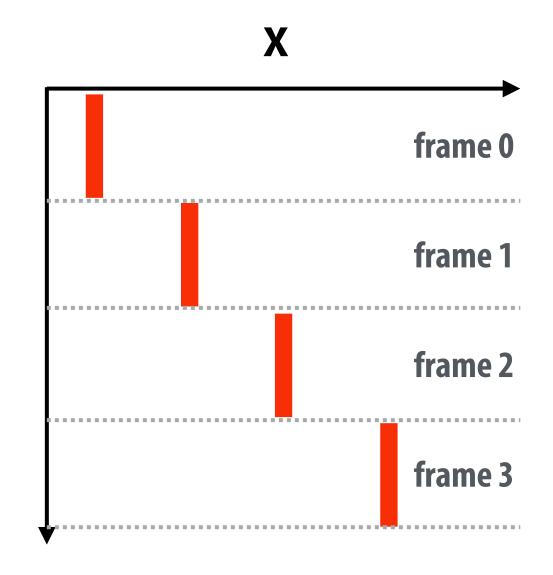


Reality (continuous)



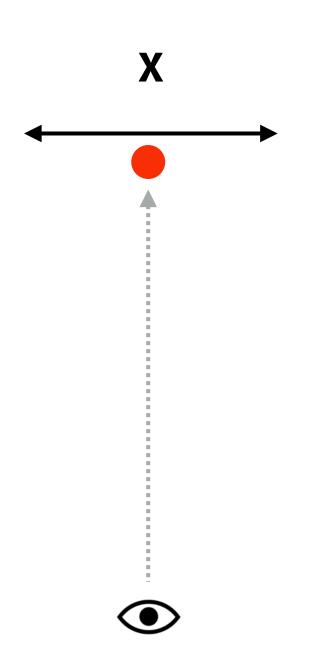
- Red object moving left to right;
- Eye gaze fixed

VR (discrete display refresh)

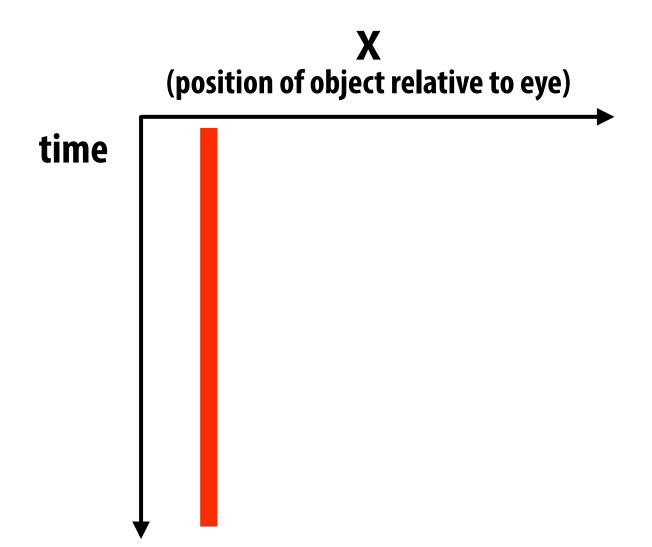


- Effect: time discretization
- OK: same perceptual effect as on regular 2D displays

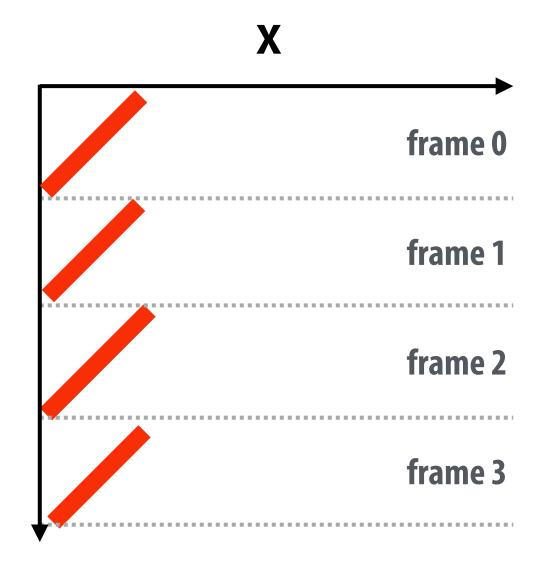
Case 3: Eye Moving to Track Moving Object



Reality (continuous)

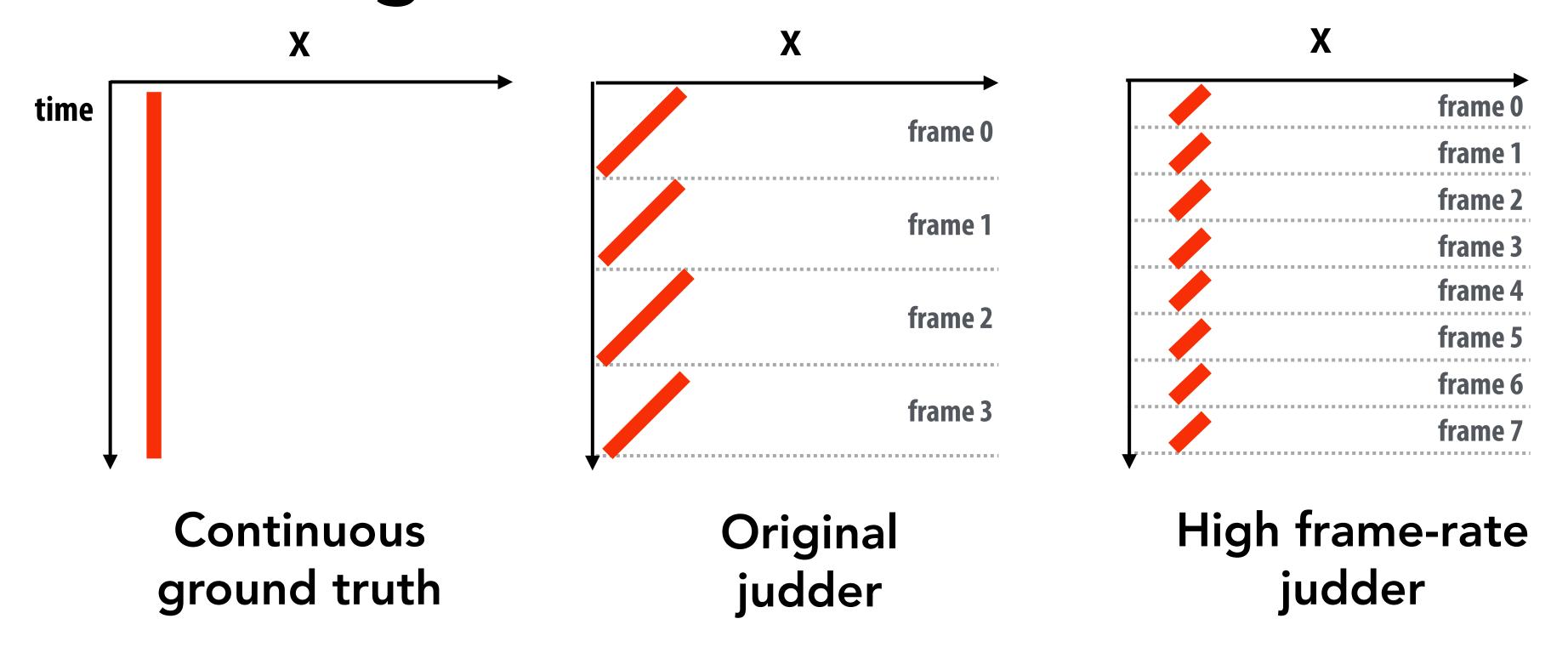


VR (discrete display refresh)



- right;
- Eye gaze moving left to right to track object
- Red object moving left to
 Eye is moving continuously relative to display
 - During each frame, image of object lags eye motion
 - Result: smearing/strobing effect ("judder")

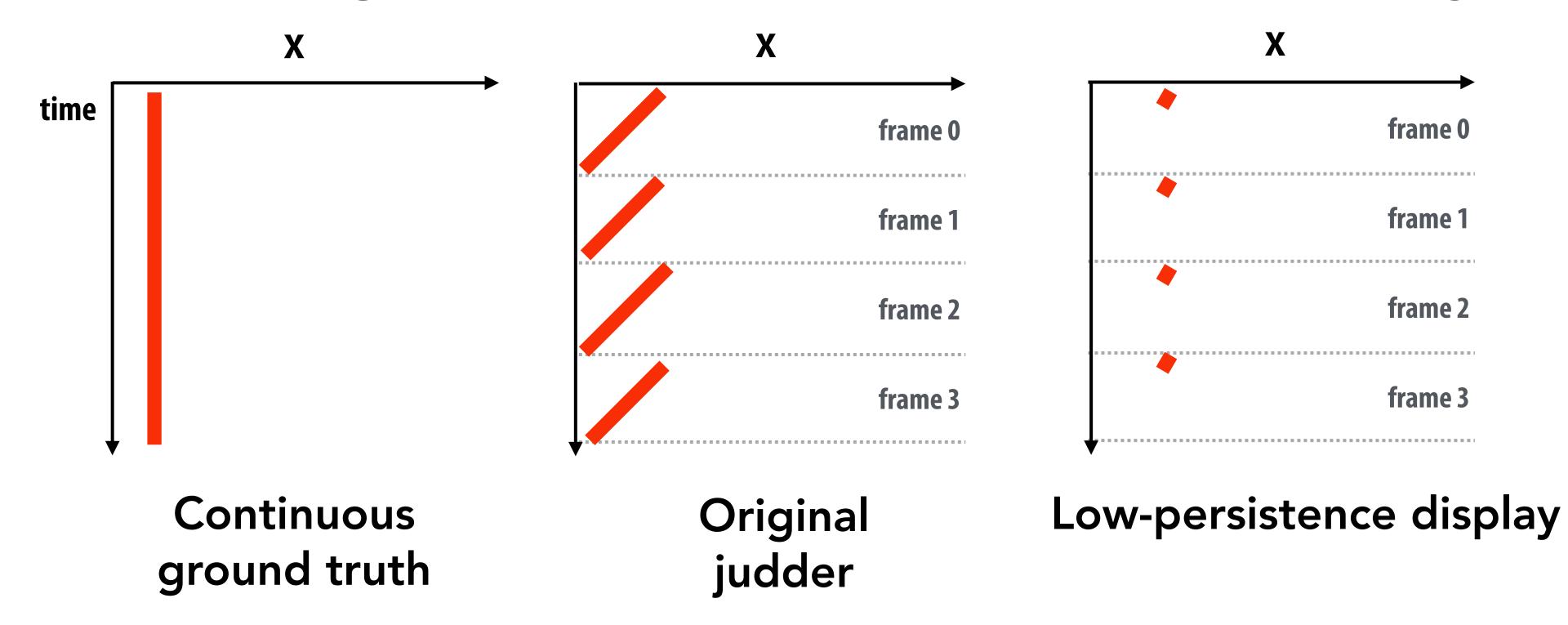
Reducing Judder: Increase Frame Rate



Higher frame rate (right-most diagram)

Closer approximation of ground truth

Reducing Judder: Low Persistence Display



Low-persistence display: pixels emit light for small fraction of frame

- Oculus DK2 OLED low-persistence display:
 - 75 Hz frame rate = ~13 ms per frame
 - Pixel persistence = 2-3 ms

Problem: Displays Exhibit "Rolling Shutter" Artifacts

- Pixel are illuminated from top to bottom sequentially in time, so light emitted from the bottom row arrives "late"
- Without compensation, this lead to image artifacts (similar to rolling shutter artifacts in cameras). E.g. VR image appears horizontally sheared when head is moving left to right.
- Compensation techniques include:
 - Perform post-process shear on rendered image
 - Render each row of image at a different time (predicted time that photons will arrive at eye)

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Rendering Challenge: High-Quality vs Low-Latency

Problem: High-Quality Rendering Can Be Slow

Constraints:

- Battery-powered device
- High-resolution outputs for both eyes

Implication:

- Can take significant time to render a frame
- This increases latency, can cause motion sickness
- This can reduce frame refresh rate

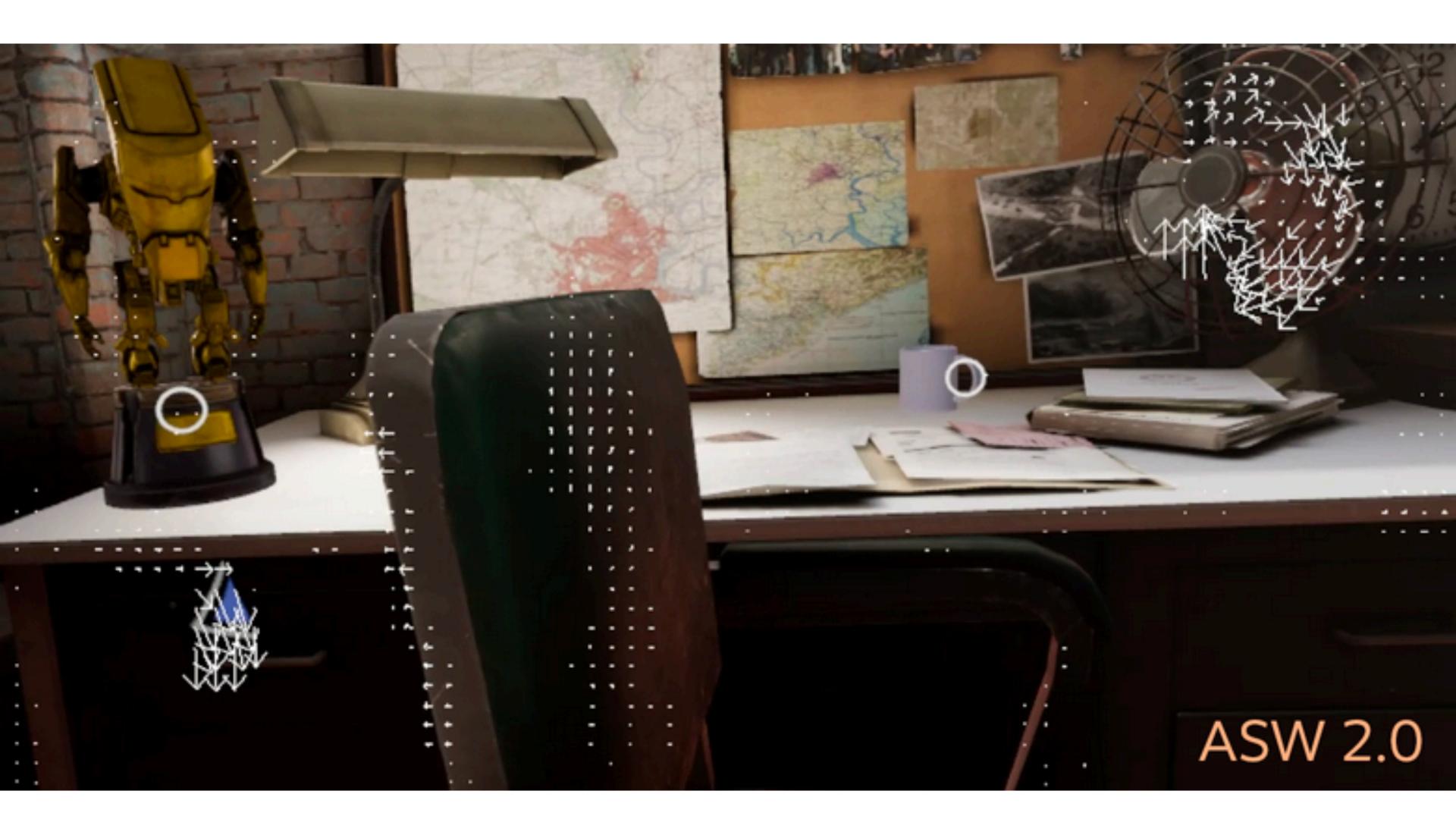
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Modern VR Engineering Solution: Reprojection

Key Ideas:

- Decouple slow, high-quality rendering of frames from fast "reprojection" immediately before display
- The high-quality frame uses then-current headtracking (which may be stale by end of render)
- Reprojection occurs extremely close in time to physical display, and warps the most recent highquality frame to the very latest head-tracking data
- Accurate reprojection warp requires both rendered image, its depth map, and potentially motion derivatives (e.g. optical flow)

Modern VR Engineering Solution: Reprojection



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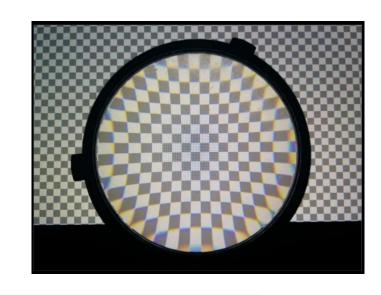
Overview of VR Topics

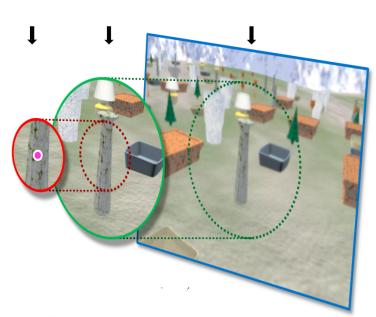
Areas we will discuss over next few lectures

VR Displays



VR Rendering





VR Imaging









Spherical Imaging (Monocular 360)

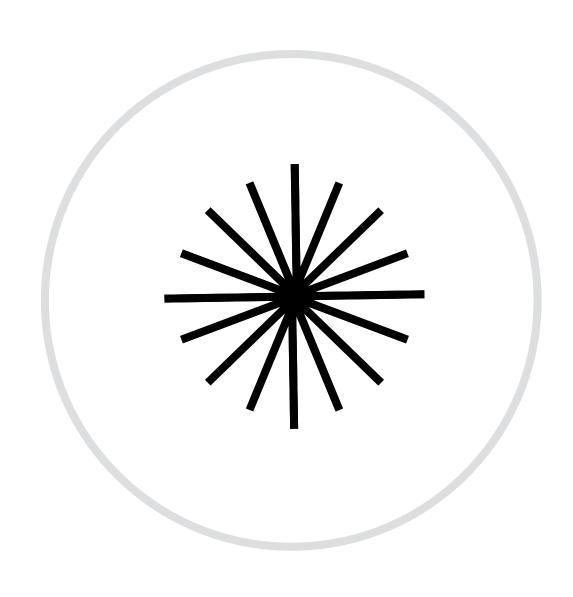
Dual Fisheye

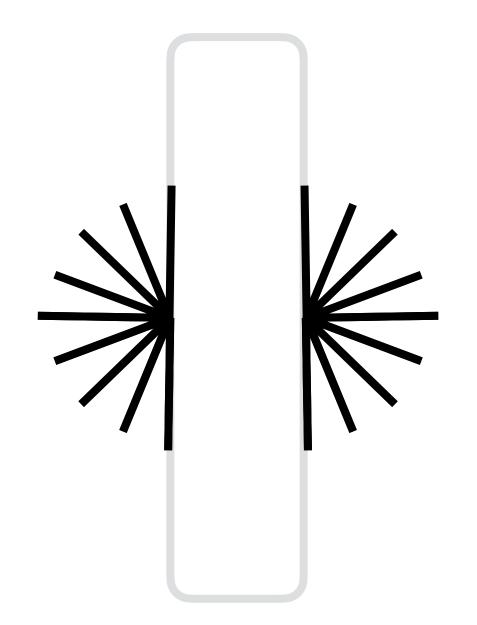






Stitching Challenges

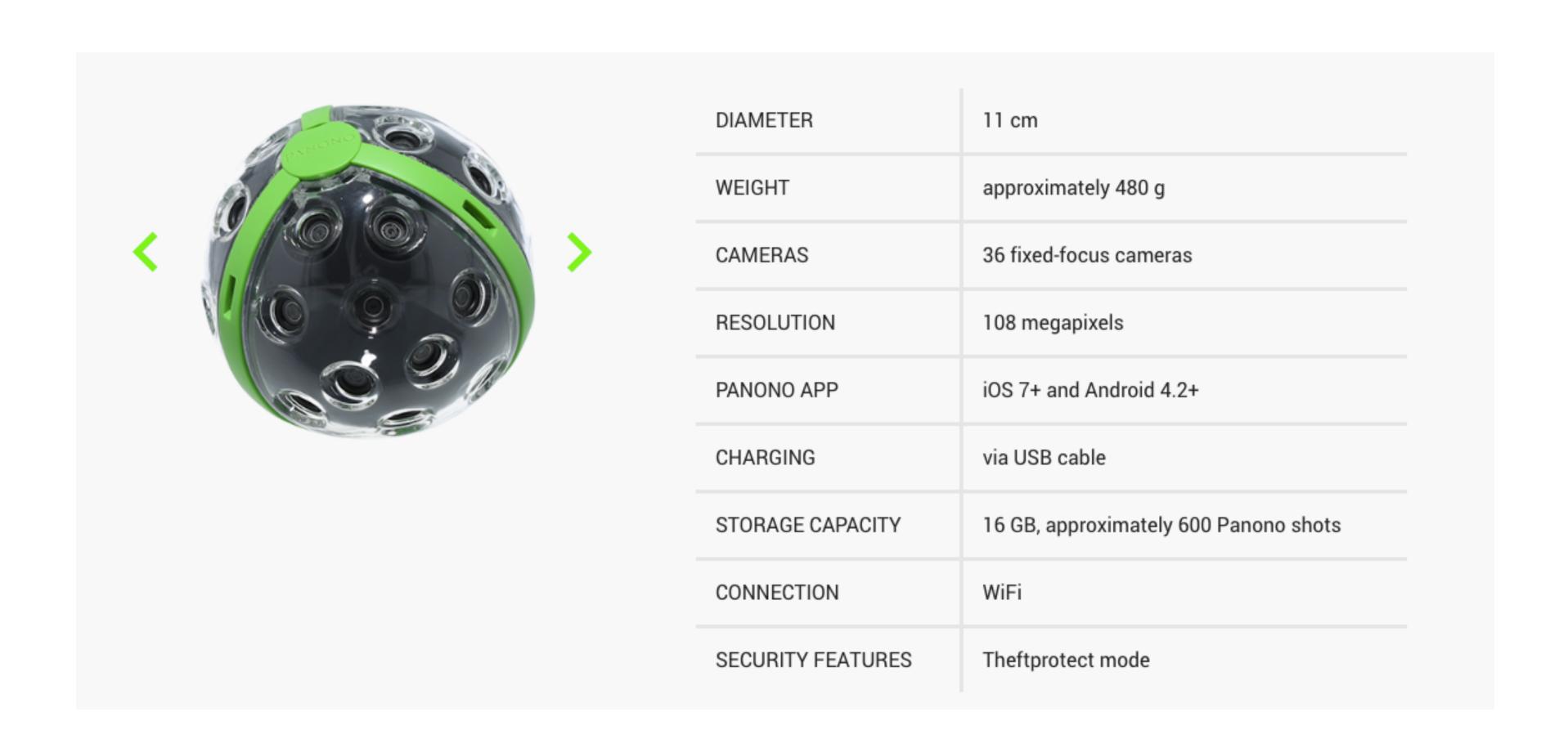




Want this ray sampling

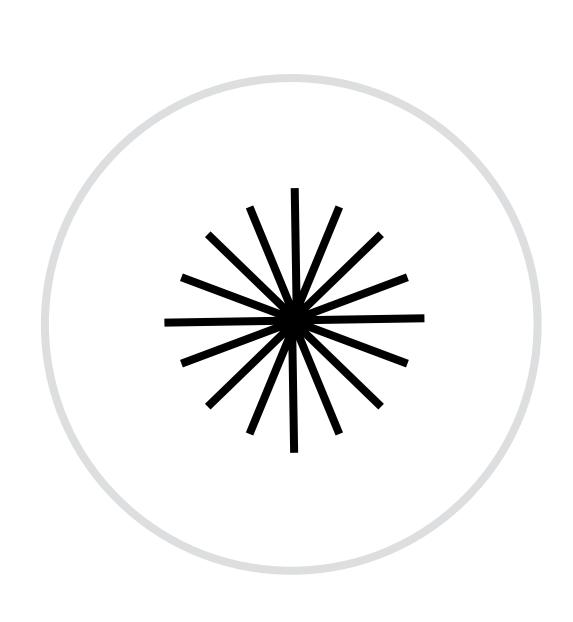
Get this ray sampling

Spherical Array of Cameras

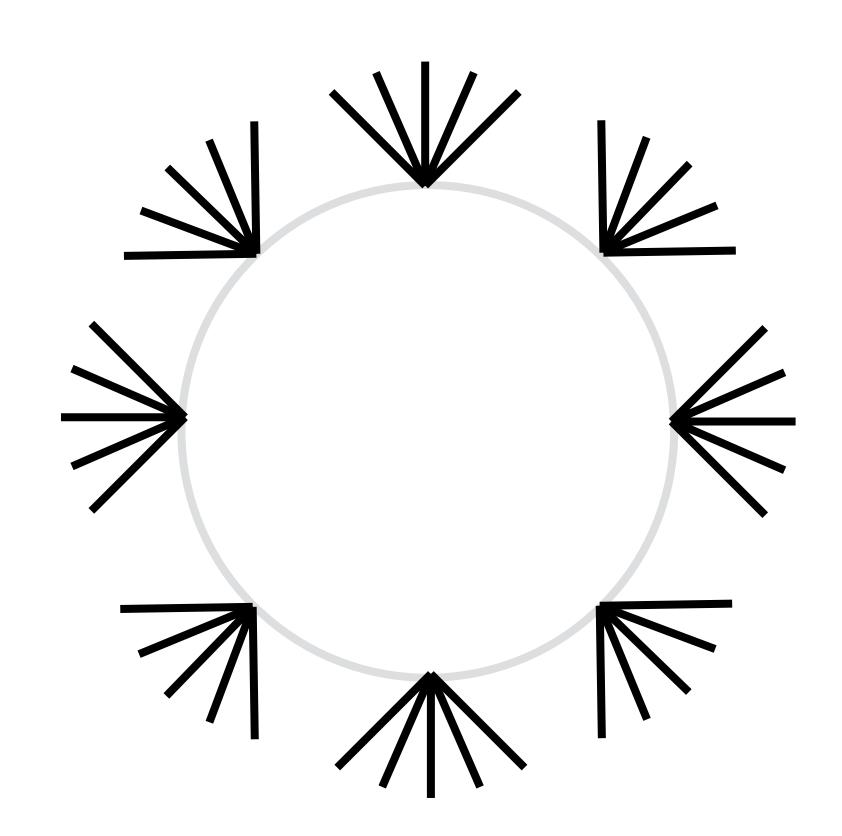


Panono 360 degree Camera

Stitching Challenges







Get this ray sampling

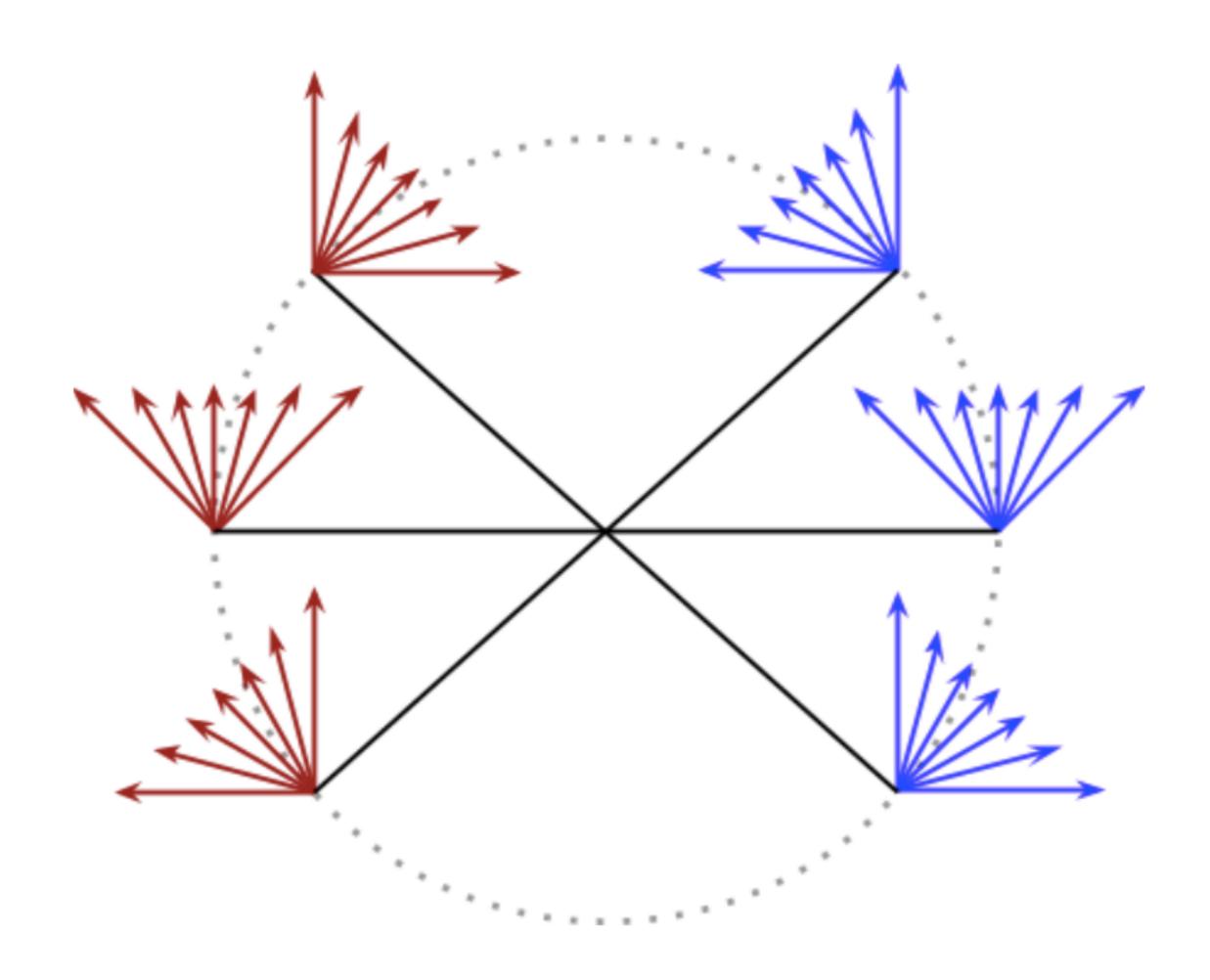
High Quality Stitching Solution Uses Computer Vision

Use computer vision techniques:

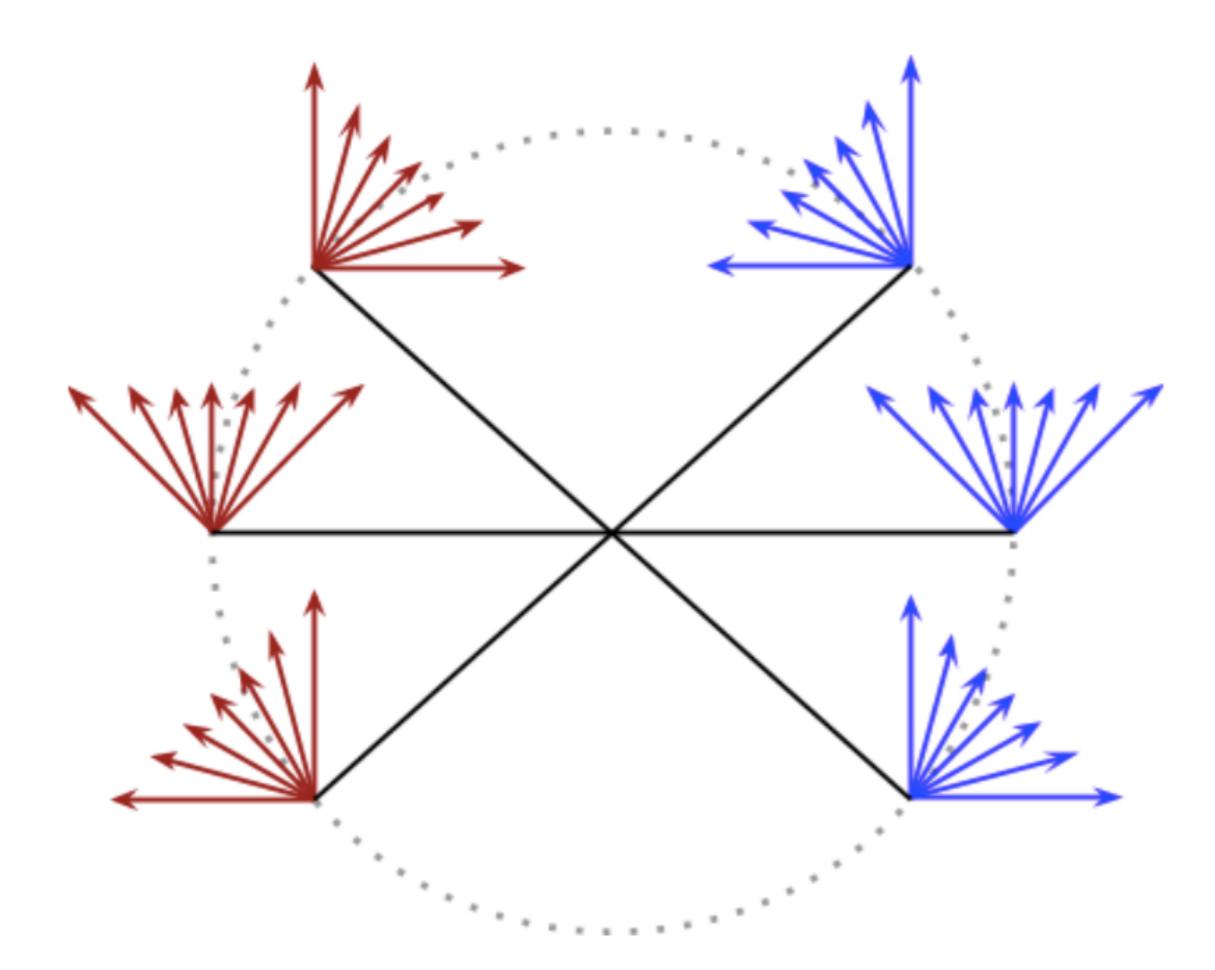
- Detect image features (like SIFT features)
- Correlate features across frames (transform)
- Warp to align frames and blend

Spherical Stereo Imaging

What Pairs of Viewpoint Positions Do We Want To Sample?



Idea: Spin a Pair of Cameras About Midpoint

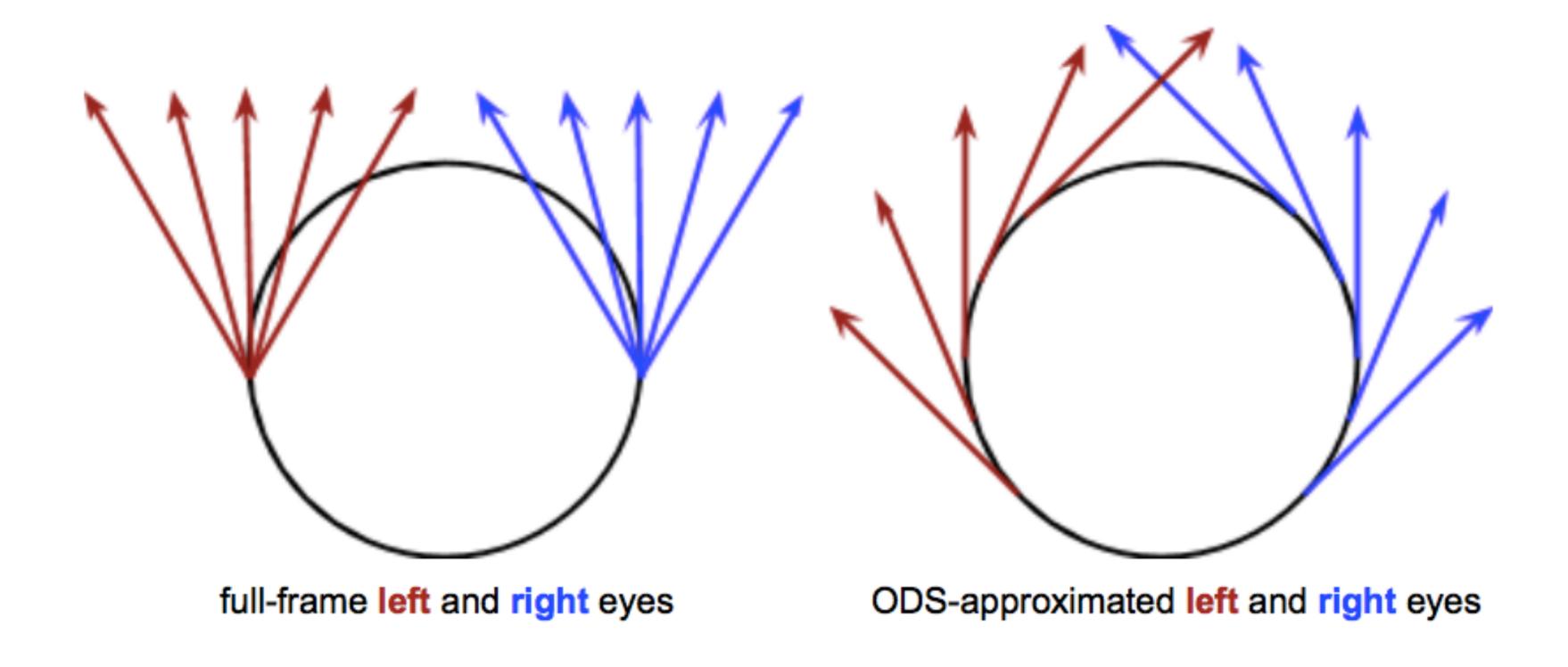


Store a set of movie pairs (one per angle)

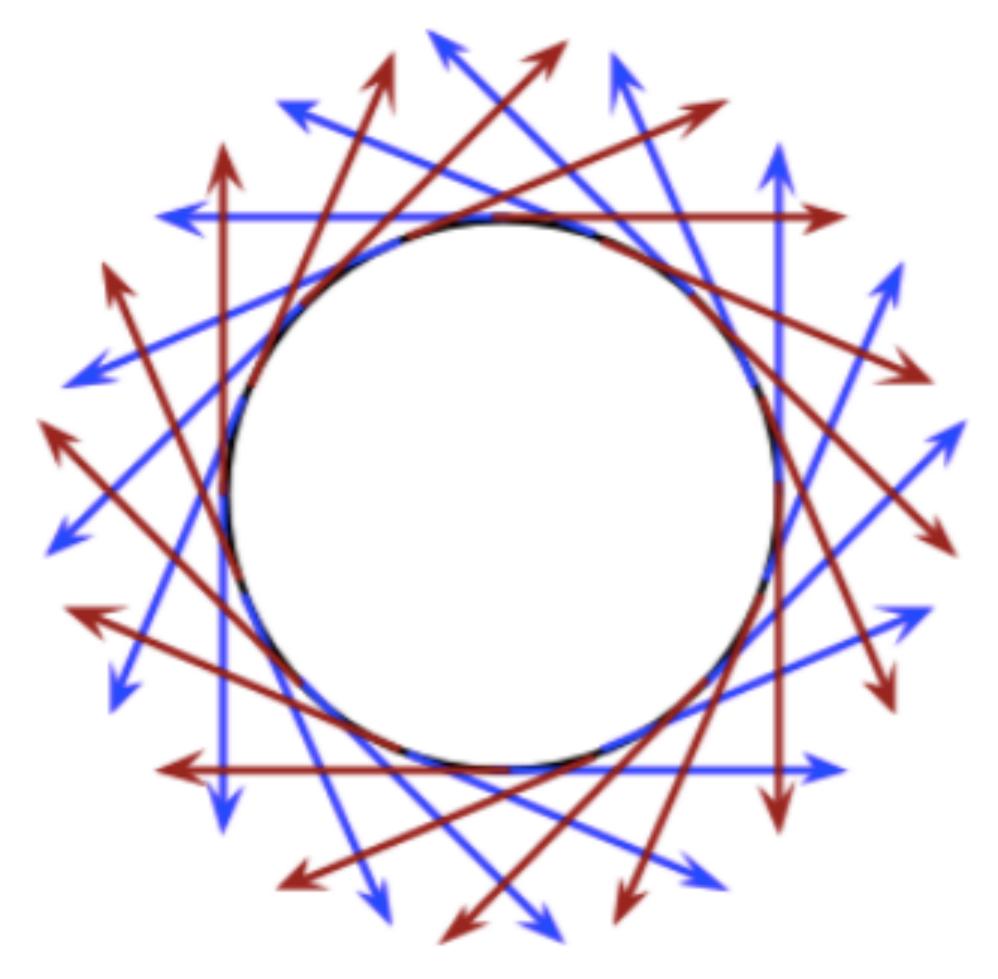
But that's a lot of data

Image Credit: Google Inc.

Omni-Directional Stereo Approximation



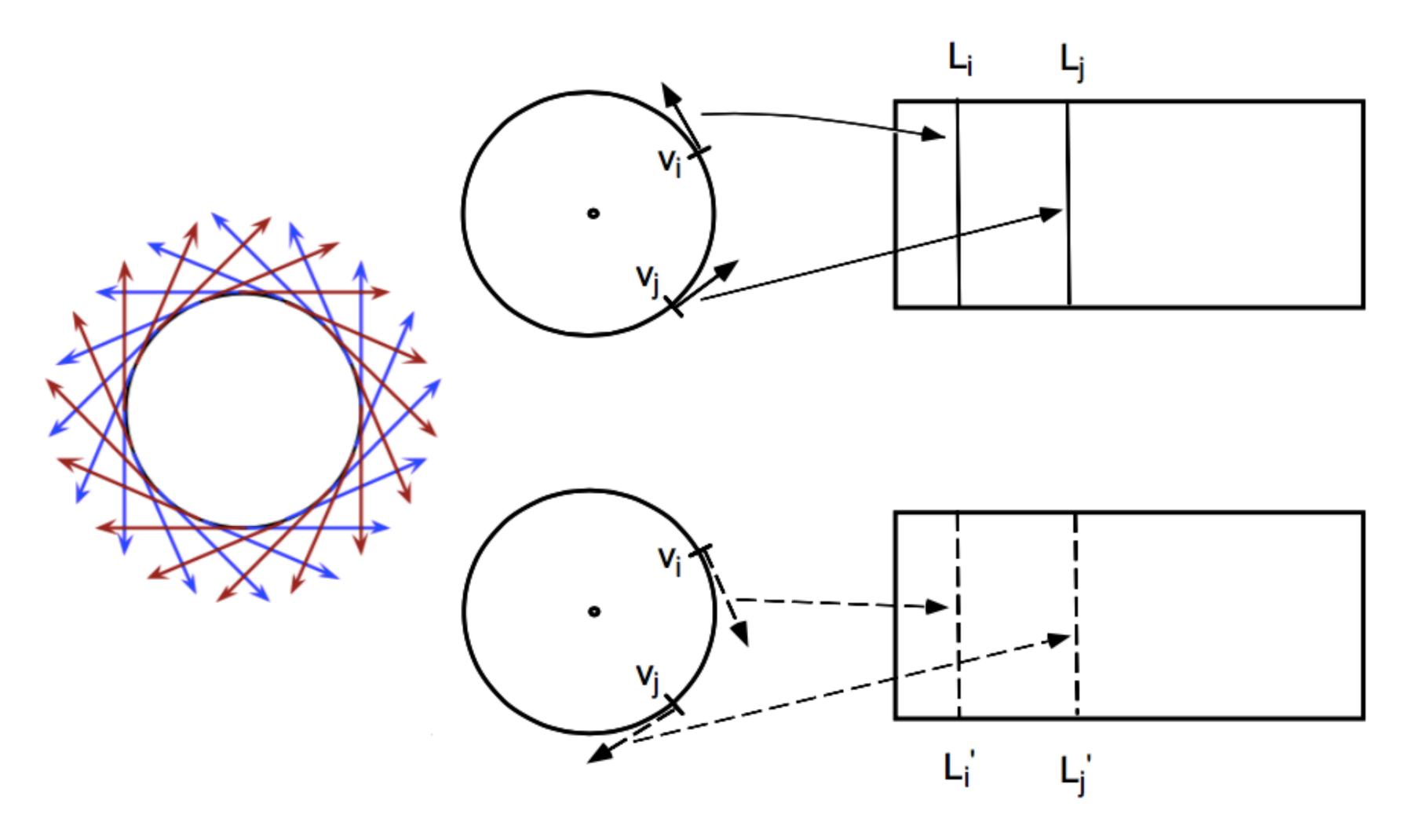
Omni-Directional Stereo Approximation



Extended to be omnidirectional

Image Credit: Google Inc.

Spinning Camera



Concentric Mosaics Shum and He, SIGGRAPH 1999

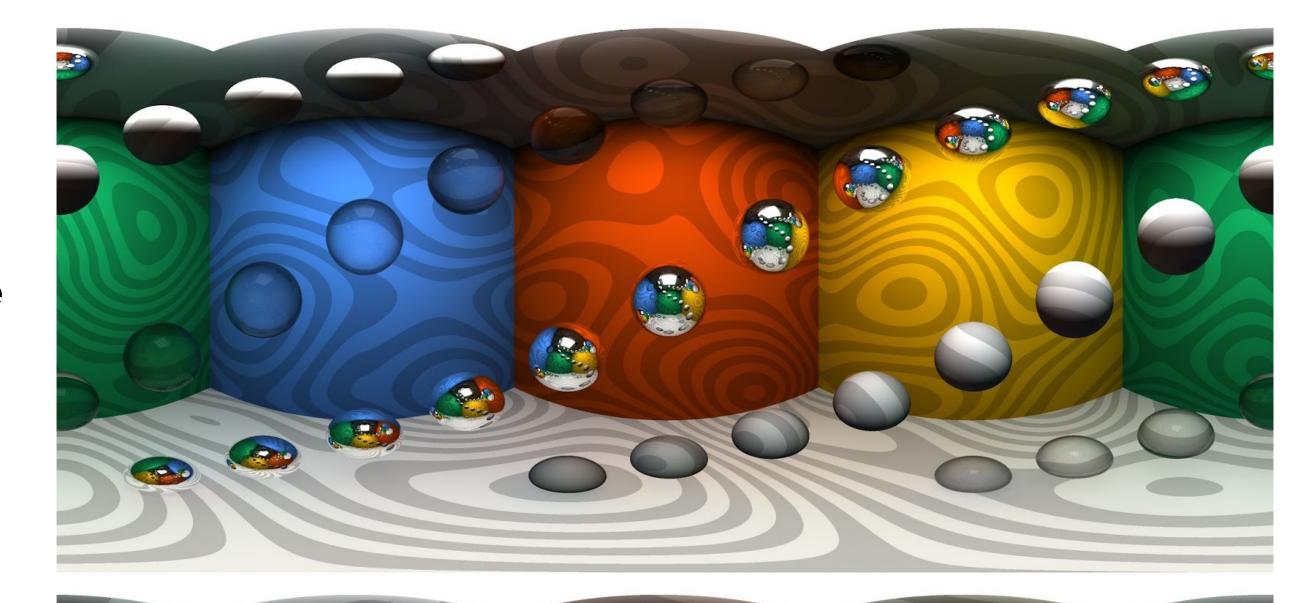
Omni-Directional Stereo Representation

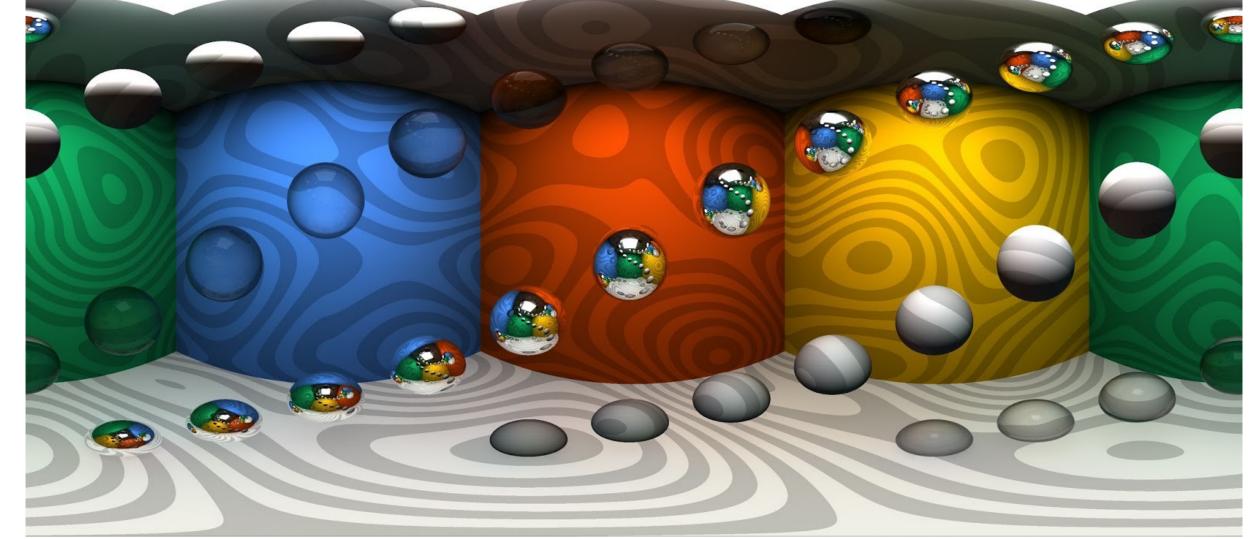
Encode left/right views as just two spherical images

- Render left and right views for each angular view independently, with regular viewing software
- Efficient and compact, but this is an approximation
 - Straight lines may appear slightly curved
 - Vertical disparity for close objects incorrect

Example (Rendered)

Left Eye



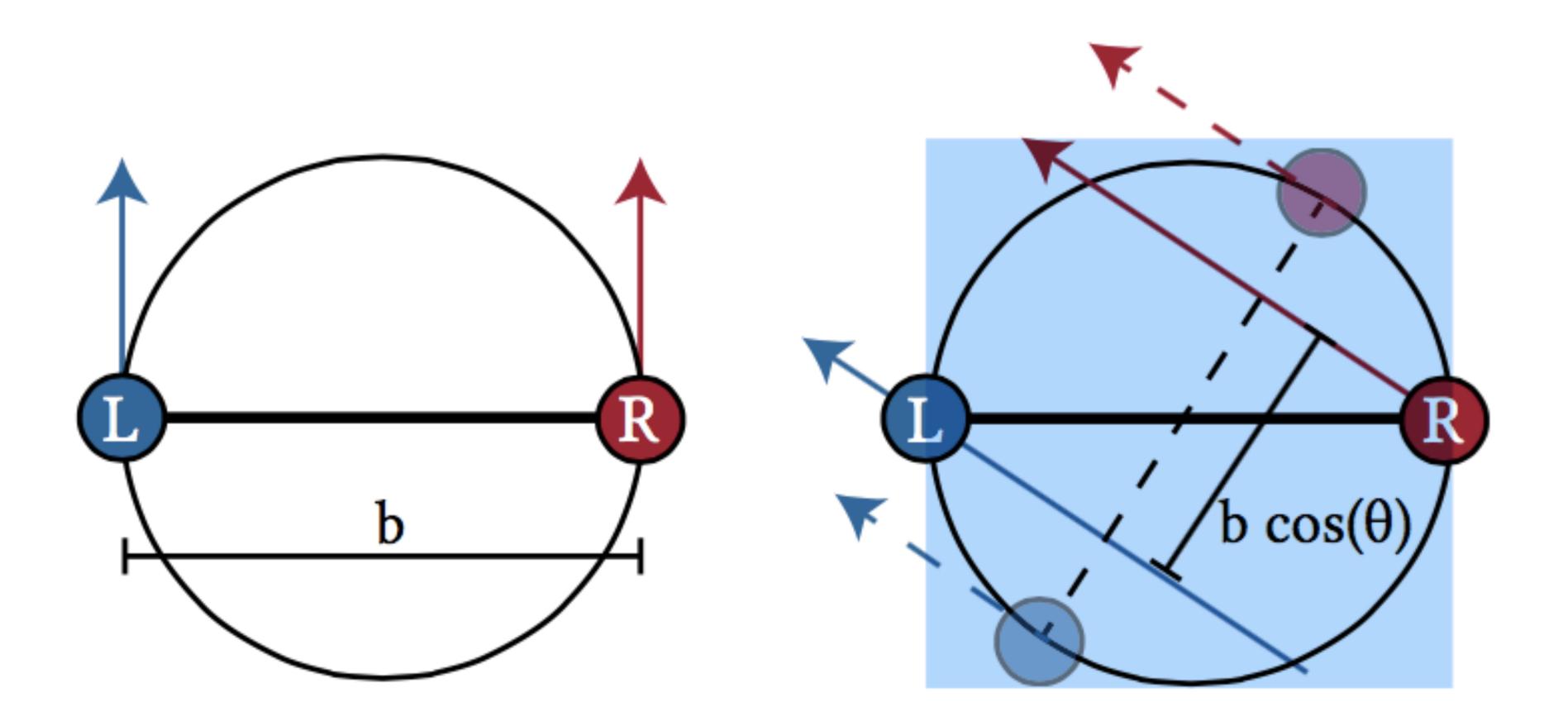


Right Eye

Two Eyes — Two Spherical Cameras?



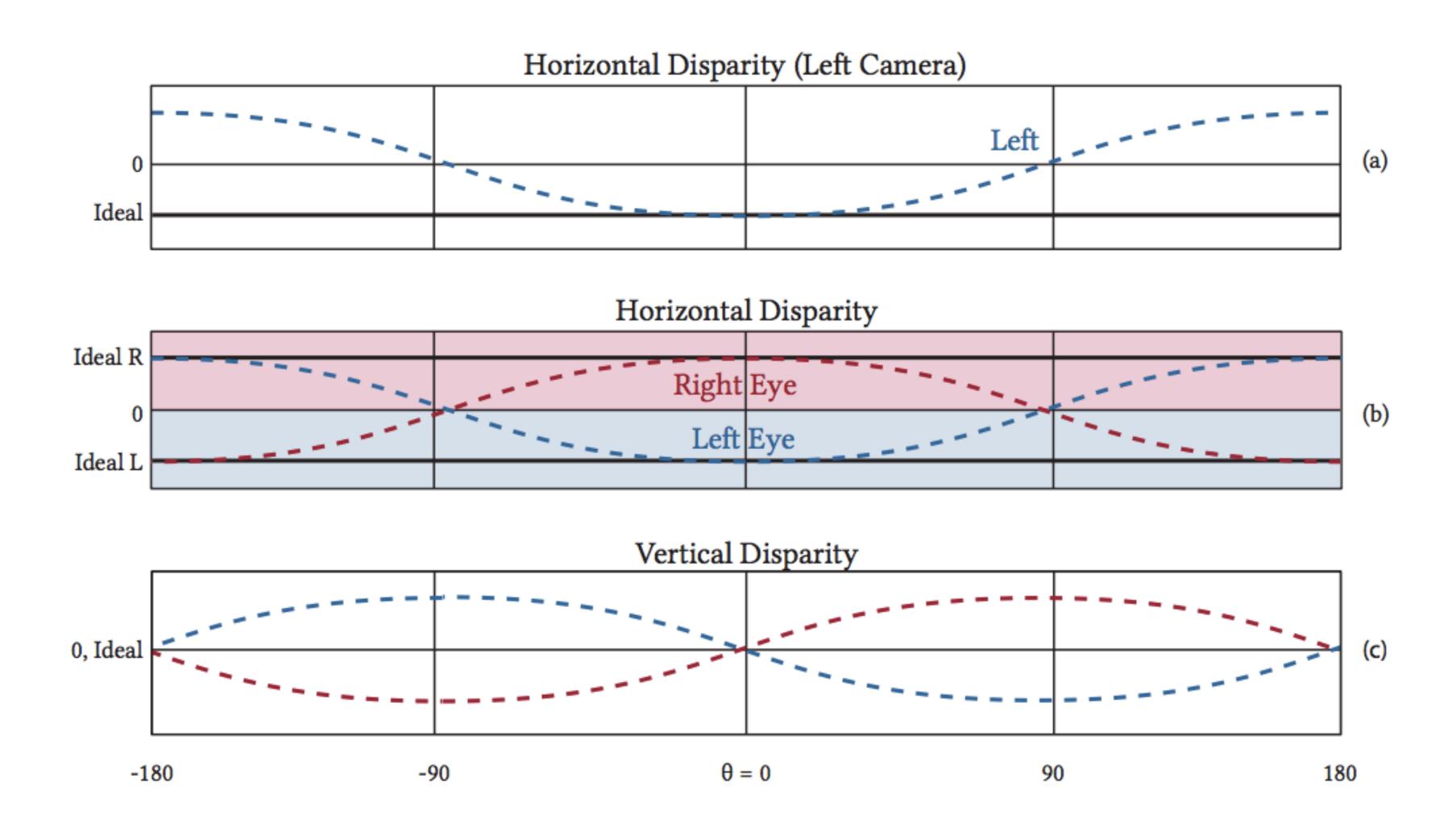
Problem: Stereo Baseline Fluctuates With View Angle



Apparent stereo baseline decreases by $cos(\theta)$ if rays are mapped directly

Matzen et al. SIGGRAPH 2017

Problem: Both Horizontal and Vertical Disparities Fluctuate



Problems

- Disparity: incorrect baseline as view angle changes
- Occlusion: each camera blocks the other's view!

Solution: Computational Photography

3D reconstruction

Computer vision on stereo views

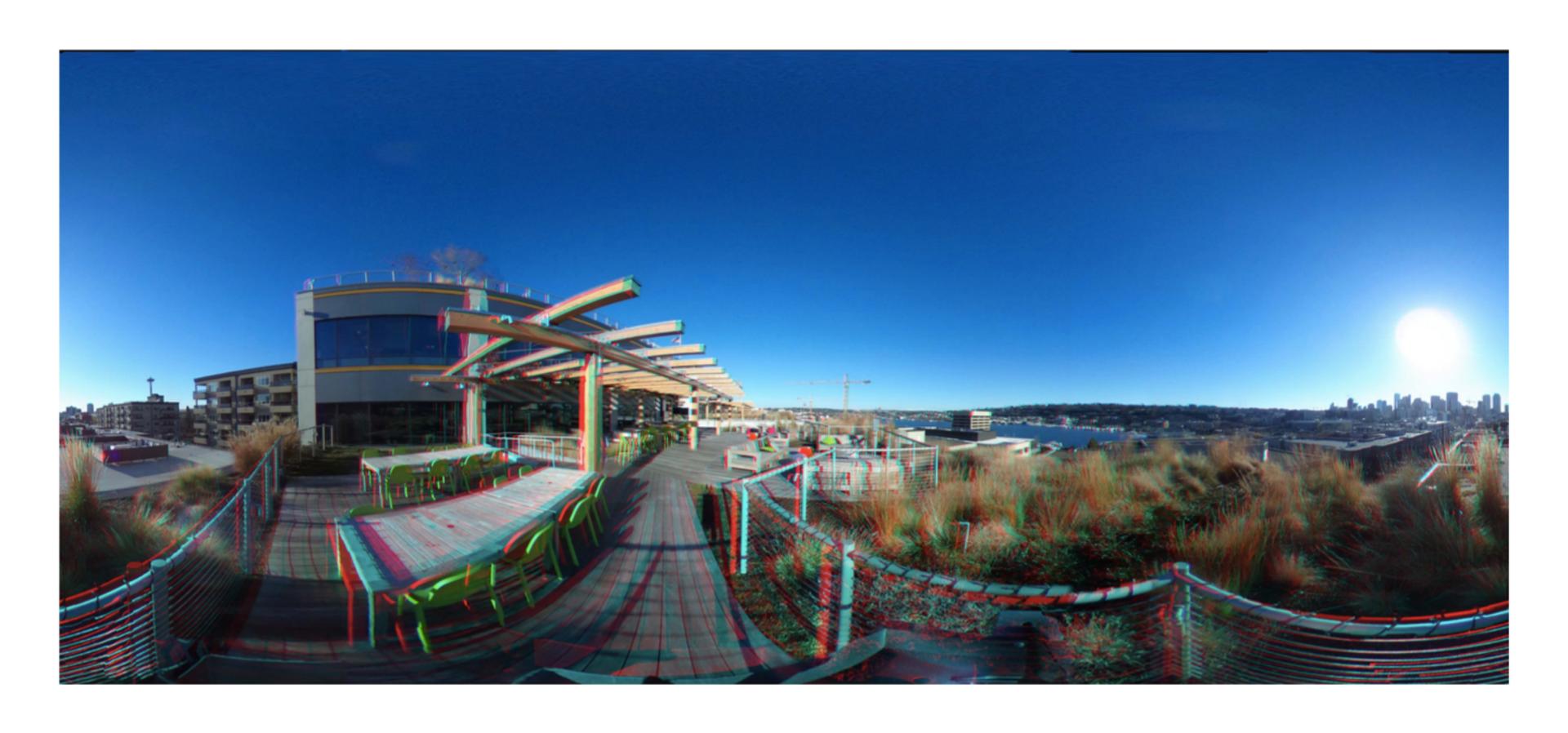
Disparity correction

- Use 3D model to correct stereo disparities
 - e.g. amplify horizontal disparities by $1/\cos(\theta)$
- Flip views when facing backwards

Hole filling

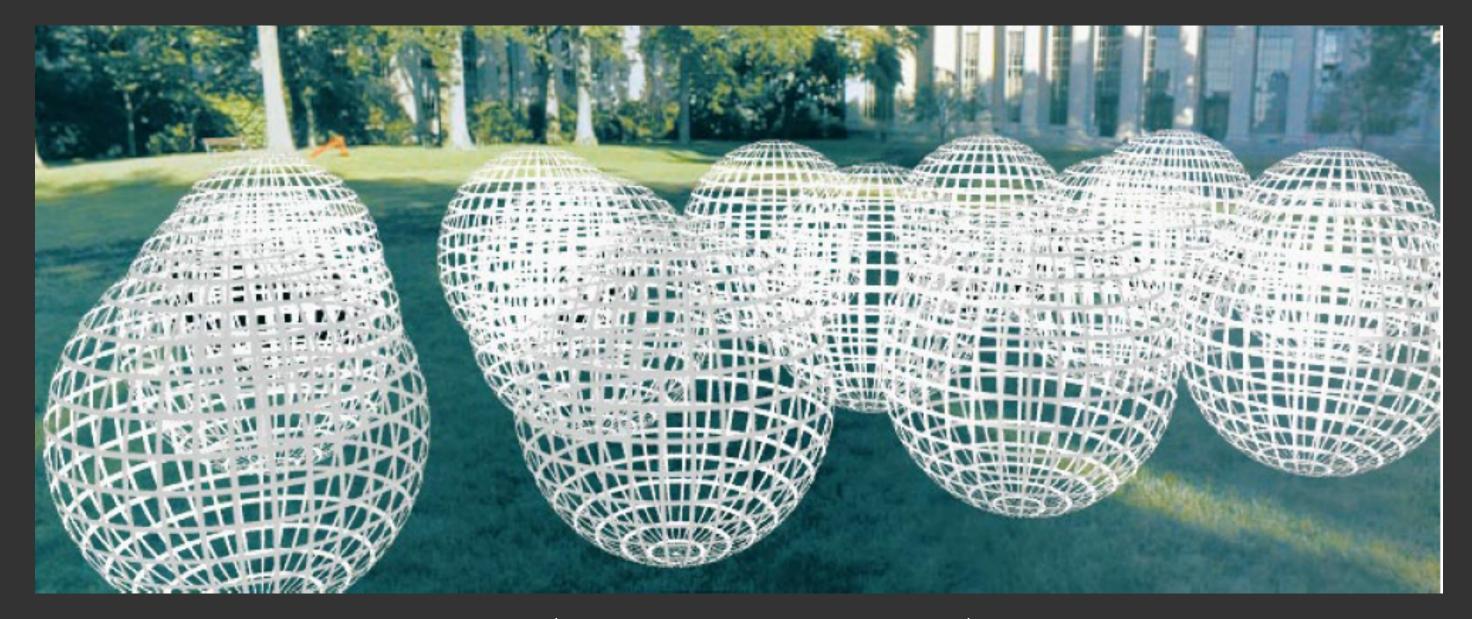
 Cut out view of other camera, and fill hole with pixels from other camera, as best possible

Spherical Stereo Result



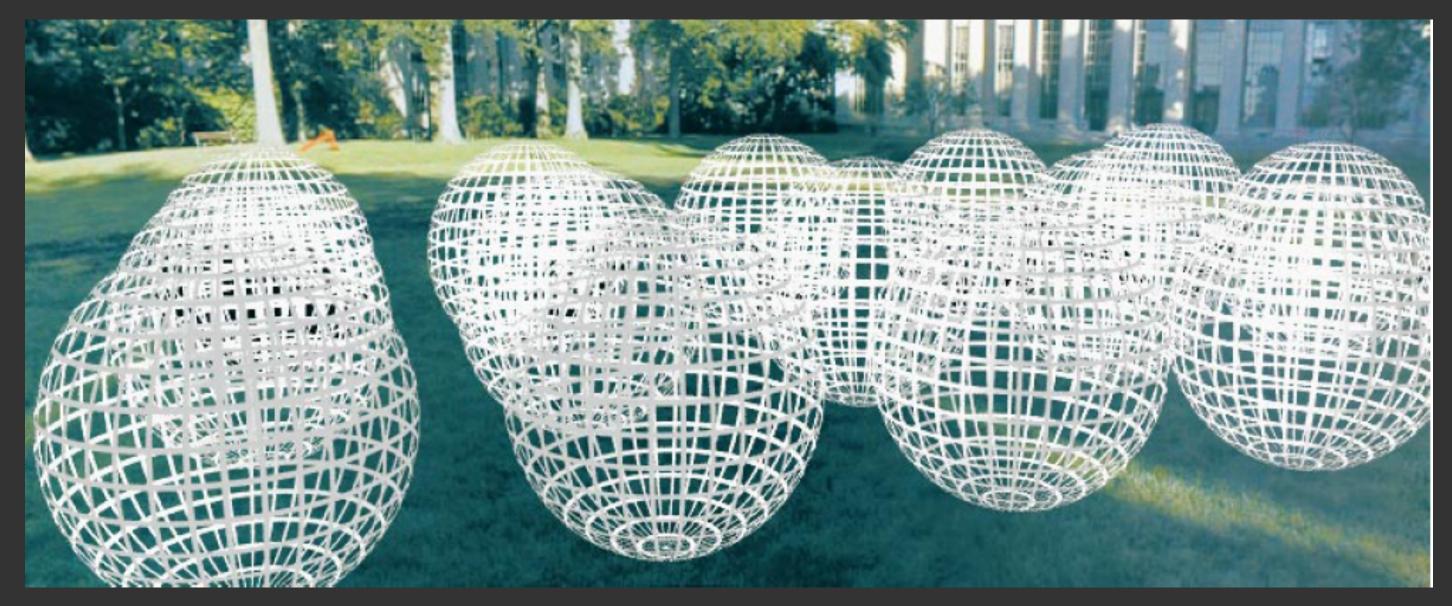
Moving-Viewpoint Imaging (Full Plenoptic Function?)

The 5D Plenoptic Function



 $P(\theta, \phi, V_x, V_y, V_z)$

4D Light Field



$$P(\theta, \phi, V_x, V_y) = P(u, v, s, t)$$

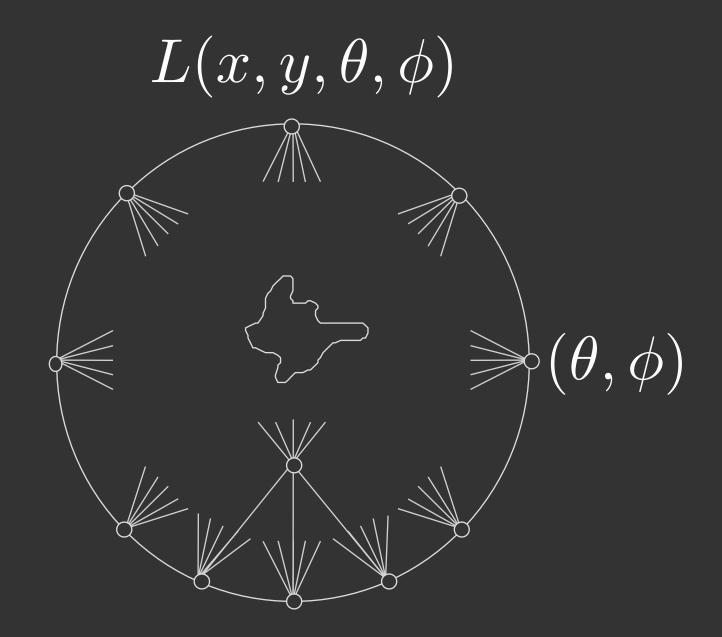
 In a region of free-space, 5D plenoptic function simplifies to 4D because light is constant along a ray

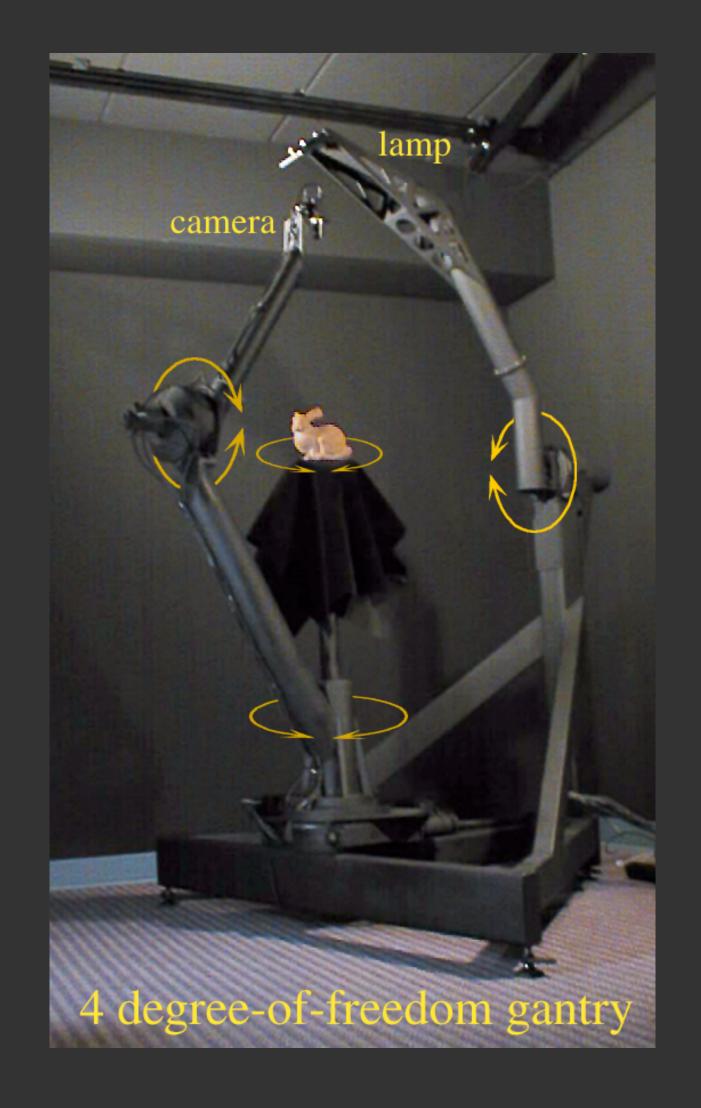
Light Field Capture Robot

Original light field rendering paper

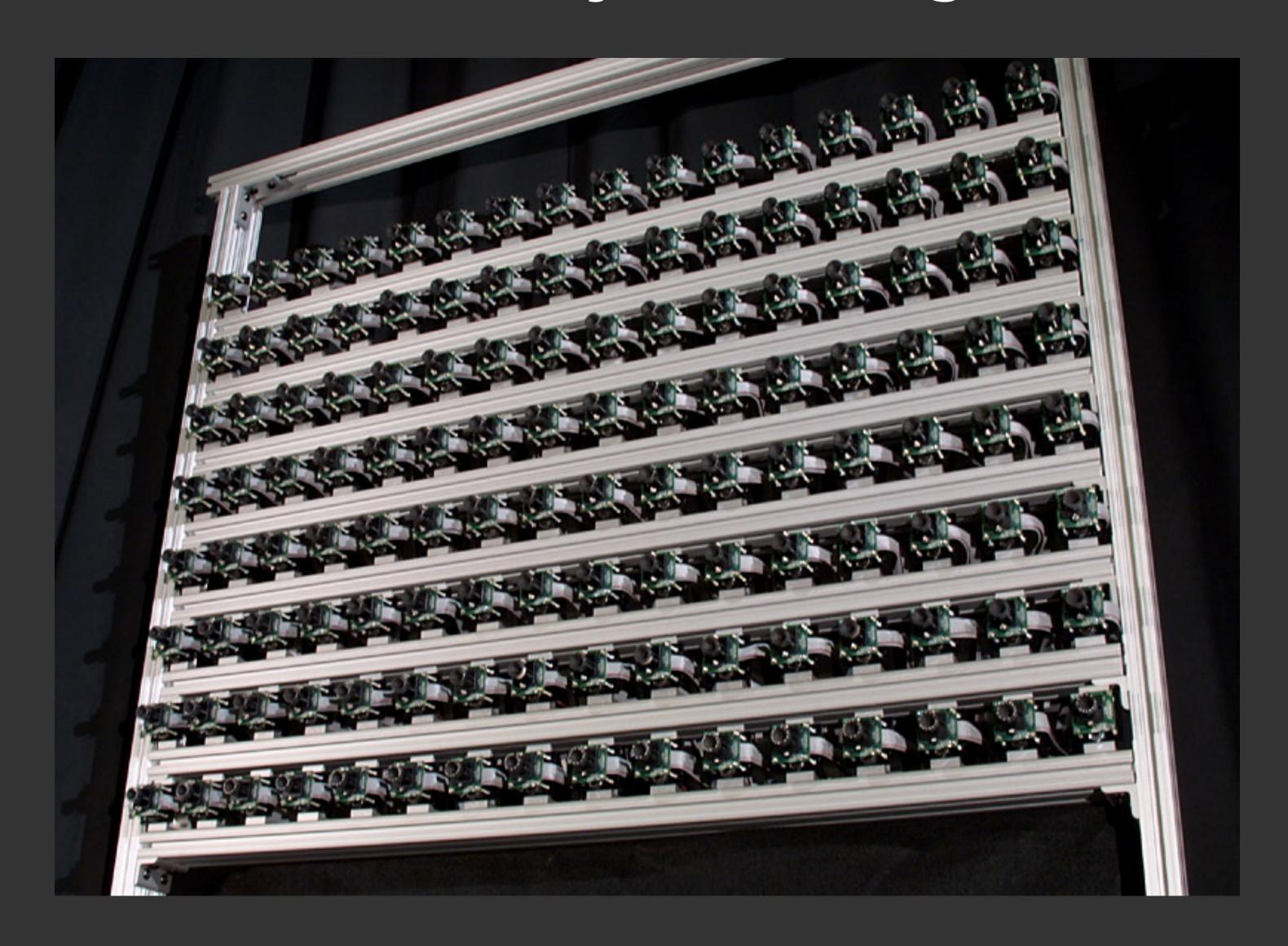
Take photographs of an object from all points on an enclosing sphere

Captures all light leaving an object – like a hologram





Multi-Camera Array ⇒ 4D Light Field





[Wilburn et al. SIGGRAPH 2005]

Handheld 4D Light Field Camera (Plenoptic Camera)

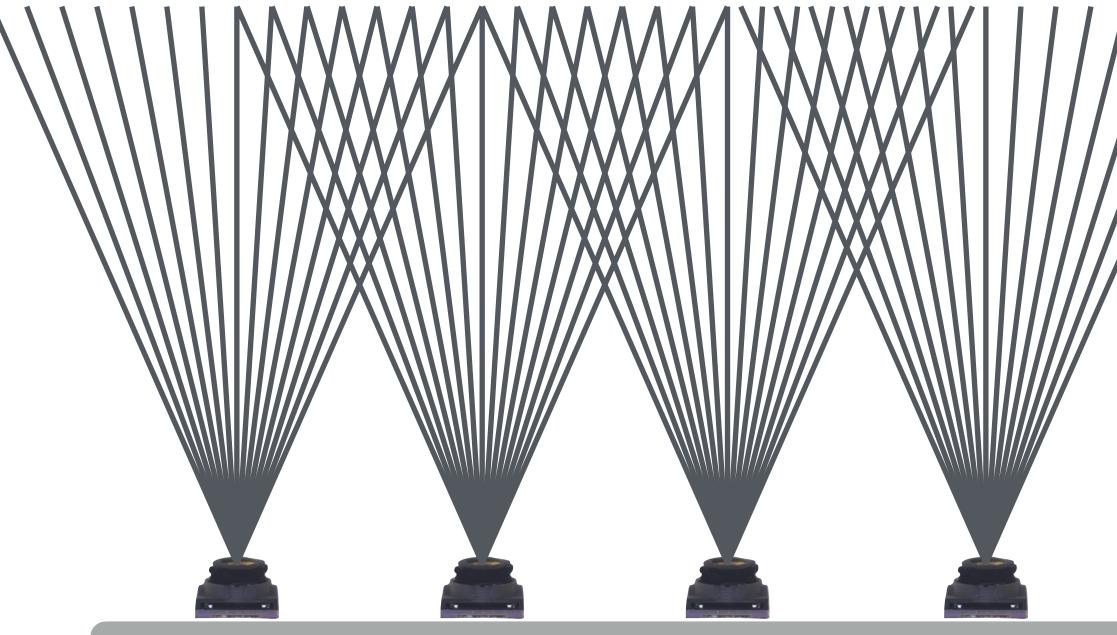


Lytro Gen-2 Light Field Camera



Handheld Light Field Camera vs Camera Array





Camera array: e.g. 10x10 views distributed across large planar support

Plenoptic camera: e.g. 14x14 views distributed across small lens pupil Note: antialiased across views, unlike camera array

The Intimacy of VR Graphics

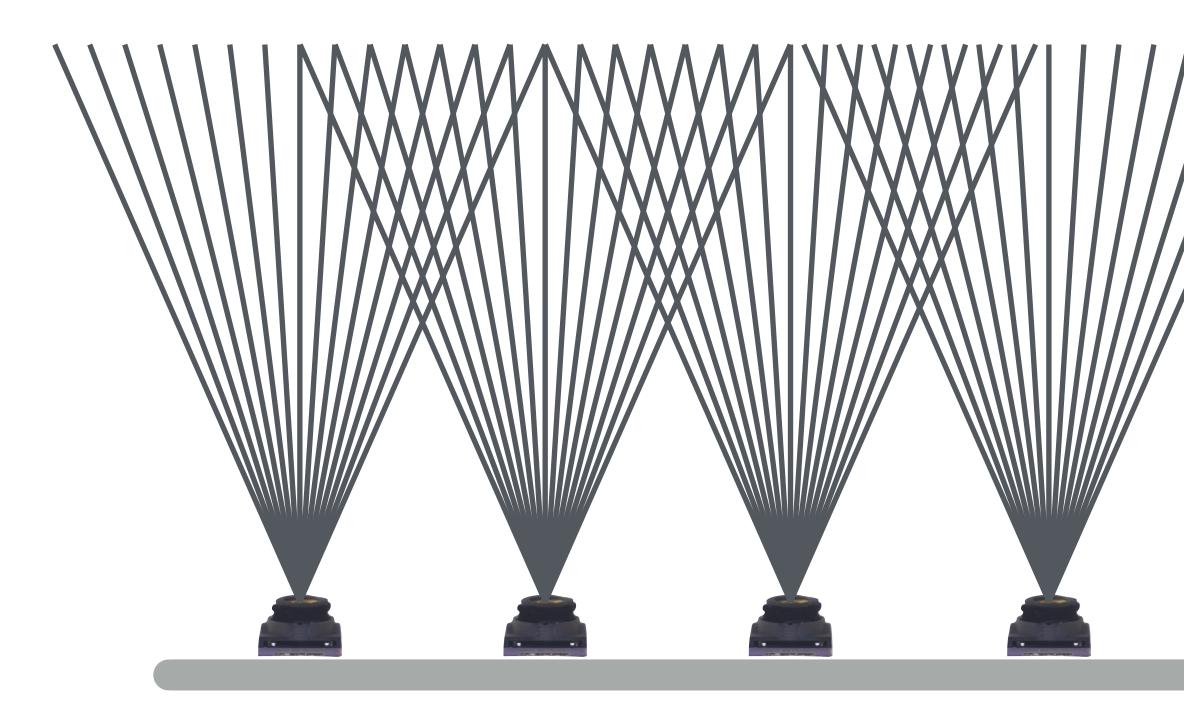


Google's Tilt Brush on HTC Vive



How Dense Are Camera Views Today?



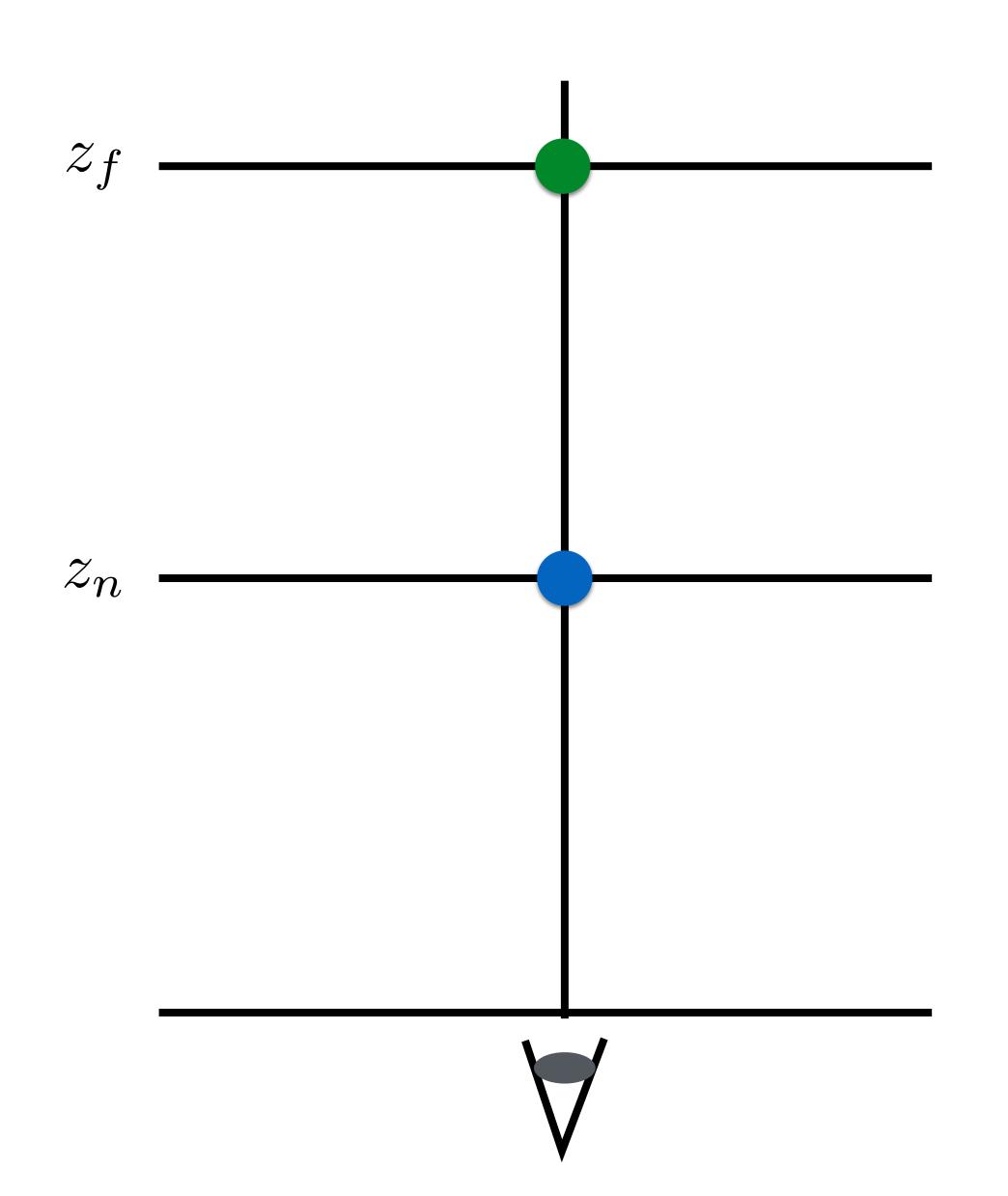


Multi-camera arrays: 50 - 100 views

Plenoptic cameras:

100 - 200 views



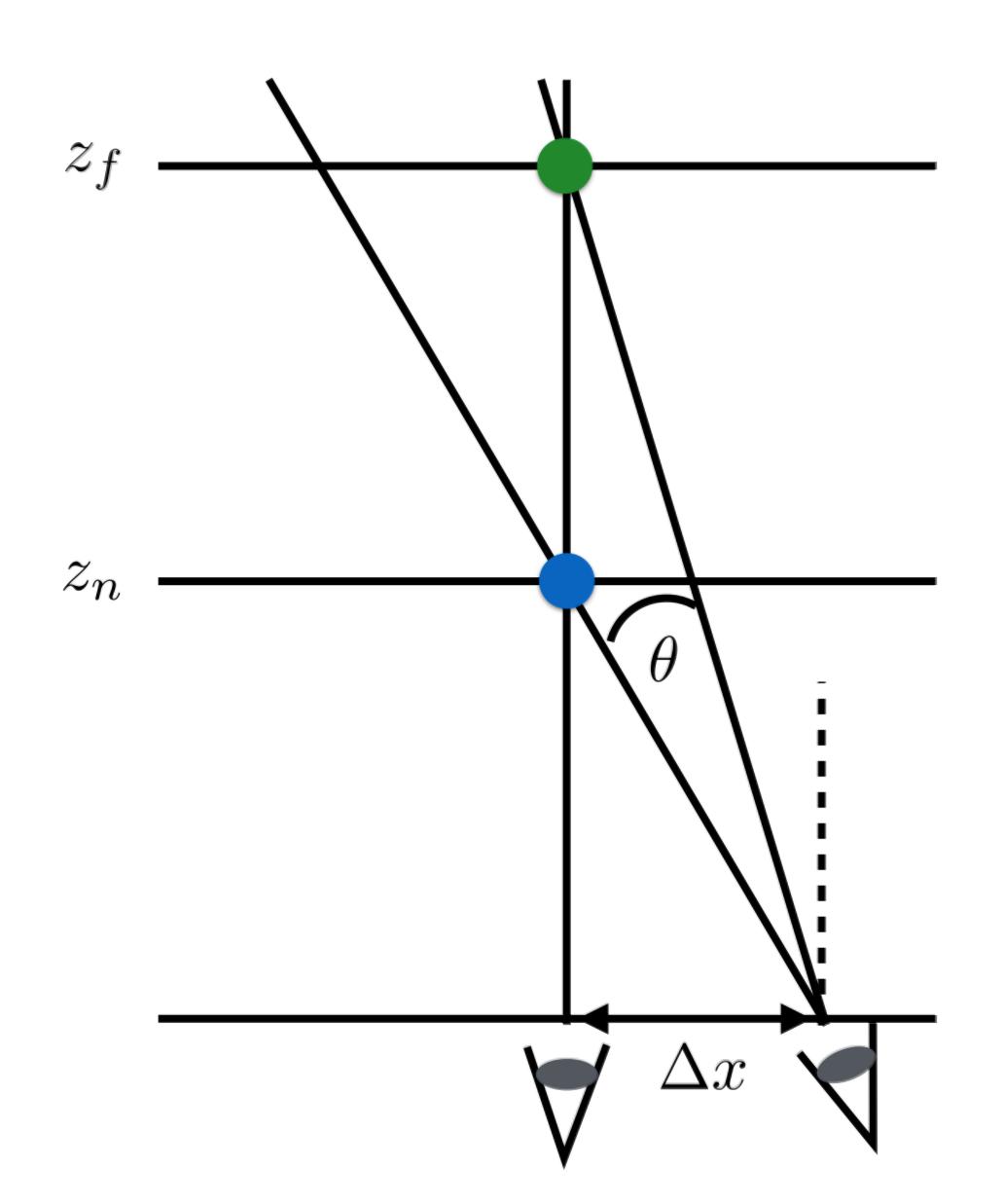


Child in lap, front to back of head

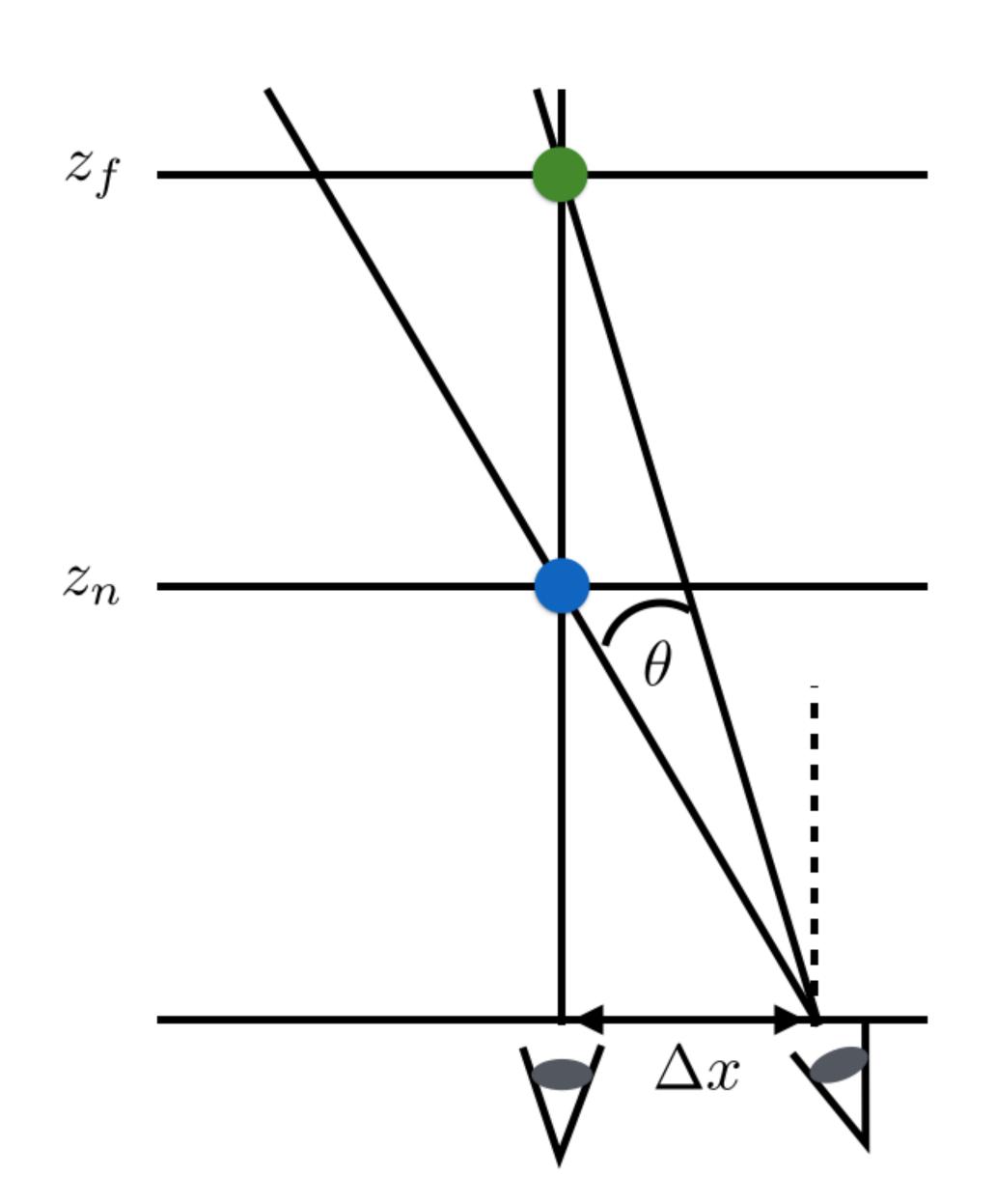


$$z_n = 0.3 \mathrm{m}$$

$$z_f = 0.6 \text{m}$$

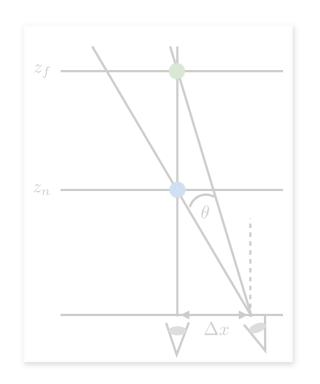


What is the minimum lateral eye movement Δx so that we can visually distinguish the close and far features?



20/20 vision: $\theta \approx (1/60)^{\circ}$

Curent HMDs: $\theta \approx (1/10)^{\circ}$



Solving for minimum lateral motion:

$$\Delta x = \frac{(z_f - z_n) - \sqrt{(z_f - z_n)^2 - 4 \tan^2 \theta z_n z_f}}{2 \tan \theta}$$



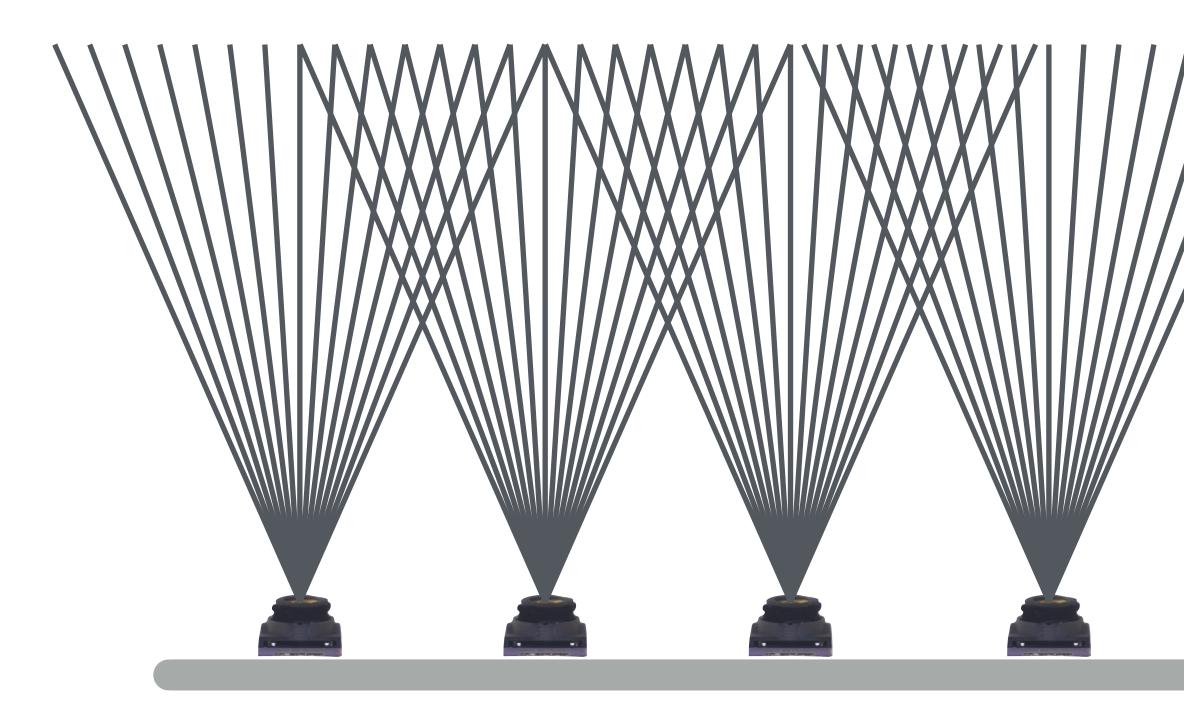
20/20 vision: $\theta \approx (1/60)^{\circ} \implies \Delta x \approx (1/1719) \mathrm{ft}$

Curent HMDs: $\theta \approx (1/10)^{\circ} \implies \Delta x \approx (1/286)/\mathrm{ft}$

20/20 vision: Current HMDs: millions of views per square foot a hundred thousand views per square foot

How Dense Are Camera Views Today?



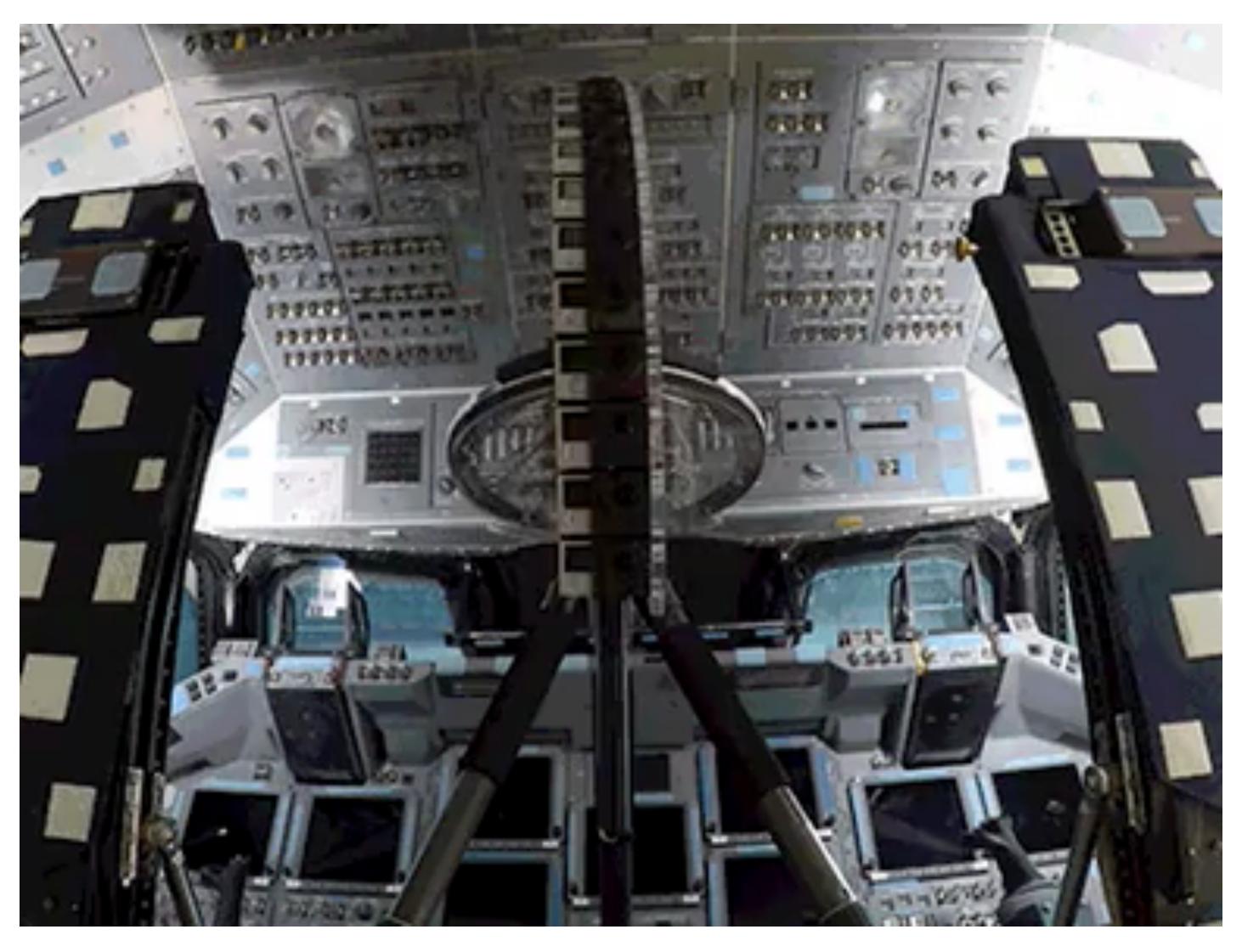


Multi-camera arrays: 50 - 100 views

Plenoptic cameras:

100 - 200 views

Google VR Camera Rig



Paul Debevec, Google

Imaging for Virtual Reality



Google 6 DOF Light Field Camera. Broxton et al. 2019.

Imaging for Virtual Reality



Google 6 DOF Light Field Camera. Broxton et al. 2019.

Active Area of Research

One important theme is applying machine learning to intelligently up-sample from tens of camera views to the very high sampling rates required for Nyquist-sampled VR rendering.

See research from my grad students Pratul Srinivasan, Ben Mildenhall and Matt Tancik in recent years on this topic, especially NERF project. This is ML-based inference of 3D volume function of the scene from a handful of photos.

Matt Tancik will give a guest lecture next time on NERFs!

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Things to Remember

VR presents many new graphics challenges!

Displays

Head-pose tracking with high accuracy and low latency

Rendering

 Low-latency, high resolution & frame-rate, wide field of view, ...

Imaging

• 360 spherical, stereo, light field

Acknowledgments

Thanks to Kayvon Fatahalian, Alyosha Efros, Brian Wandell and Pratul Srinivasan for lecture resources and slides!