

**Lecture 23:**

**Special Topics:**

**Neural Radiance Fields**

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**Computer Graphics and Imaging**

**UC Berkeley CS184/284A**

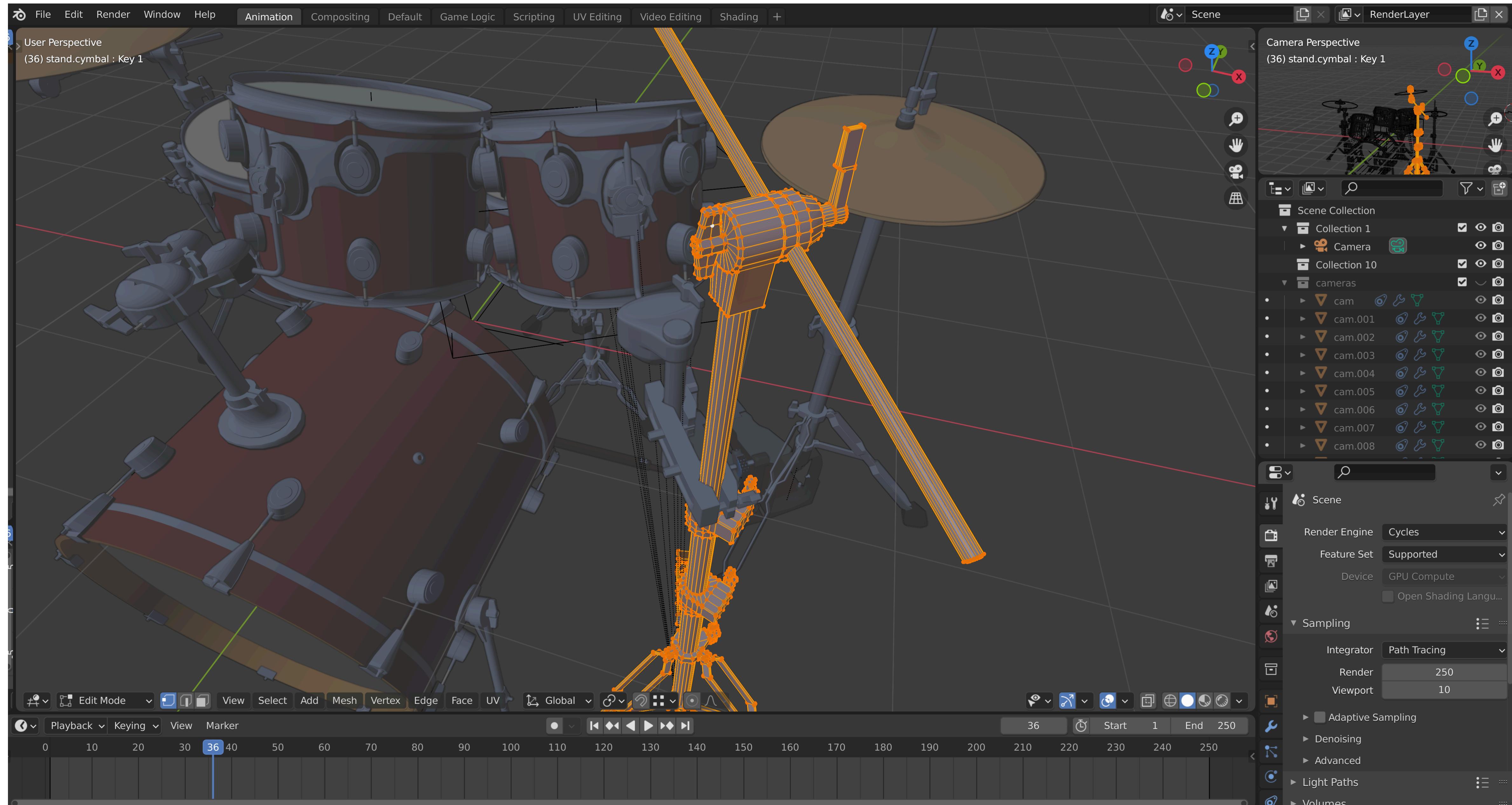
# Where does the 3D model come from?



Jun Yan, Tracy Renderer

San Miguel Scene, 10.7M triangles

# 3D Modeling Software is Complex





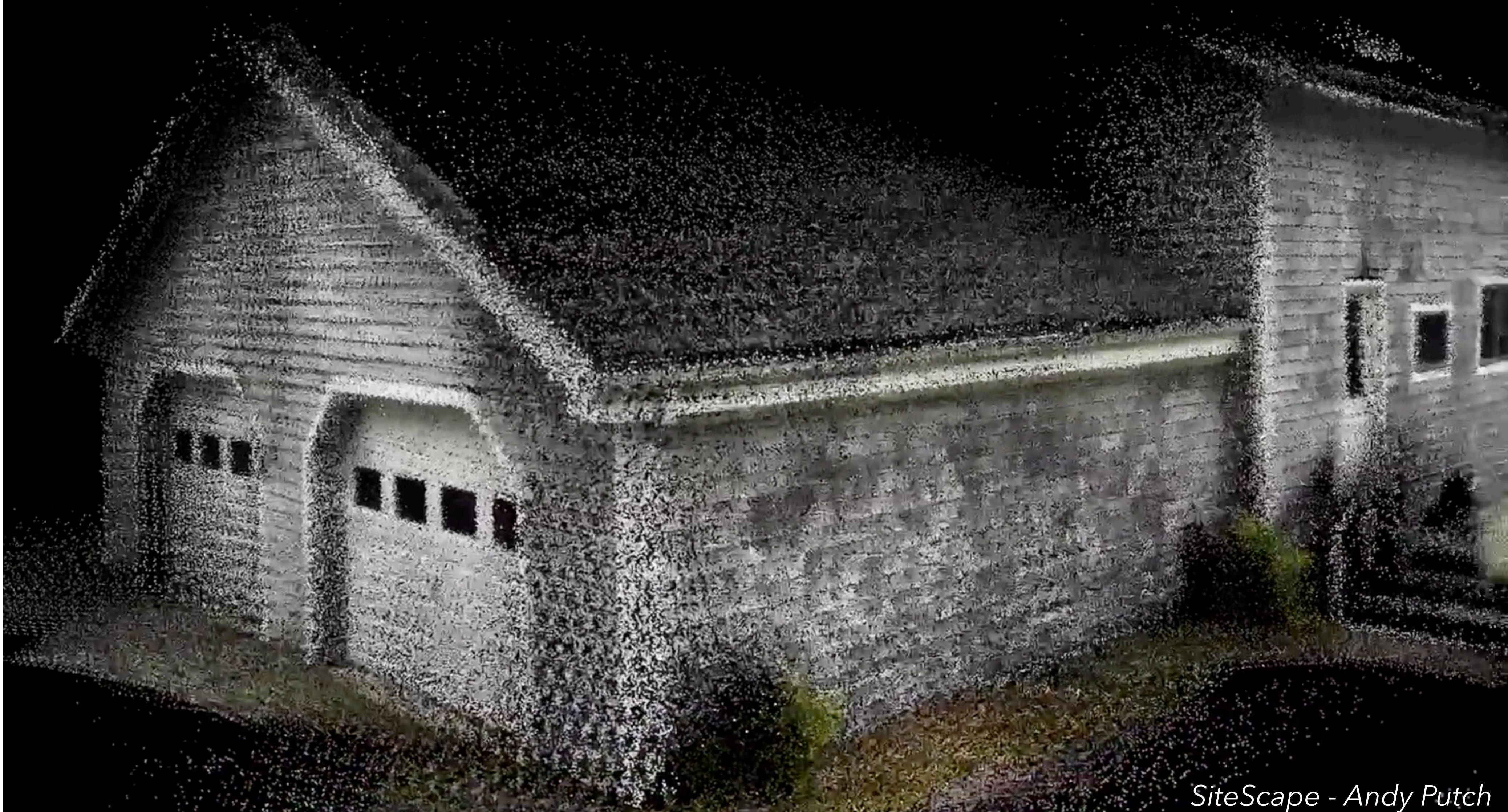
*The Next Leap: How A.I. will change the 3D industry, Andrew Price*

# Depth Sensors



Microsoft Kinect

# iPhone Depth Sensor

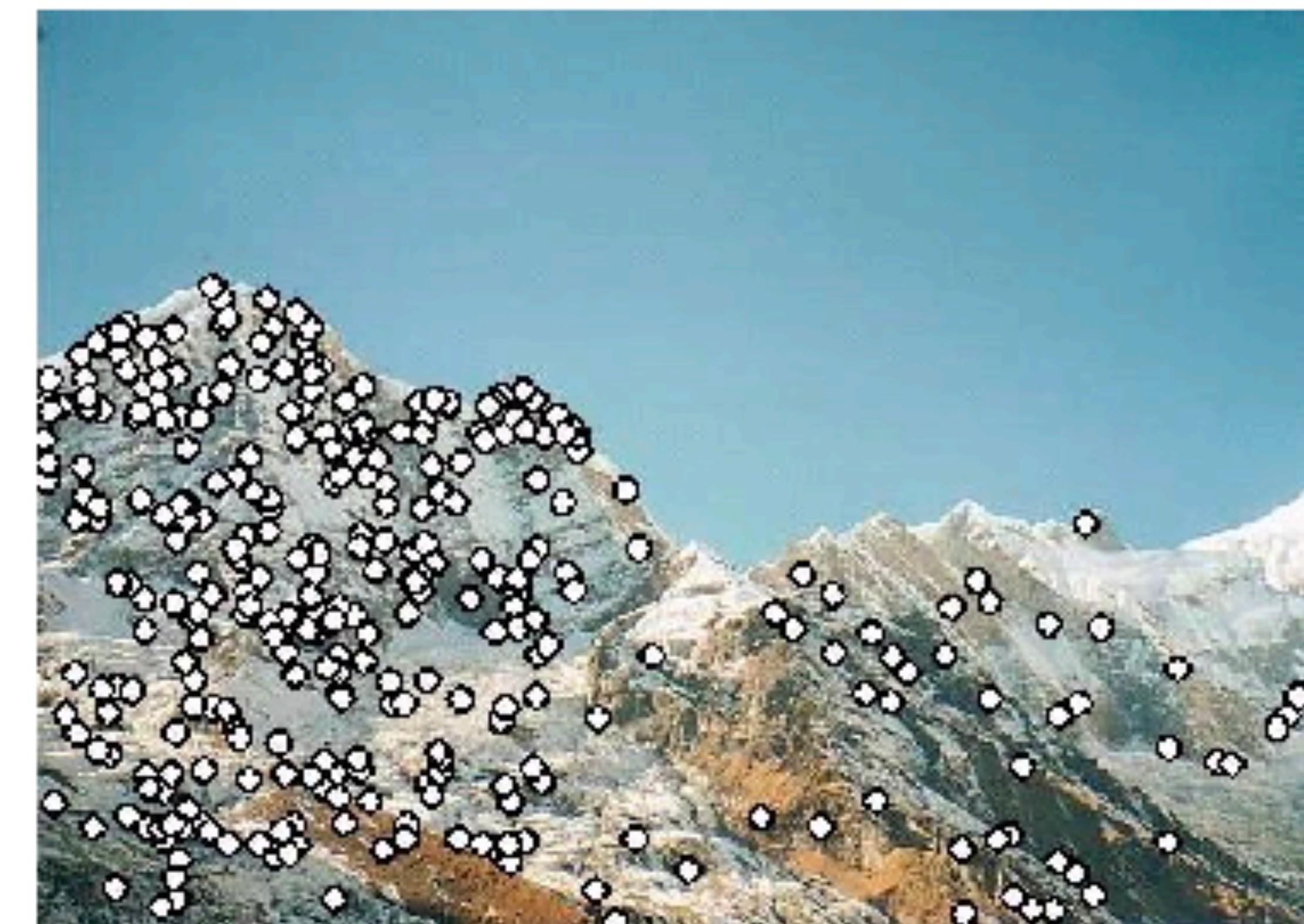
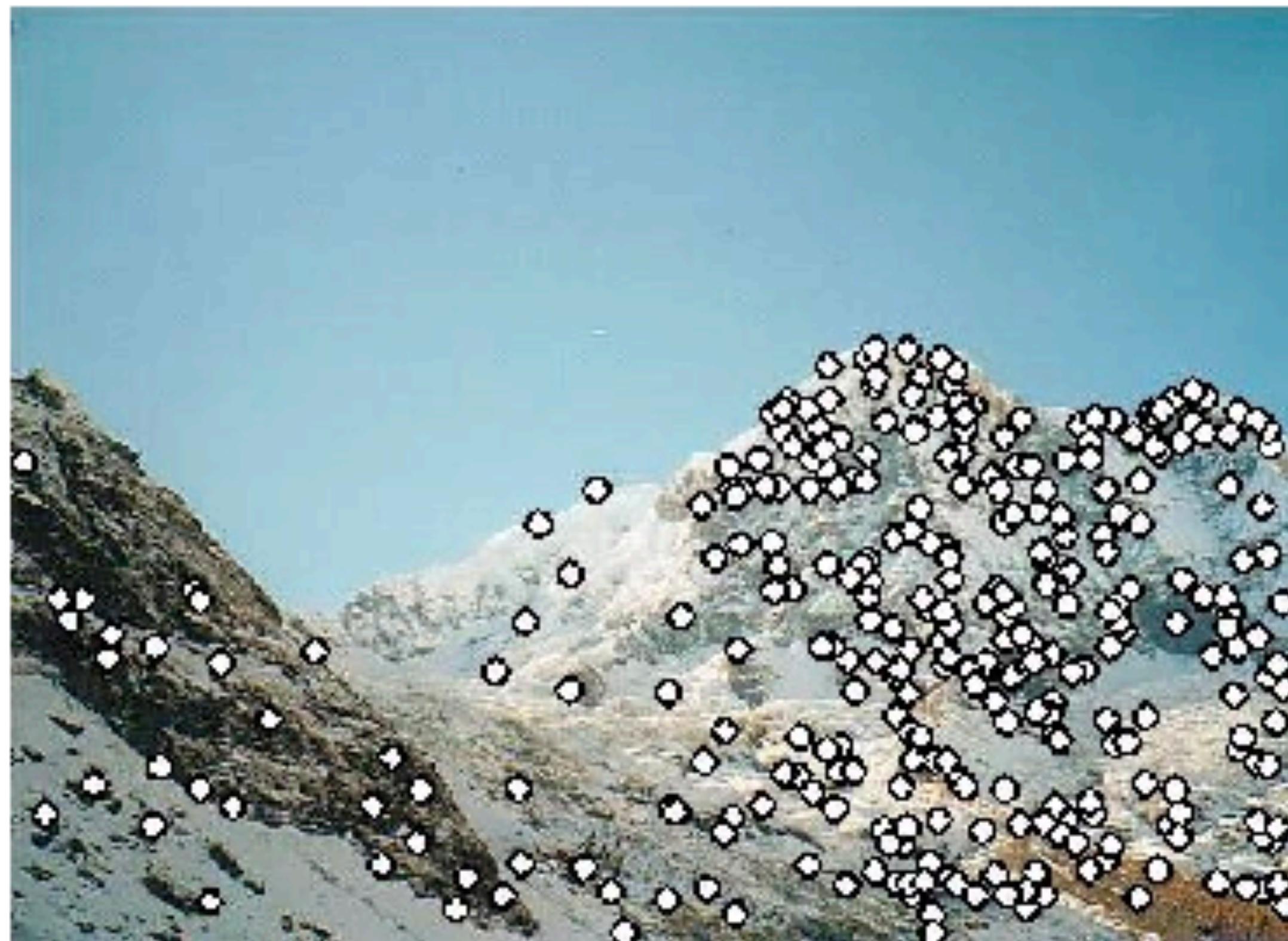


What if you don't have depth?

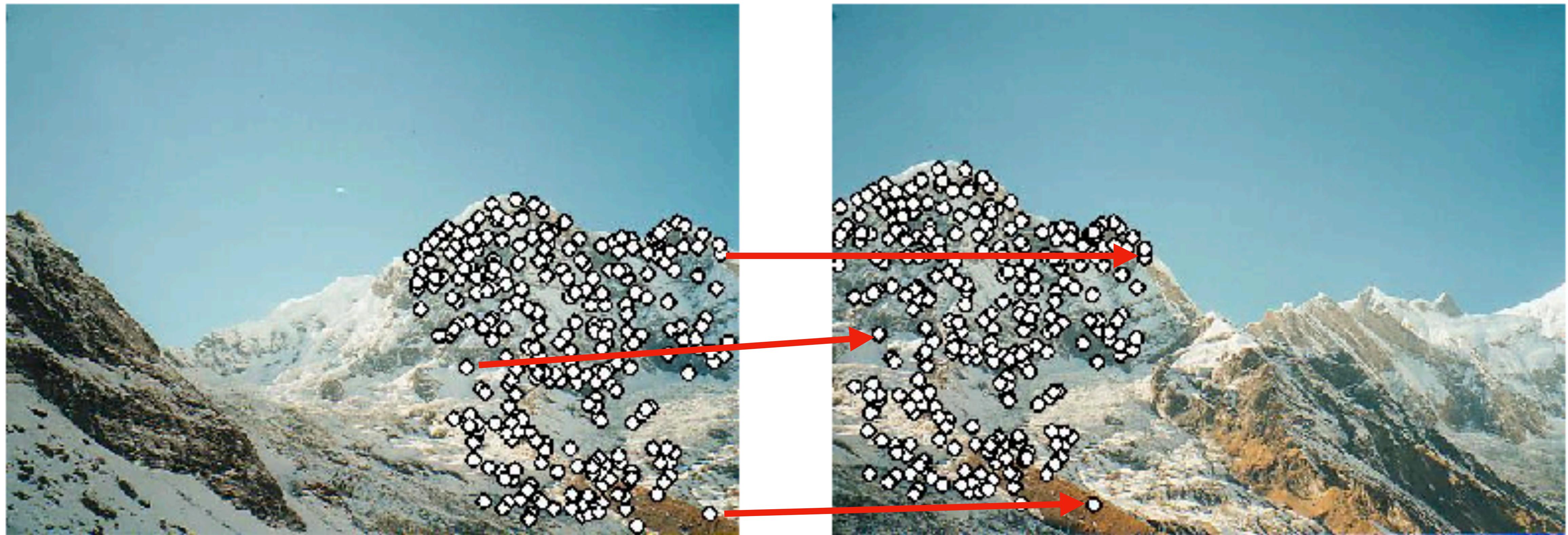
# Point Cloud from Images



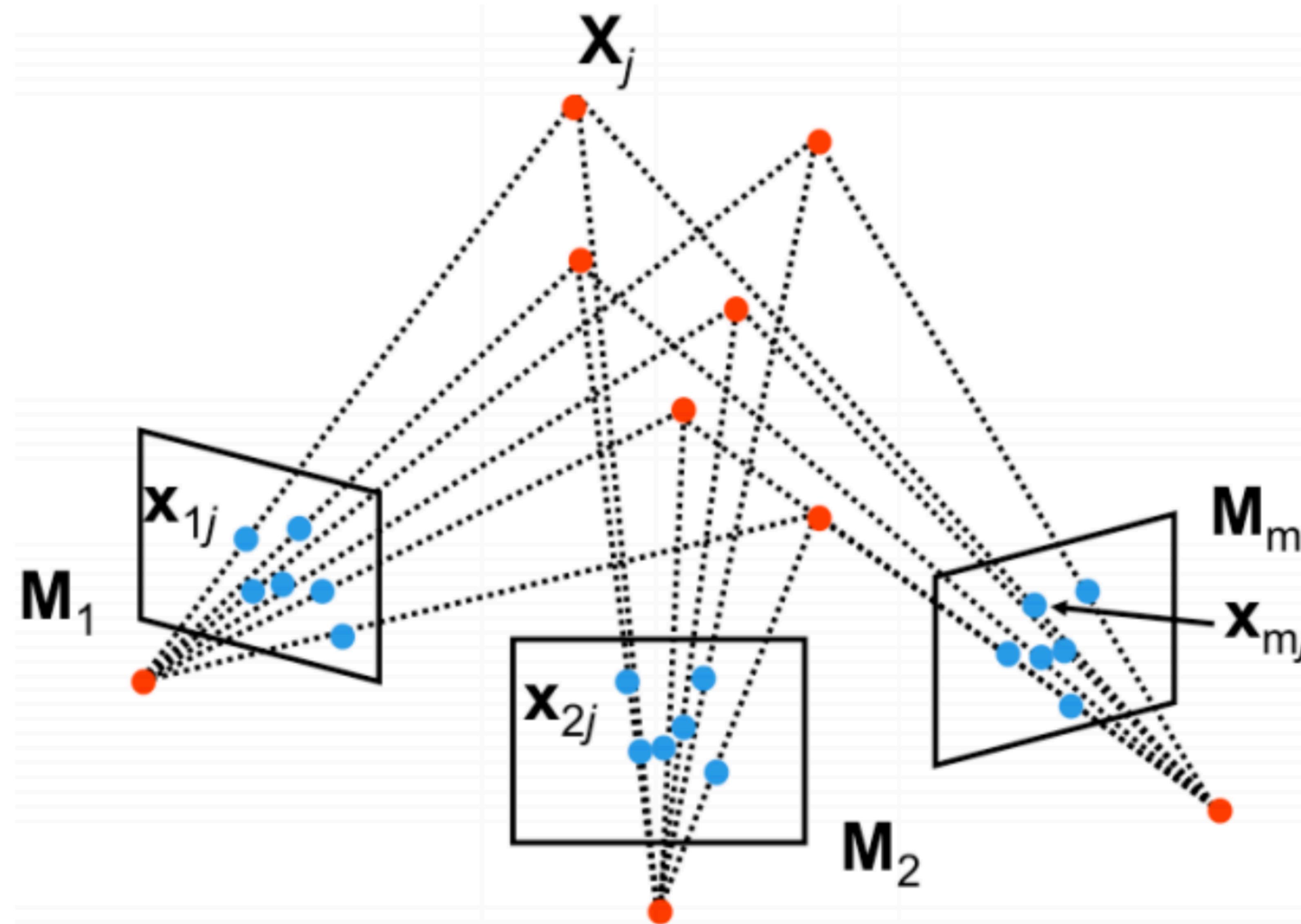
# Point Cloud from Images



# Point Cloud from Images

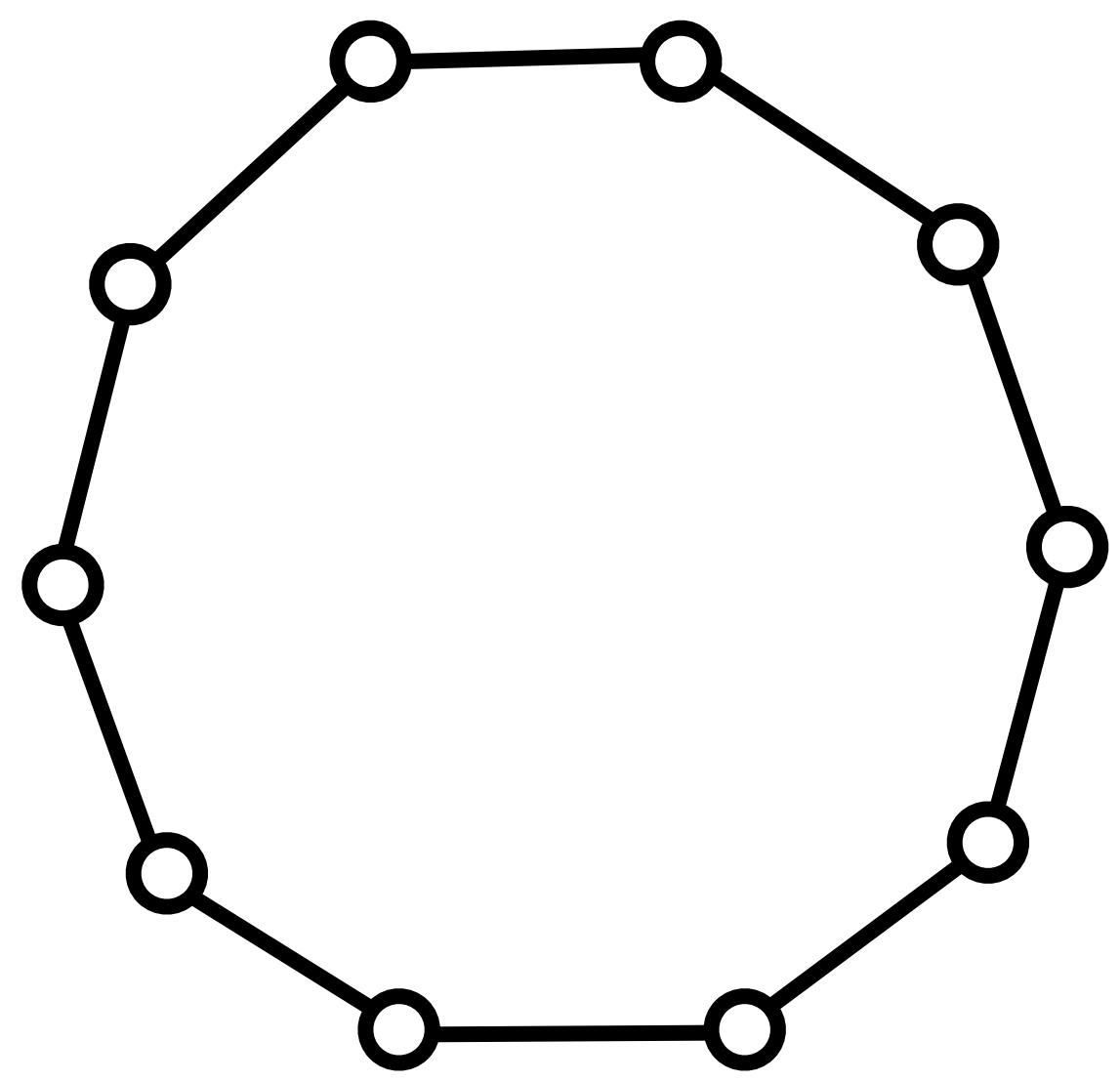


# Point Cloud from Images

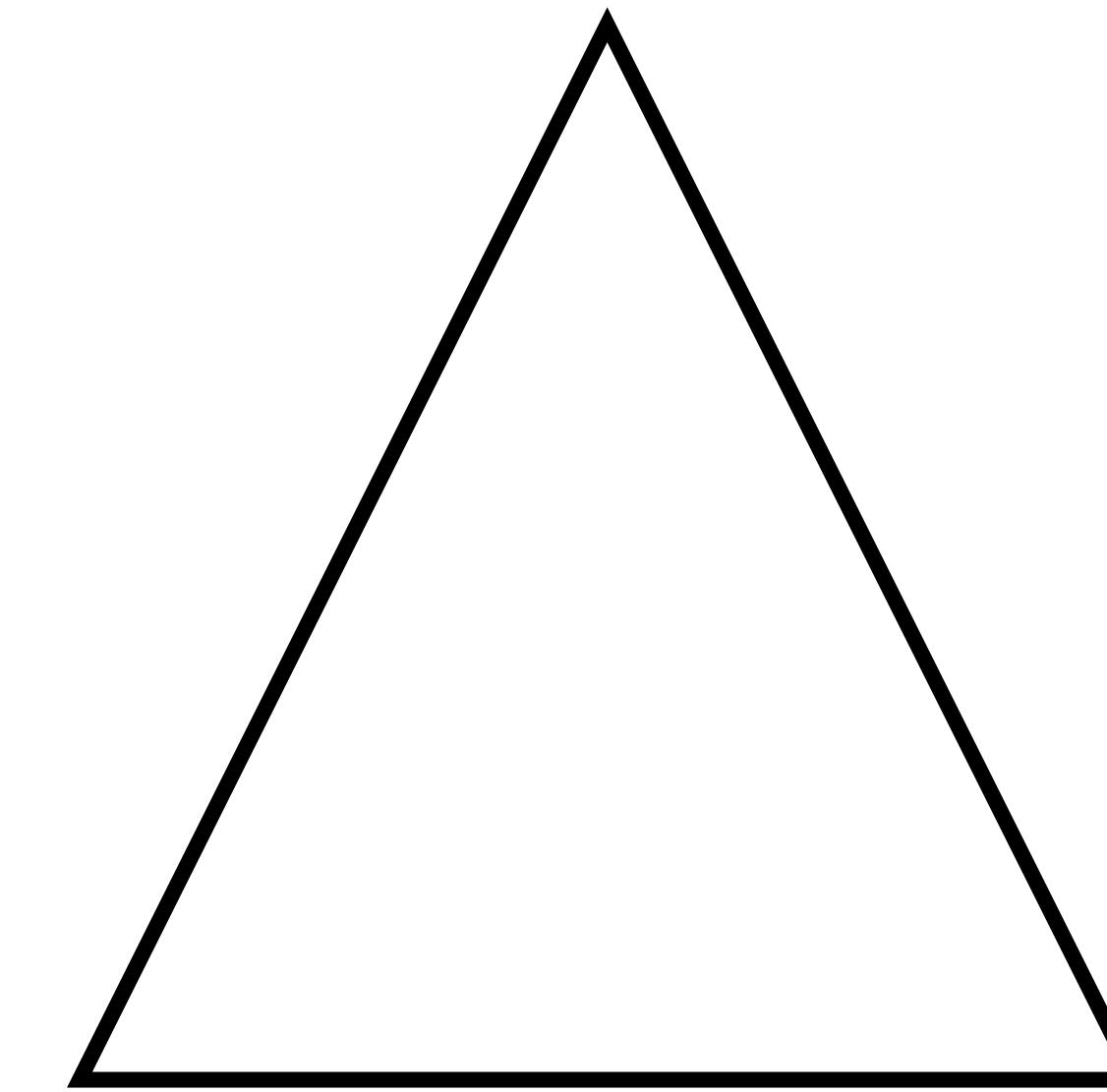


Can we operate on the geometry directly?

# Gradient Based Optimization

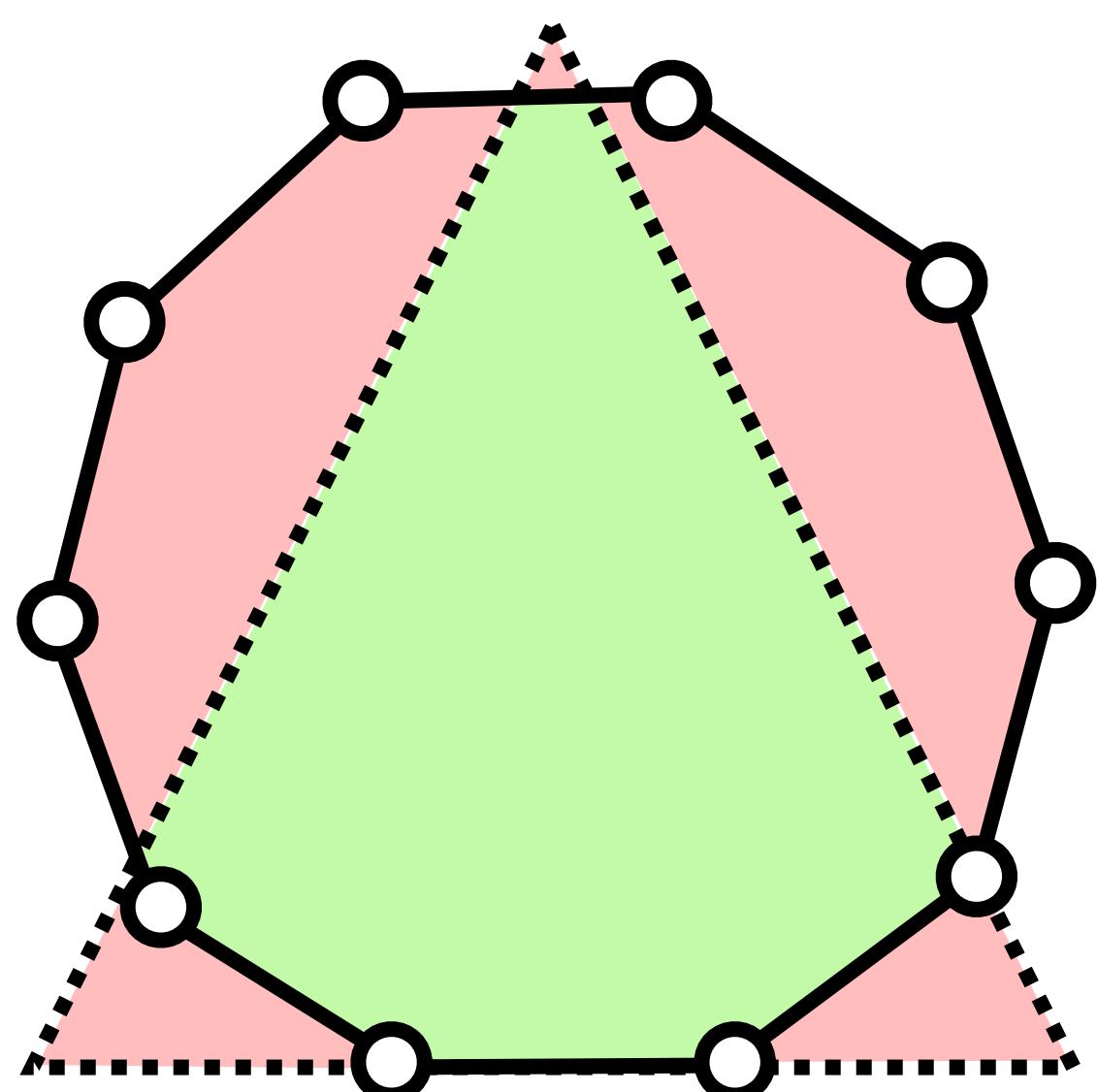


Initial Geometry

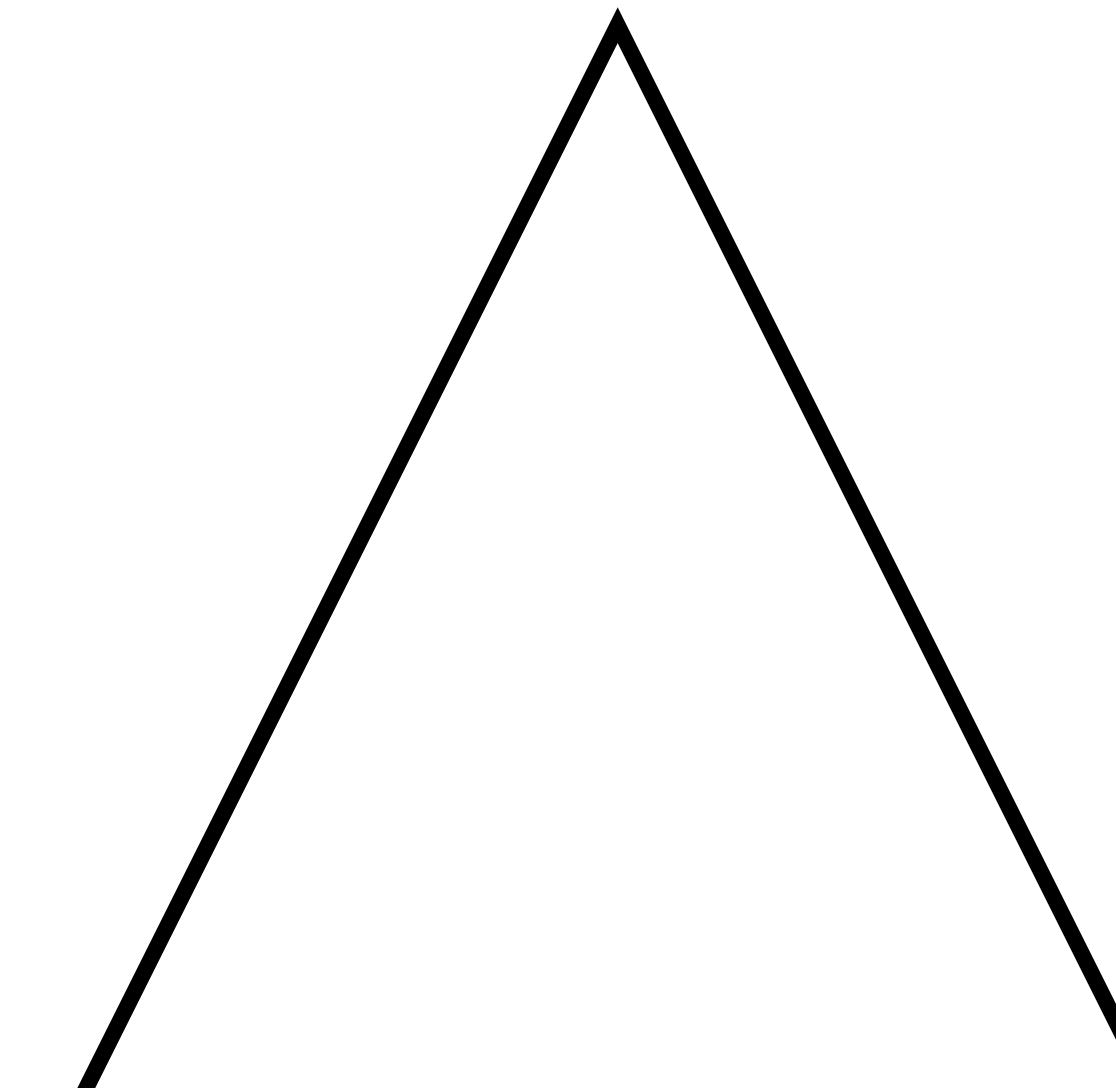


Target Geometry

# Gradient Based Optimization

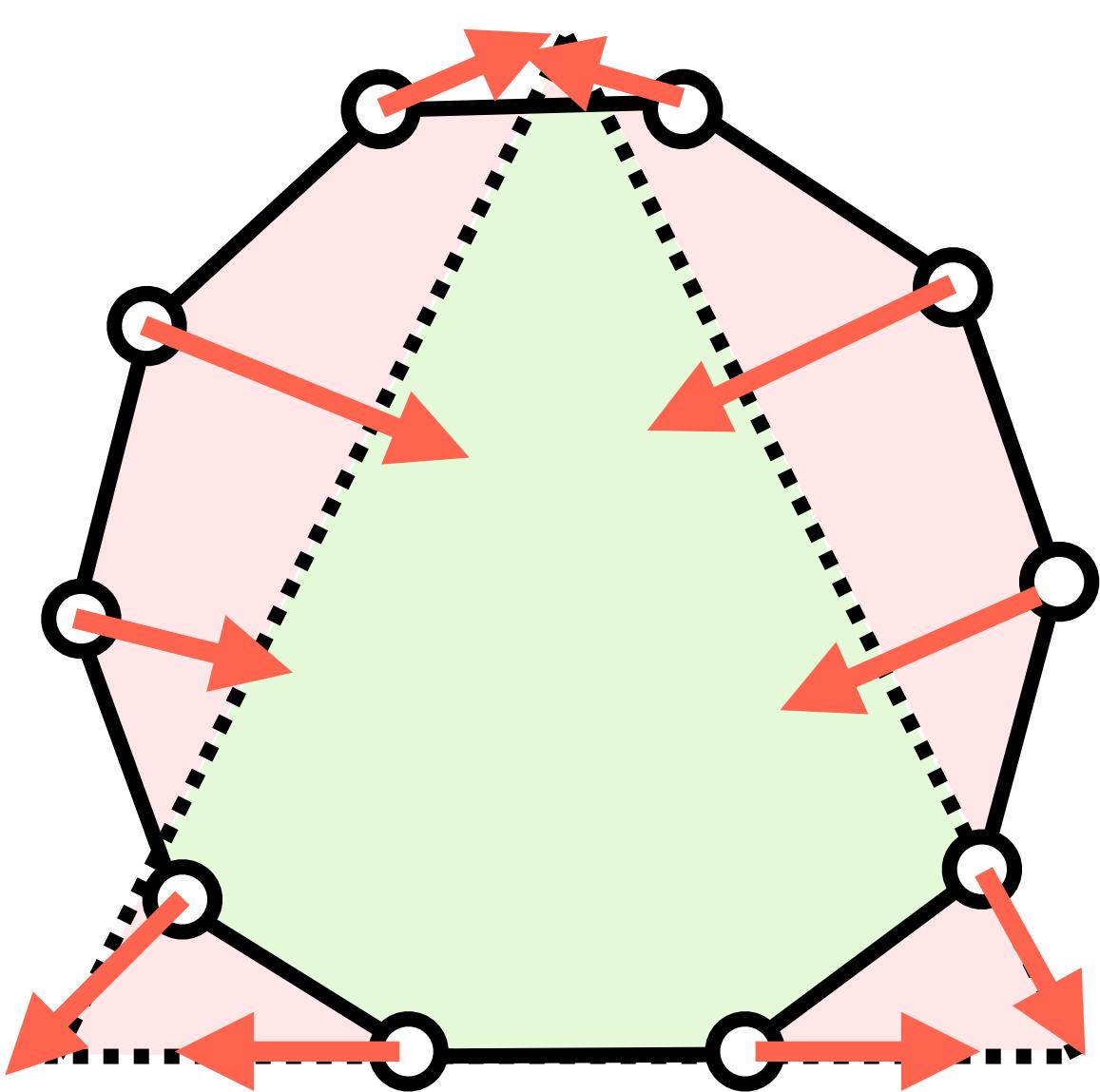


Compute Gradients

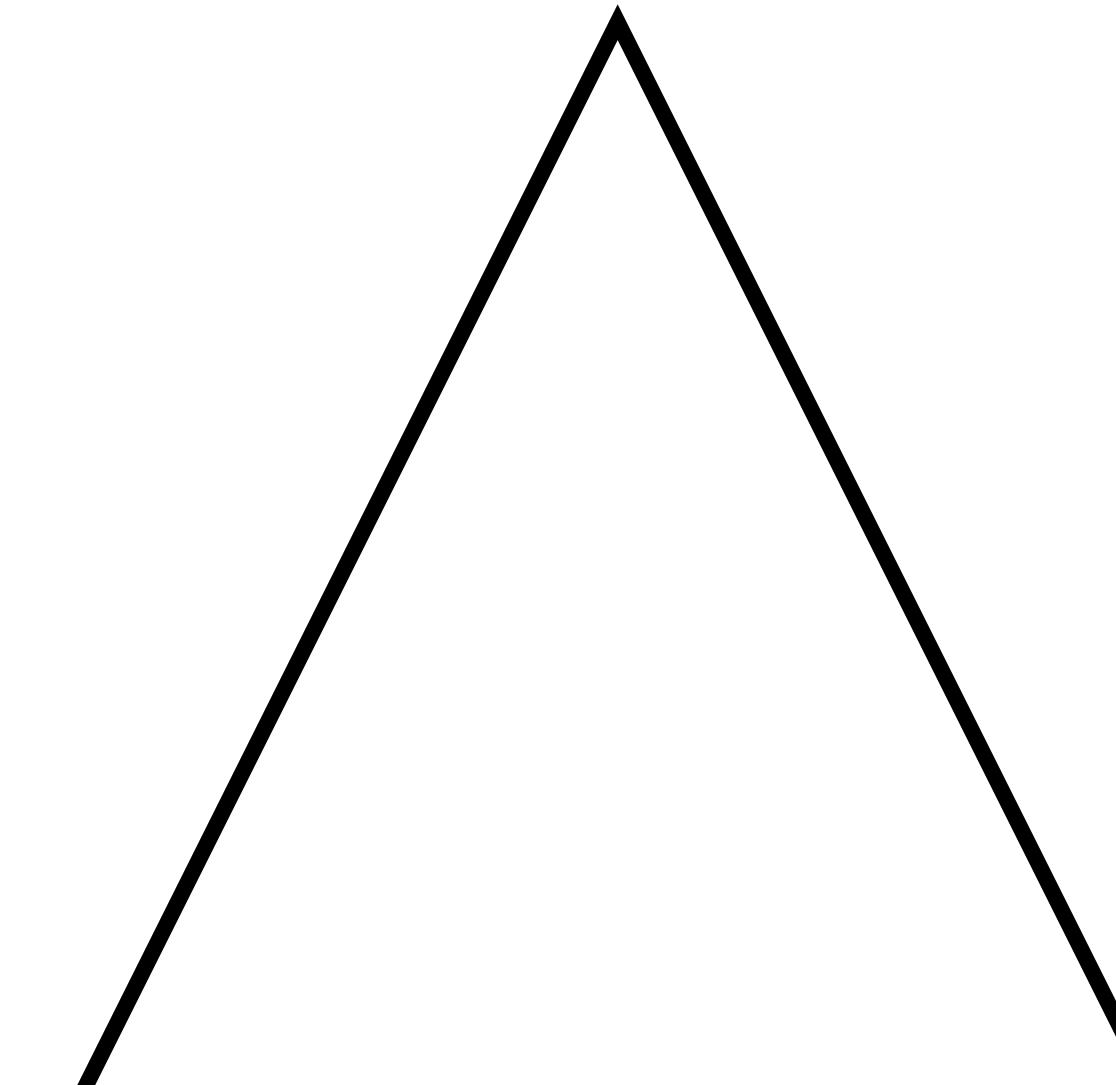


Target Geometry

# Gradient Based Optimization

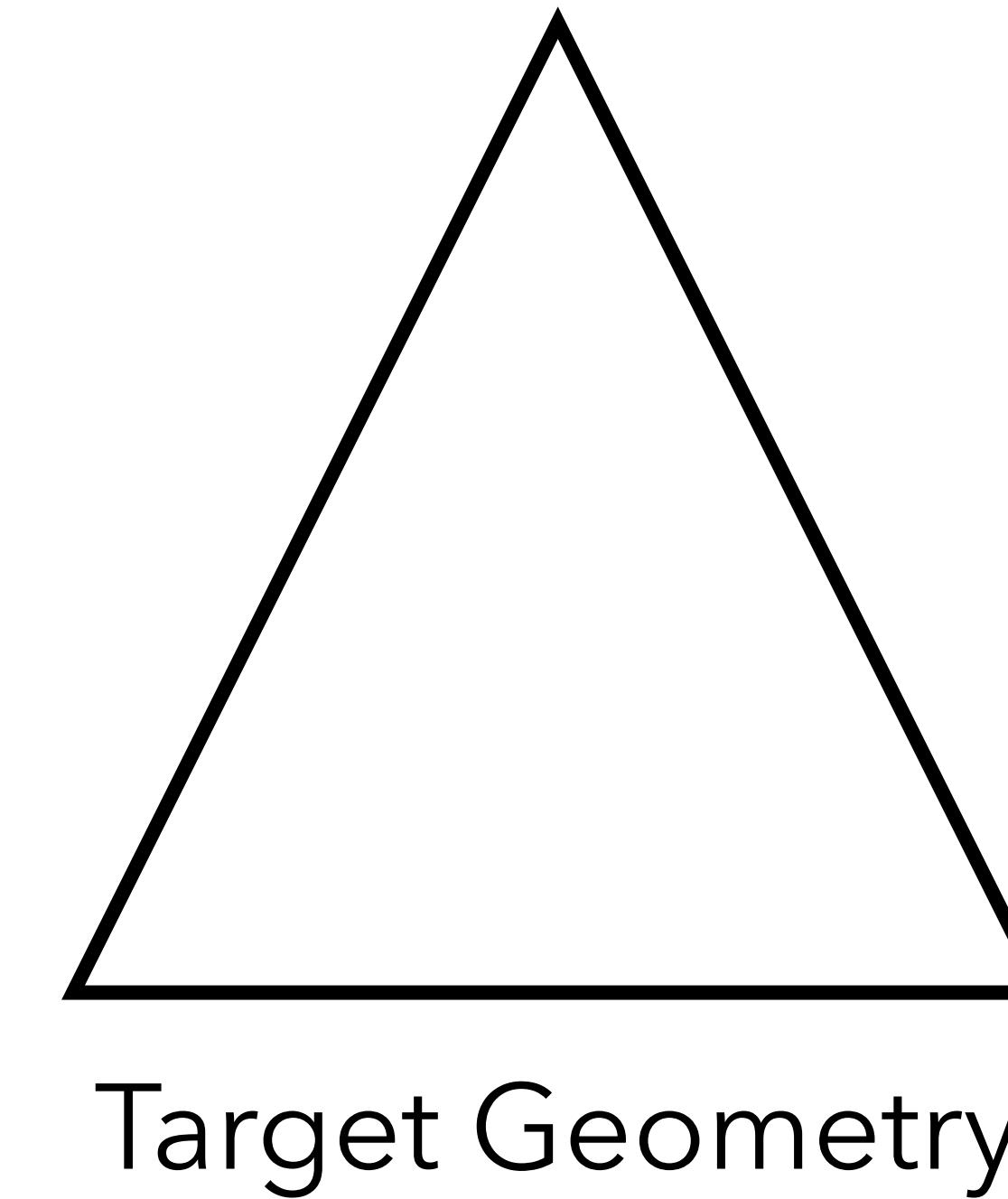
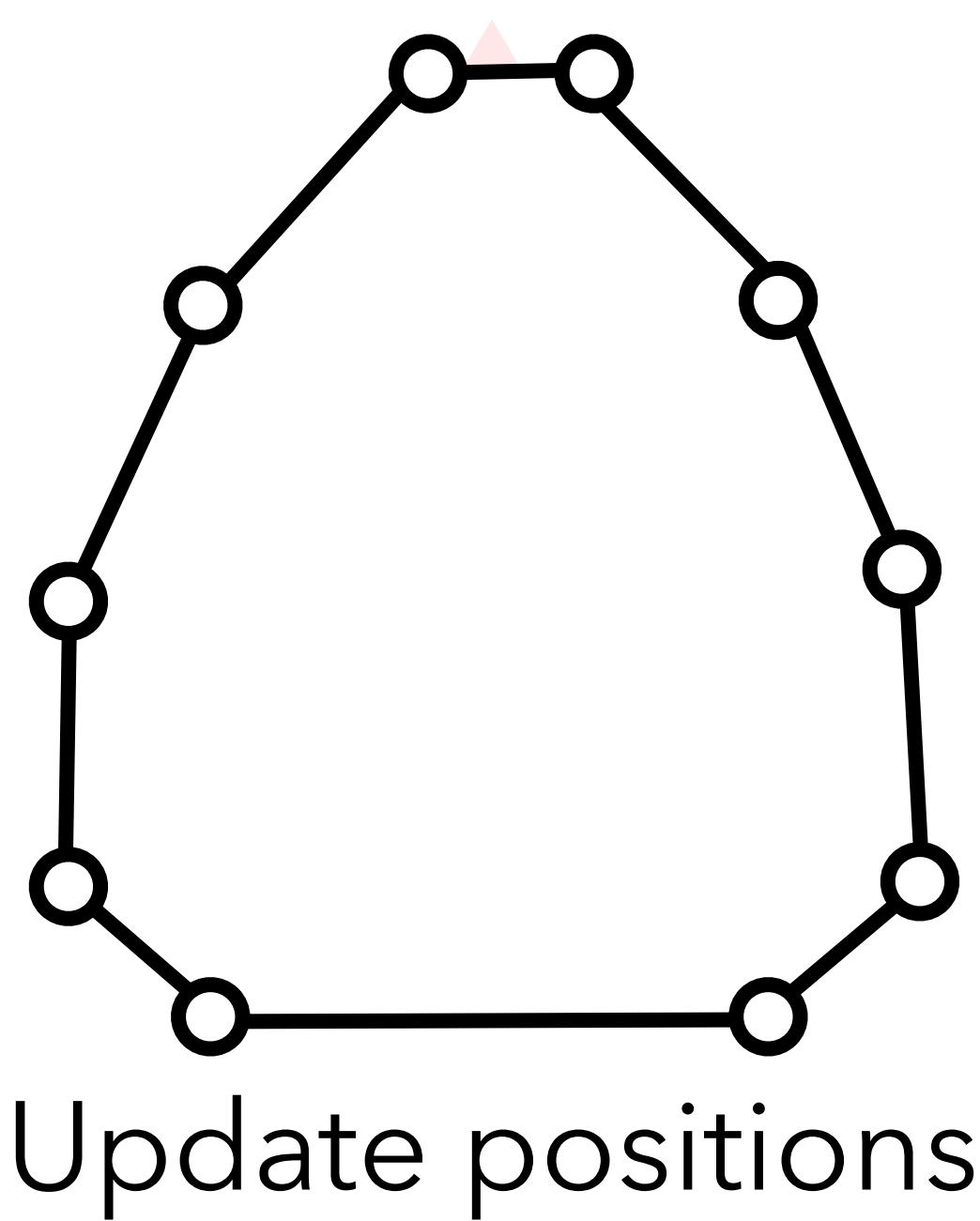


Compute Gradients

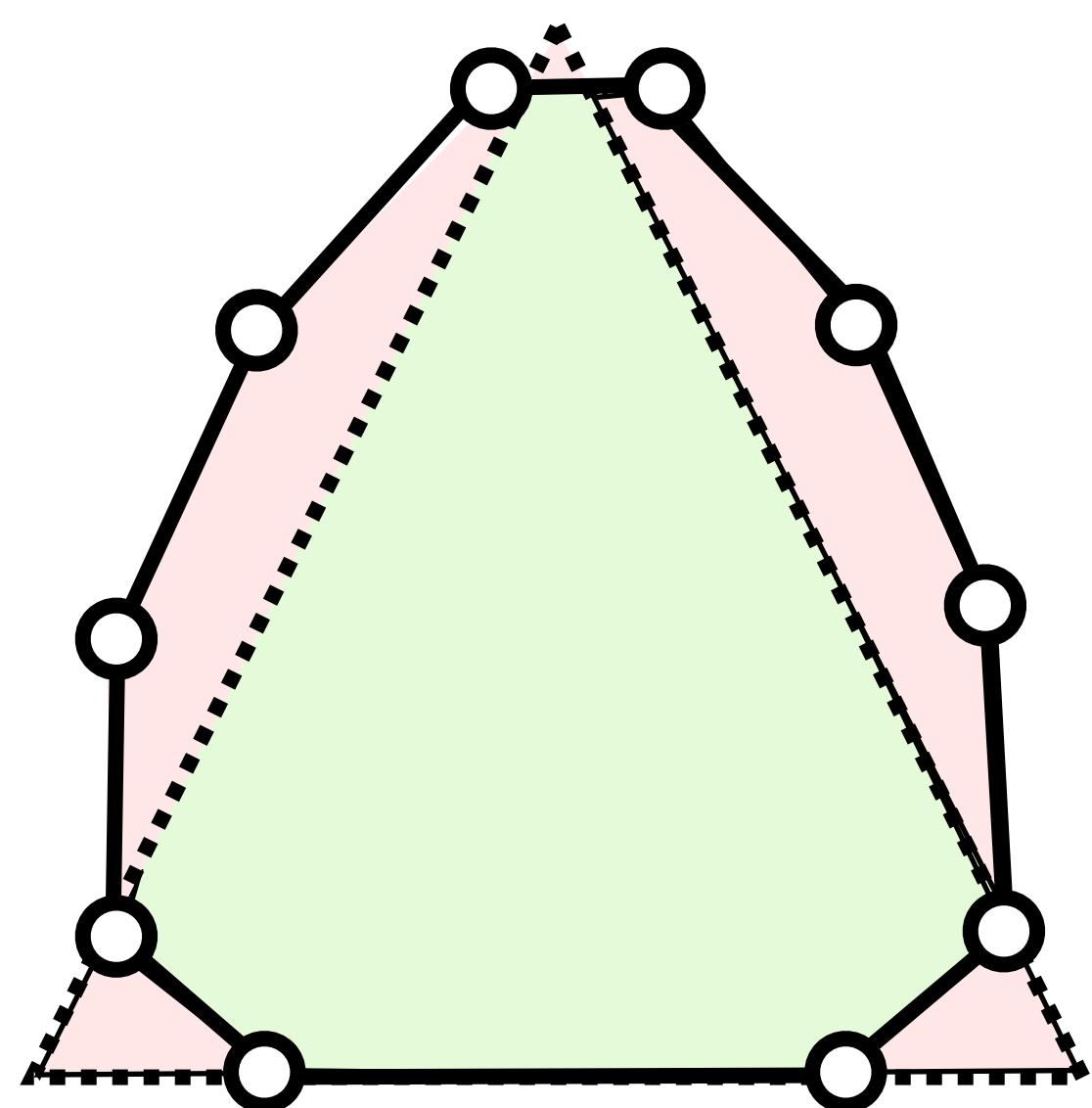


Target Geometry

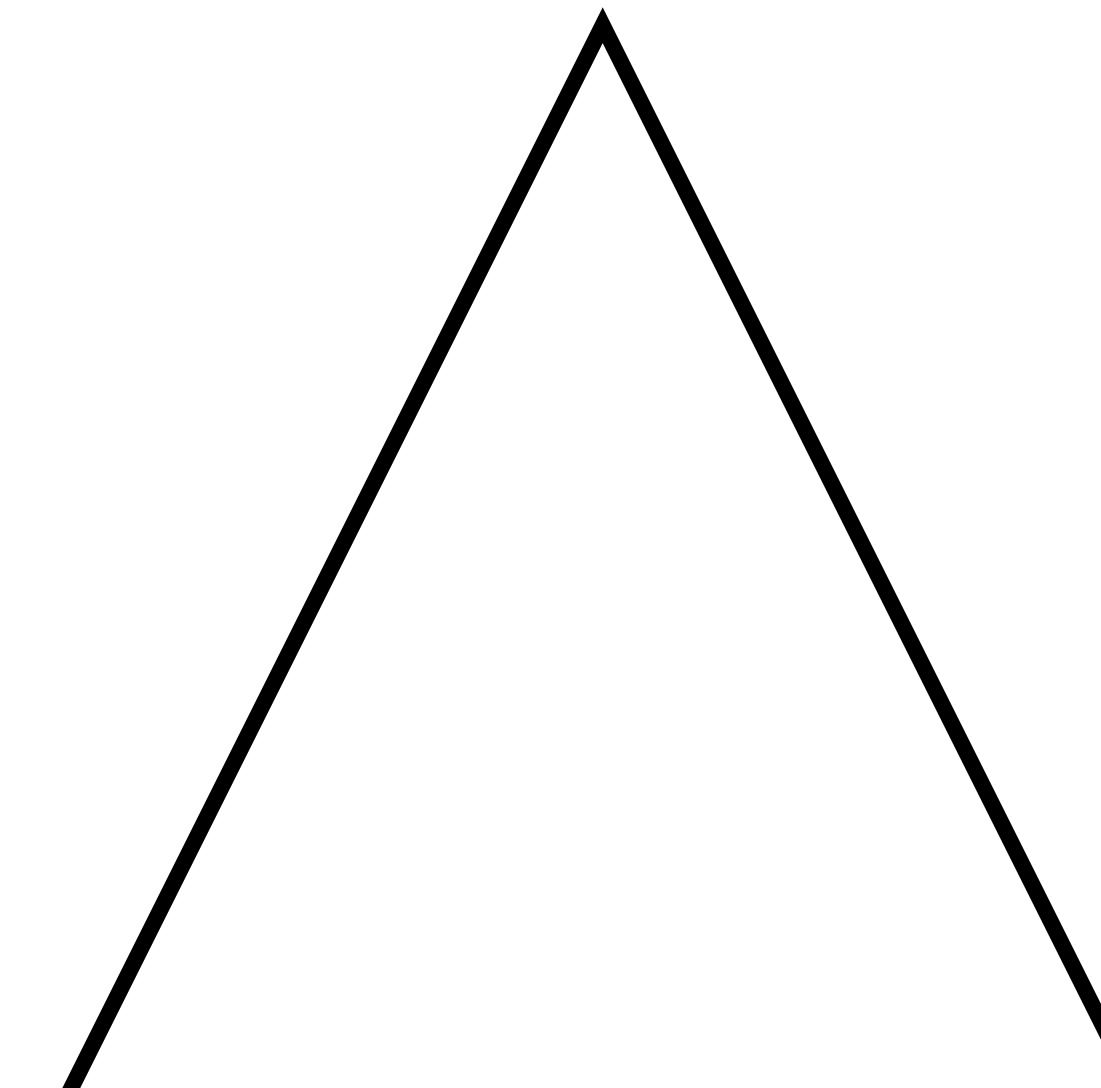
# Gradient Based Optimization



# Gradient Based Optimization

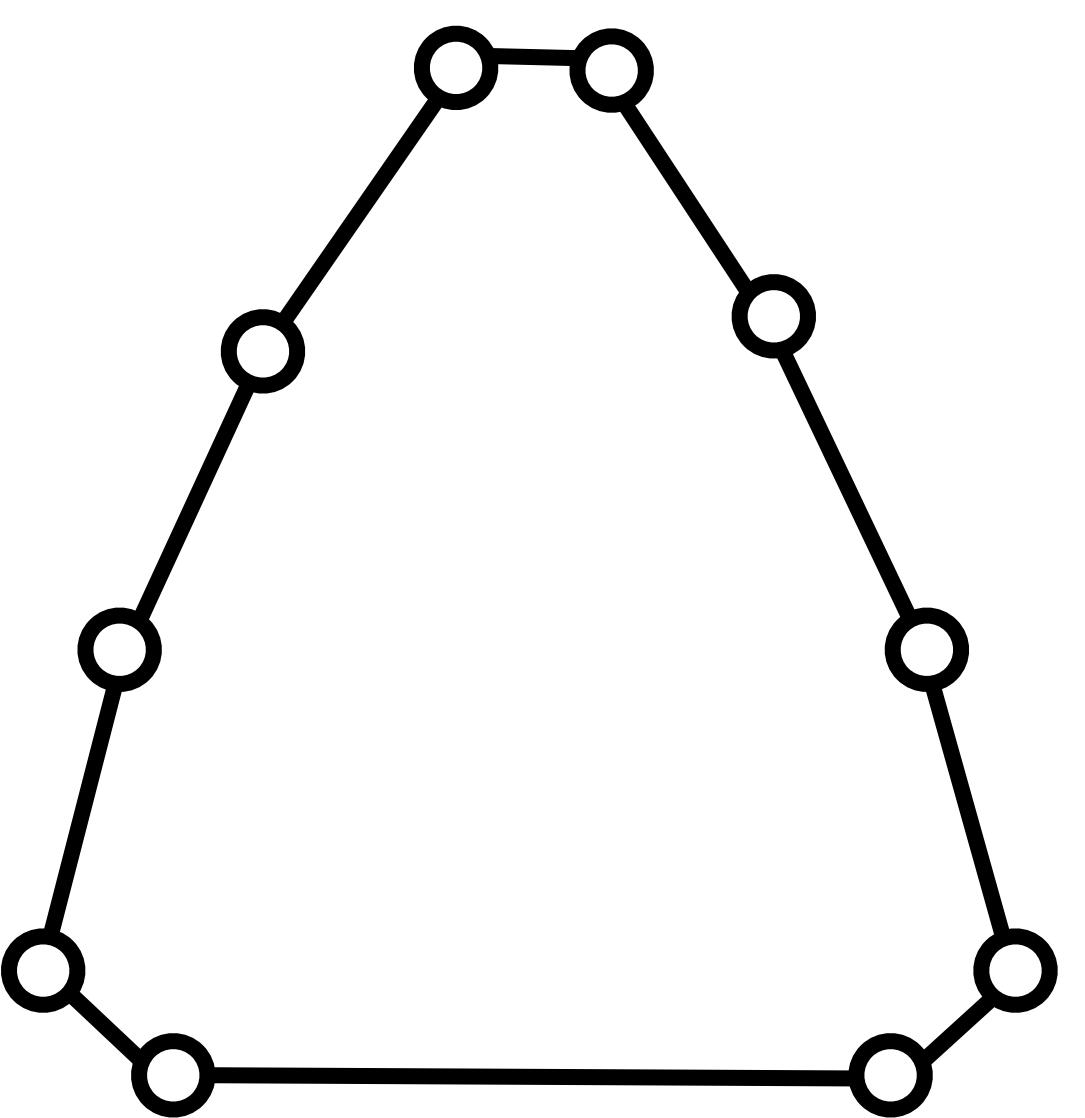


Compute New Error

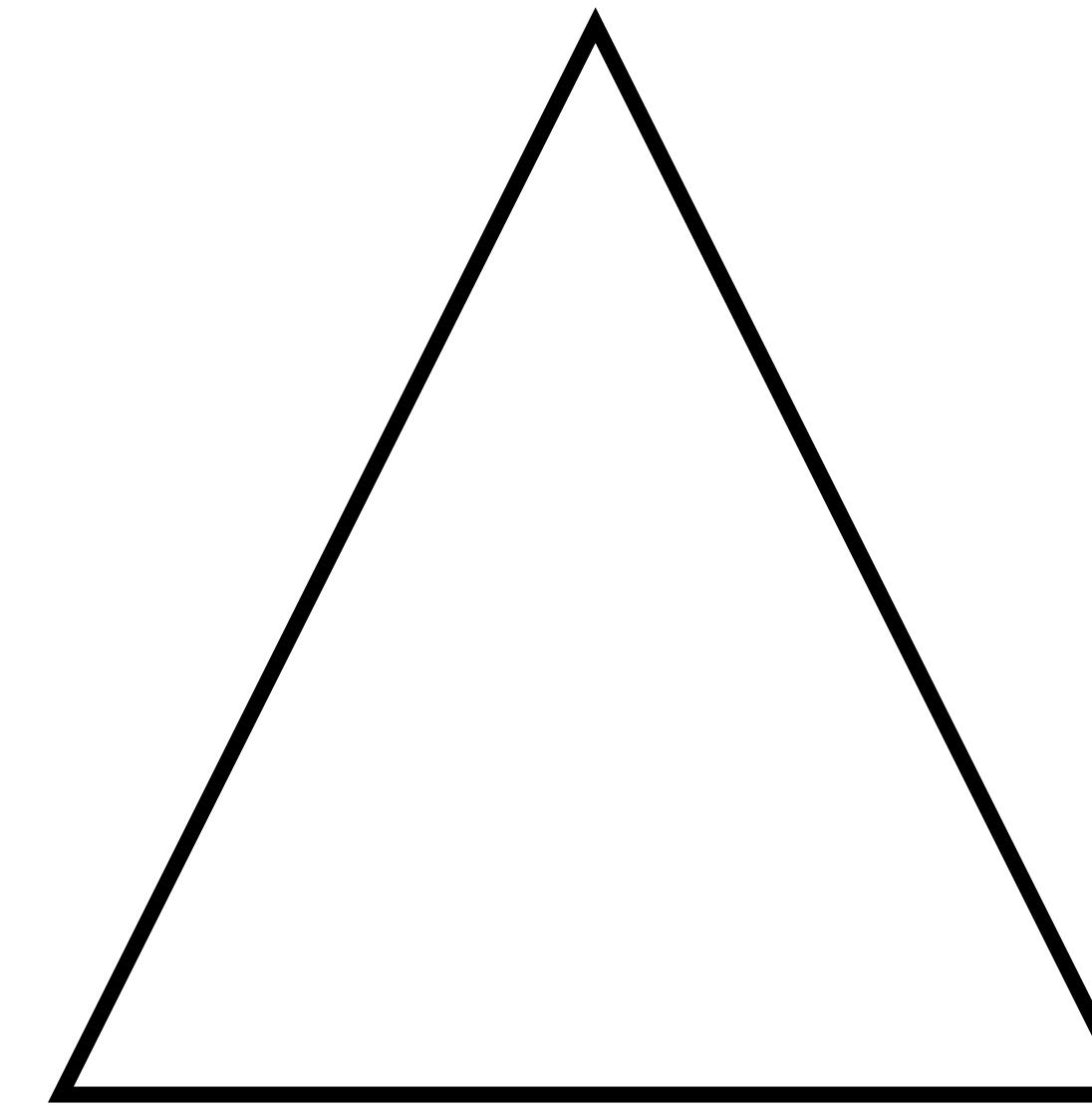


Target Geometry

# Gradient Based Optimization

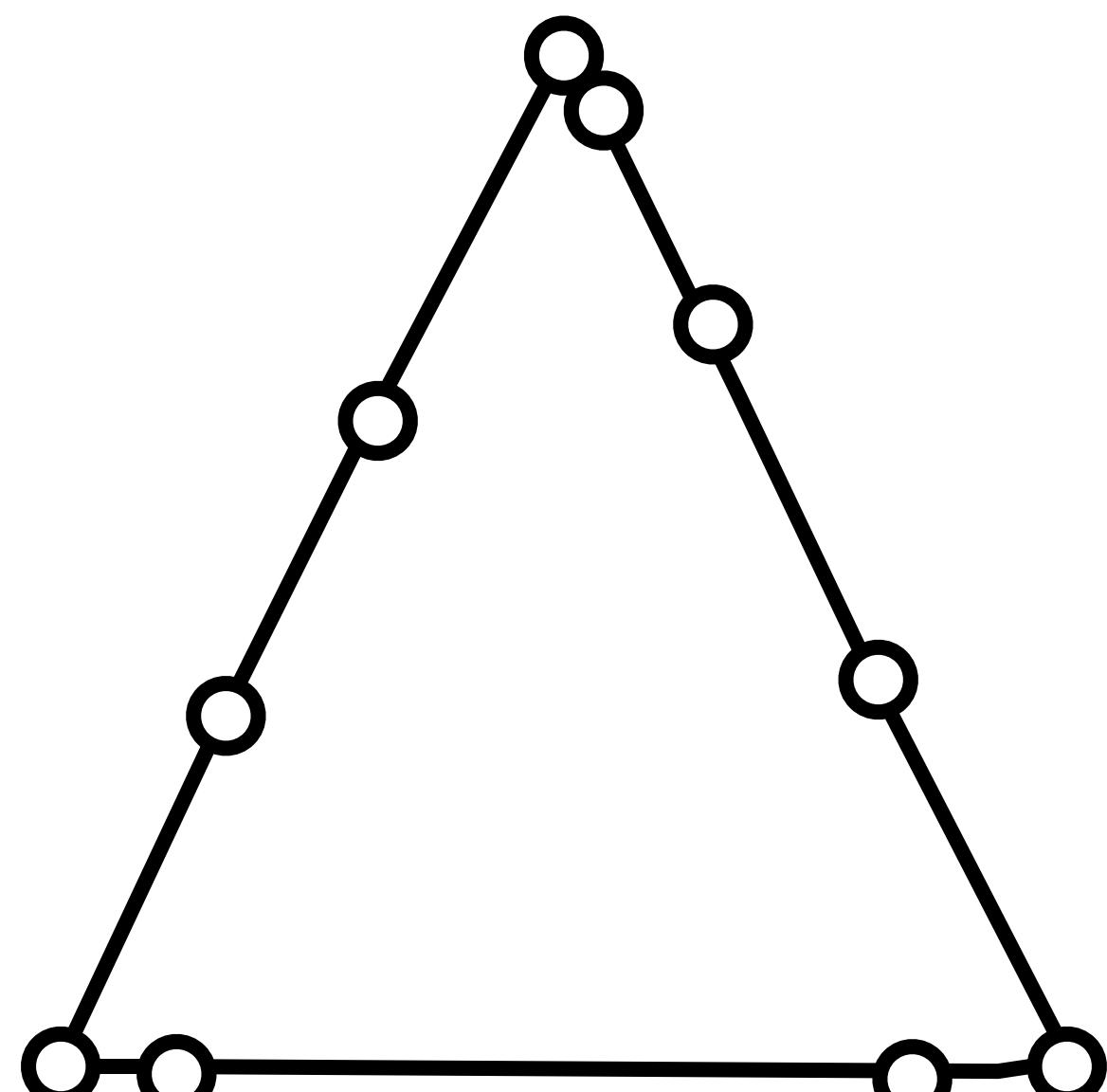


Repeat

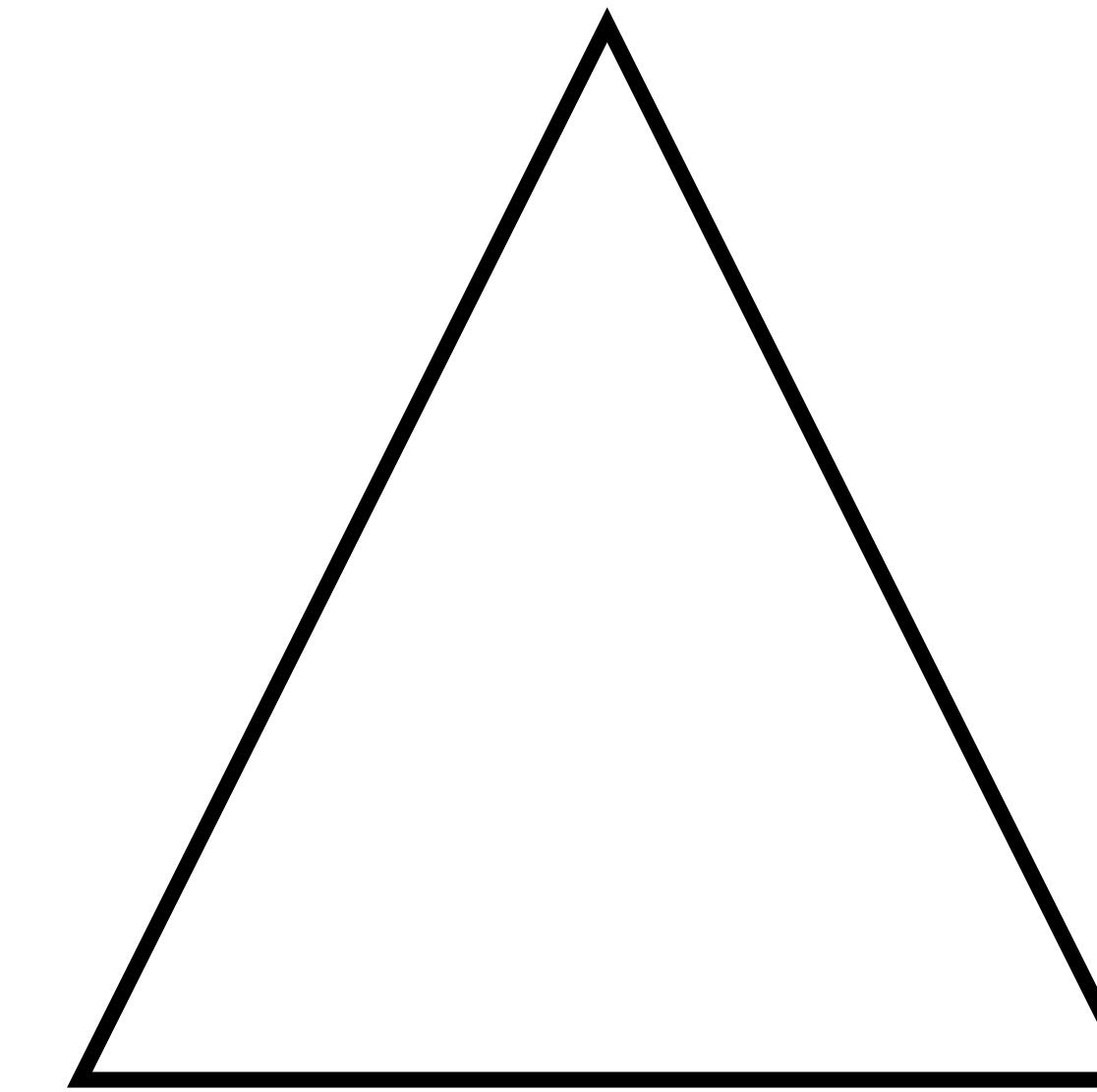


Target Geometry

# Gradient Based Optimization

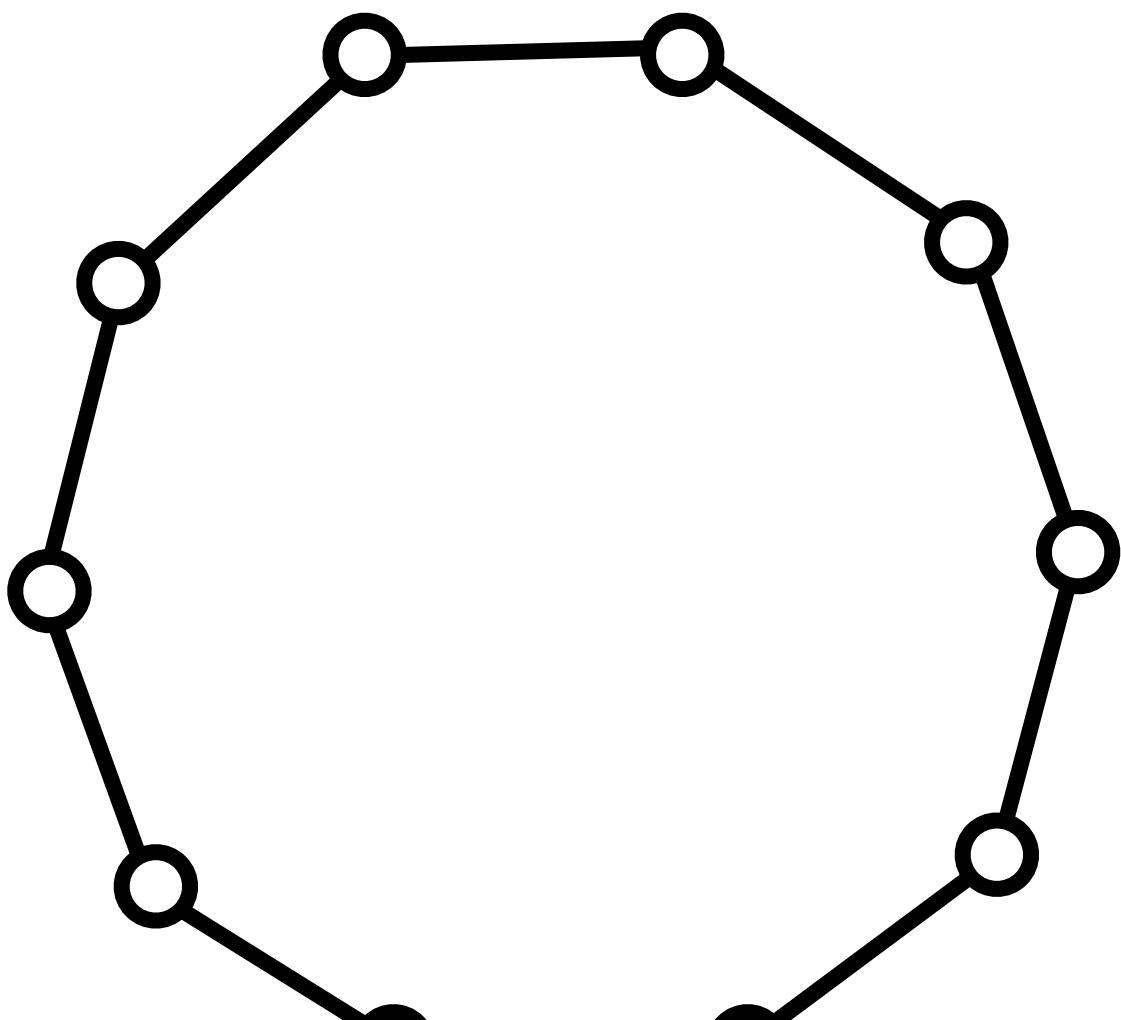


# Repeat

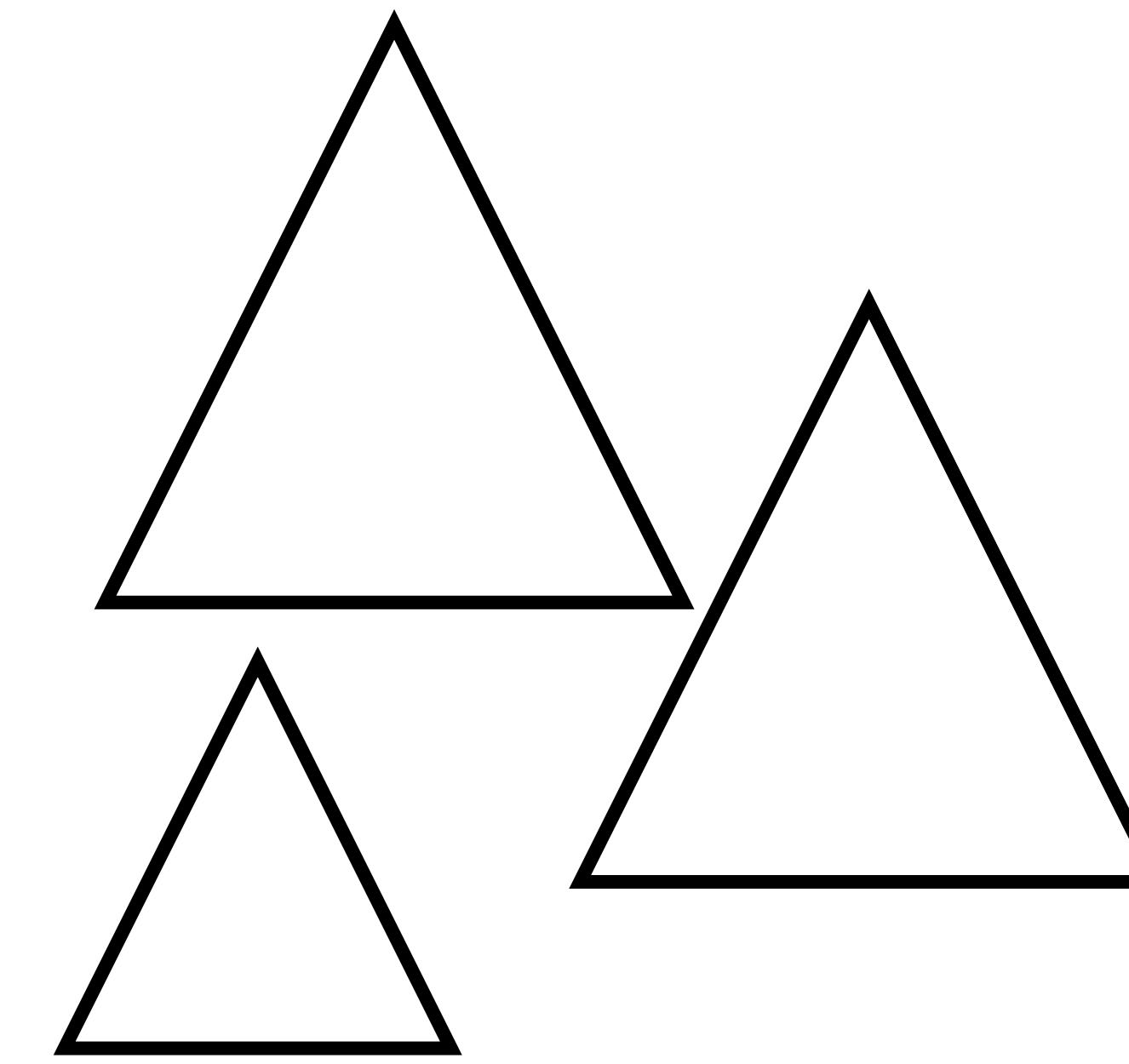


# Target Geometry

# Gradient Based Optimization

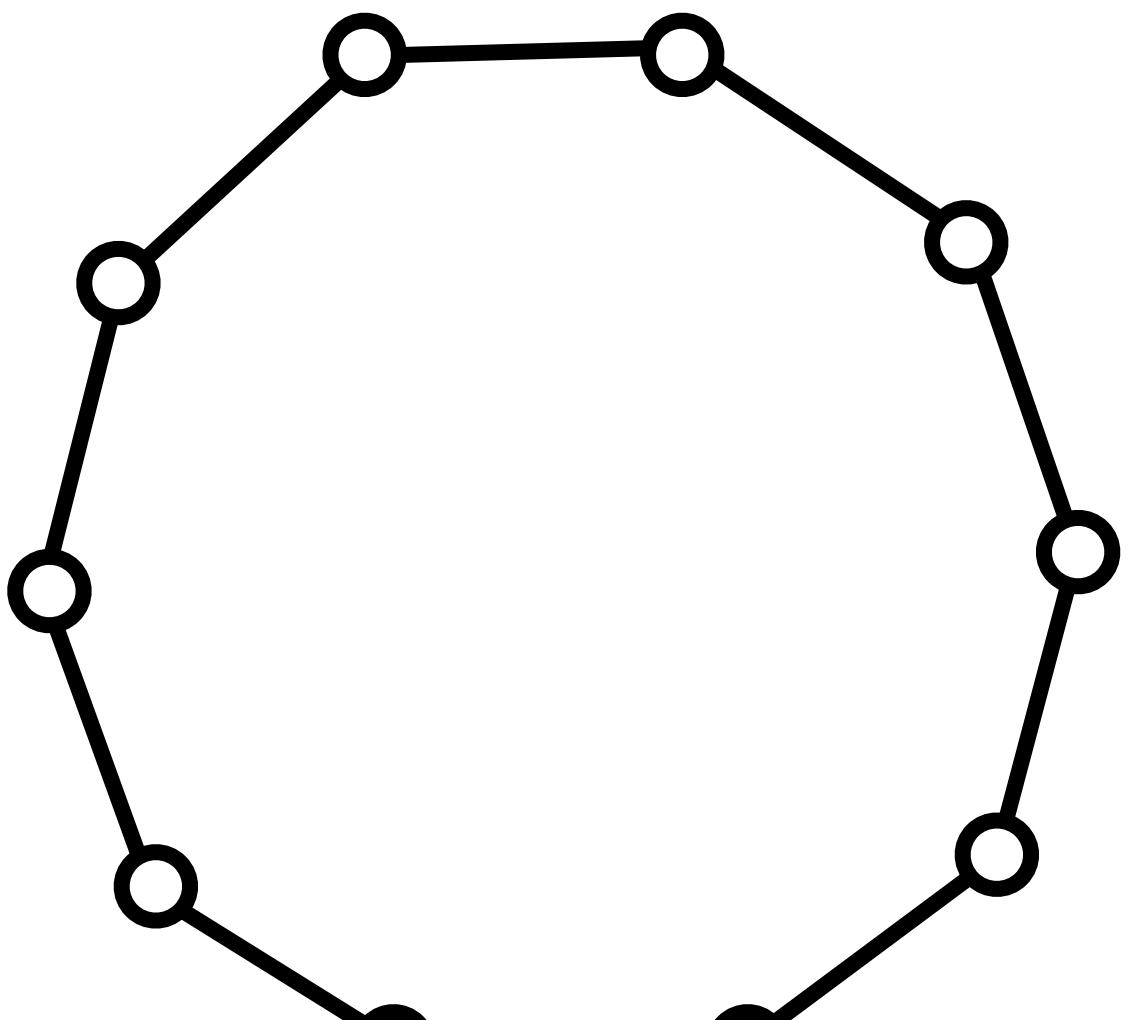


Initial Geometry

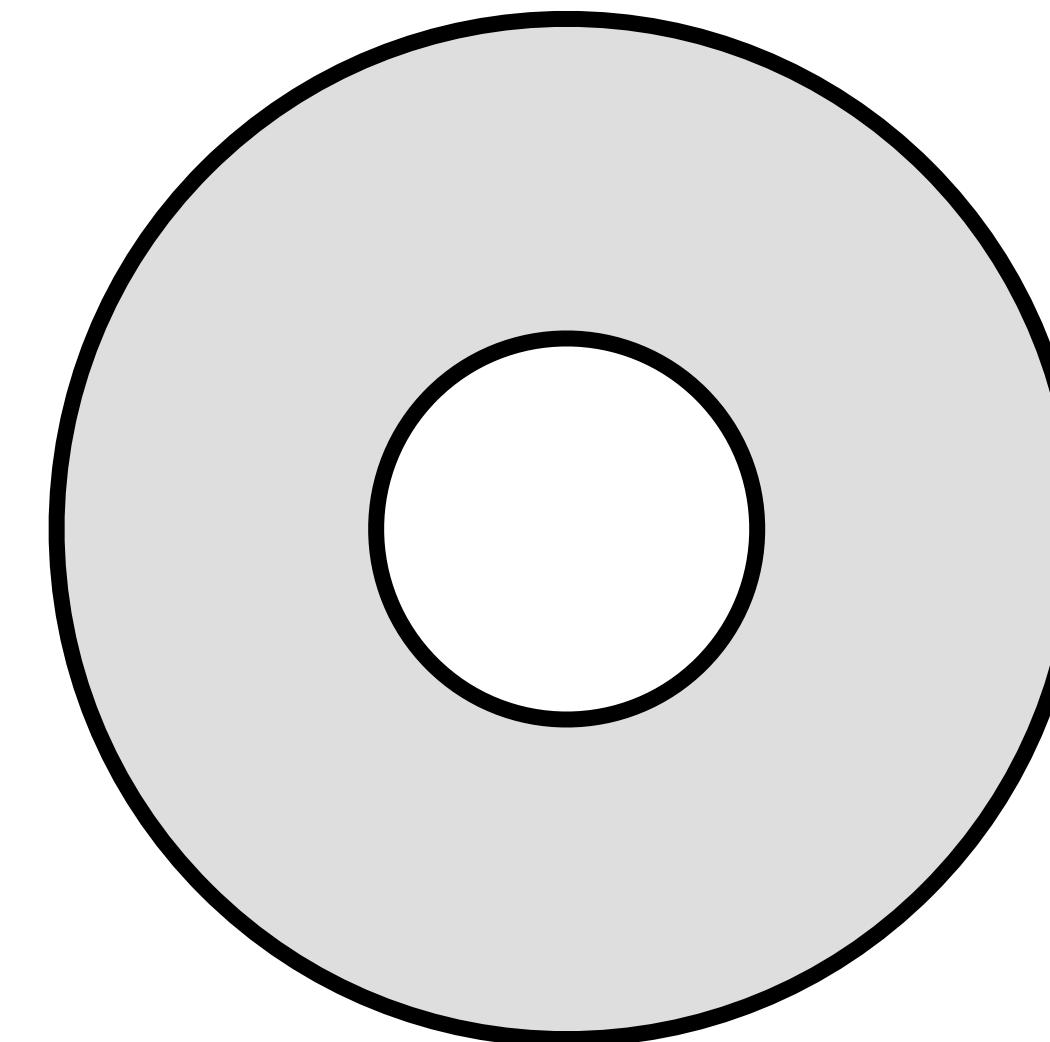


Target Geometry

# Gradient Based Optimization

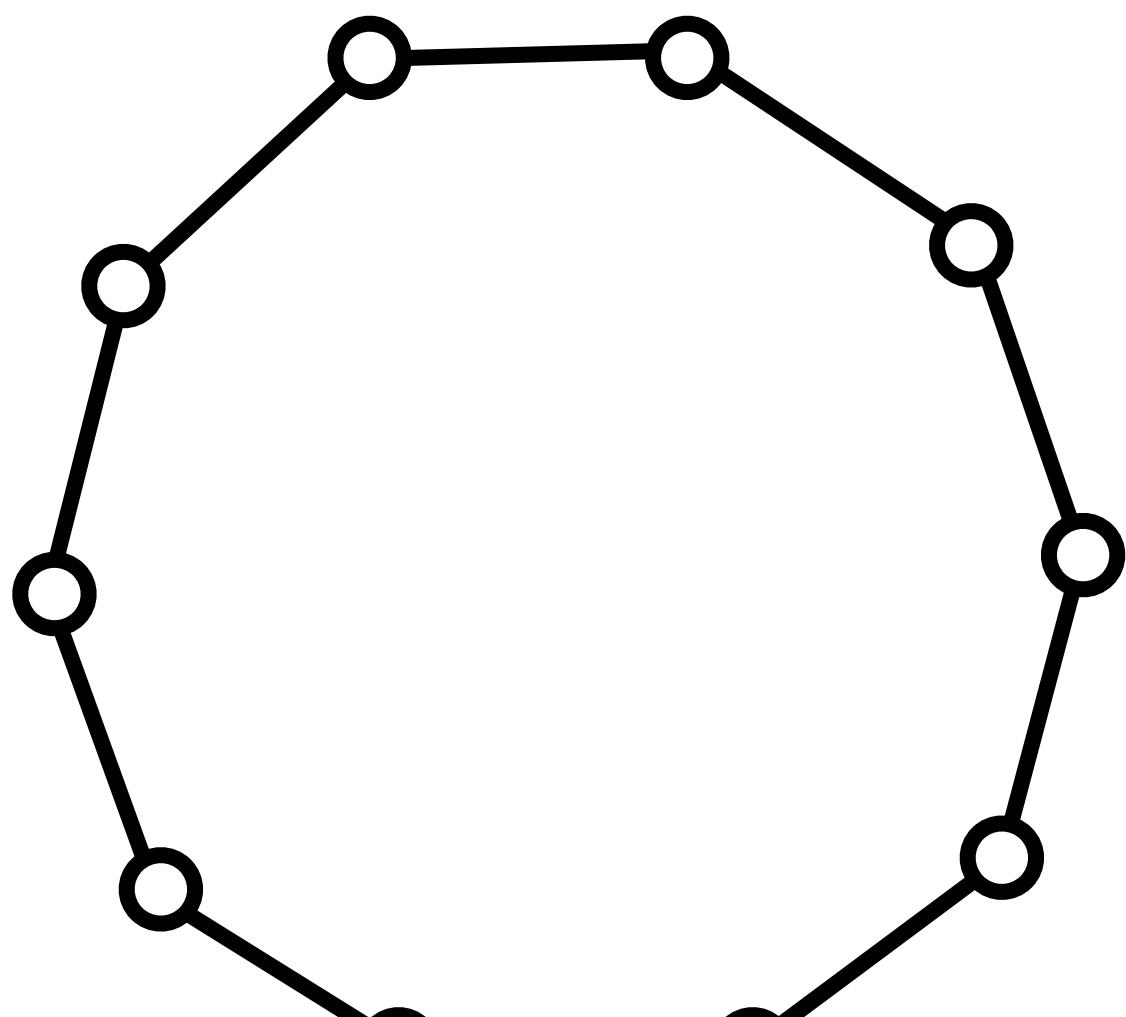


Initial Geometry

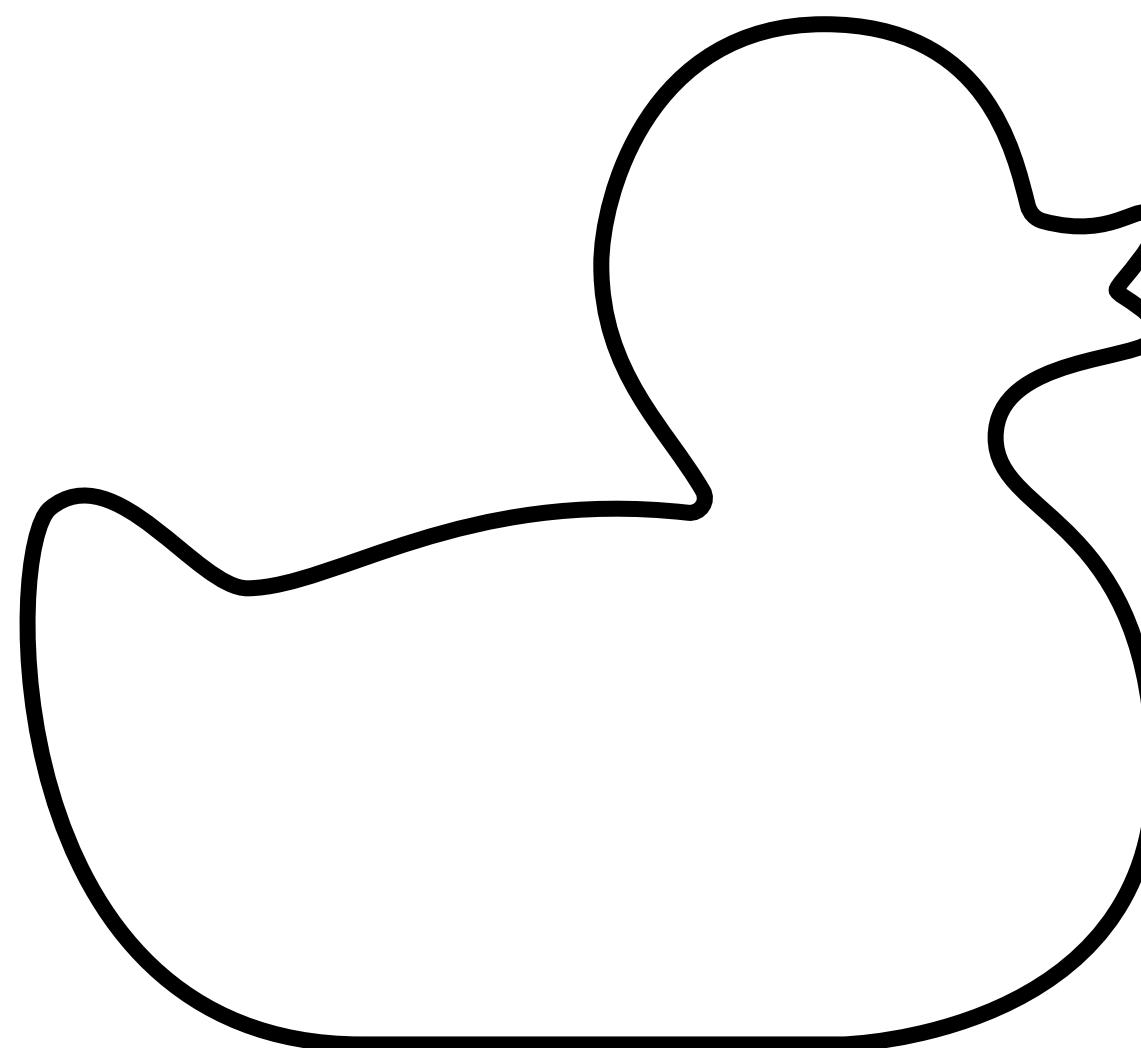


Target Geometry

# Gradient Based Optimization



Initial Geometry

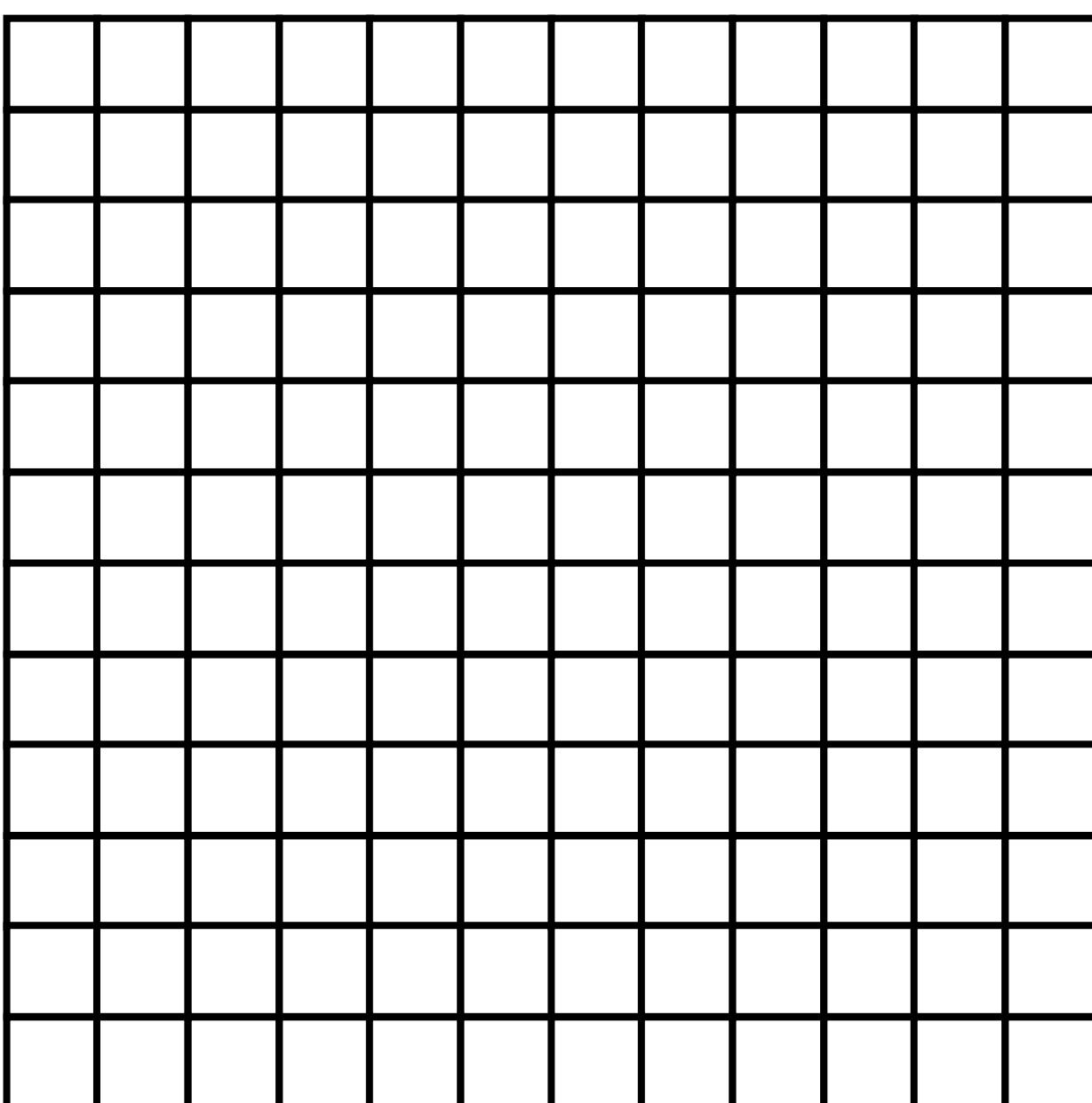


Target Geometry

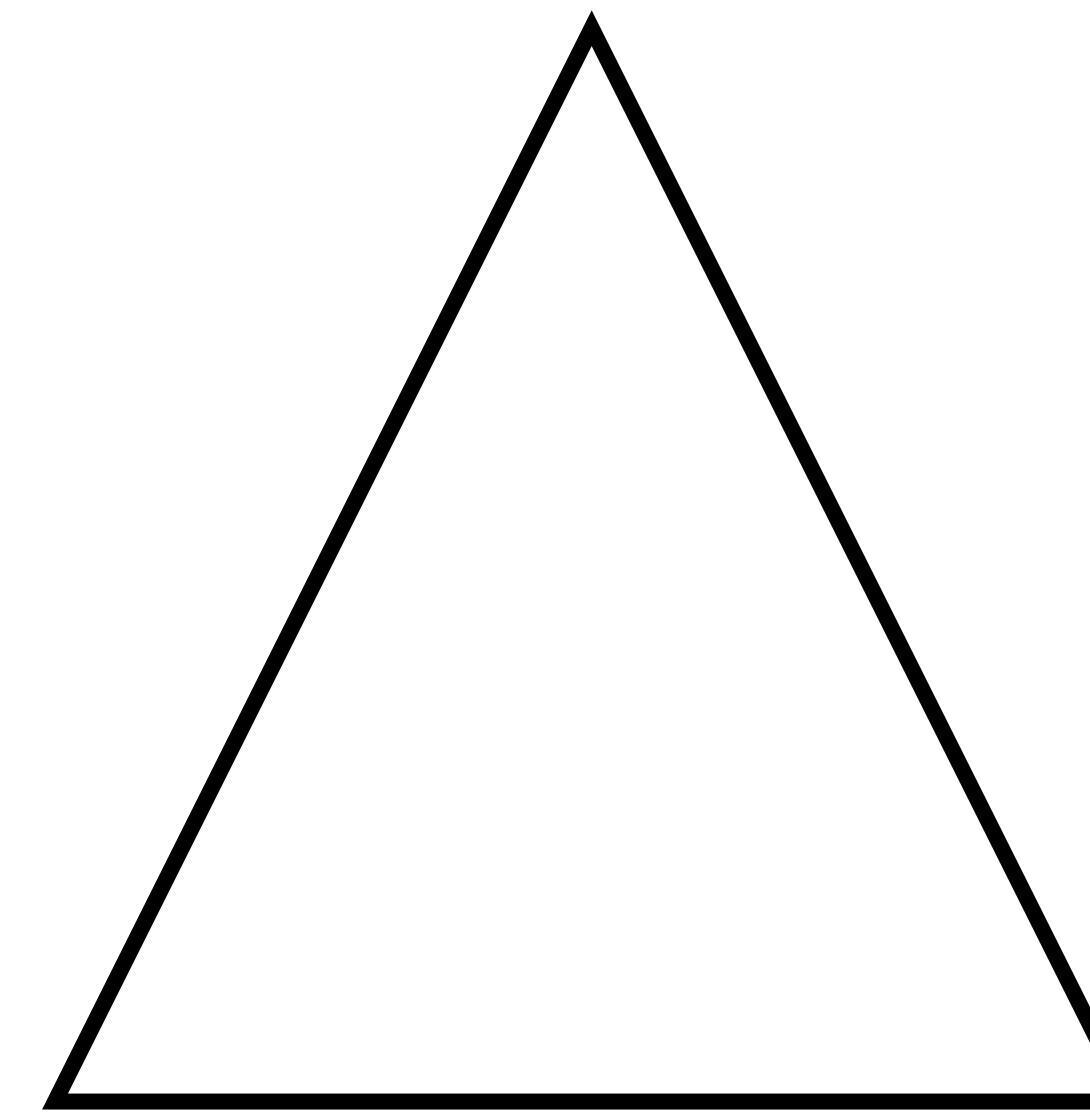
# Voxel Representation



# Gradient Based Optimization

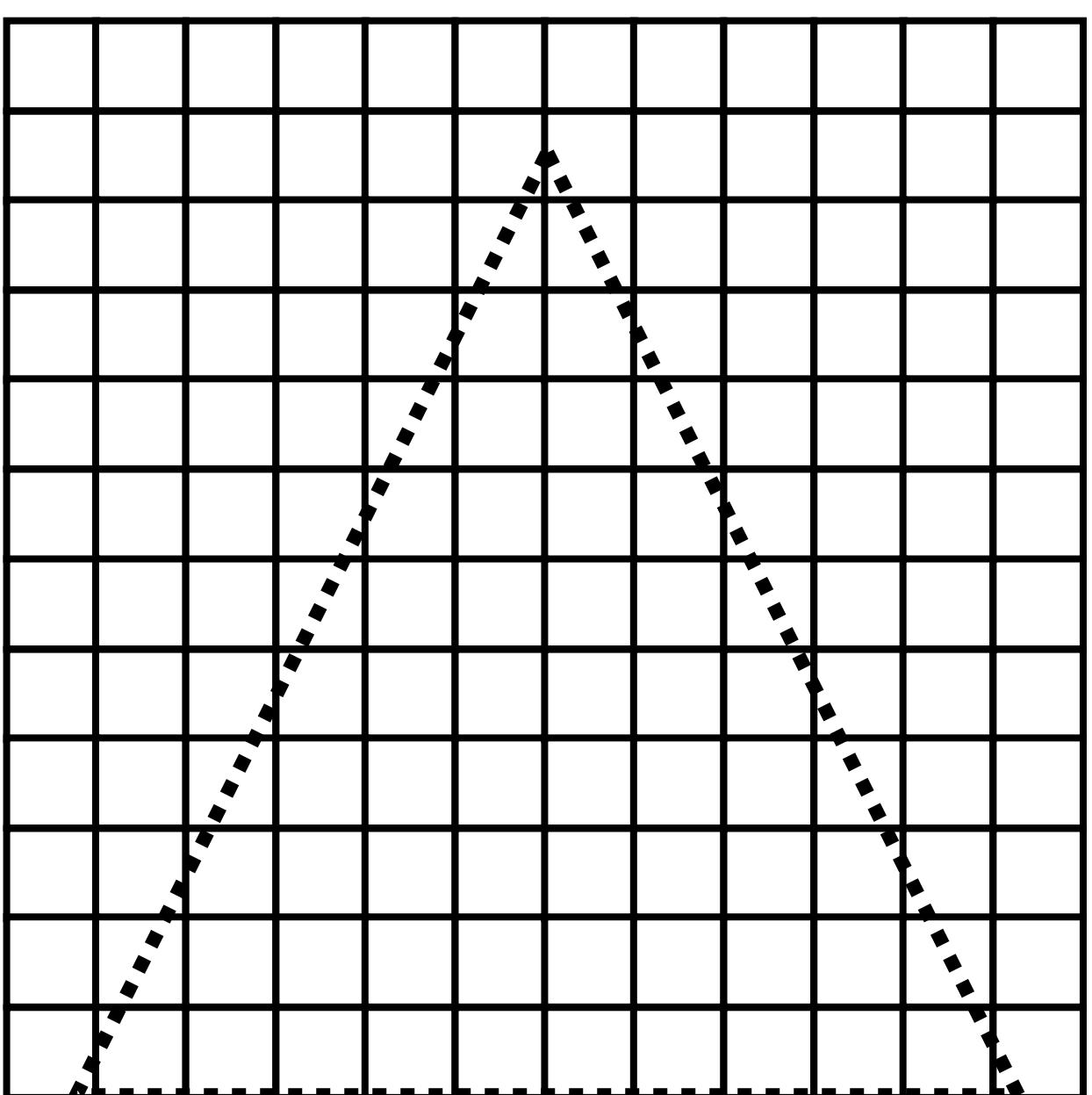


Initialized Grid

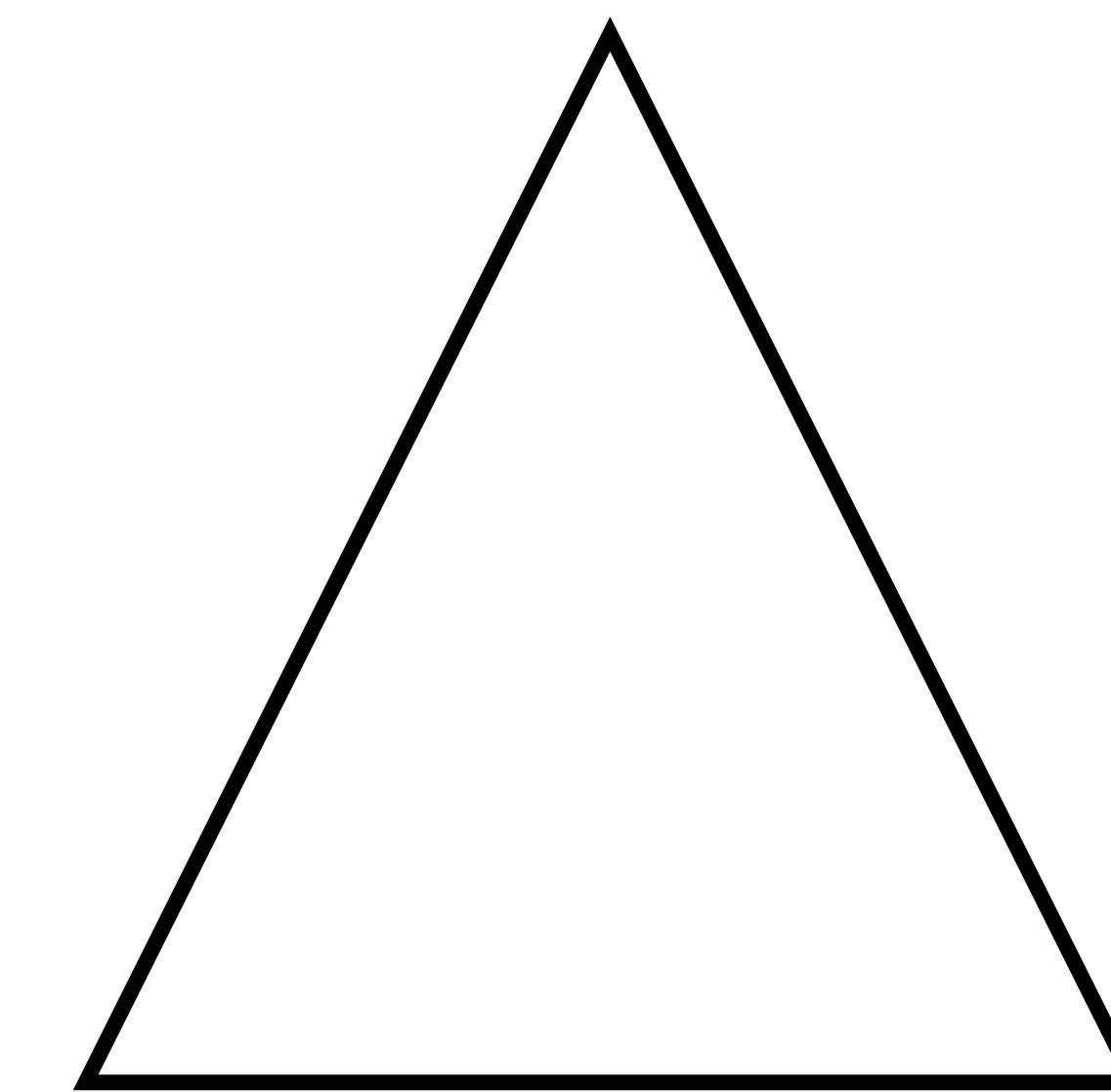


Target Geometry

# Gradient Based Optimization

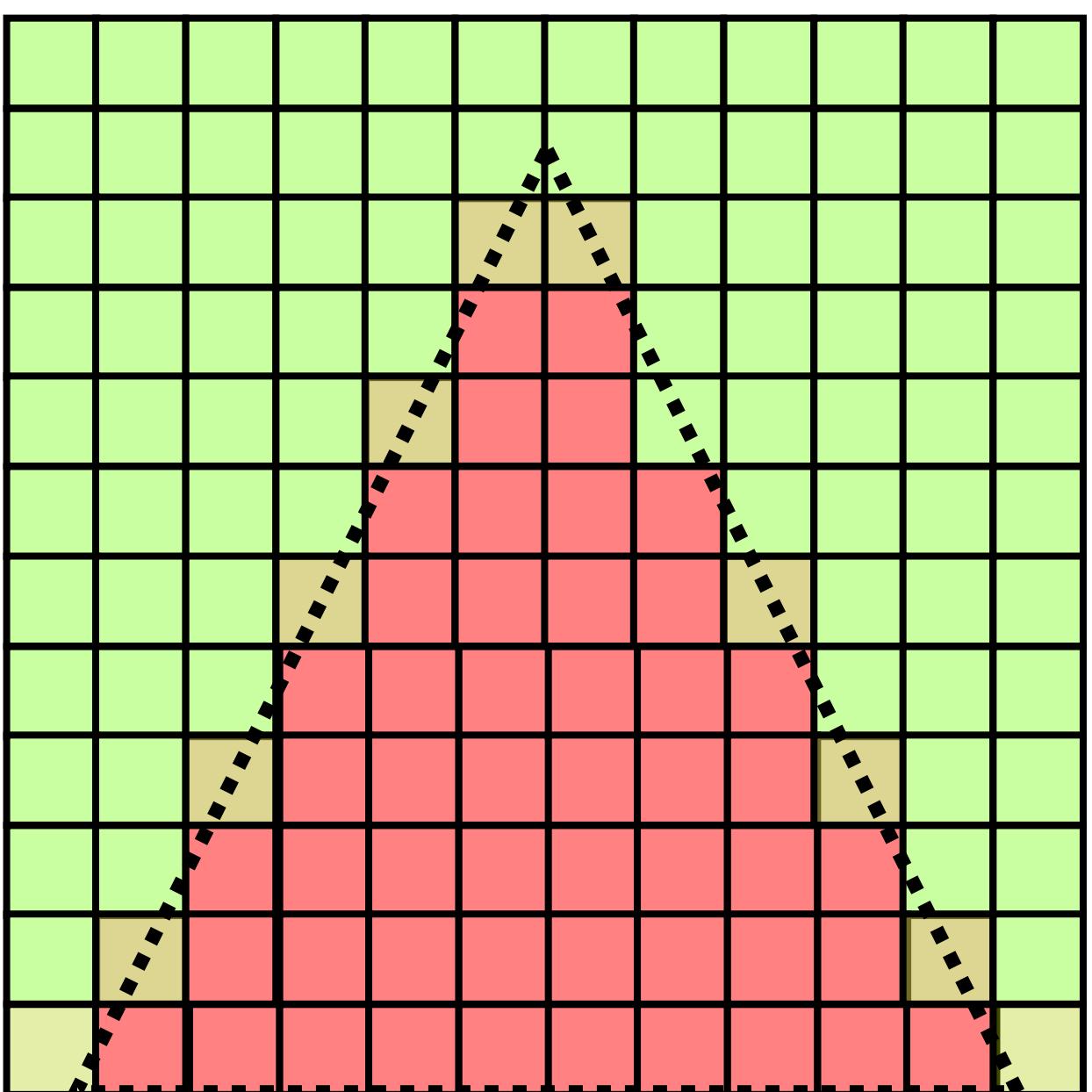


Initialized Grid

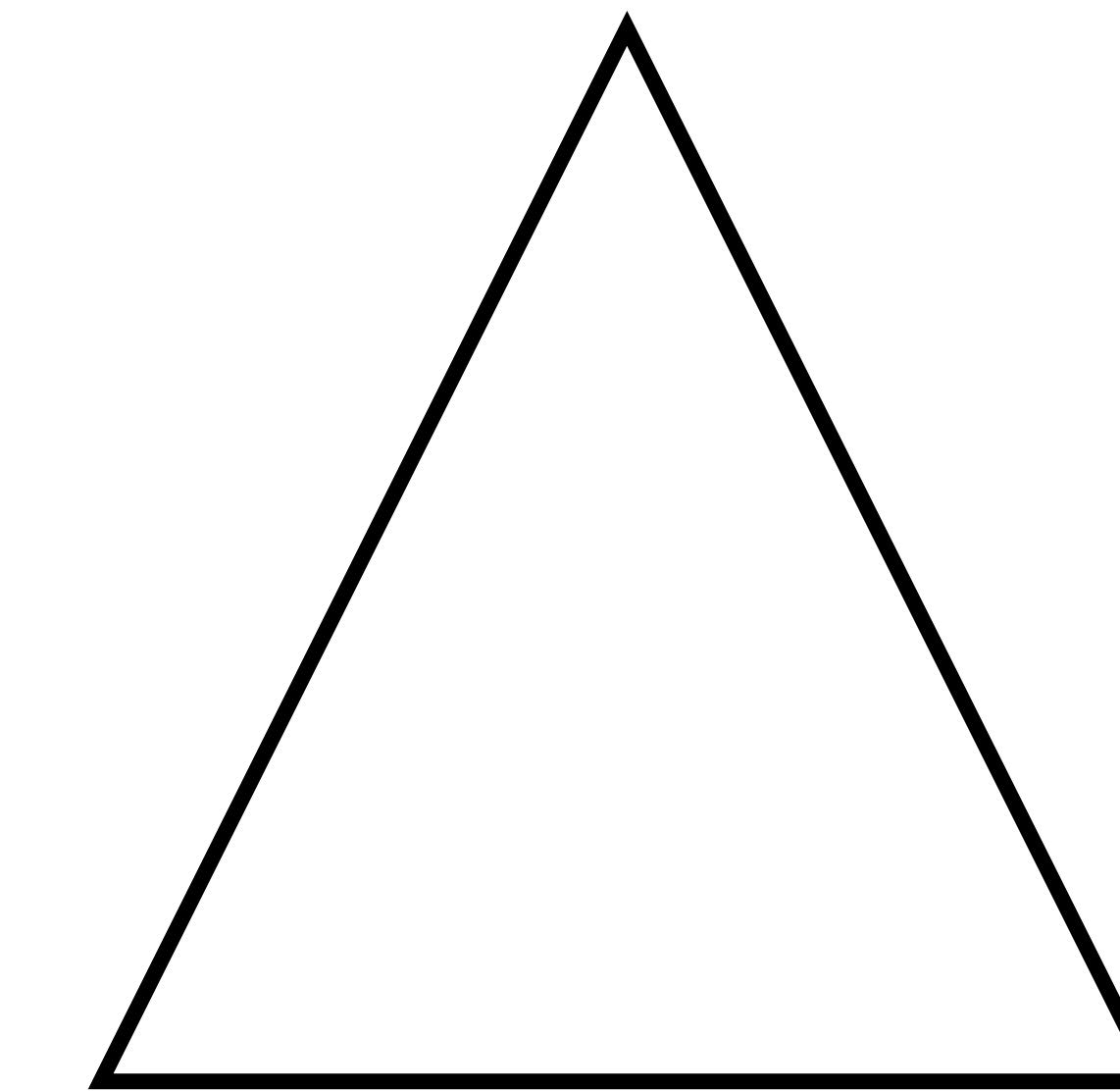


Target Geometry

# Gradient Based Optimization

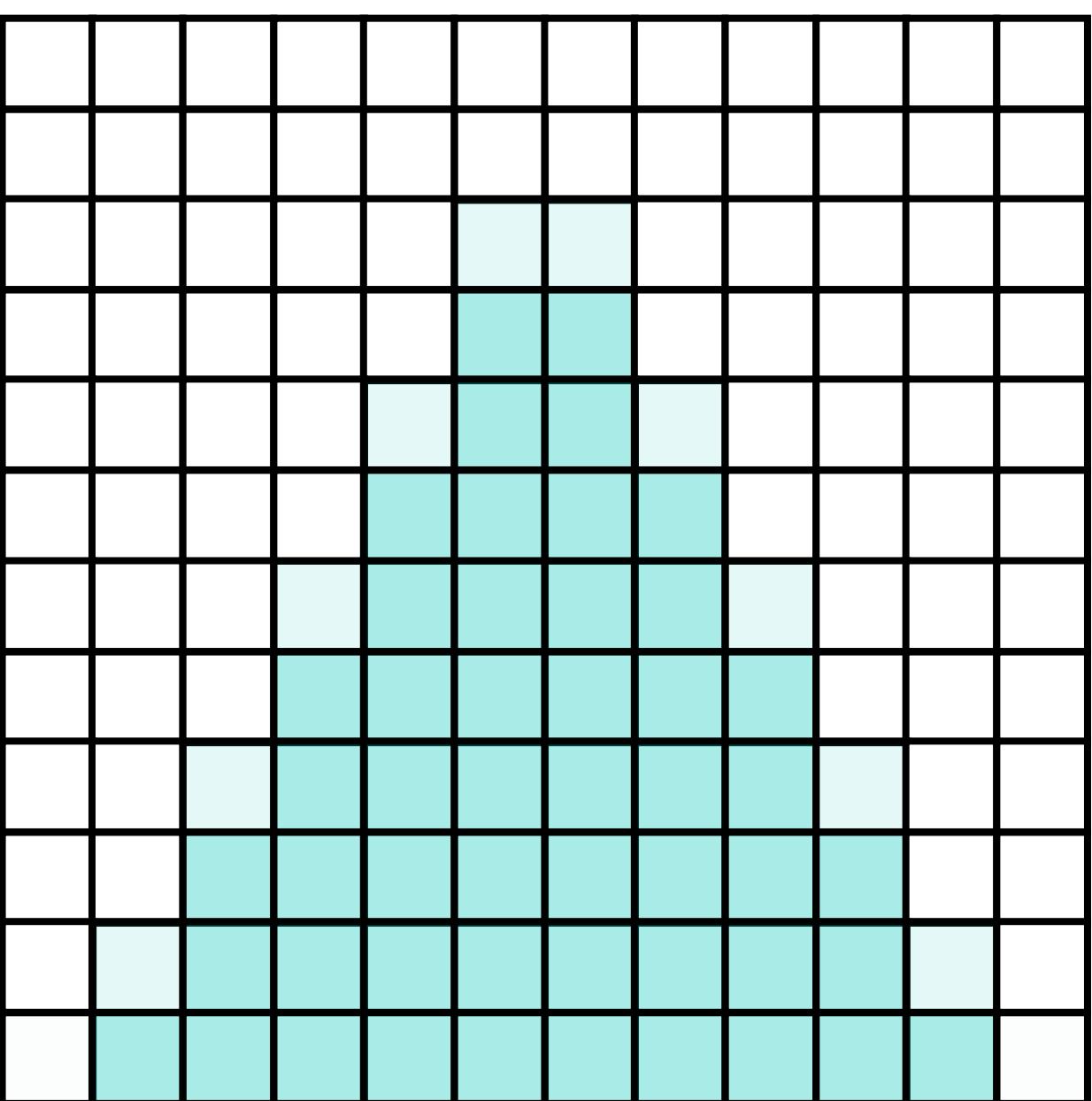


Loss

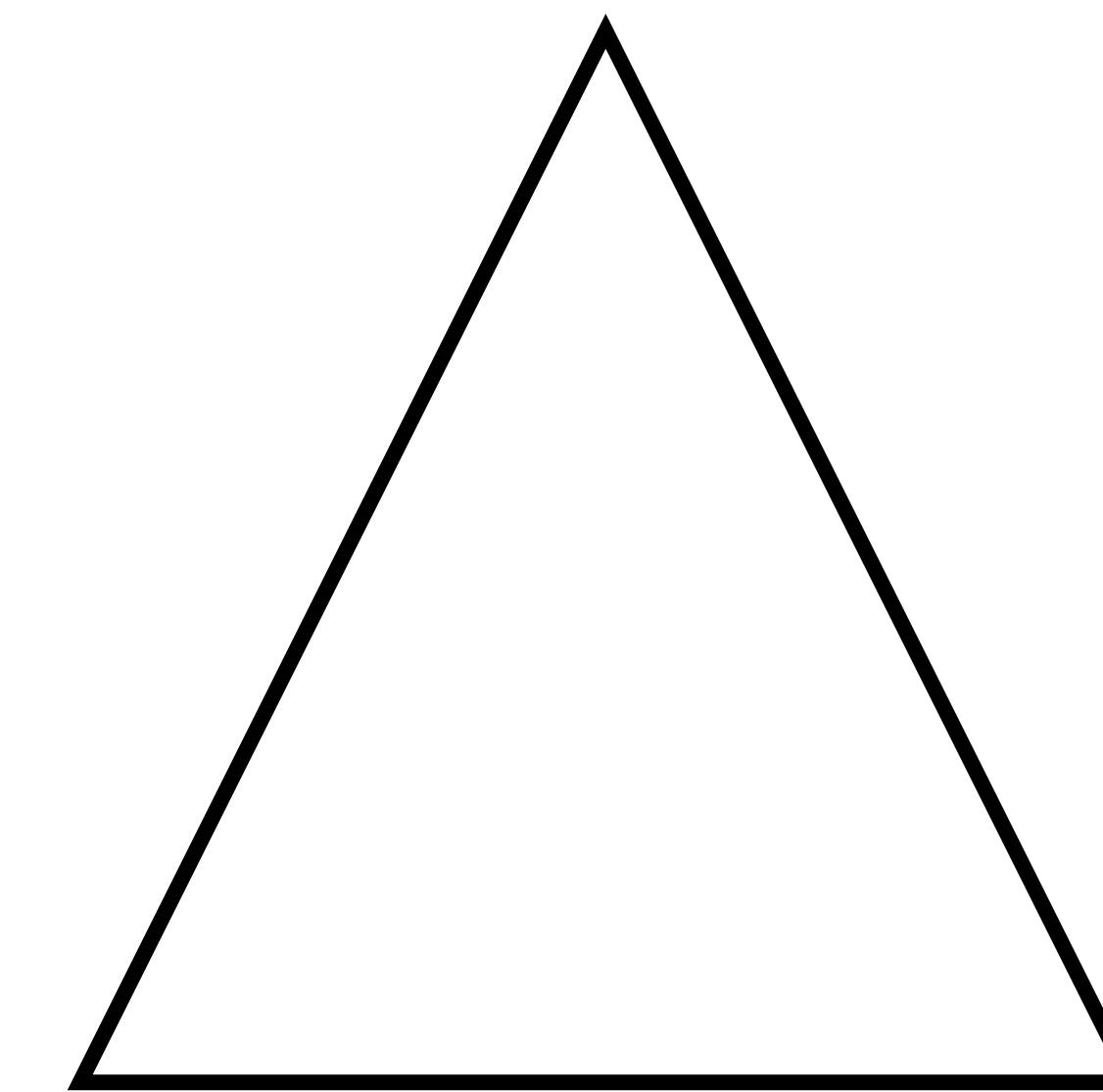


Target Geometry

# Gradient Based Optimization

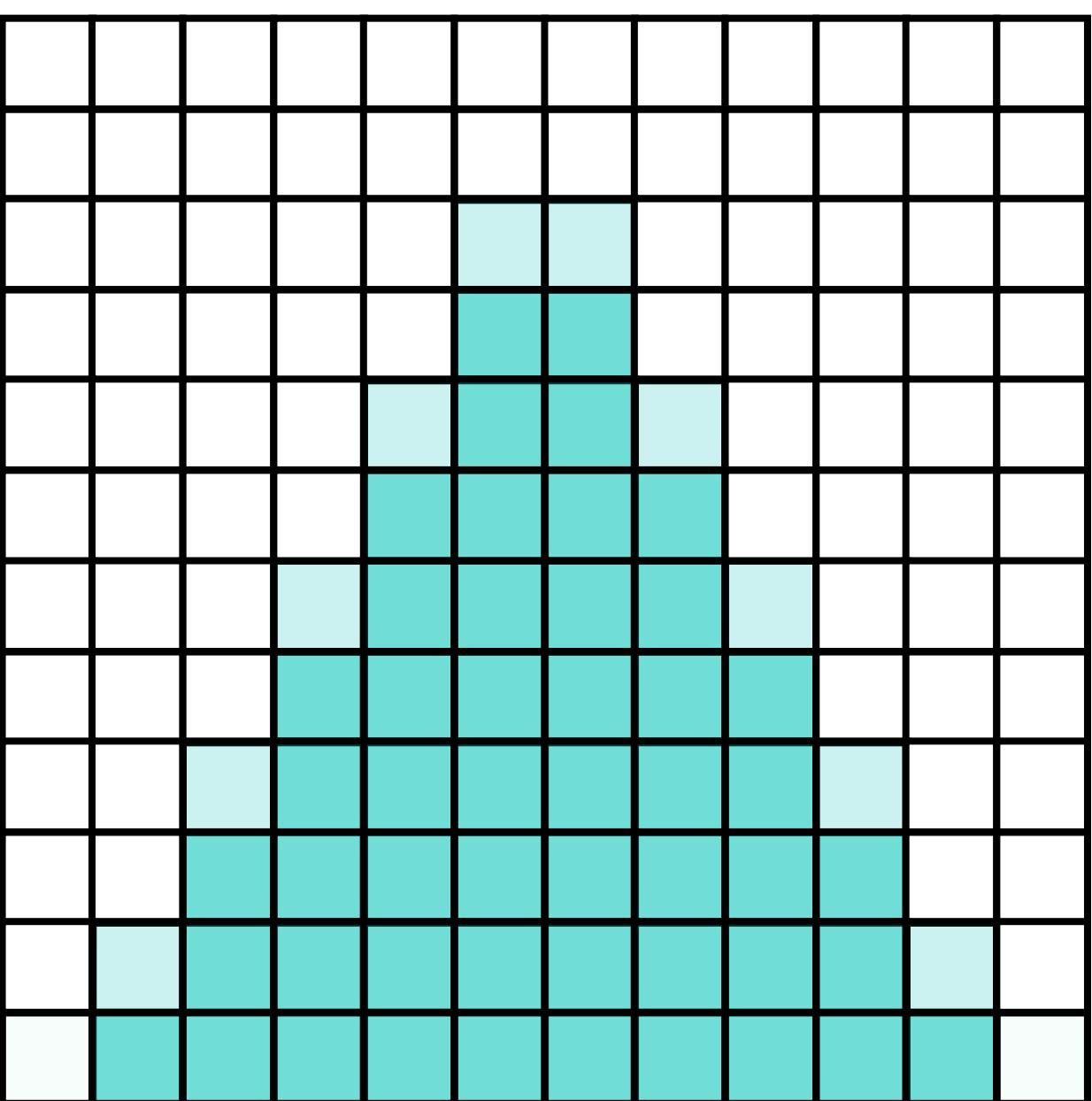


Gradient Step

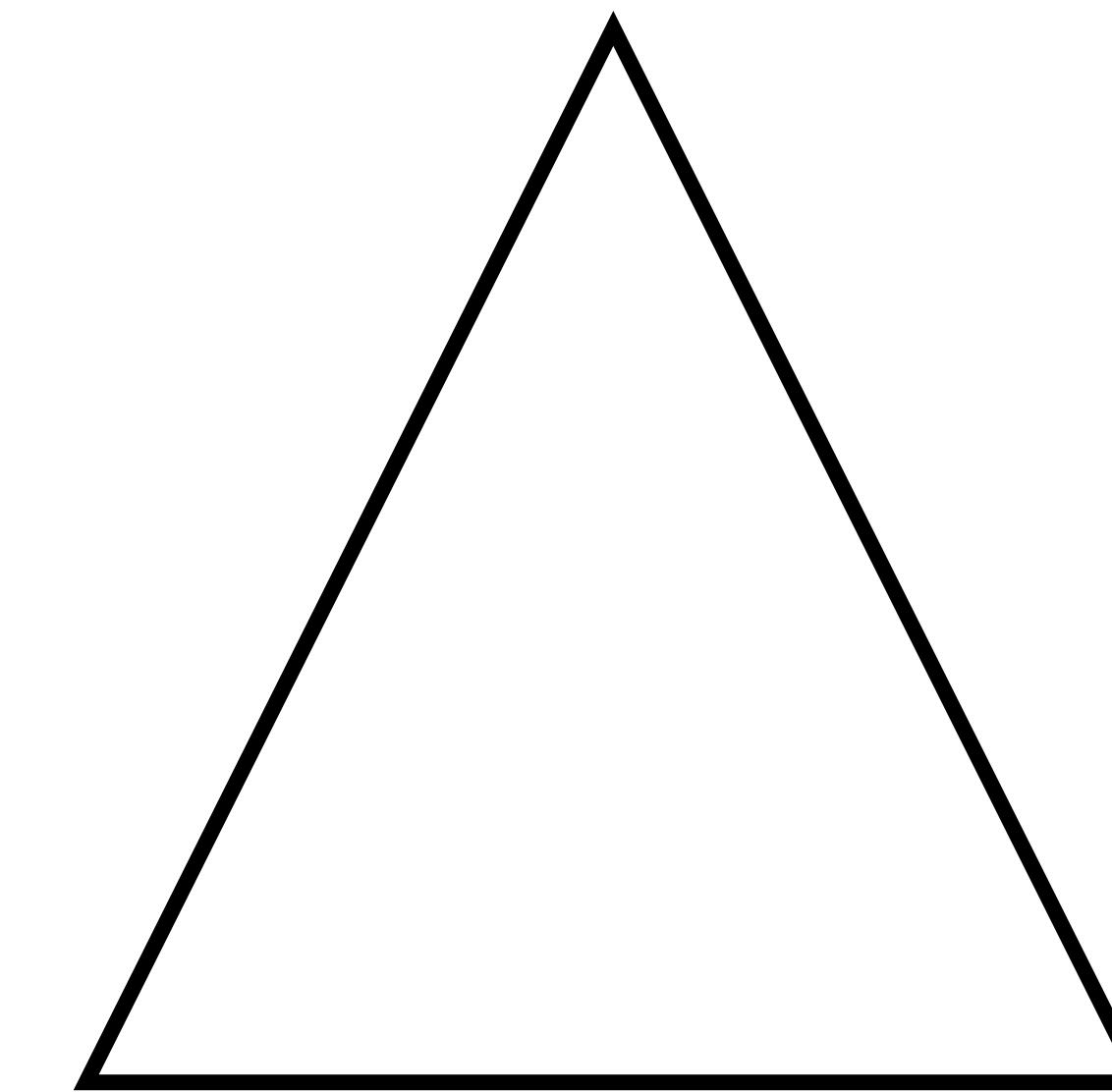


Target Geometry

# Gradient Based Optimization

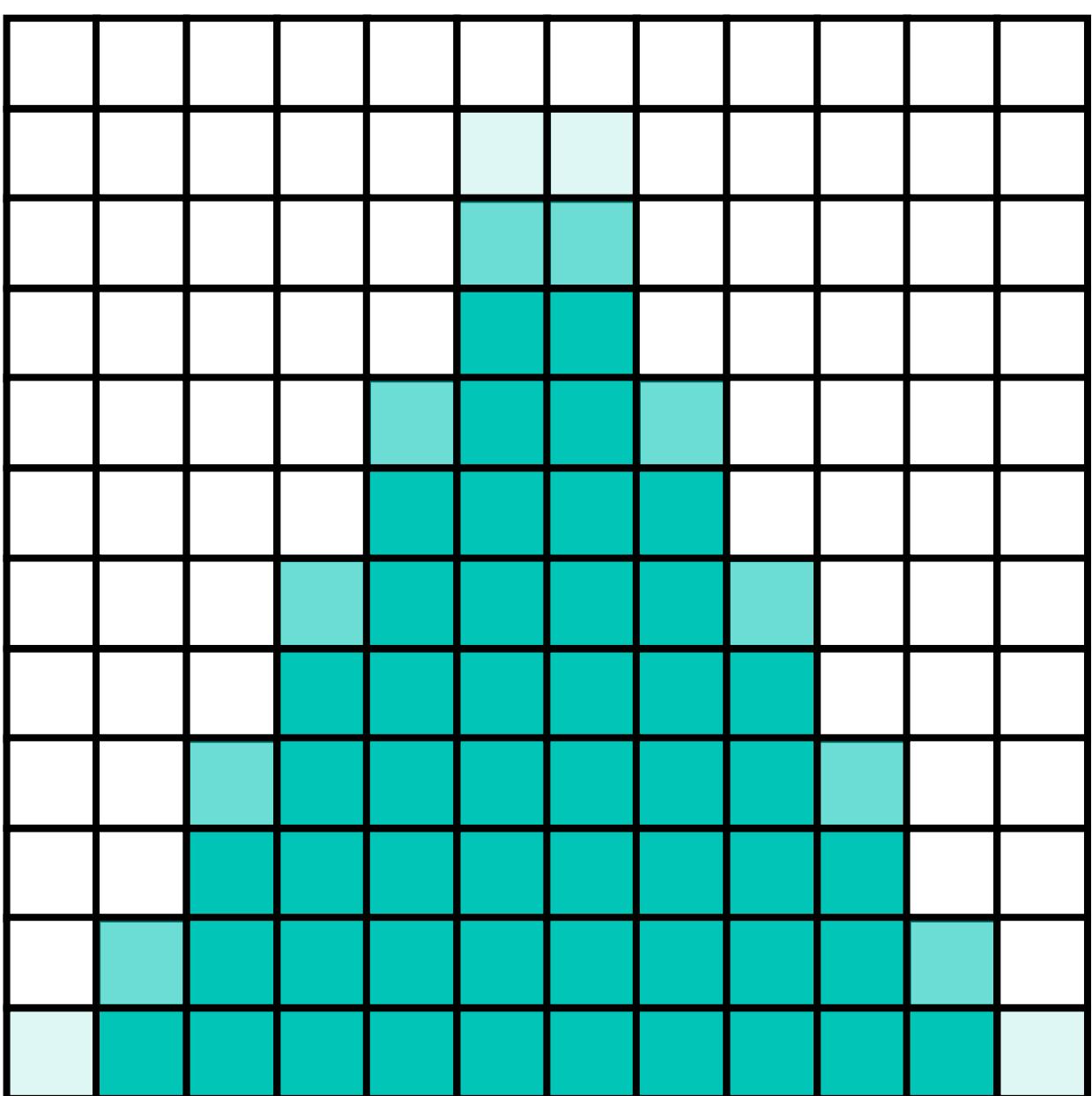


Repeat

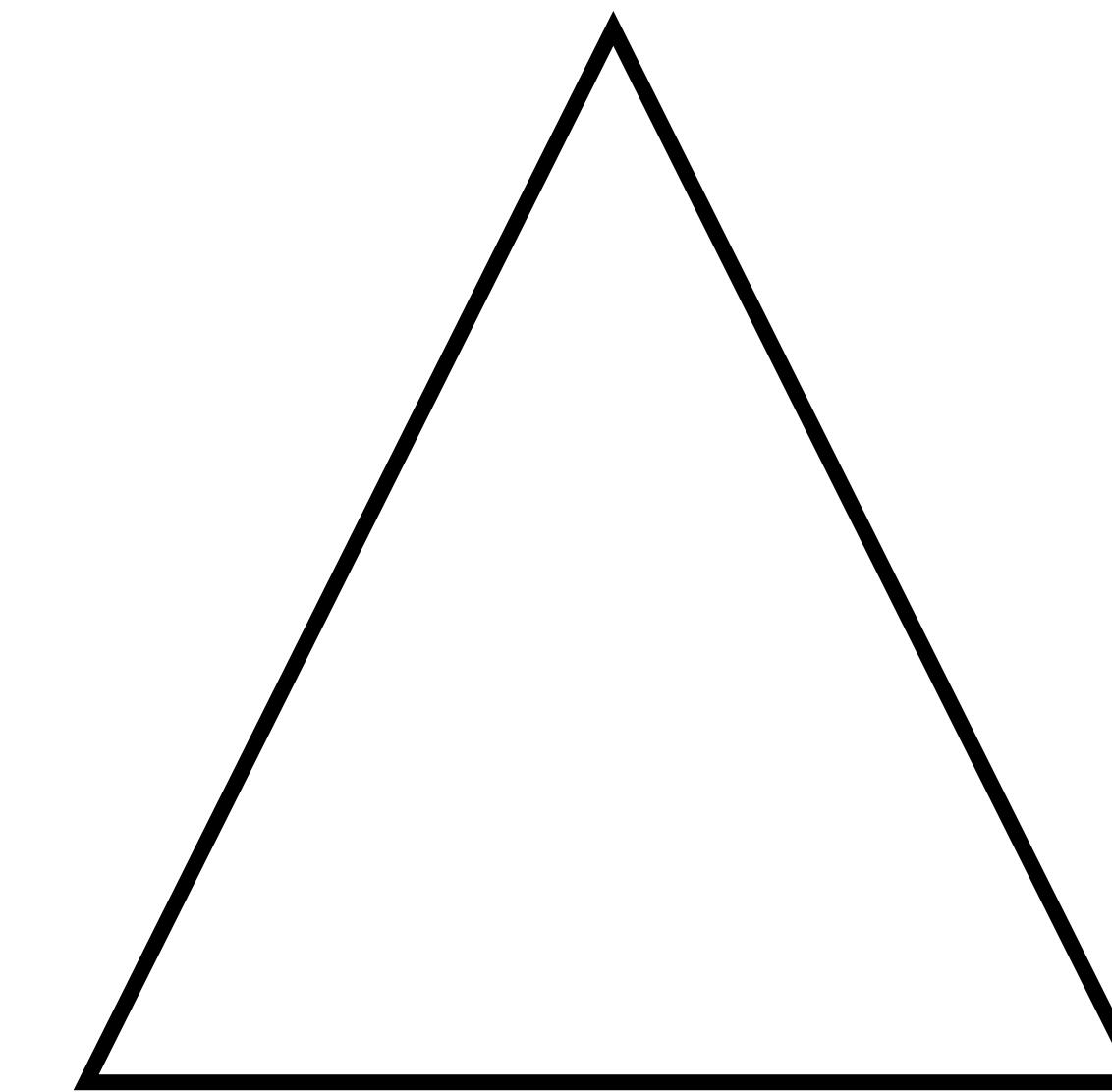


Target Geometry

# Gradient Based Optimization

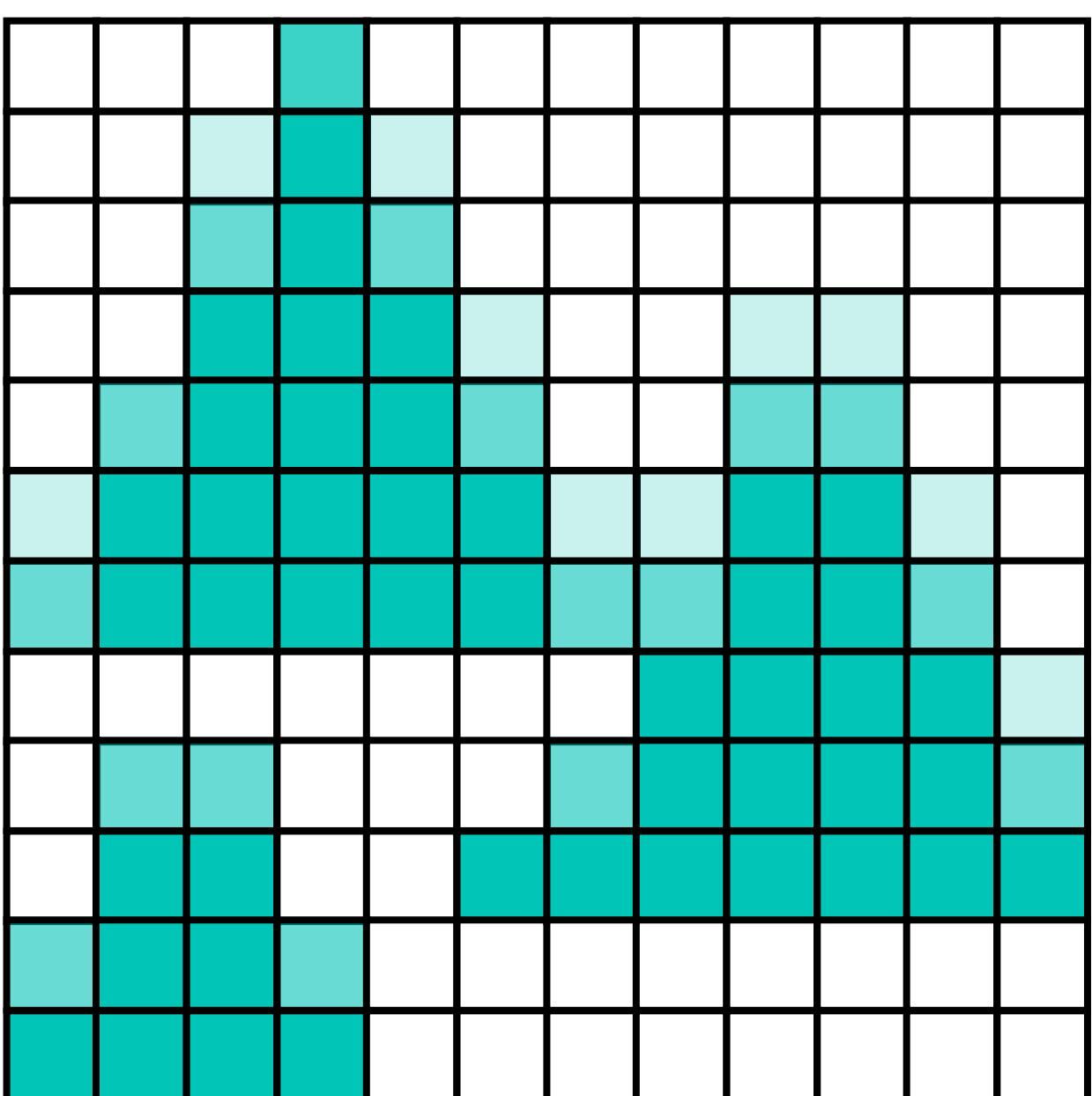


Repeat

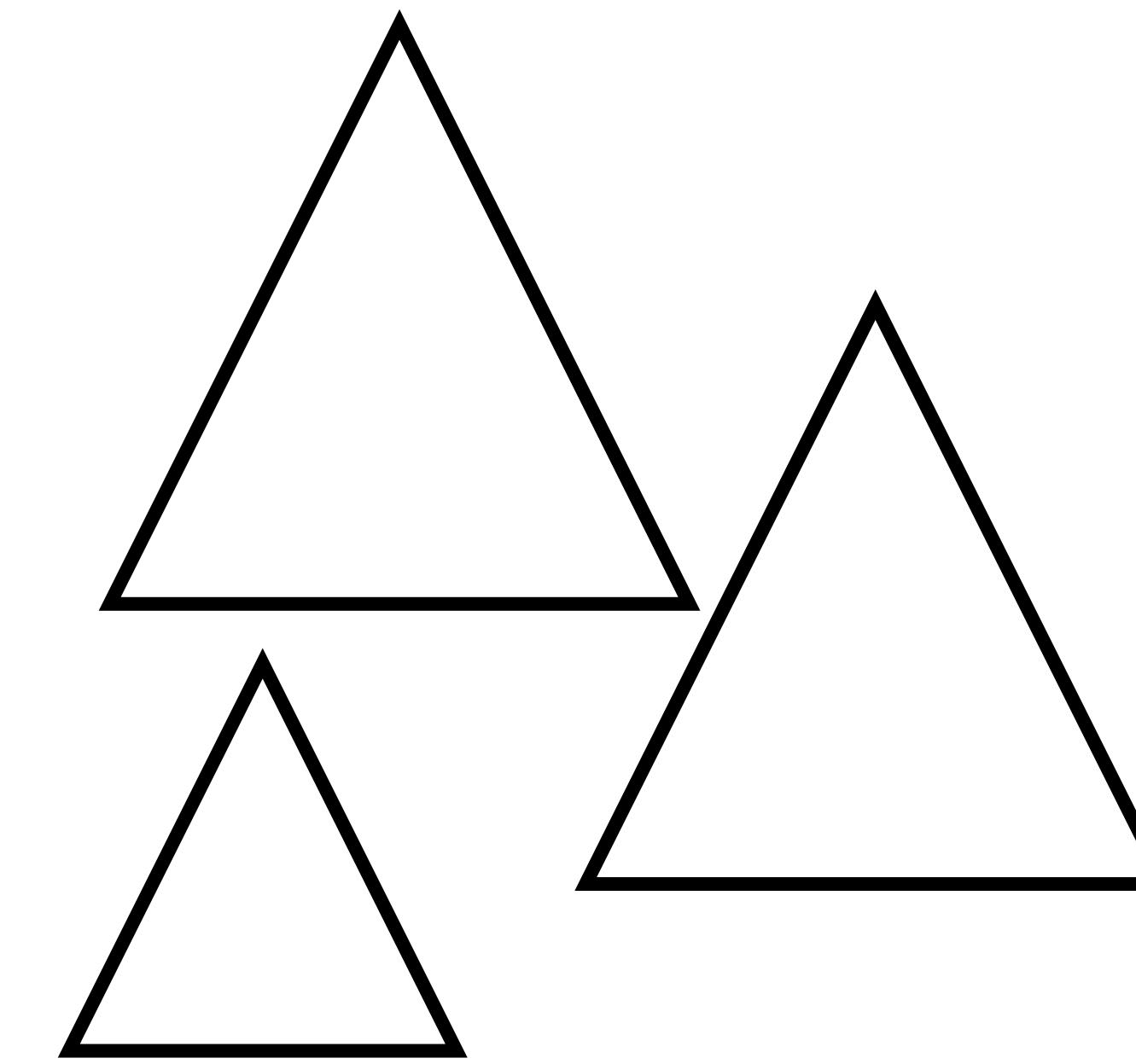


Target Geometry

# Gradient Based Optimization

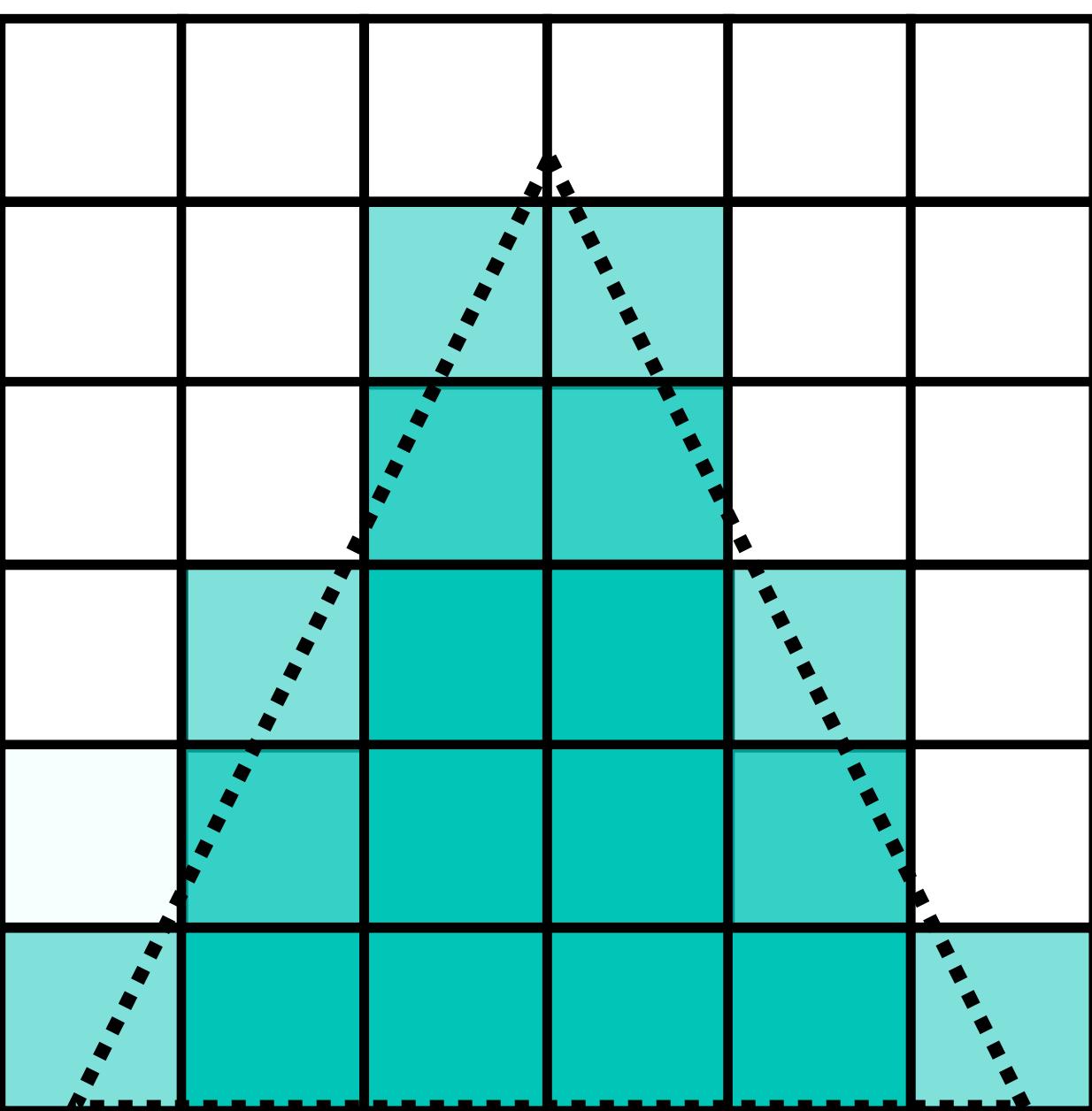


Reconstruction

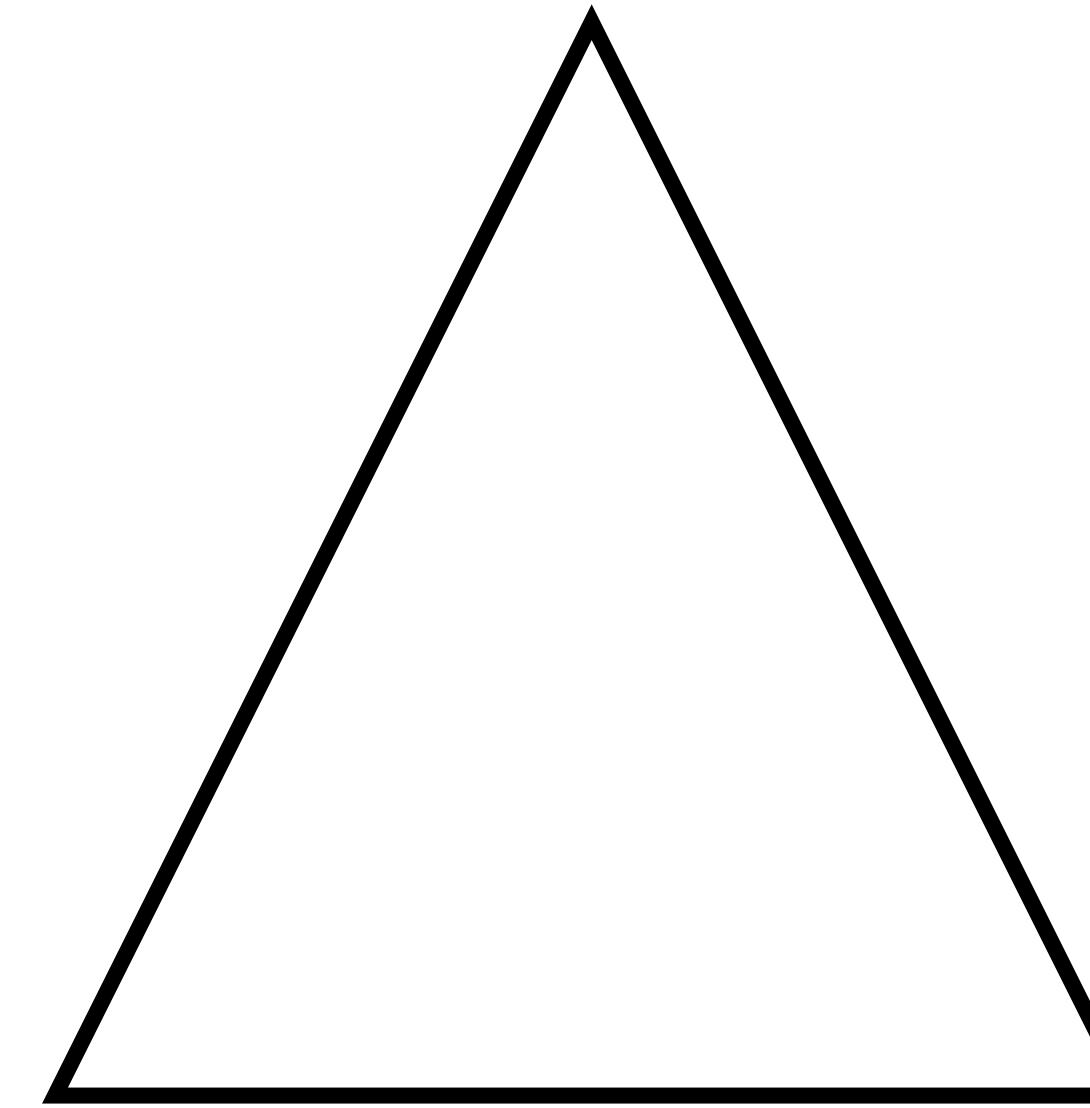


Target Geometry

# Gradient Based Optimization

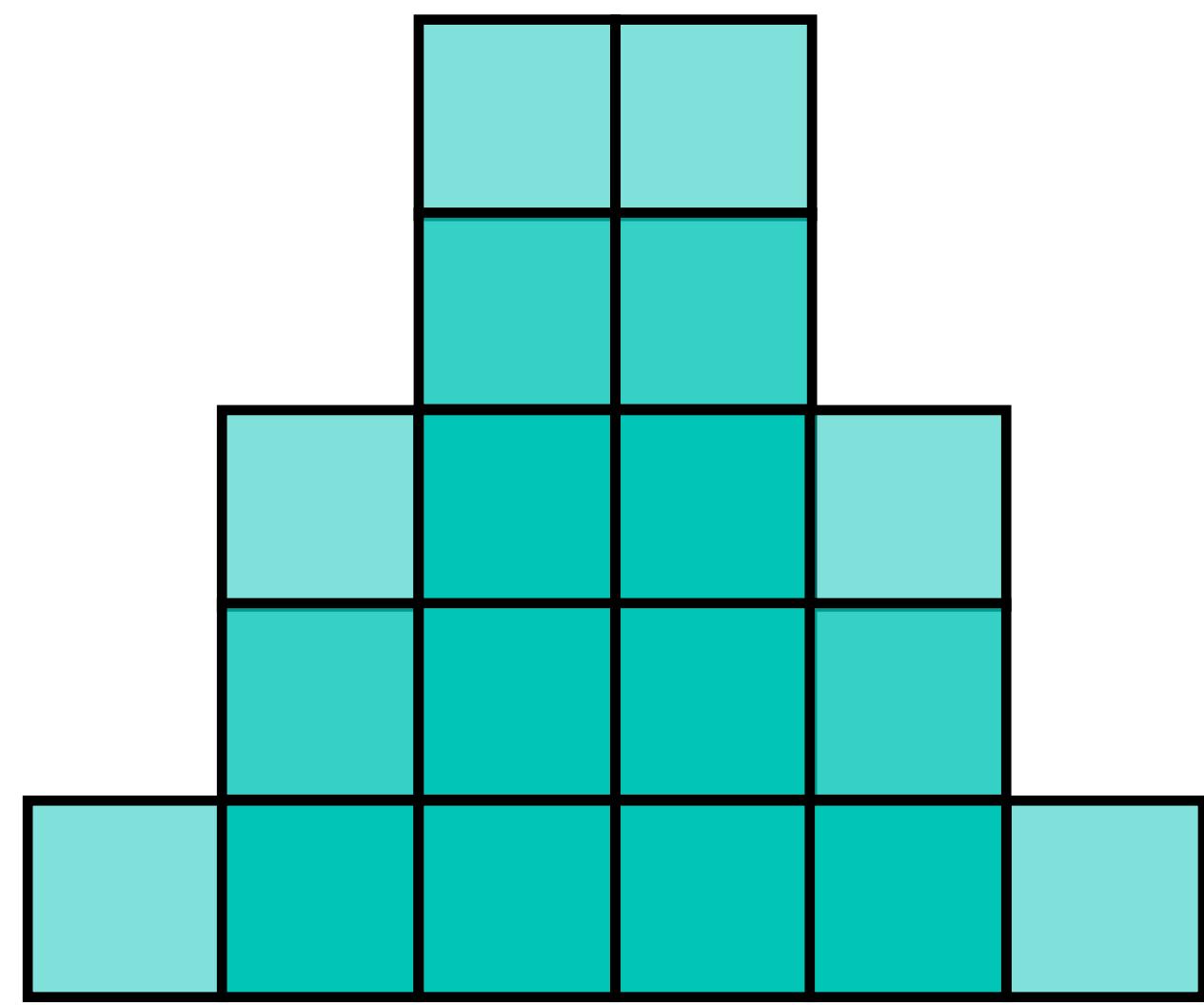


Reconstruction

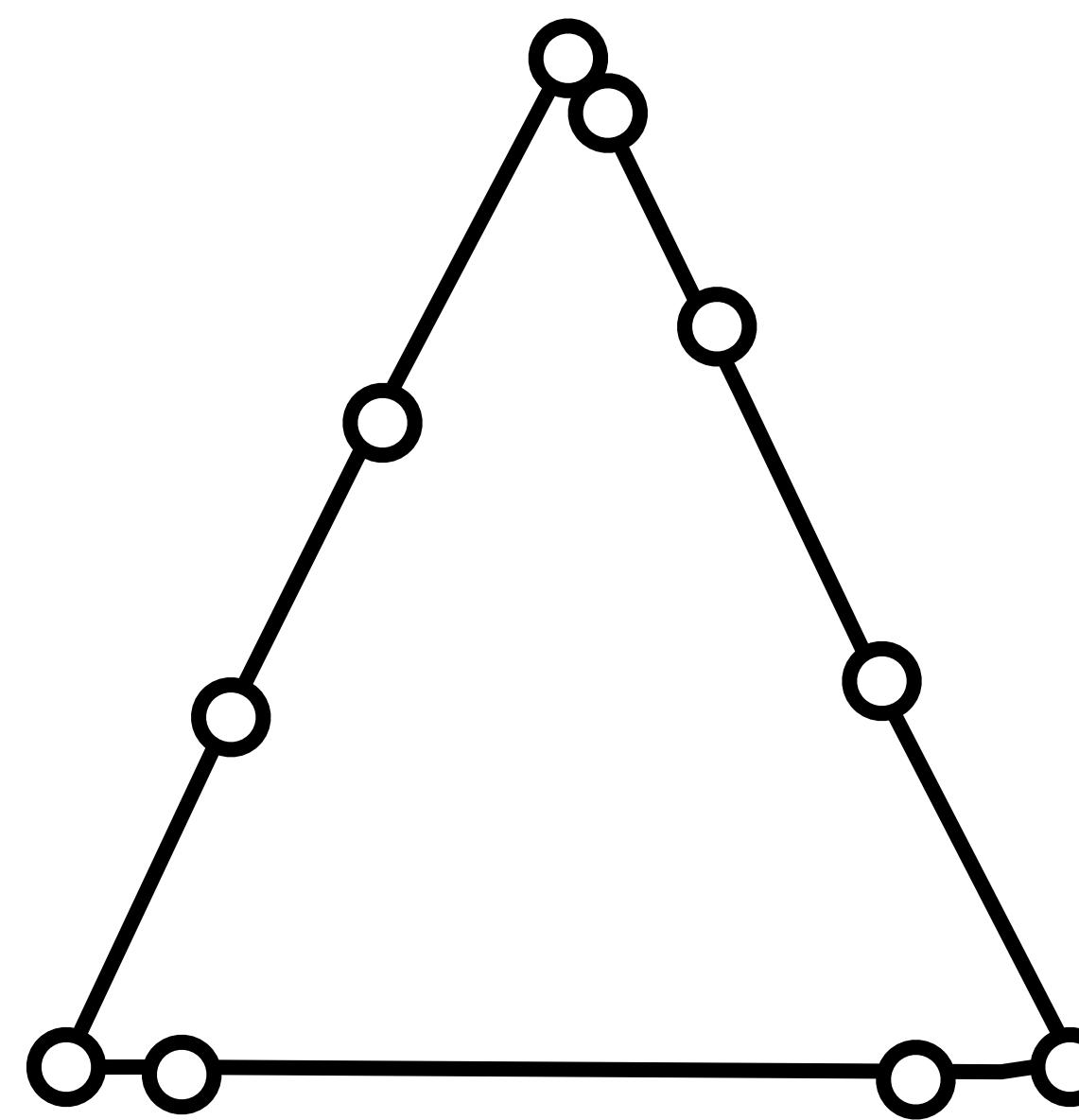


Target Geometry

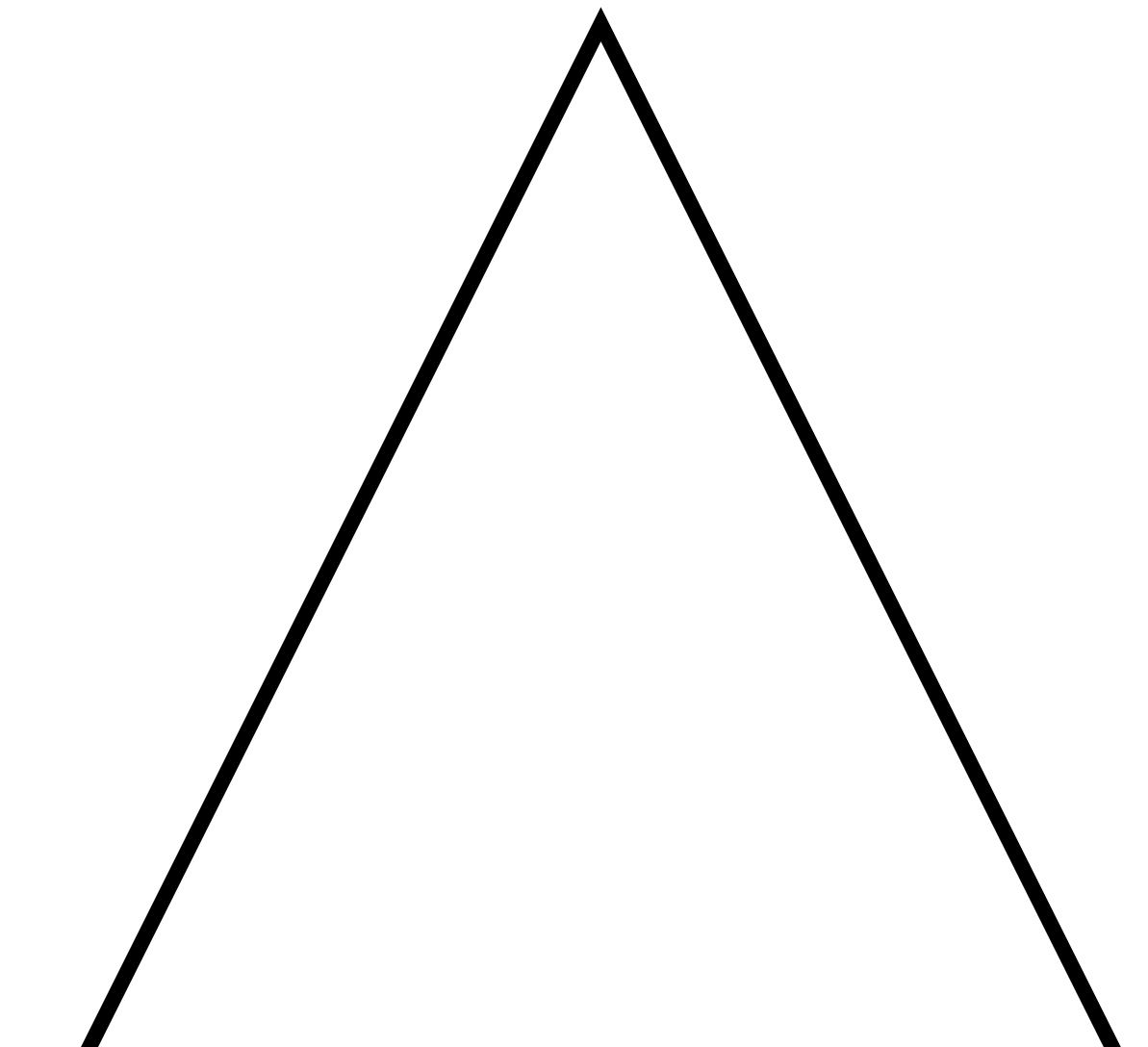
# Gradient Based Optimization



Voxel

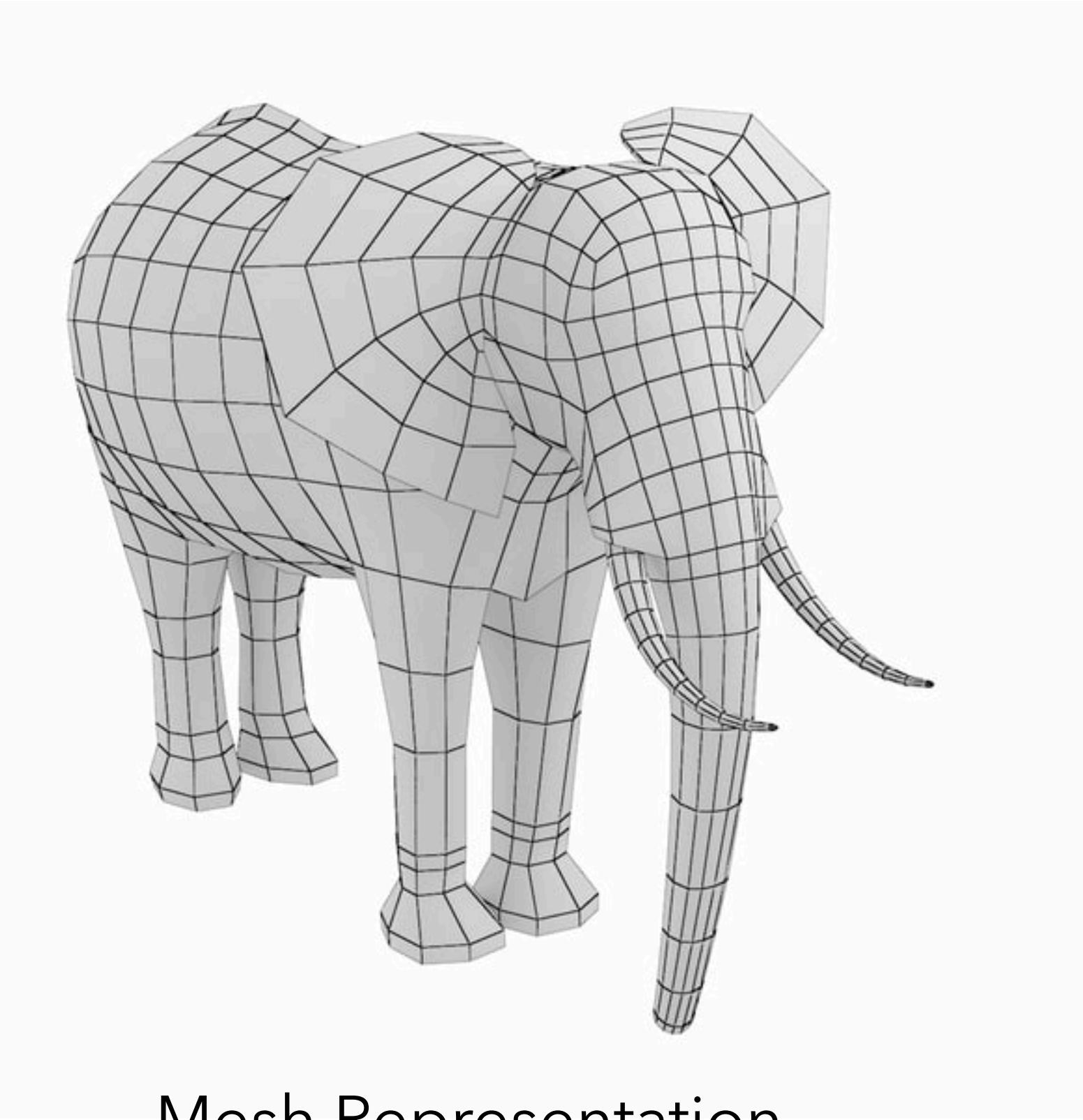


Mesh



Target Geometry

# Geometry Representations



Mesh Representation

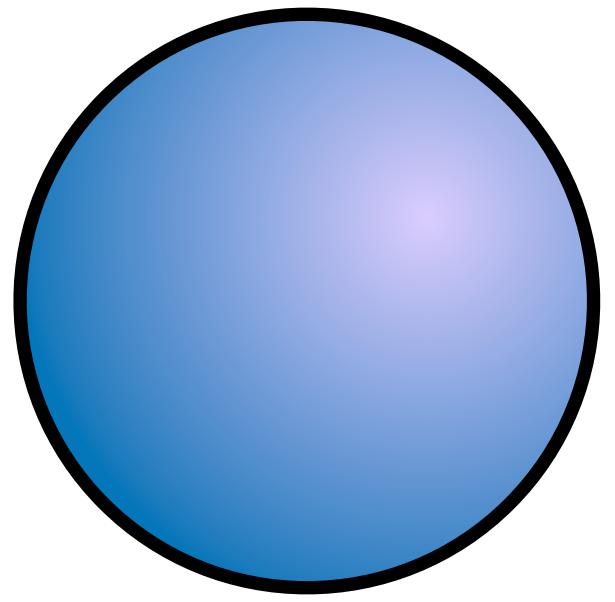
Small memory footprint  
Hard to optimize



Voxel Representation

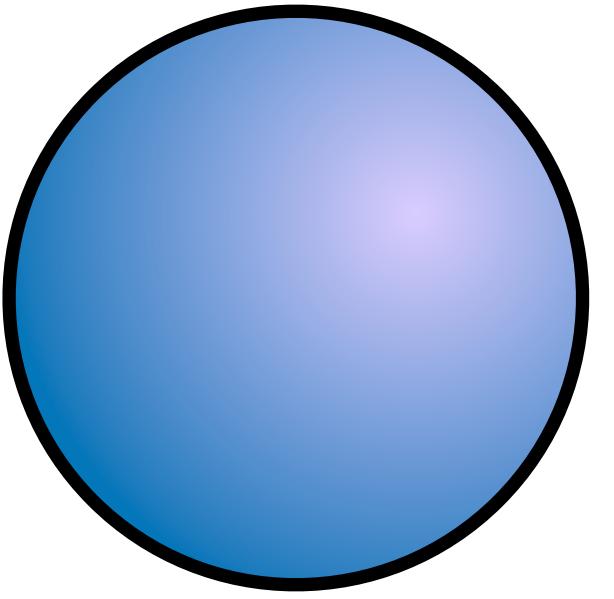
Easy to optimize  
Large memory footprint

# Implicit Functions

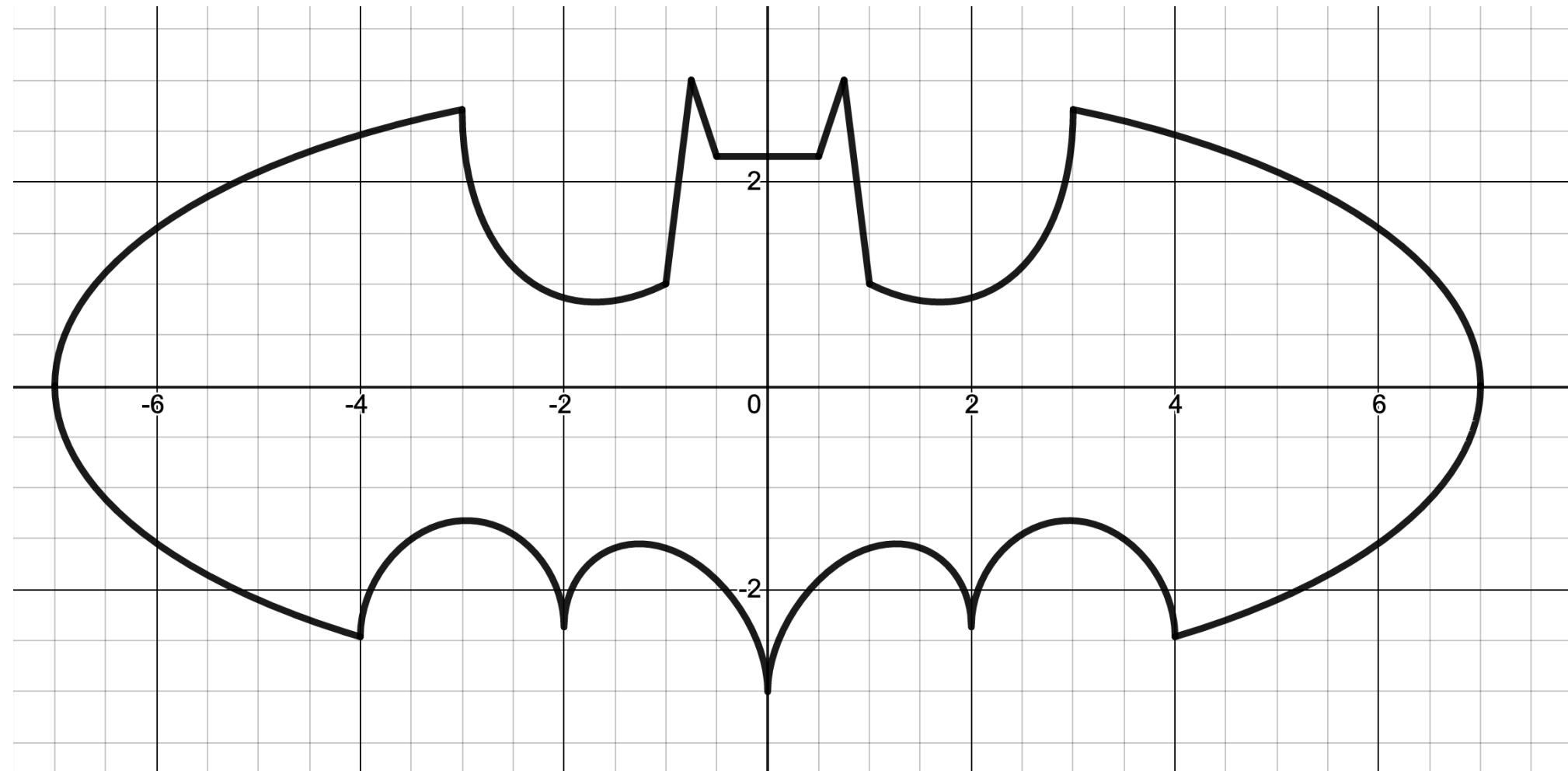


$$x^2 + y^2 + z^2 = 1$$

# Implicit Functions



$$x^2 + y^2 + z^2 = 1$$



$$\left\{ |x| > 3.3 \sqrt{-\left(\frac{x}{7}\right)^2 + 1} \right\}$$

$$\left\{ |x| > 4.3 \sqrt{-\left(\frac{x}{7}\right)^2 + 1} \right\}$$

$$\left| \frac{x}{2} \right| - \frac{3\sqrt{33}}{112} x^2 + \sqrt{1 - (\text{abs}(|x| - 2) - 1)}$$

$$\{ .75 < |x| < 1 : 9 - 8|x| \}$$

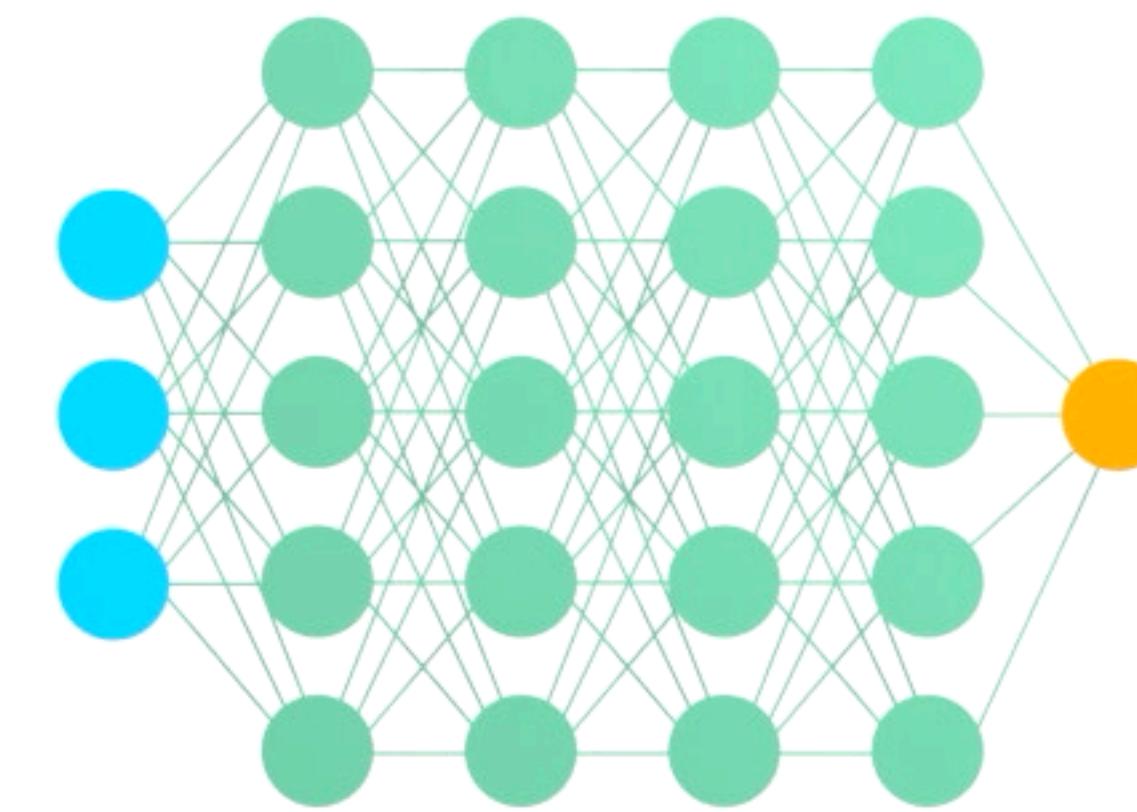
$$\{ .5 < |x| < .75 : 3|x| + .75 \}$$

$$\{ |x| < .5 : 2.25 \}$$

$$\{ |x| > 1.5 - .5|x| - \frac{6\sqrt{10}}{14} (\sqrt{3 - x^2} + 2|x|)$$

# Coordinate Based Neural Network

Input  
Coordinate

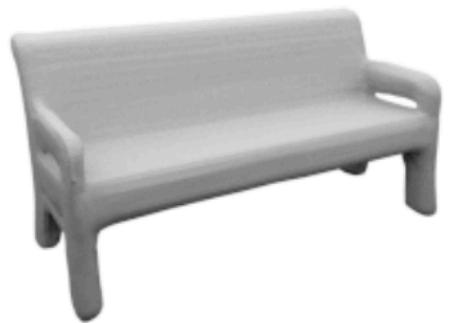
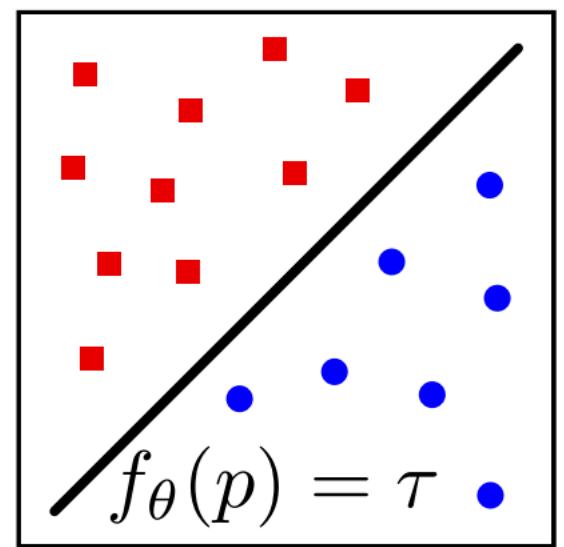


Multi Layer Perceptron  
MLP

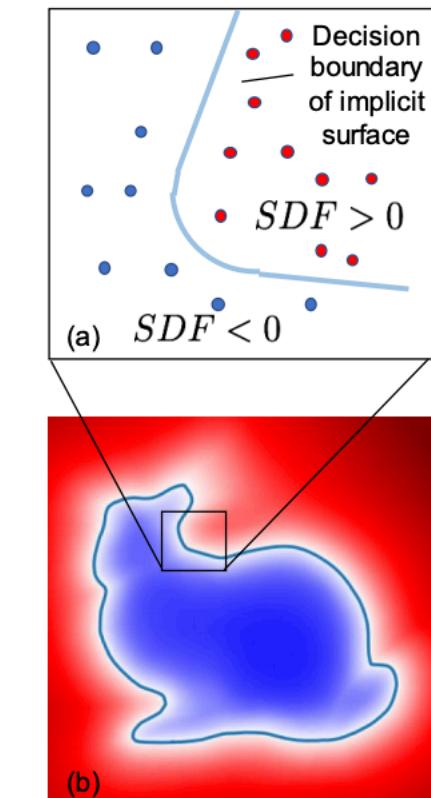
Value at  
Coordinate

# Neural networks as a continuous shape representation

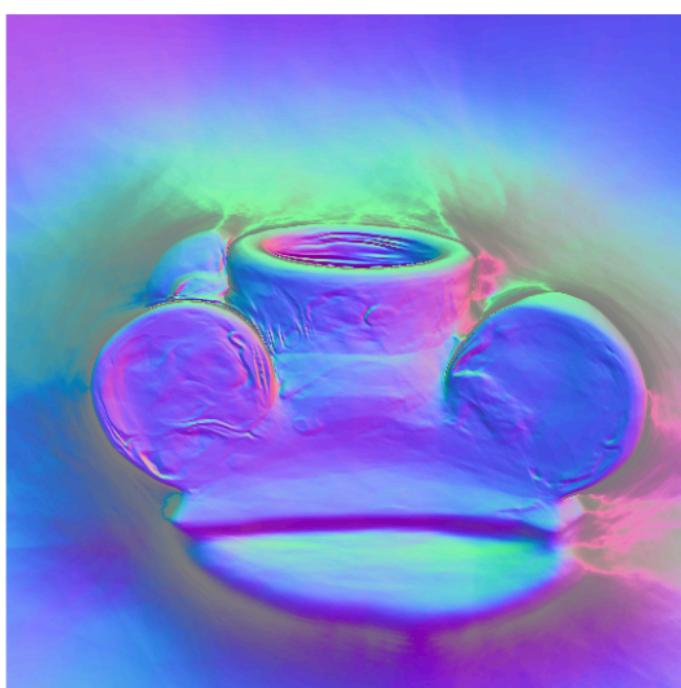
**Occupancy Networks**  
(Mescheder et al. 2019)  
 $(x, y, z) \rightarrow \text{occupancy}$



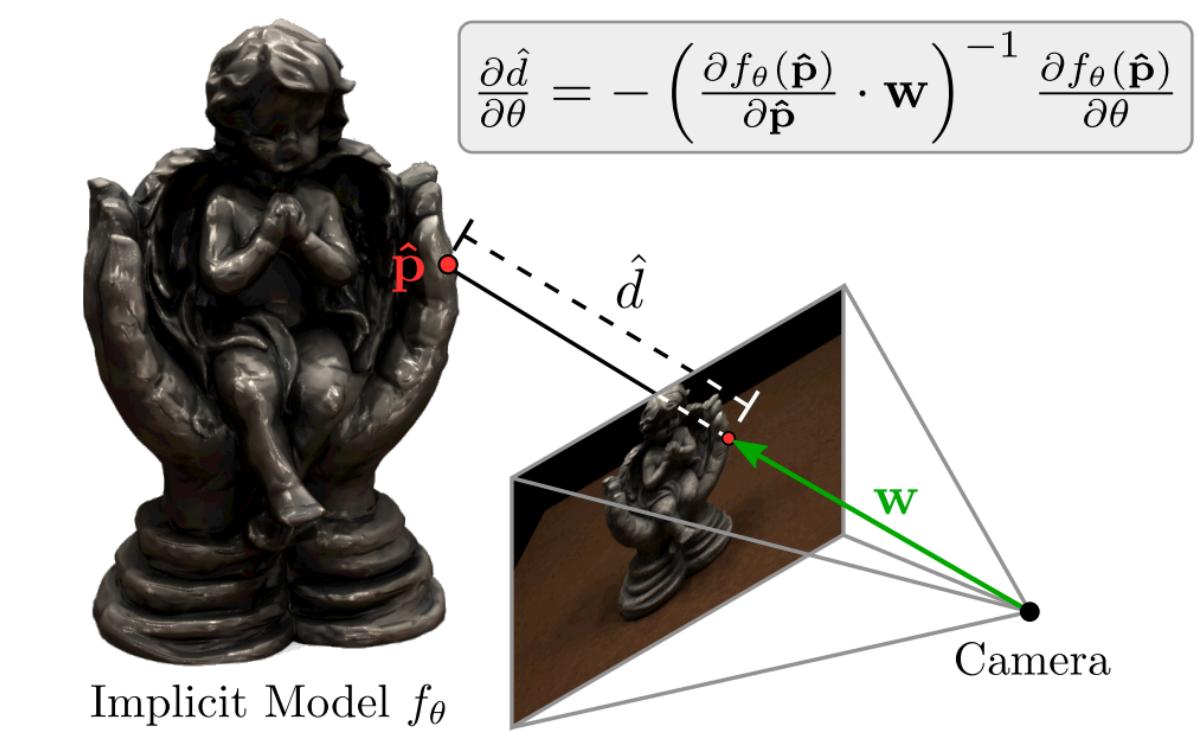
**DeepSDF**  
(Park et al. 2019)  
 $(x, y, z) \rightarrow \text{distance}$



**Scene Representation Networks**  
(Sitzmann et al. 2019)  
 $(x, y, z) \rightarrow \text{latent vec. (color, dist.)}$



**Differentiable Volumetric Rendering**  
(Niemeyer et al. 2020)  
 $(x, y, z) \rightarrow \text{color, occ.}$

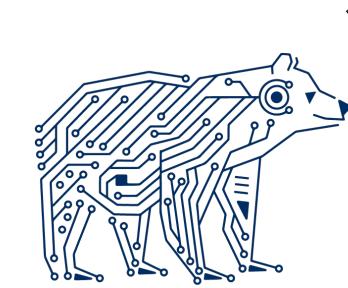


# NeRF: Representing Scenes as Neural Radiance Fields for View Synthesis



Matthew Tancik<sup>\*1</sup>

Jonathan T. Barron<sup>3</sup>



Pratul P. Srinivasan<sup>\*1,3</sup>

Ravi Ramamoorthi<sup>2</sup>

UC San Diego<sup>2</sup>

Ben Mildenhall<sup>\*1,3</sup>

Ren Ng<sup>1</sup>

**Google**<sup>3</sup>

<sup>\*</sup> Denotes Equal Contribution

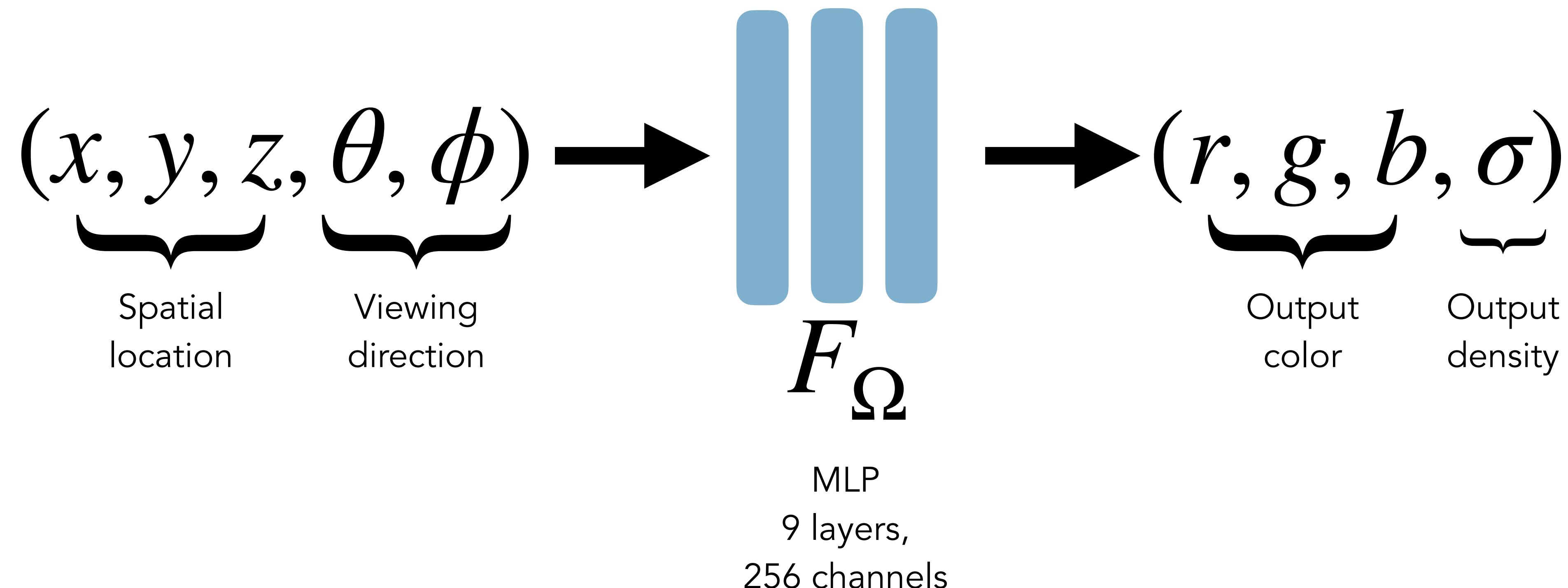
# Radiance



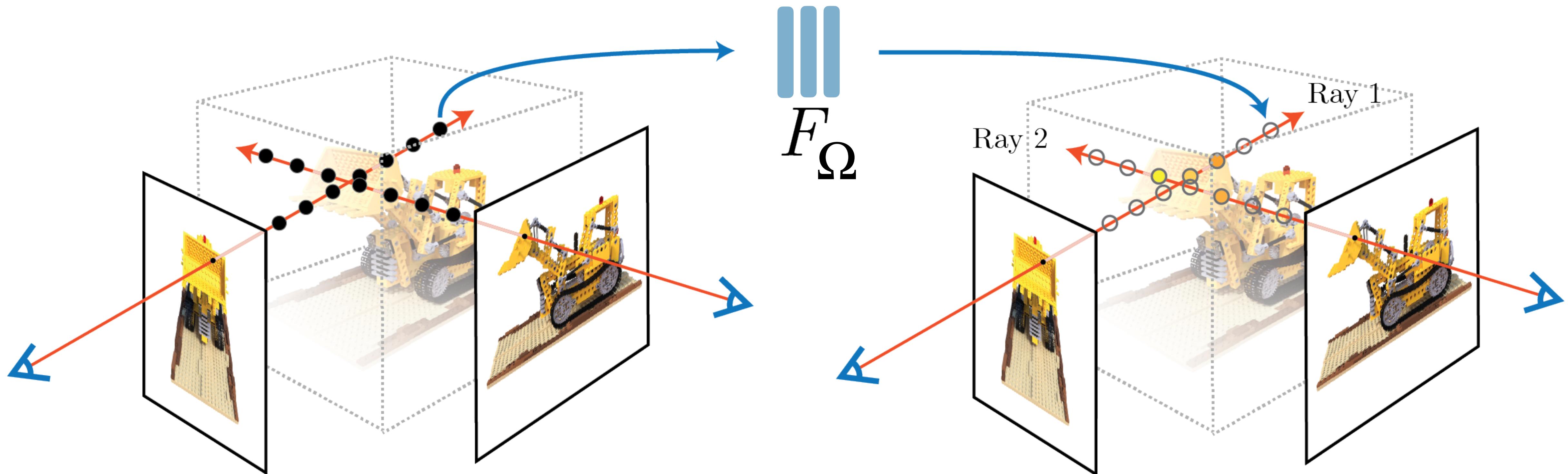
Light Traveling Along A Ray

1. Radiance is the fundamental field quantity that describes the distribution of light in an environment
  - Radiance is the quantity associated with a ray
  - Rendering is all about computing radiance
2. Radiance is invariant along a ray in a vacuum

# Representing a scene as a continuous 5D function



# Generate views with traditional volume rendering



# Generate views with traditional volume rendering

Rendering model for ray  $r(t) = o + td$ :

$$C \approx \sum_{i=1}^N T_i \alpha_i c_i$$

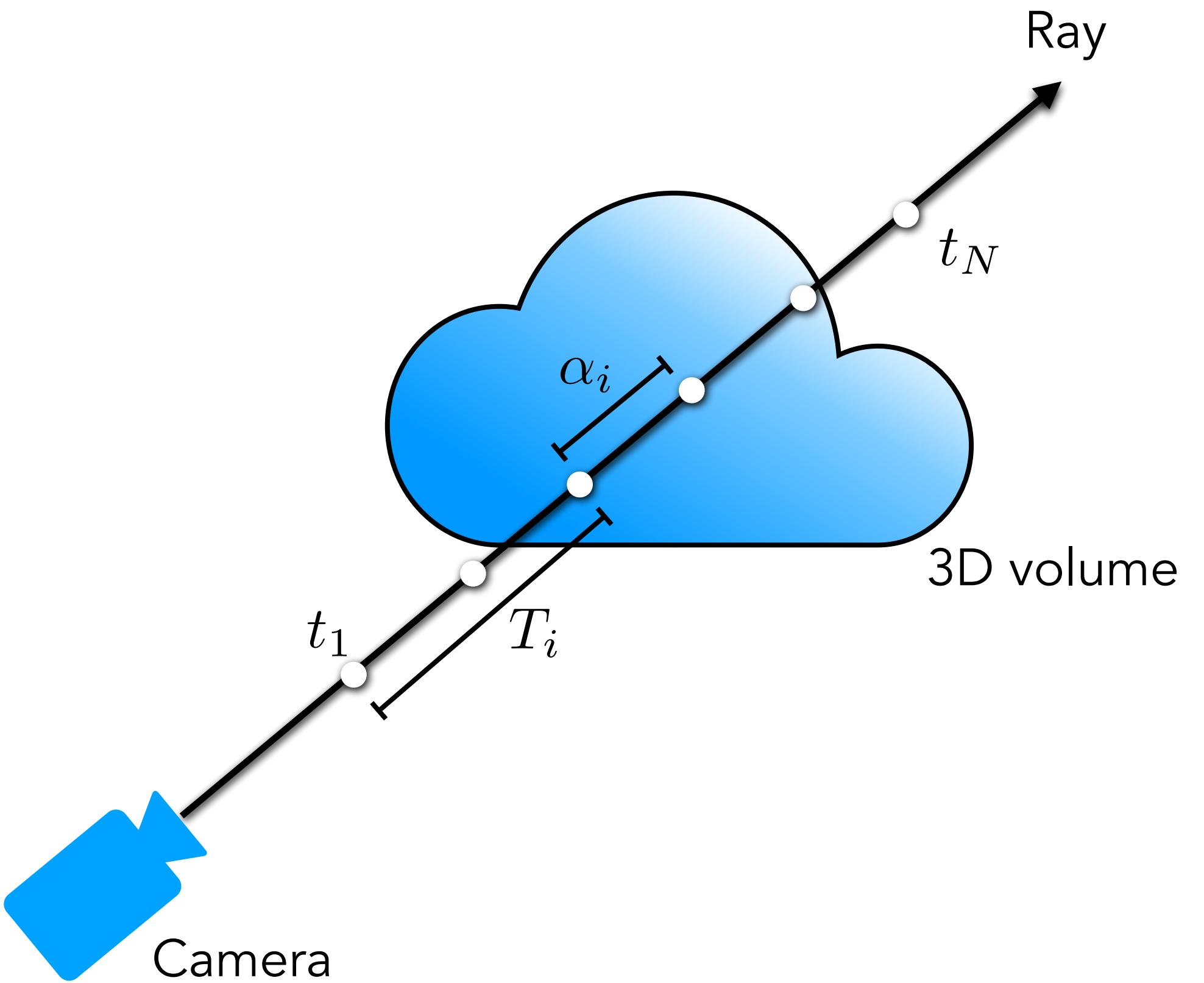
weights                      colors

How much light is blocked earlier along ray:

$$T_i = \prod_{j=1}^{i-1} (1 - \alpha_j)$$

How much light is contributed by ray segment  $i$ :

$$\alpha_i = 1 - e^{-\sigma_i \delta t_i}$$



# Effective resolution is tied to distance between samples

Rendering model for ray  $r(t) = o + td$ :

$$C \approx \sum_{i=1}^N T_i \alpha_i c_i$$

weights                      colors

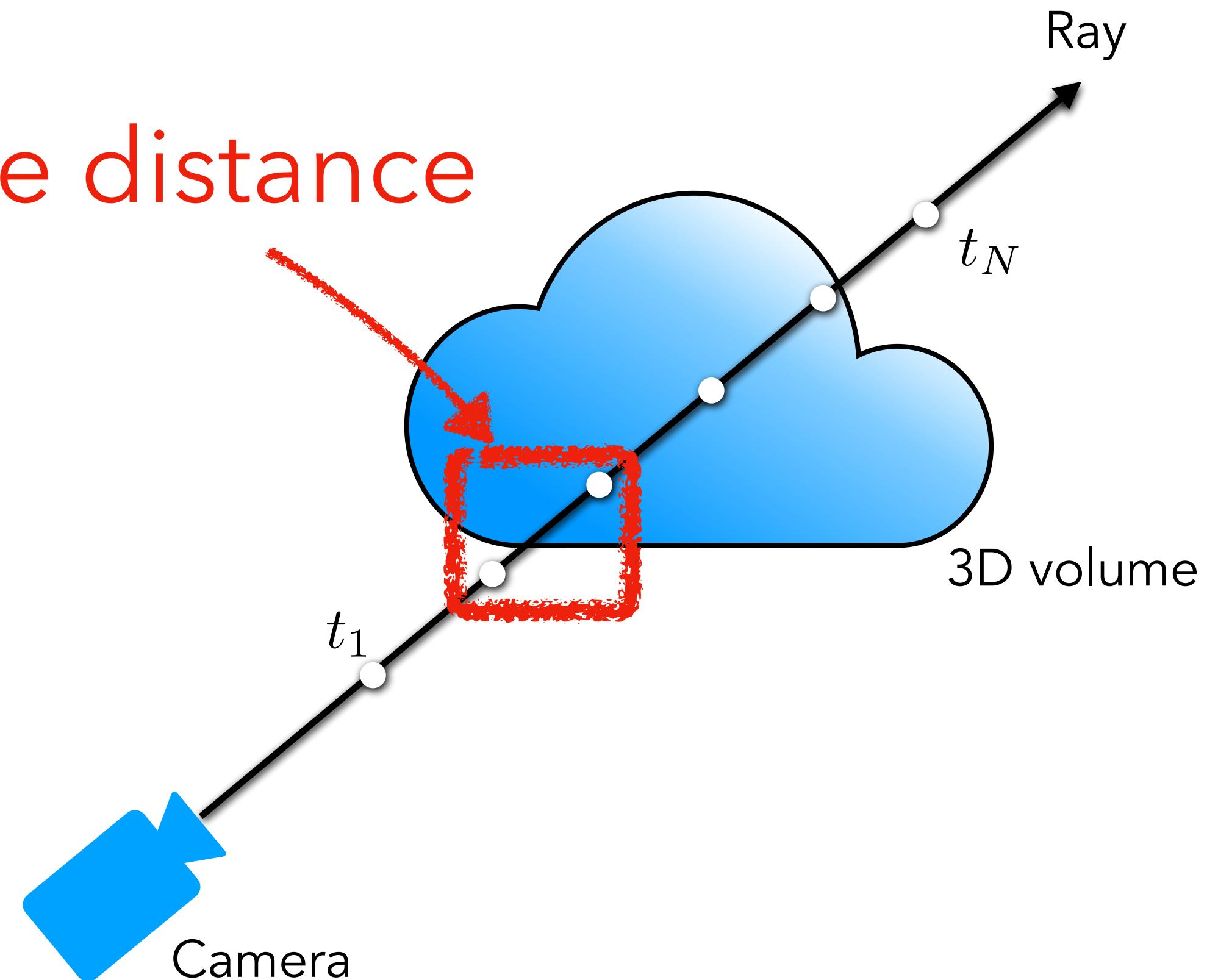
How much light is blocked earlier along ray:

$$T_i = \prod_{j=1}^{i-1} (1 - \alpha_j)$$

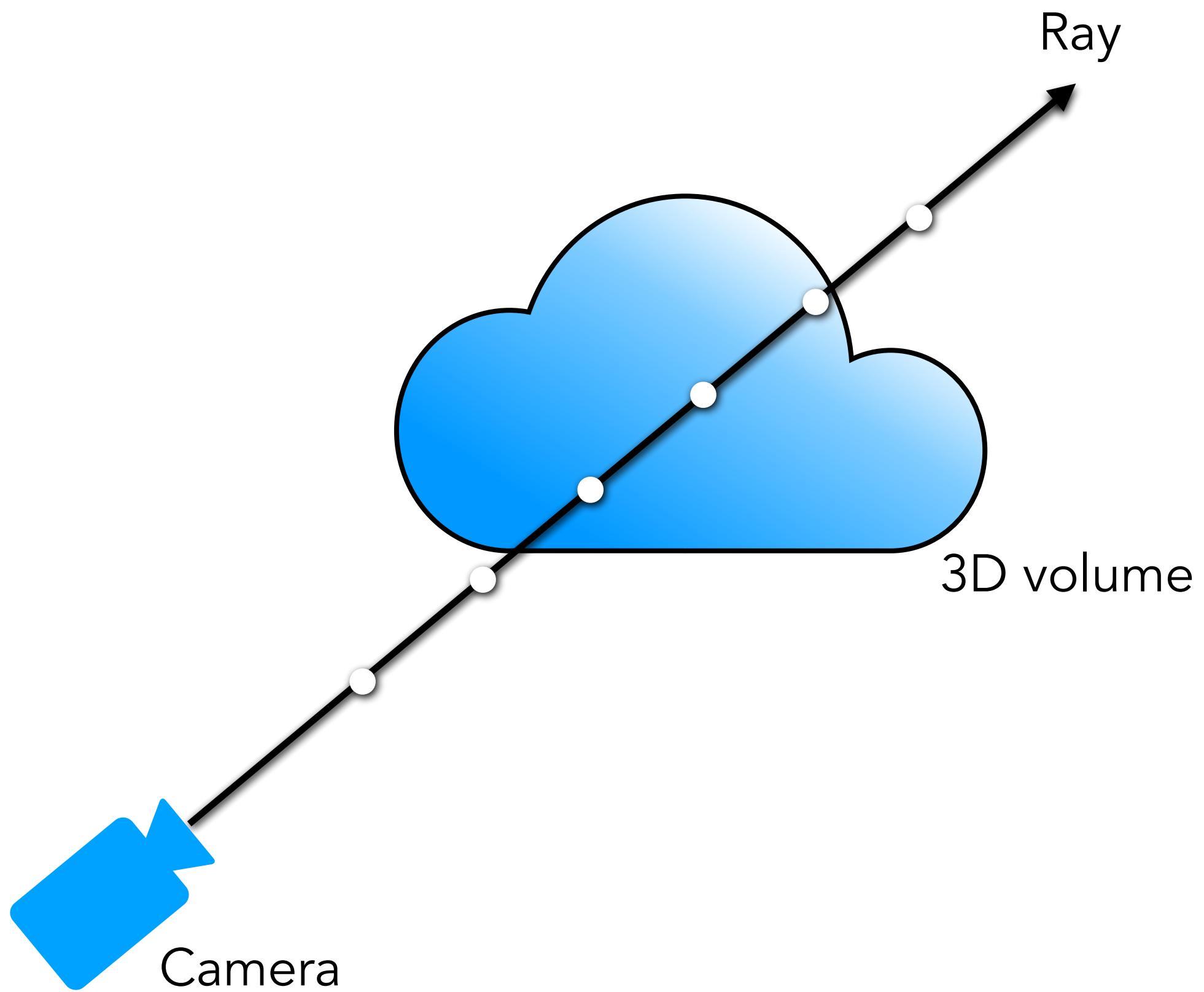
How much light is contributed by ray segment  $i$ :

$$\alpha_i = 1 - e^{-\sigma_i \delta t_i}$$

sample distance



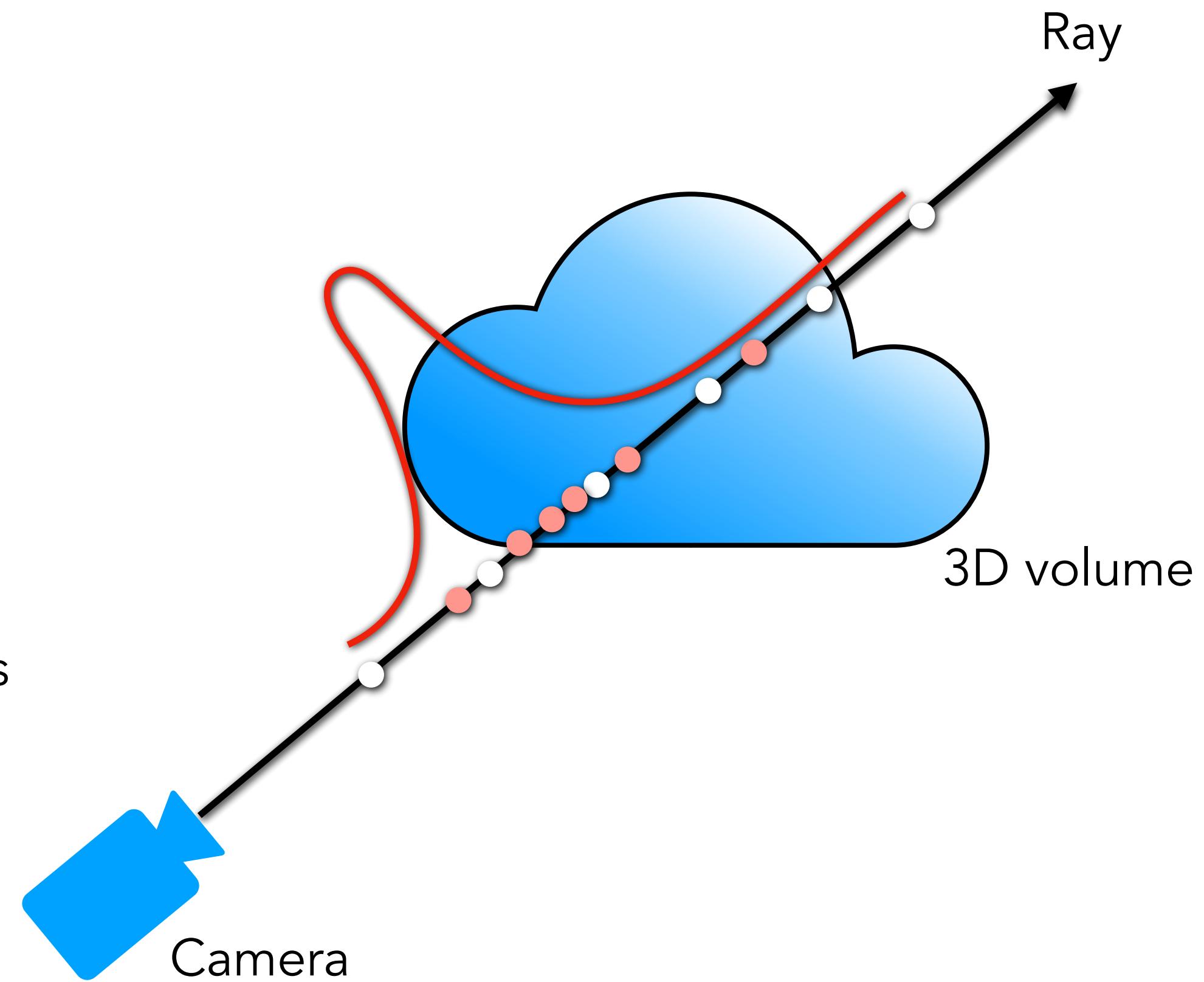
Can we allocate samples more efficiently? Two pass rendering



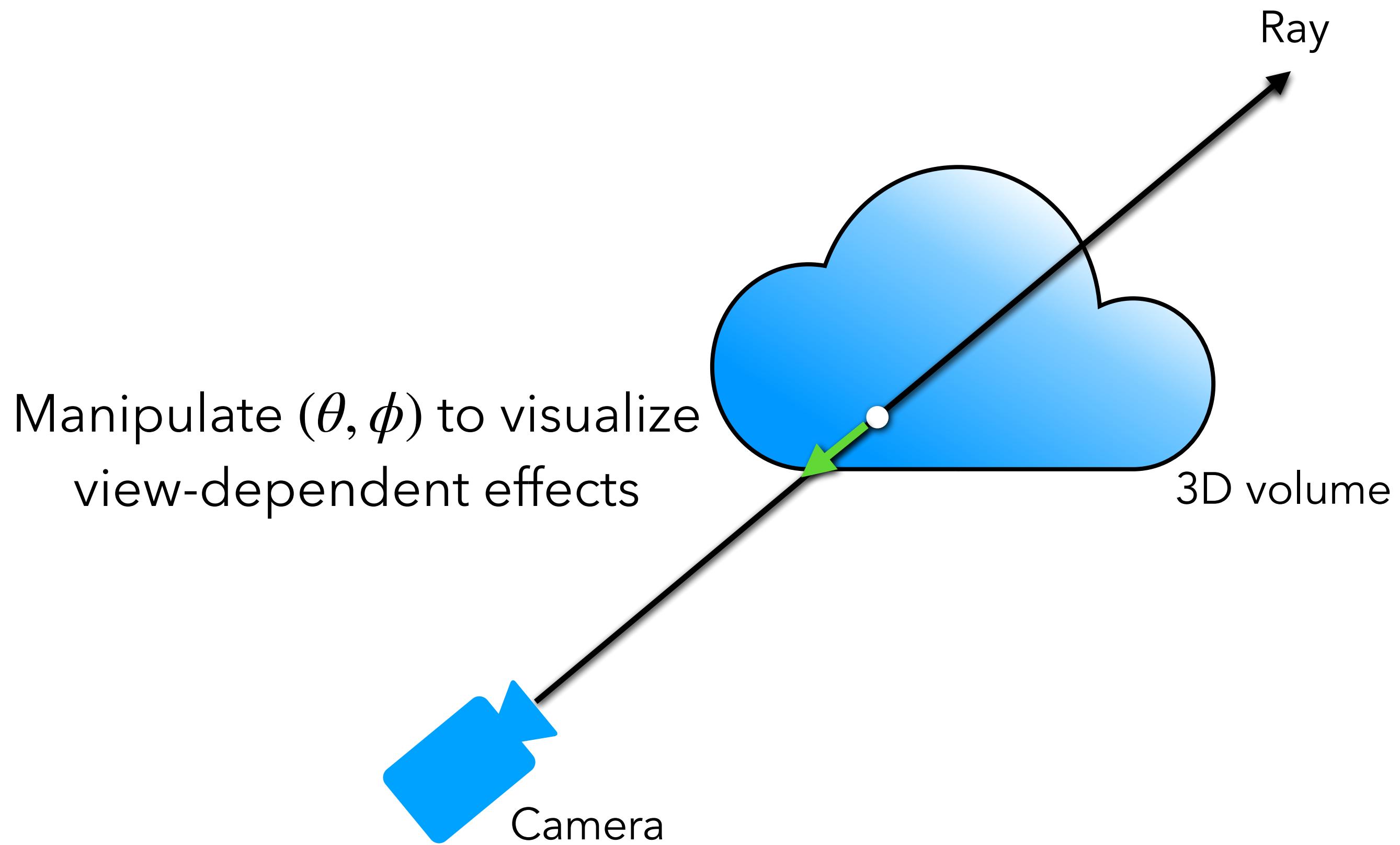
# Two pass rendering: fine

$$C \approx \sum_{i=1}^N T_i \alpha_i c_i$$

treat weights as probability distribution for new samples



# Viewing directions as input



# Volume rendering is differentiable

Rendering model for ray  $r(t) = o + td$ :

$$C \approx \sum_{i=1}^N T_i \alpha_i c_i$$

differentiable w.r.t.

weights

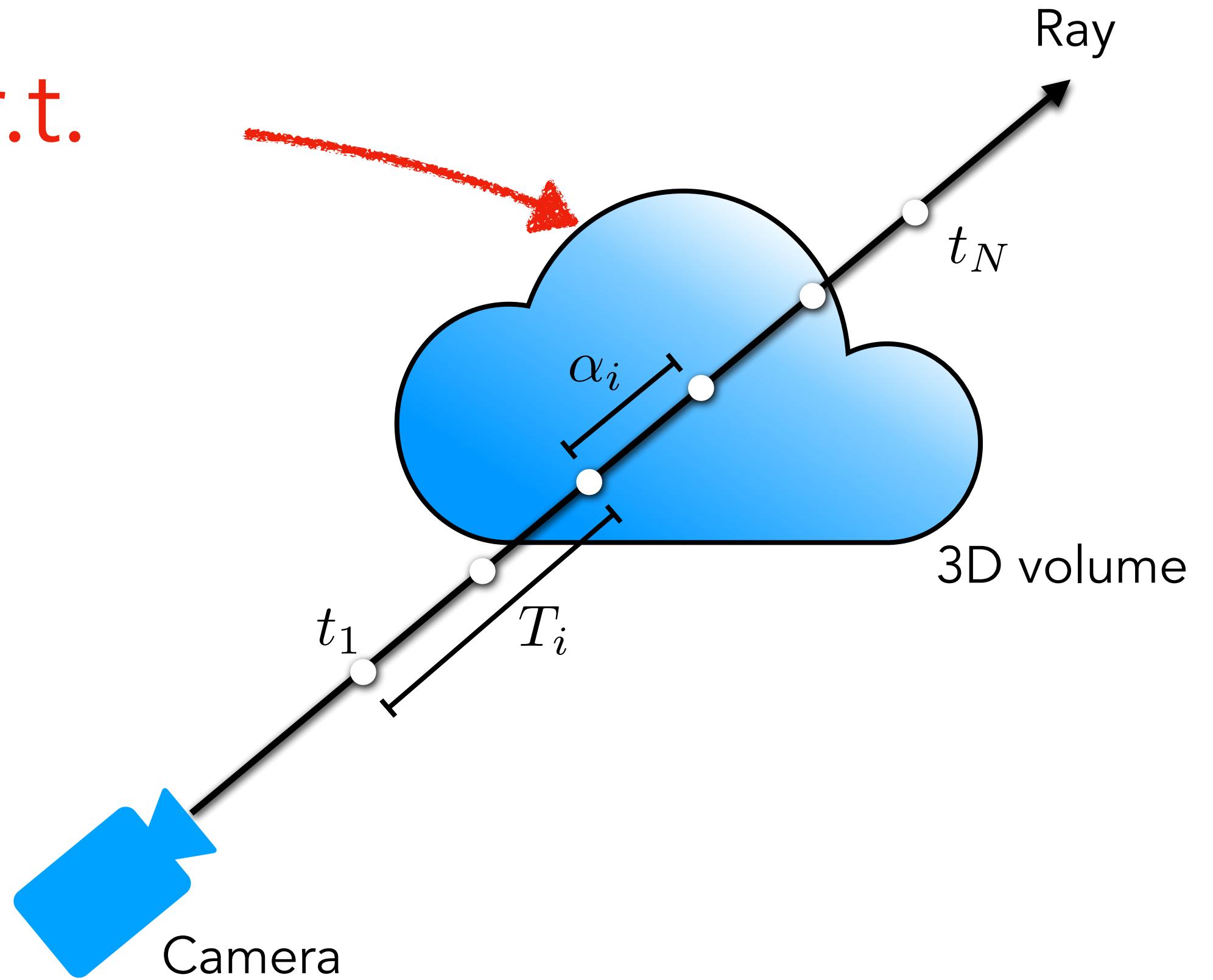
colors

How much light is blocked earlier along ray:

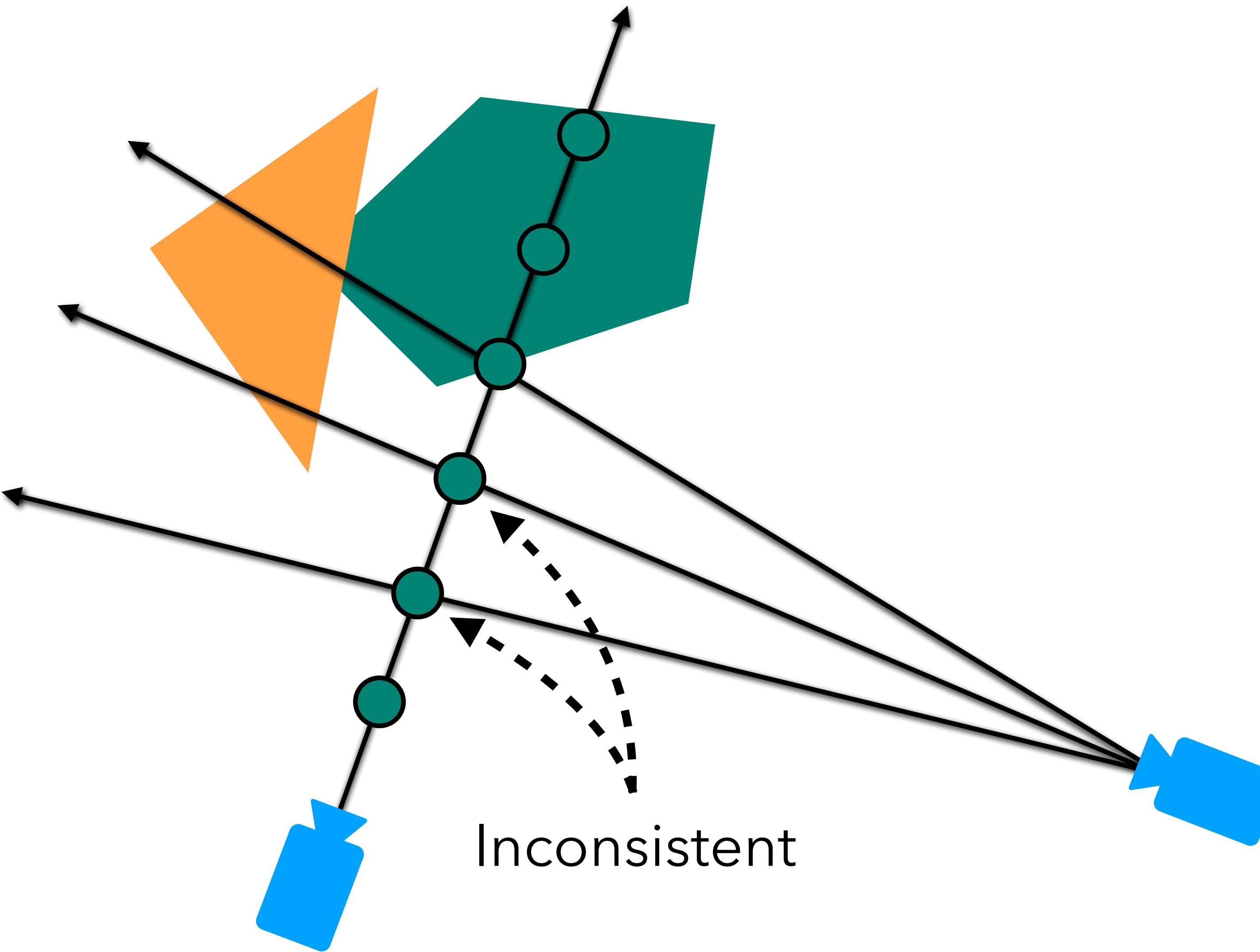
$$T_i = \prod_{j=1}^{i-1} (1 - \alpha_j)$$

How much light is contributed by ray segment  $i$ :

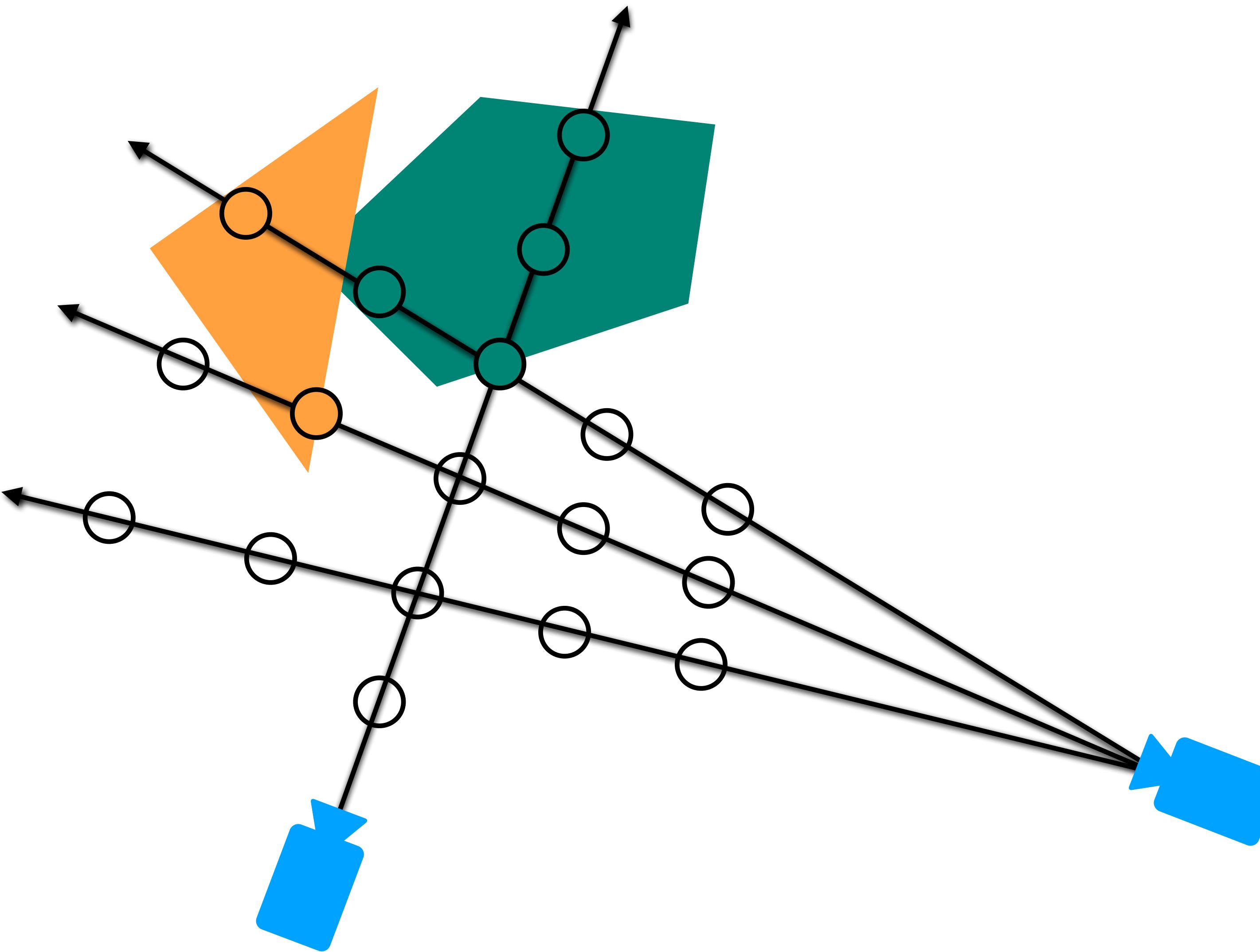
$$\alpha_i = 1 - e^{-\sigma_i \delta t_i}$$

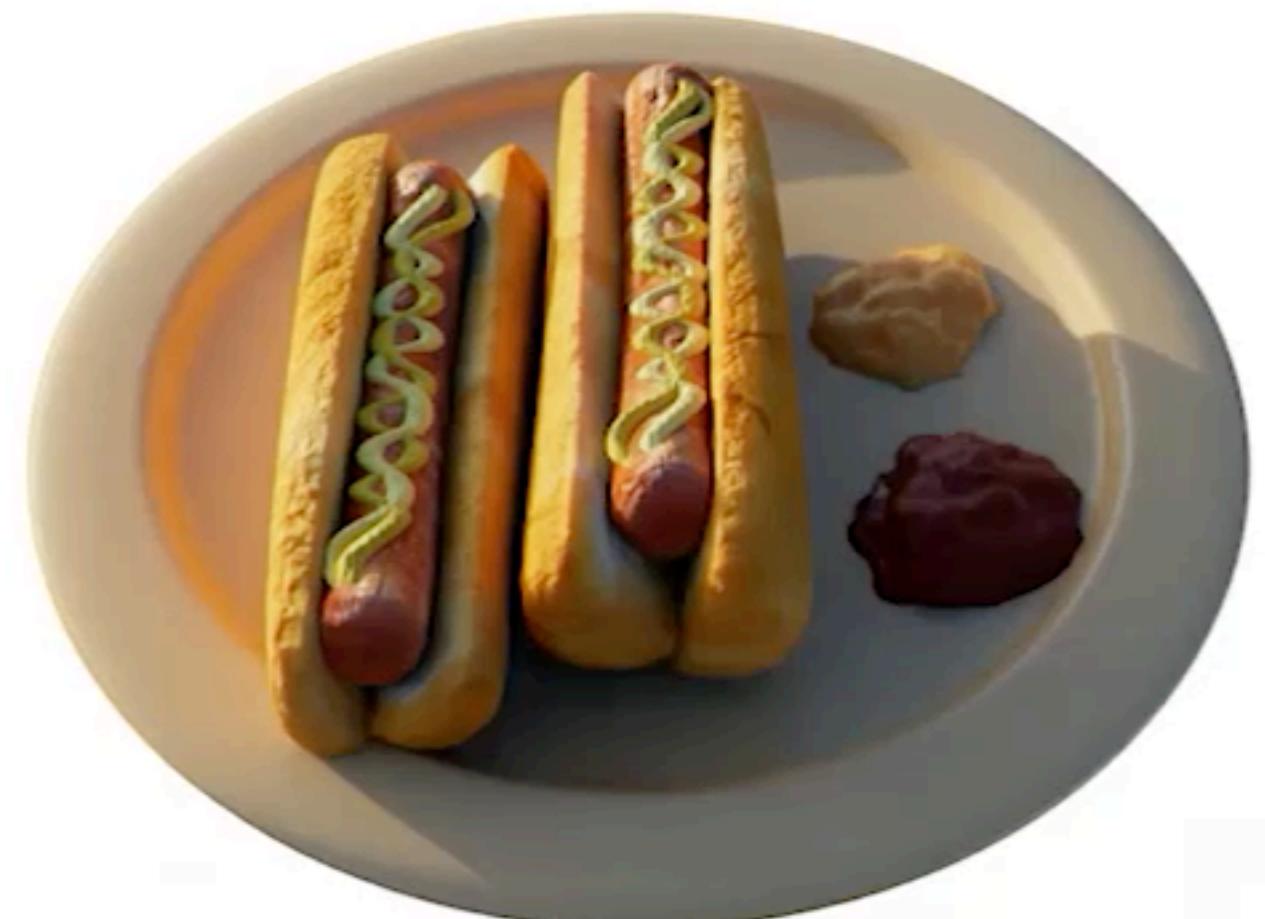
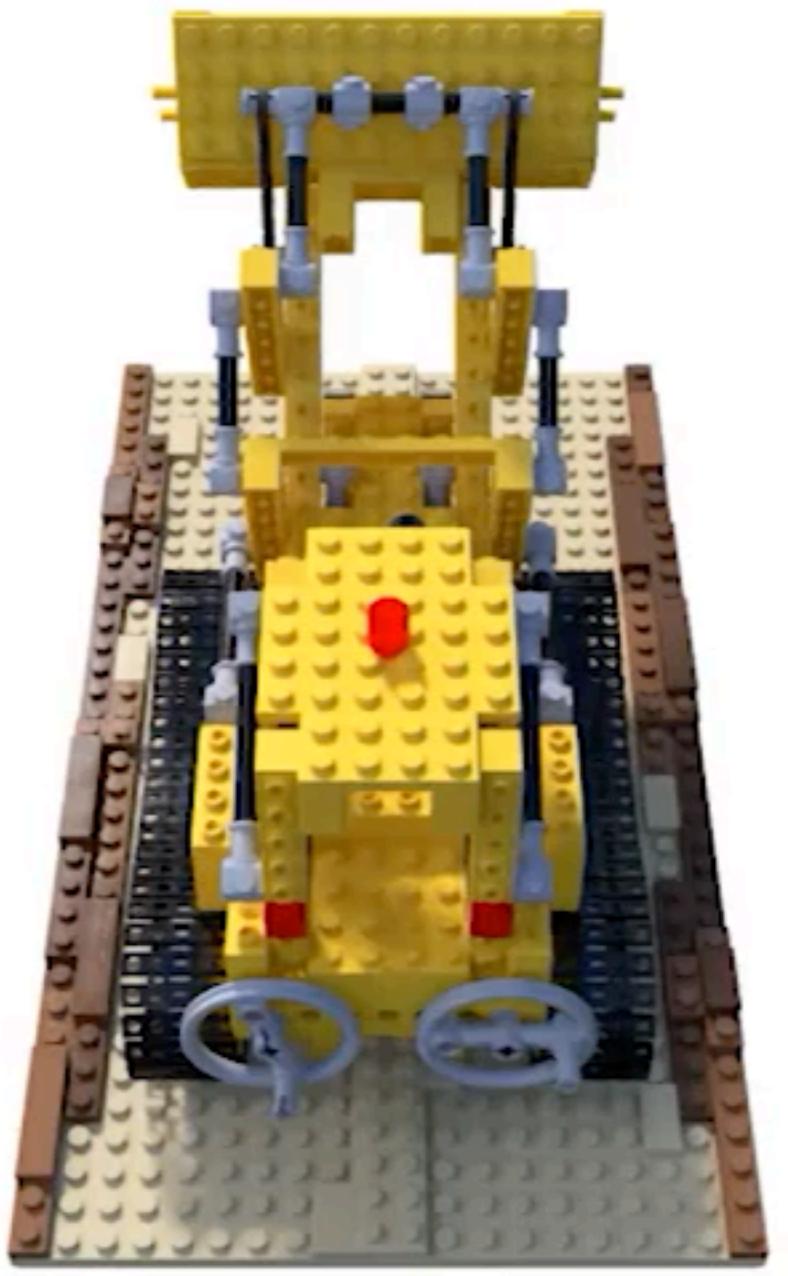


# Multiview Consistency as Supervision



# Multiview Consistency as Supervision







# NeRF encodes convincing view-dependent effects using directional dependence



NeRF encodes convincing view-dependent effects using directional dependence



NeRF encodes detailed scene geometry with occlusion effects



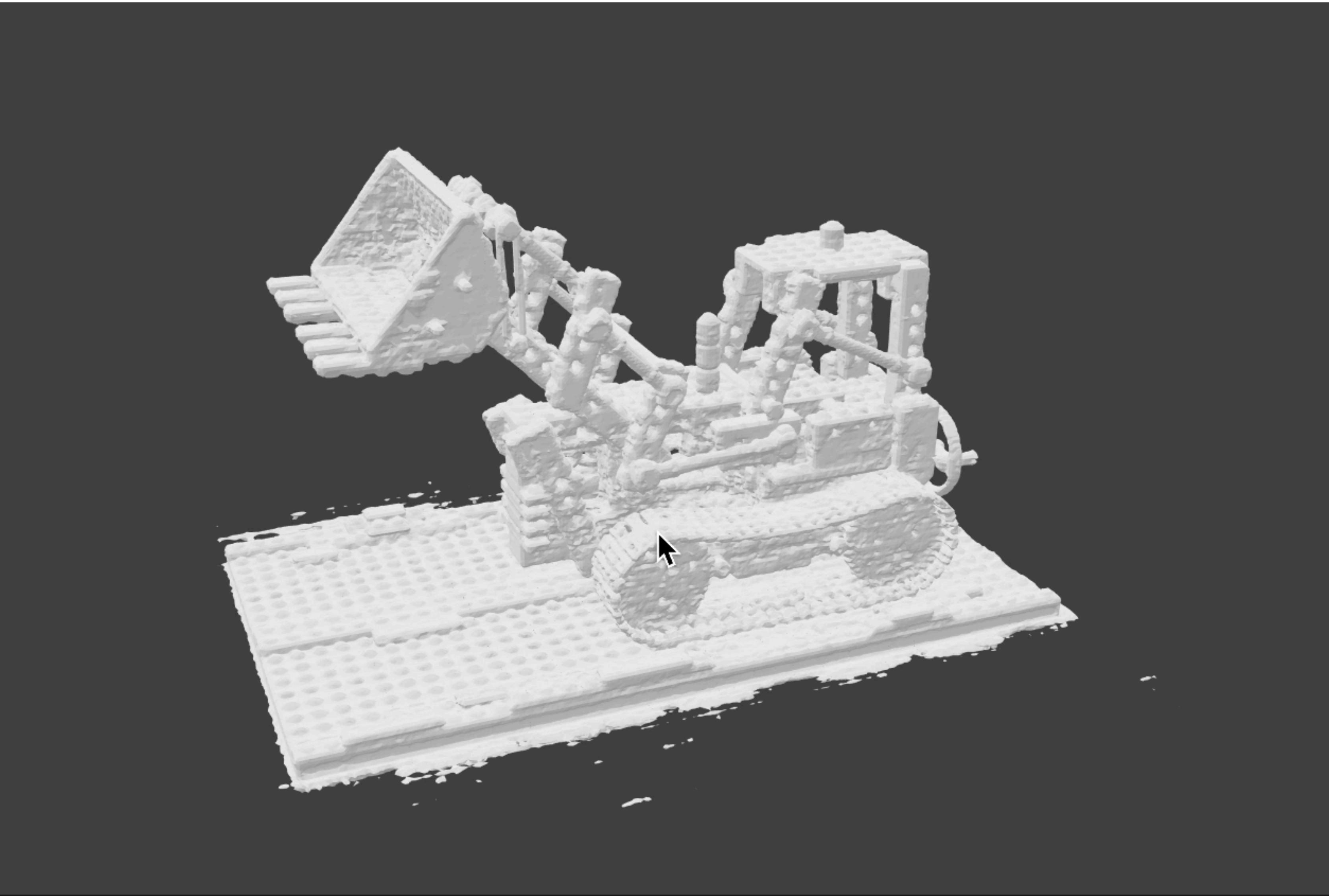
NeRF encodes detailed scene geometry with occlusion effects



# NeRF encodes detailed scene geometry with occlusion effects



# NeRF encodes detailed scene geometry



# Naive implementation produces blurry results



NeRF (Naive)

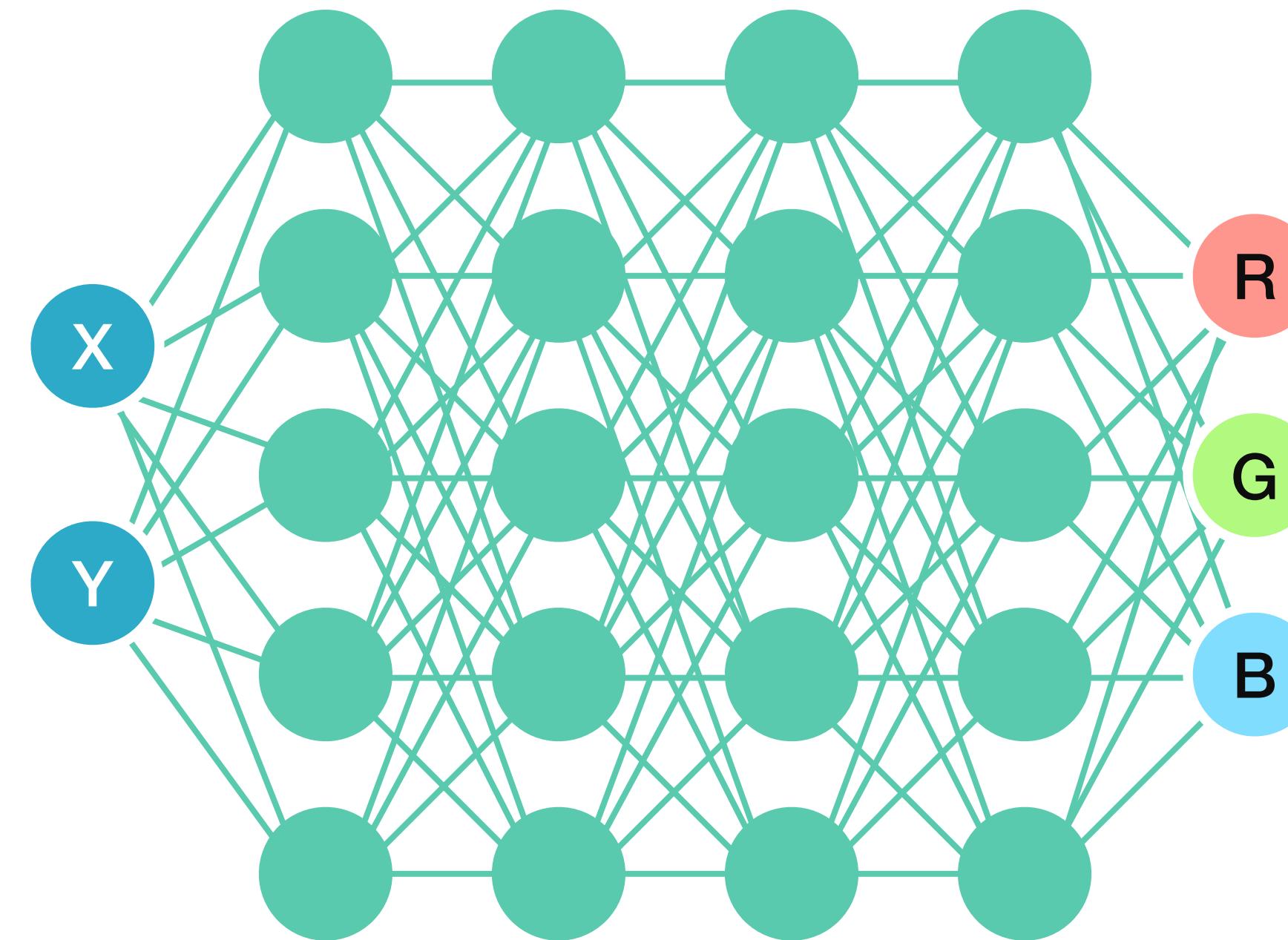


NeRF (with positional encoding)

# Challenge:

How to get MLPs to represent higher frequency functions?

# Image Representation



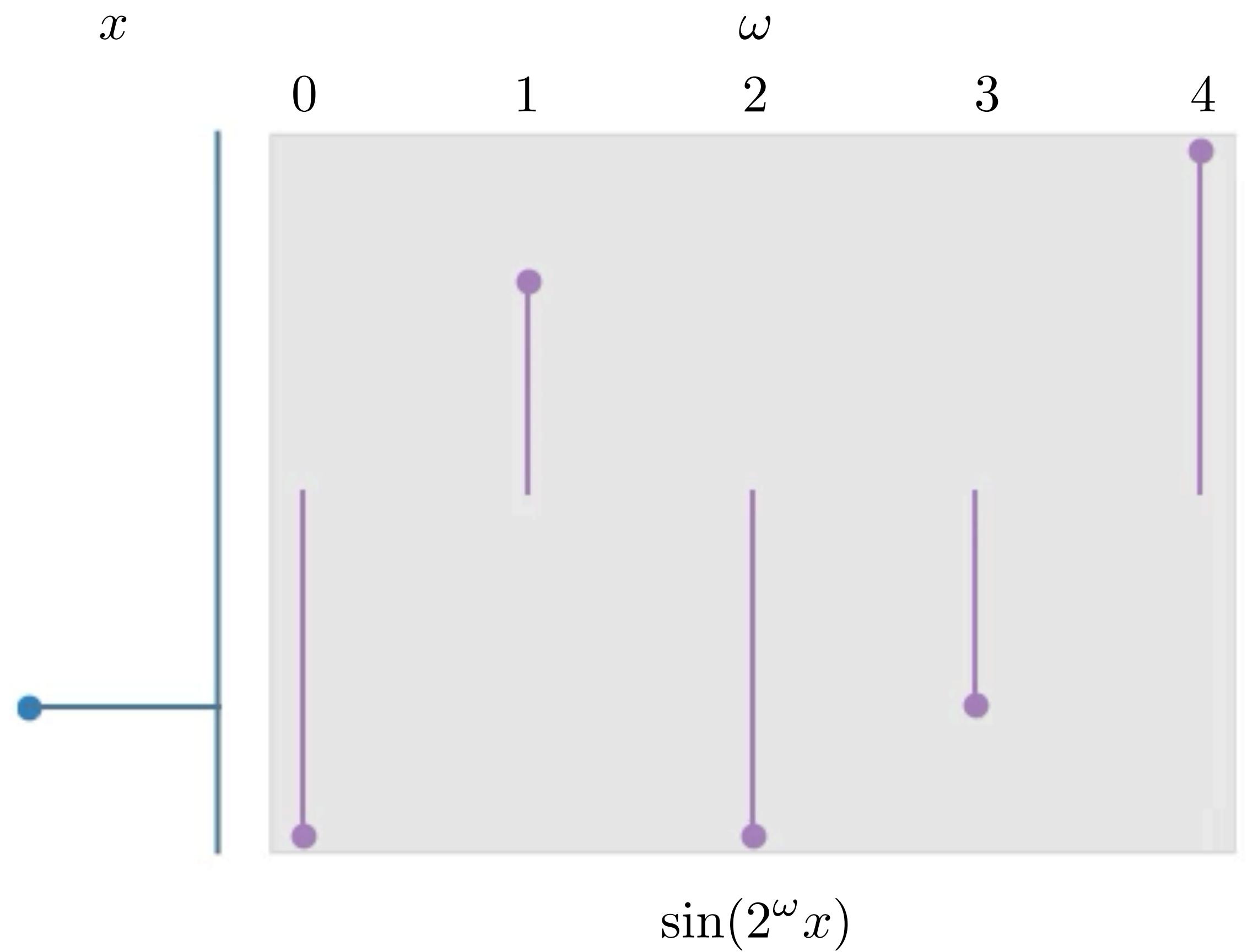


MLP output

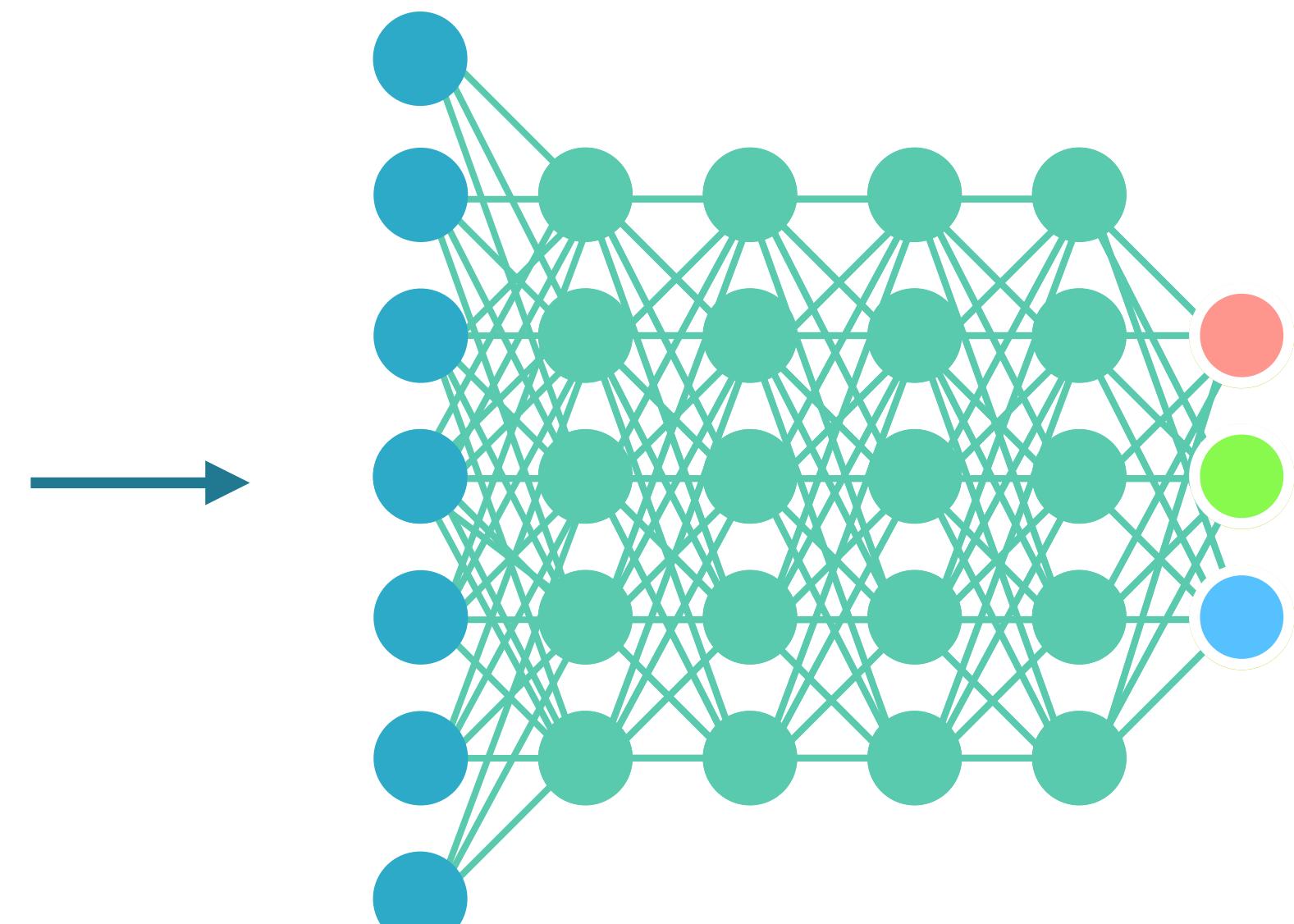


Supervision image

Standard input

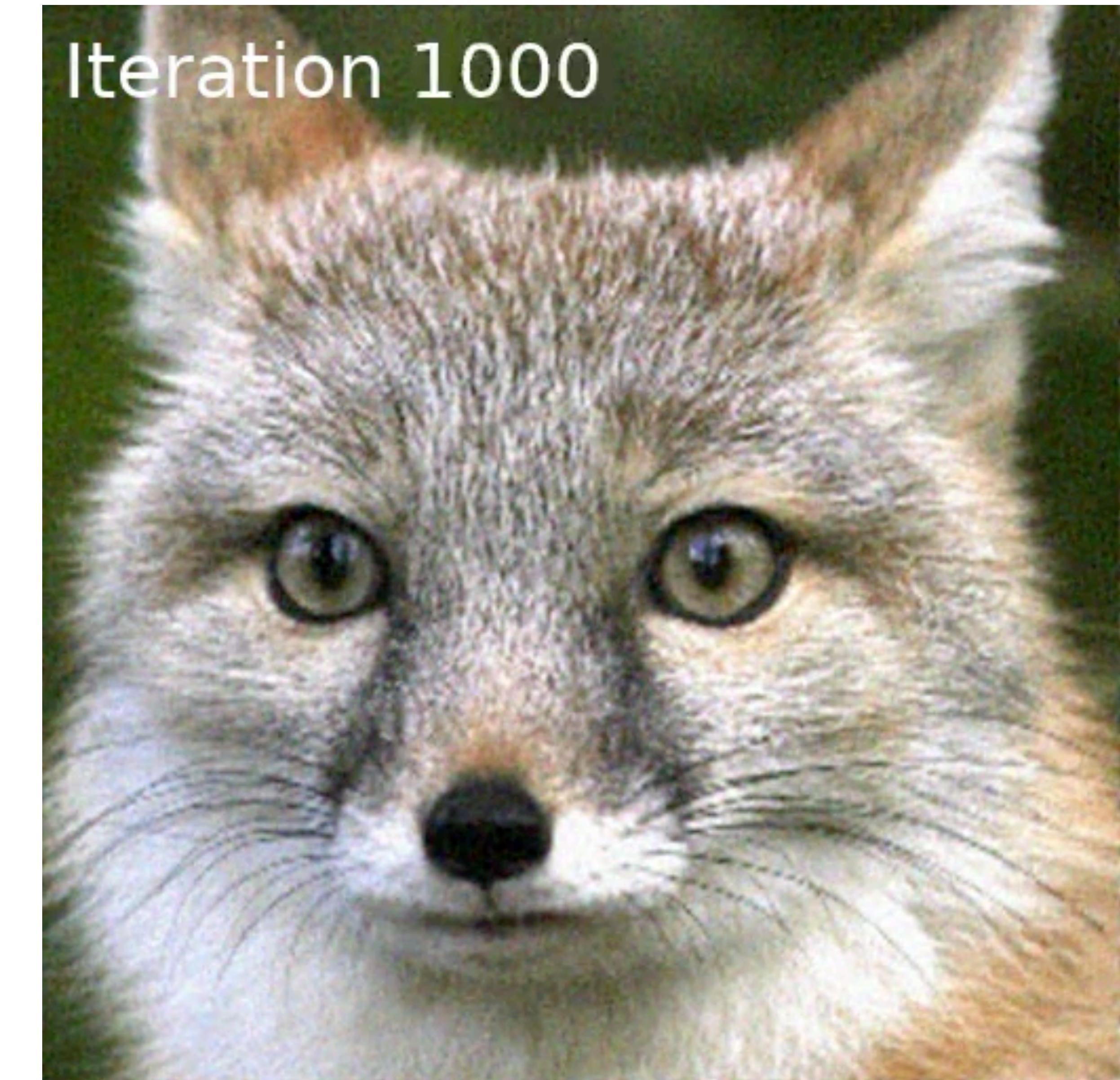


Fourier feature input



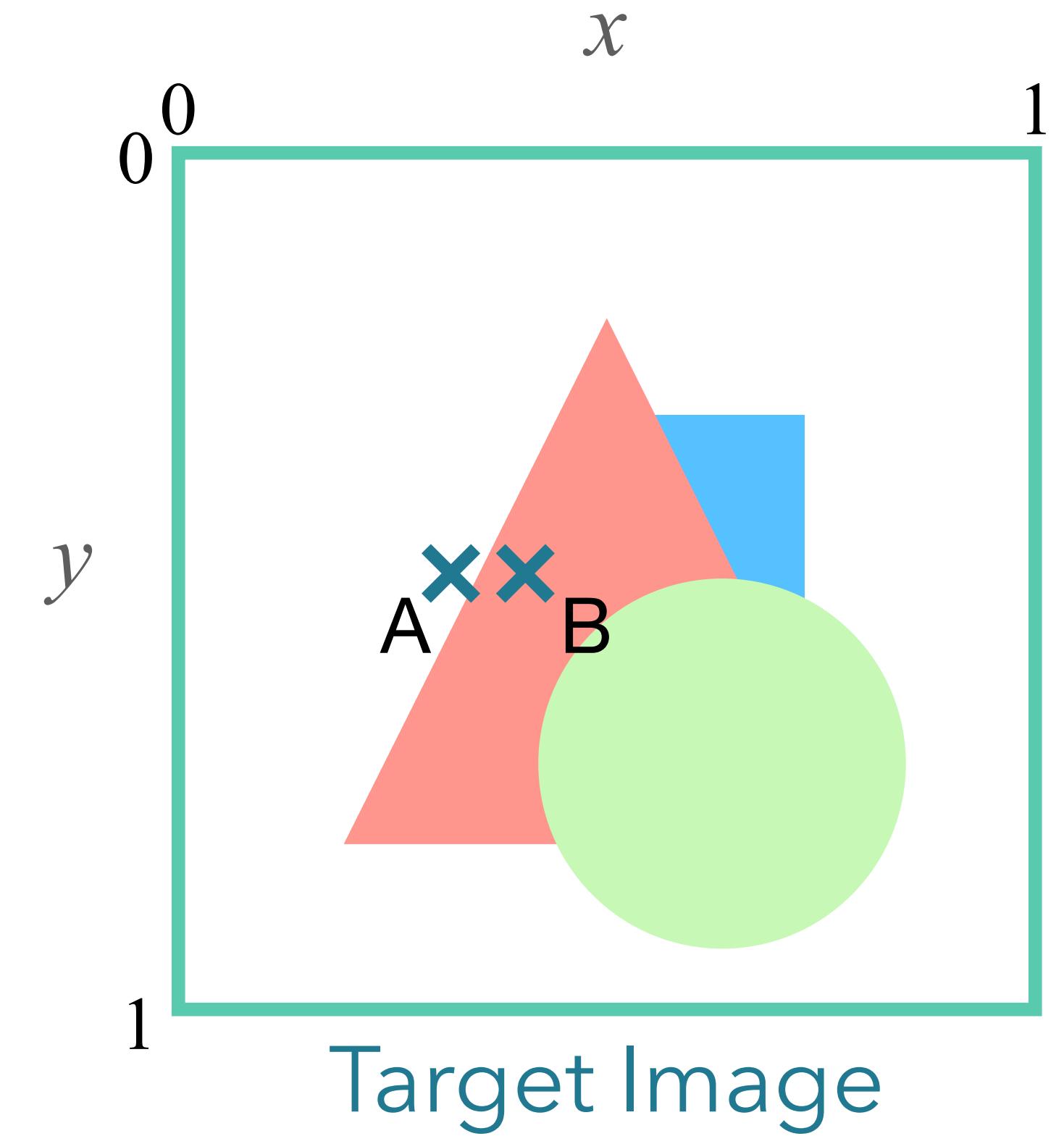
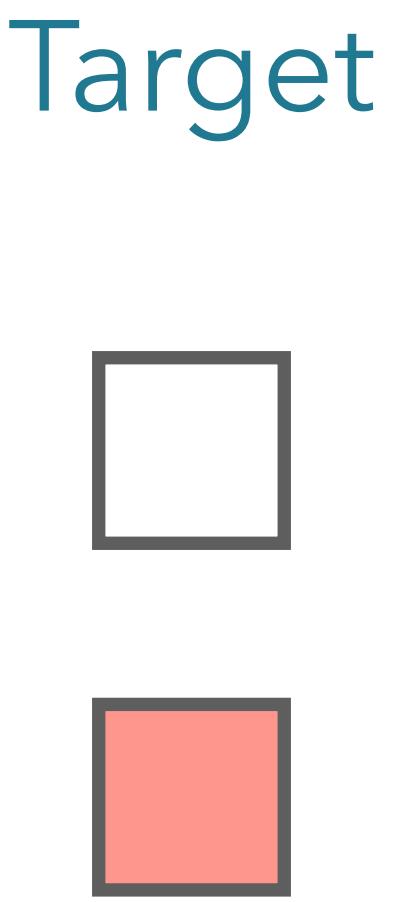


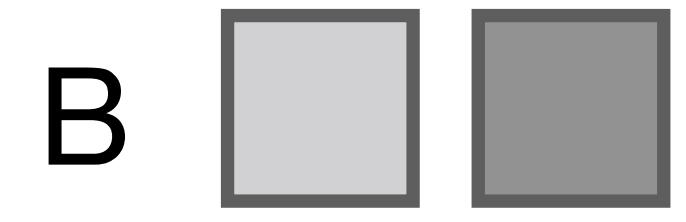
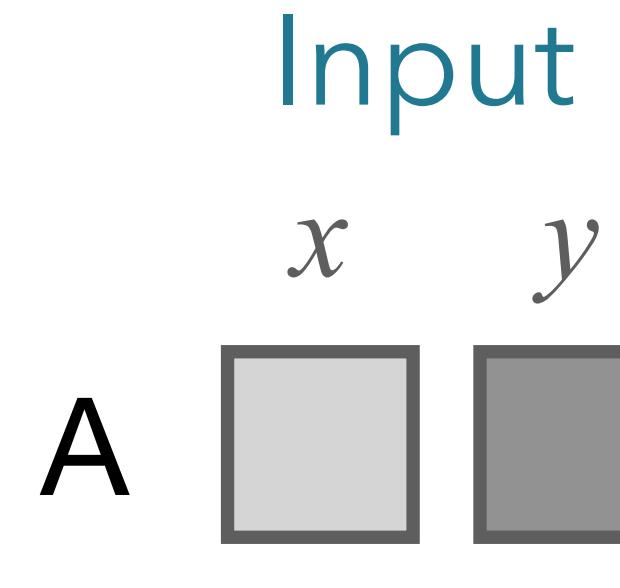
Standard MLP



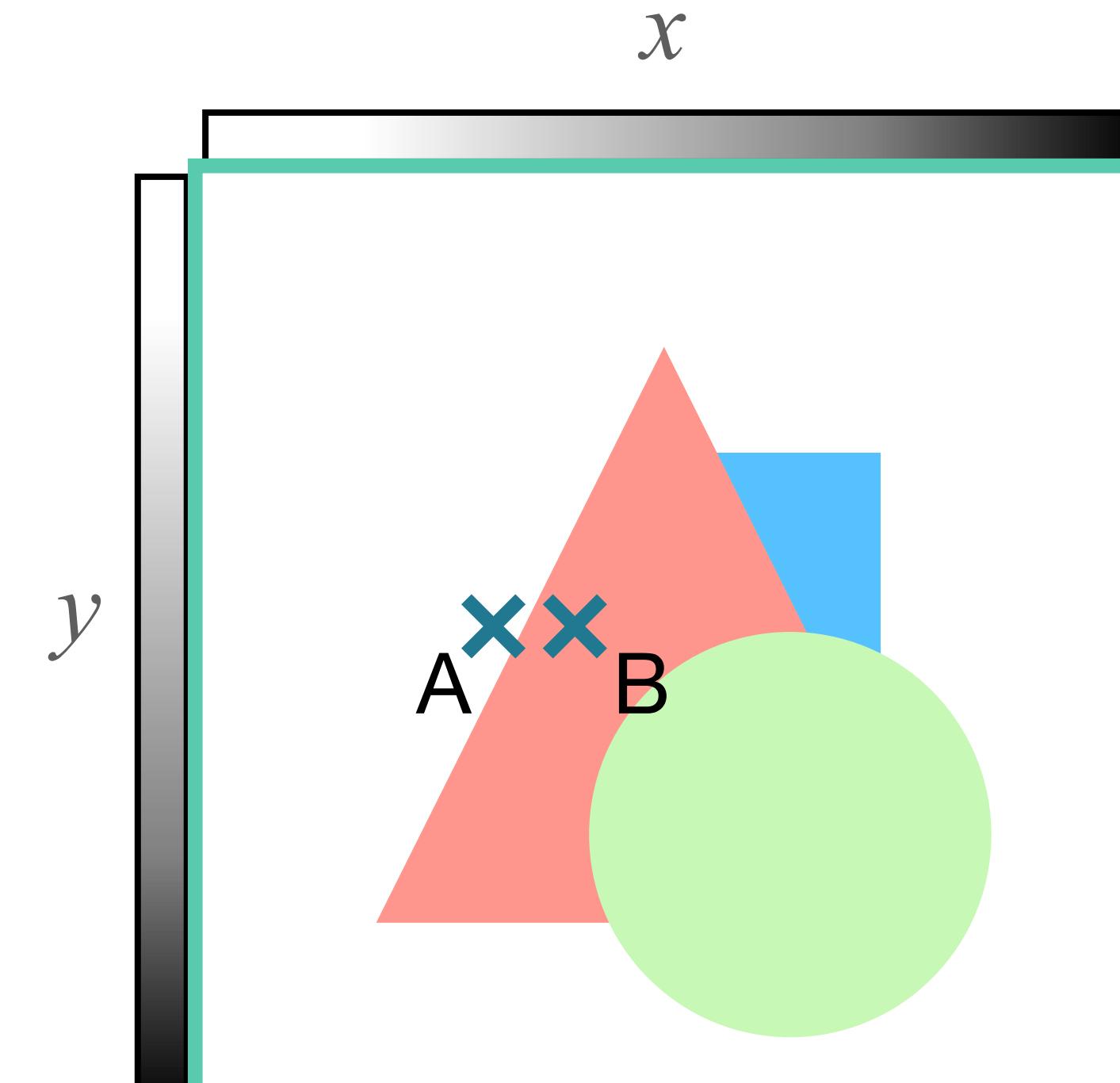
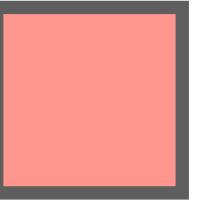
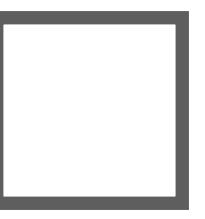
MLP with Fourier features

	Input	
	$x$	$y$
A	.36	.5
B	.38	.5





**Target**

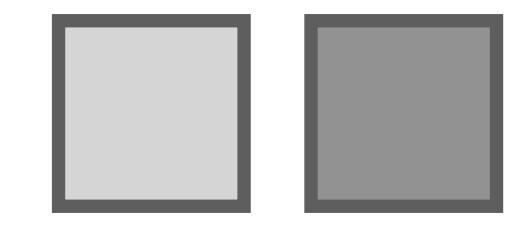


A  B

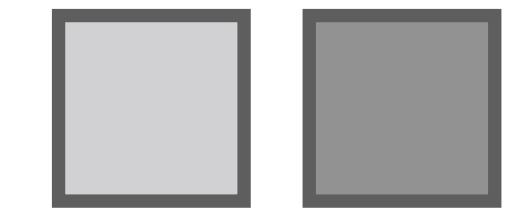
Input

$x$        $y$

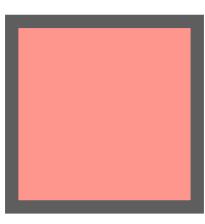
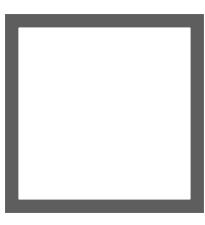
A



B



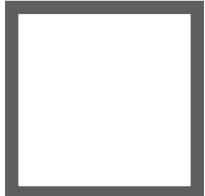
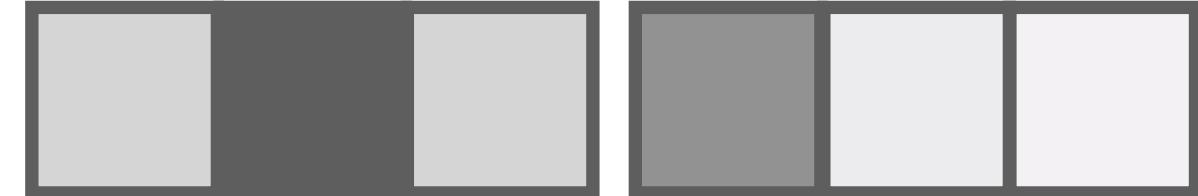
Target



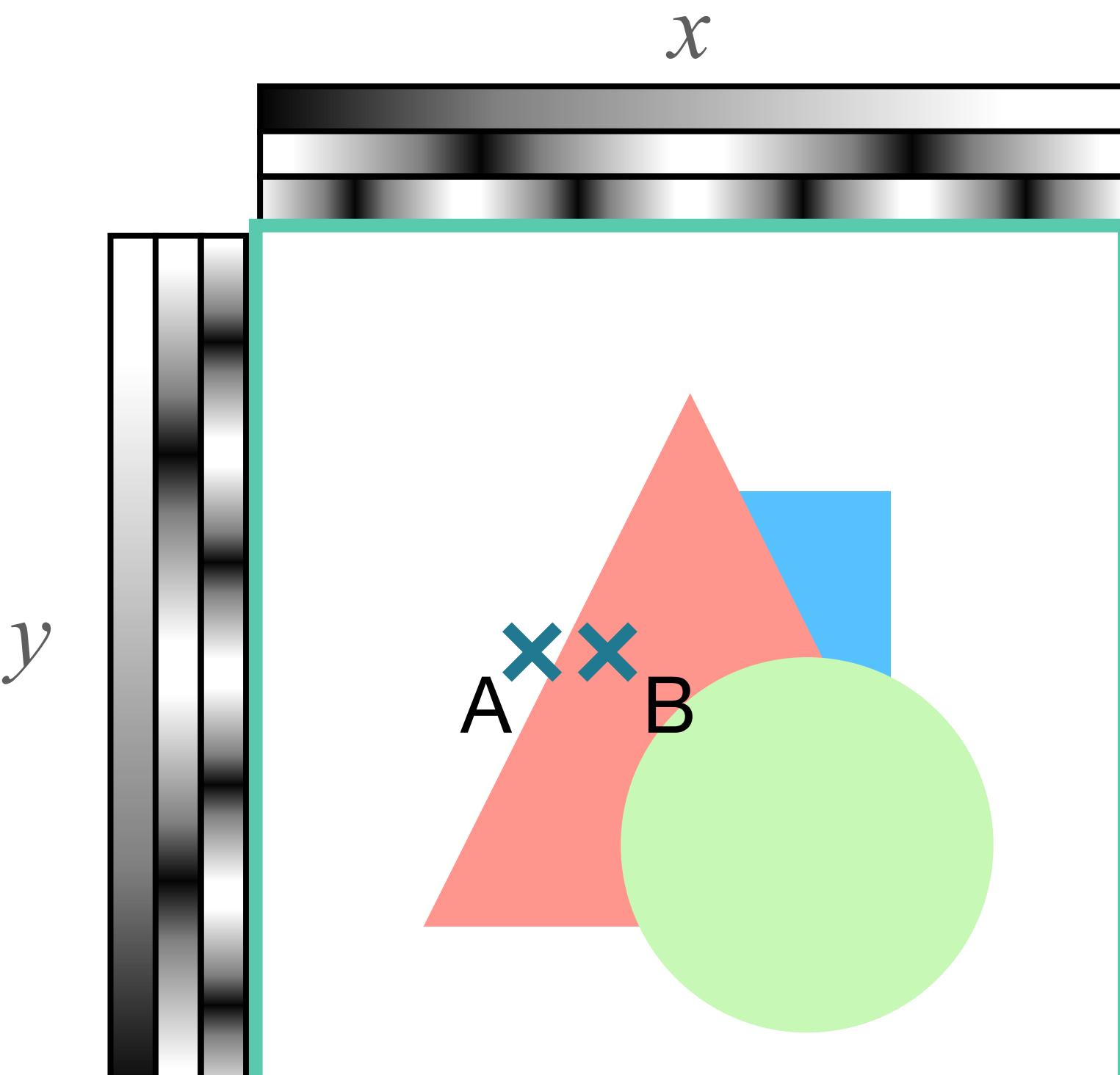
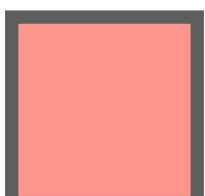
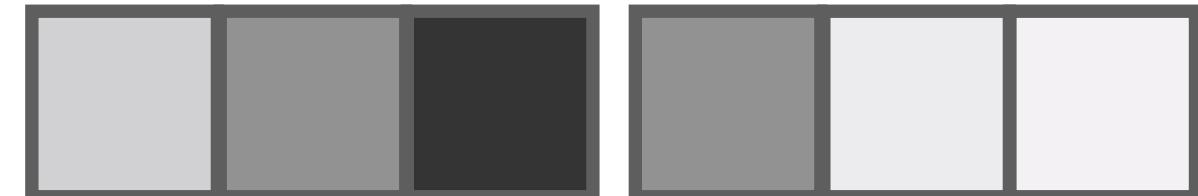
With Positional Encoding

$x$        $y$

A



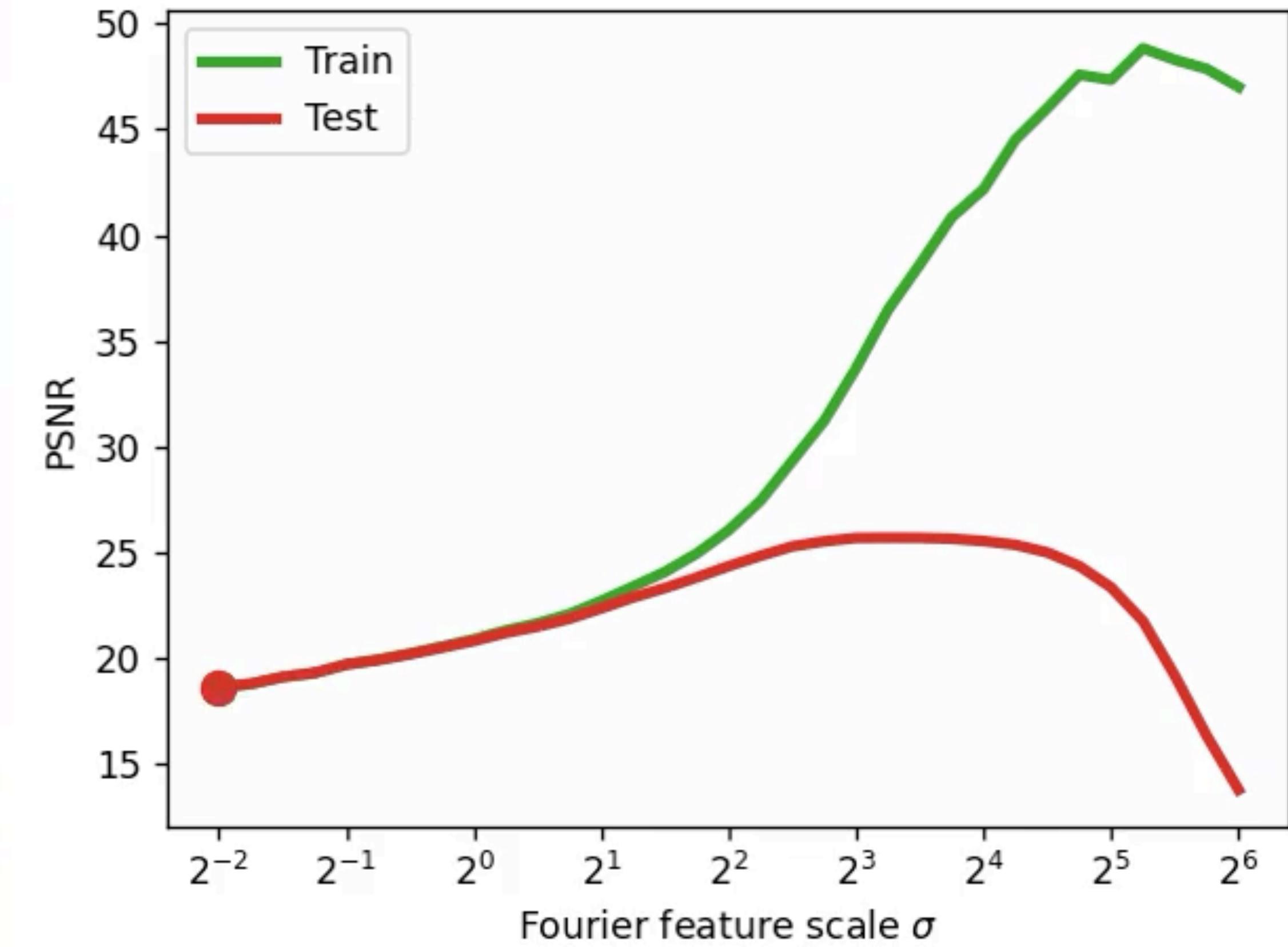
B



# Performance depends on max encoding frequency



Network output



Performance vs. scale value

# Mapping Code

## Original

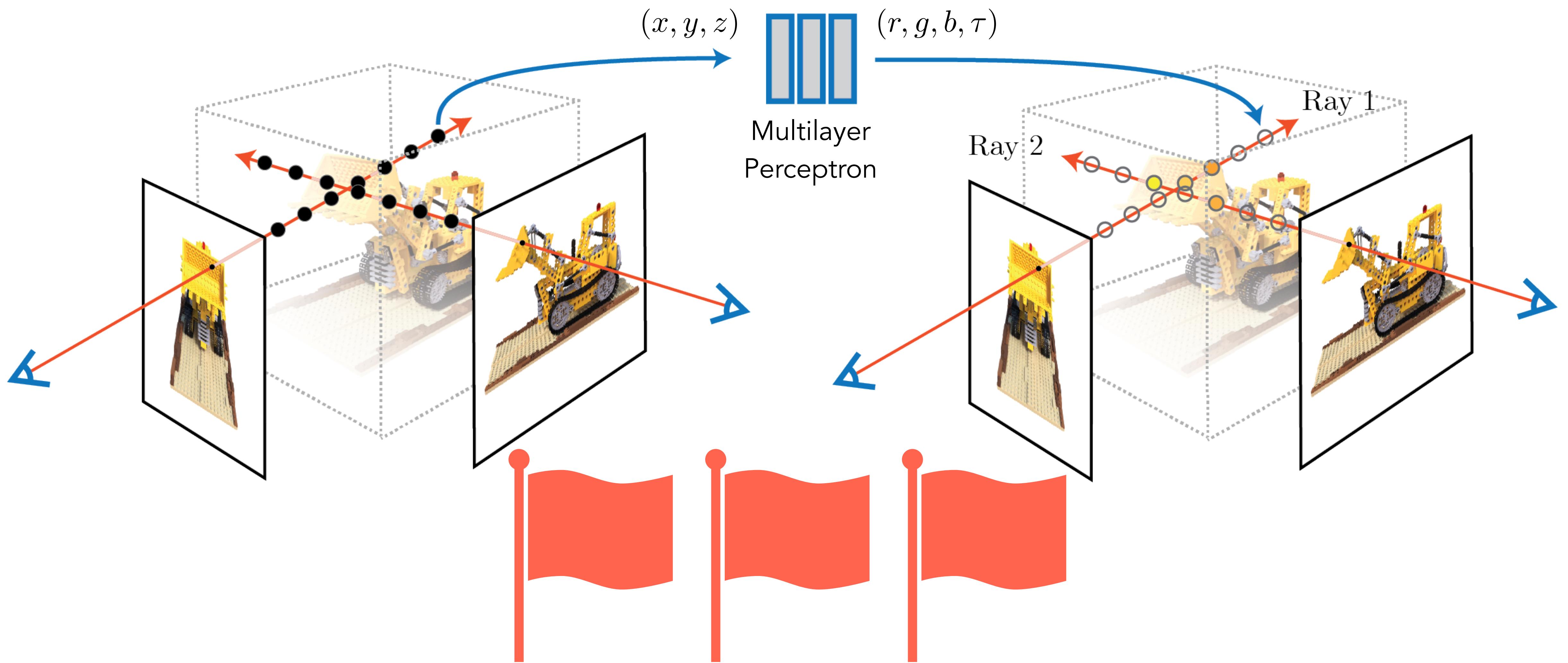
```
x = input_coordinate  
x = nn.Dense(x, features=256)  
⋮
```

## With Positional Encoding

```
x = input_coordinate  
B = SCALE * np.random.normal(shape=(input_dims, NUM_FEATURES))  
rff_input = np.concatenate([np.sin((2*np.pi*x) @ B), np.cos((2*np.pi*x) @ B)], axis=-1)  
x = nn.Dense(rff_input, features=256)  
⋮
```

# NeRF Extensions

# Point Samples of a Continuous Function



# Solution: Prefiltering with a mipmap

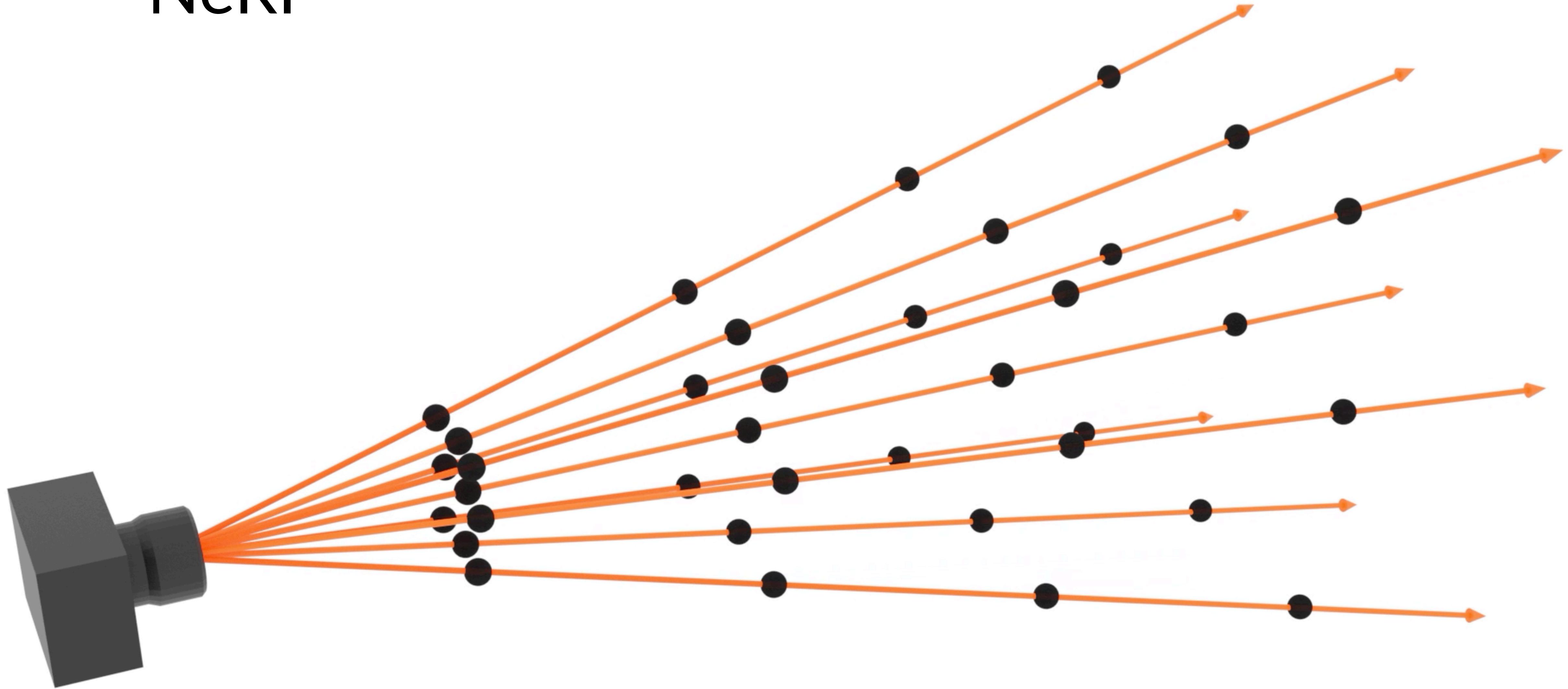


mipmaps reduce image aliasing

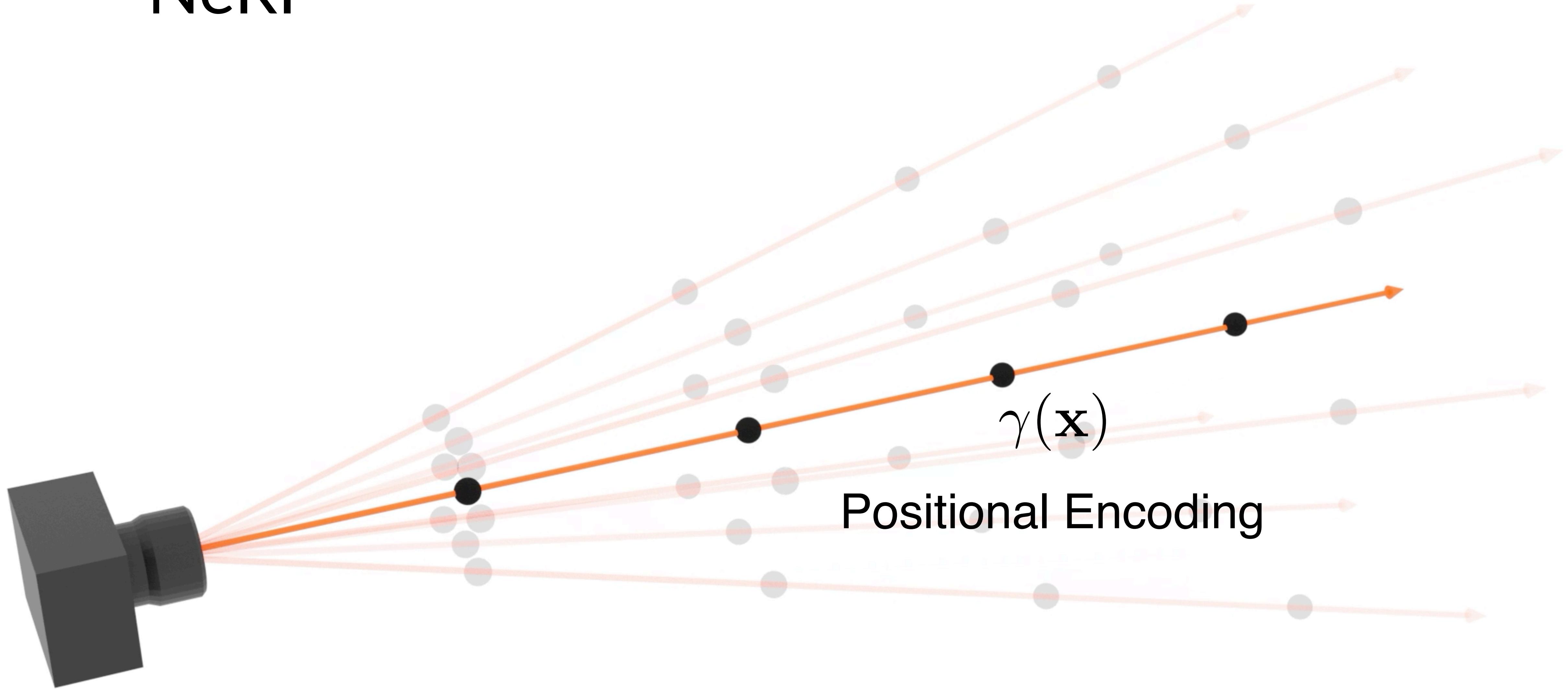
mip-NeRF reduces NeRF aliasing

How can we prefilter a neural network?

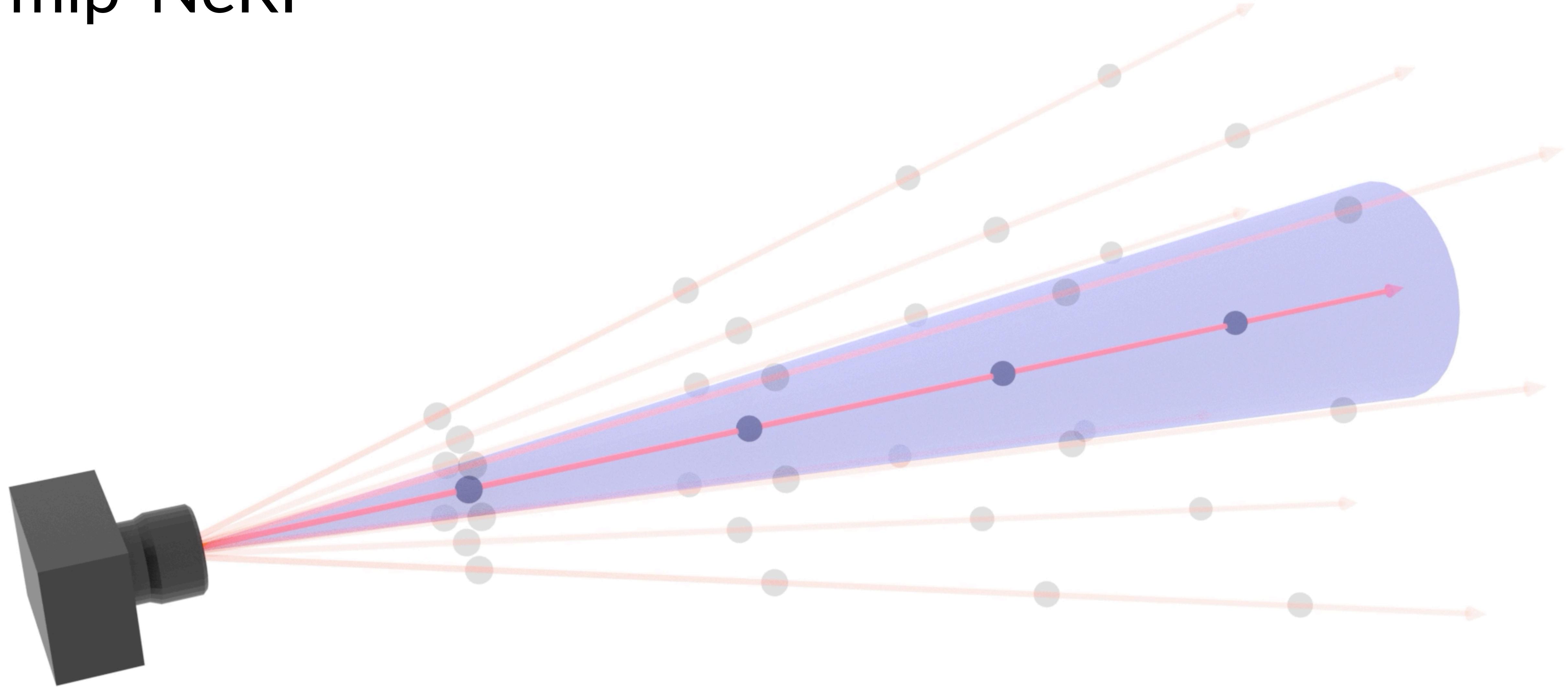
# NeRF



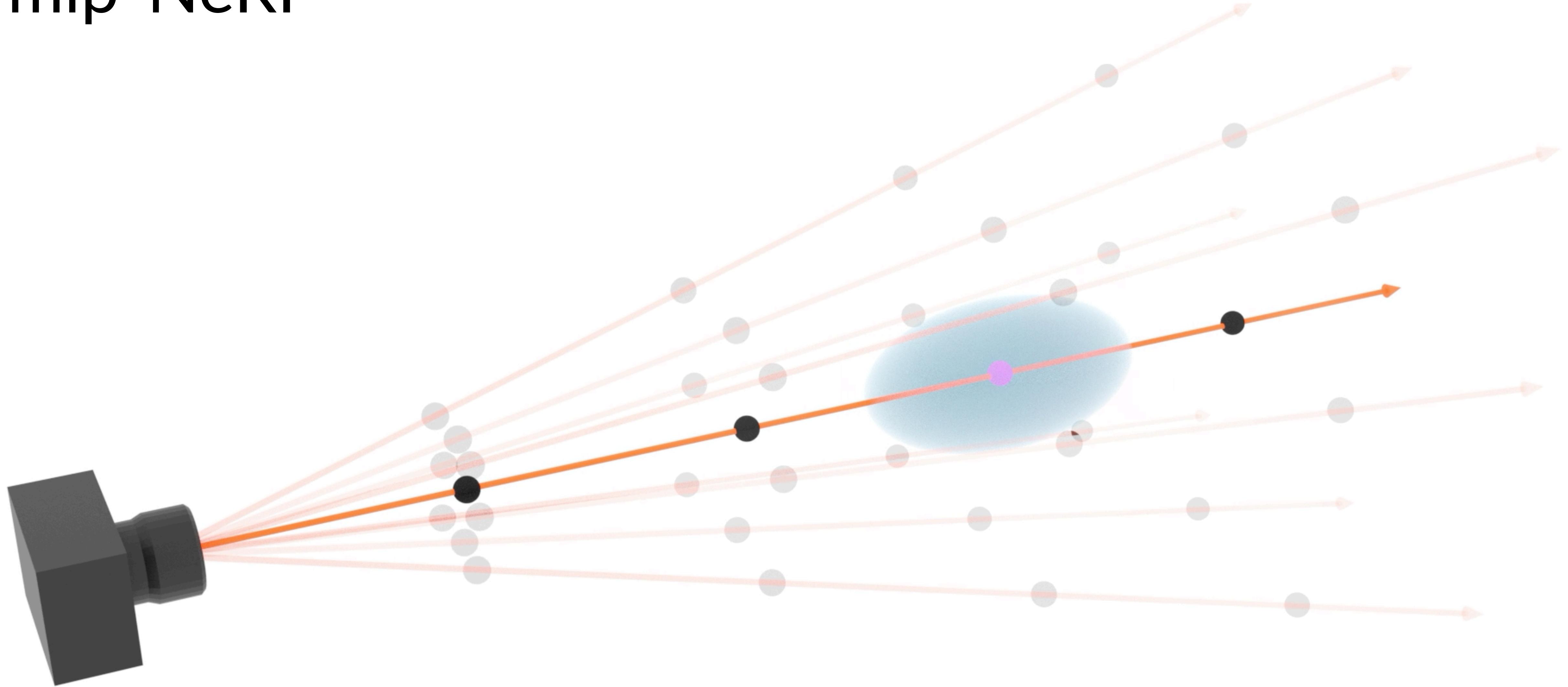
# NeRF



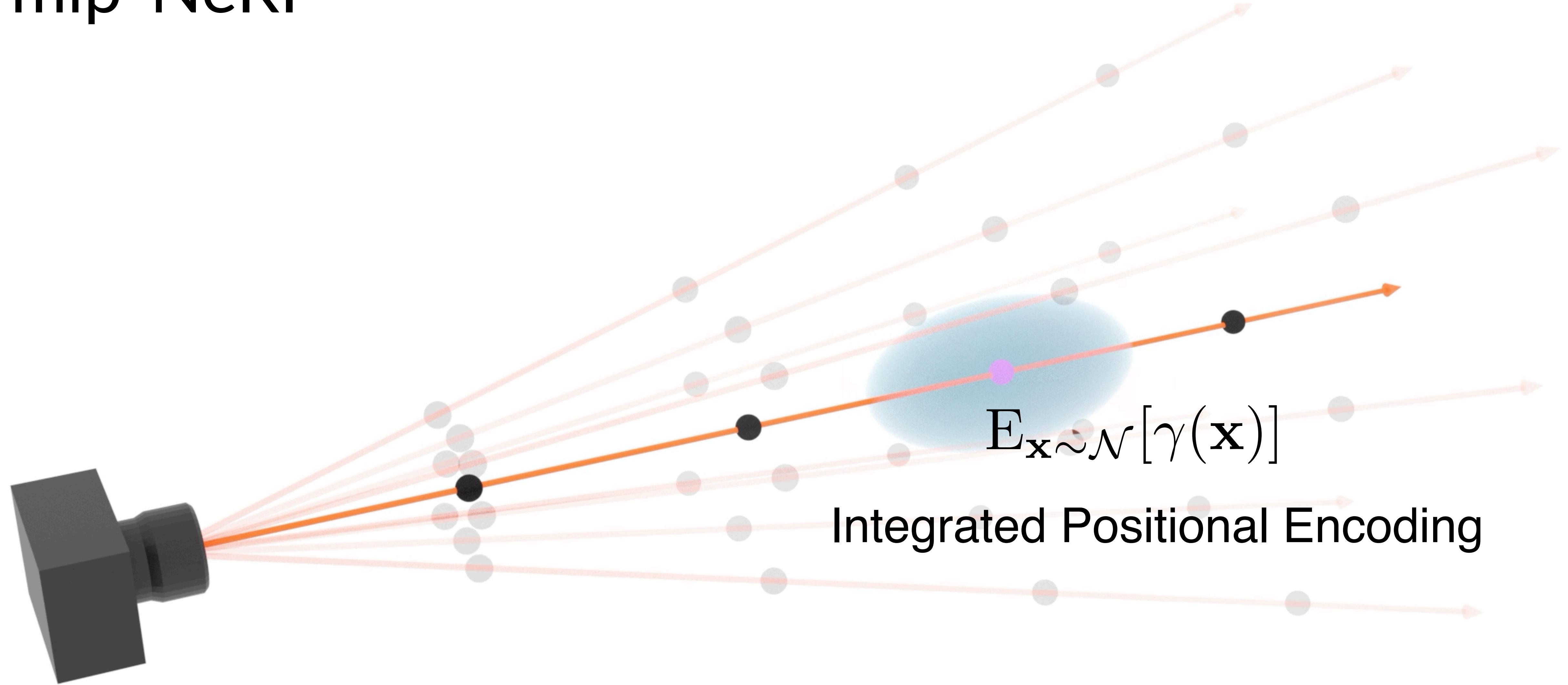
# mip-NeRF

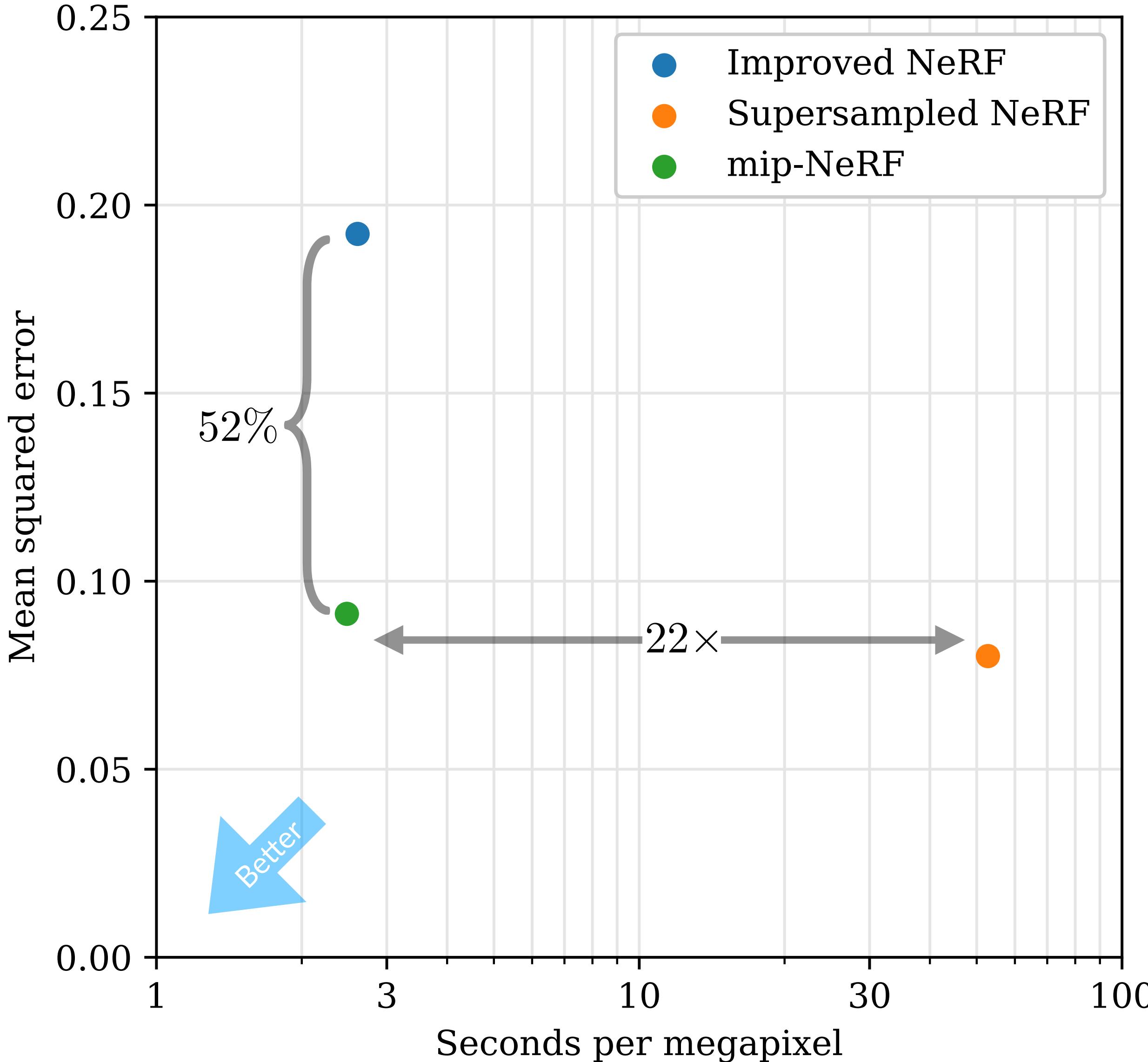


# mip-NeRF



# mip-NeRF





7% faster training  
50% smaller model



Improved NeRF



Mip-NeRF

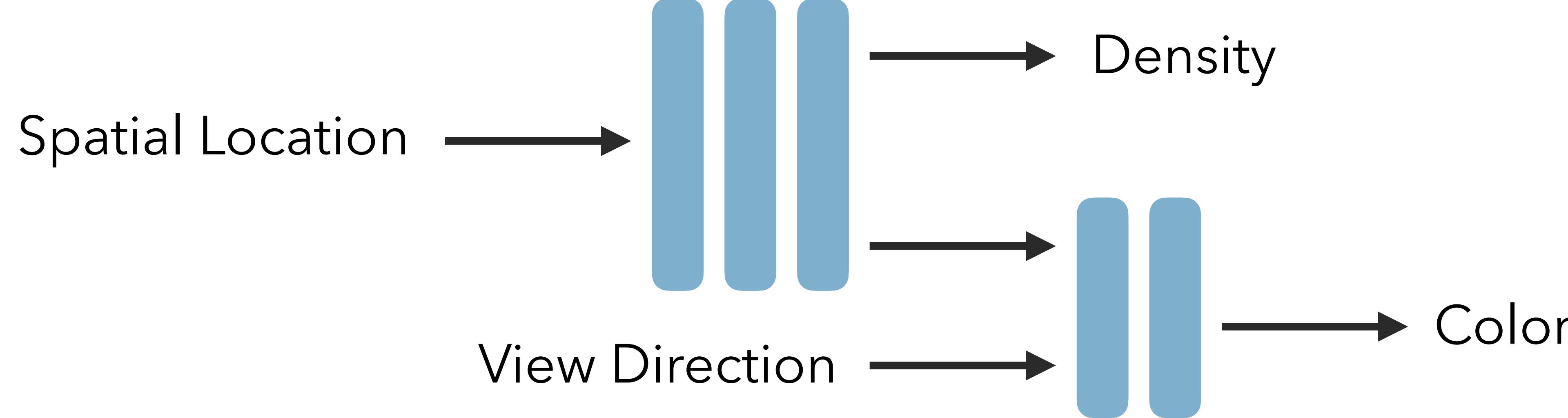
# NeRF in the Wild



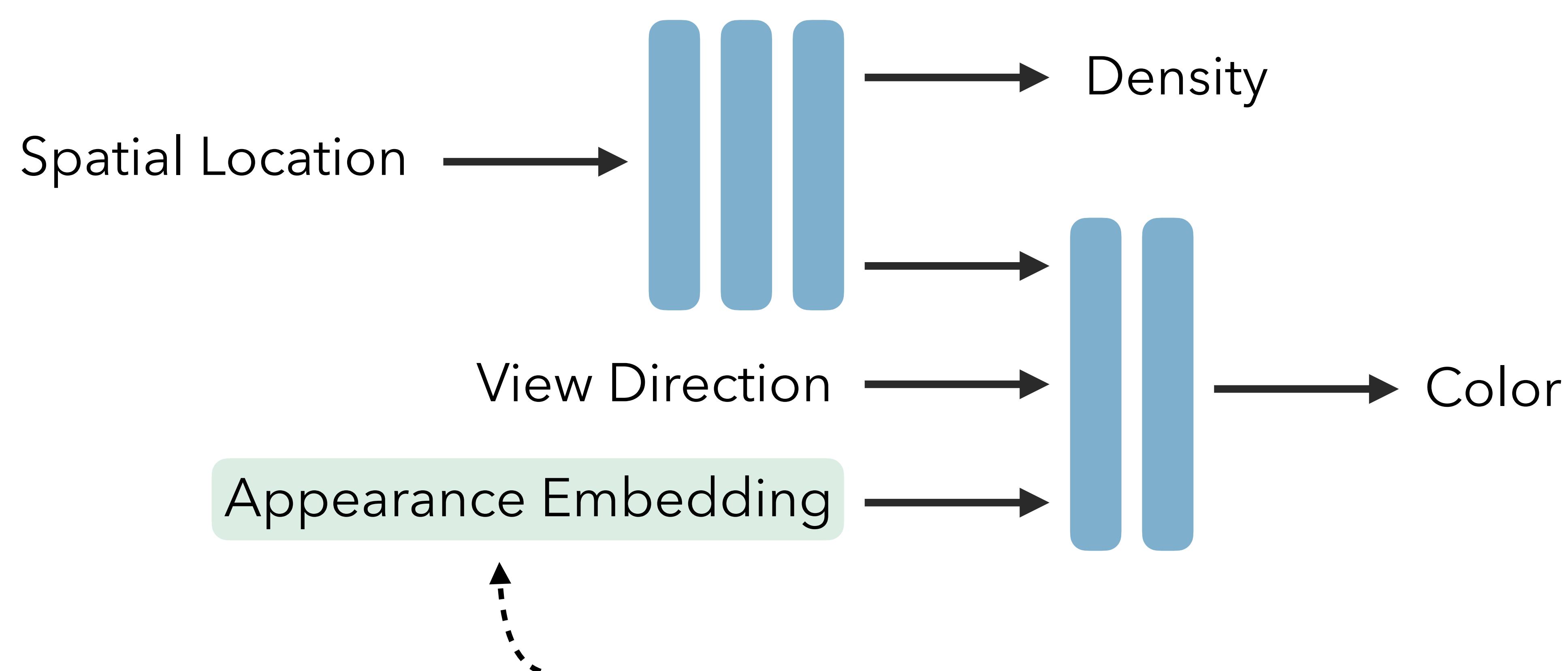
“In the wild” photographs



# Modifications to NeRF



# Modifications to NeRF



Learnable higher dimensional input that is unique for each input value.

A dark, atmospheric photograph of Old Town Square in Prague at night. The scene is dominated by the large, illuminated Powder Tower (Prague Castle) in the background. In the foreground, the silhouettes of people walking on a bridge are visible against the bright lights of the square. The overall mood is mysterious and historic.

# Old Town Square

Prague, Czech Republic

# Block-NeRF: Scalable Large Scene Neural View Synthesis

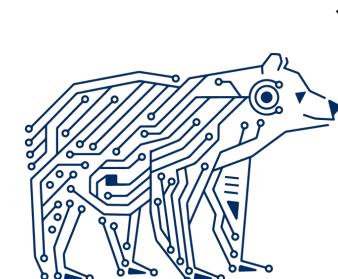


Matthew Tancik<sup>1</sup>  
Ben Mildenhall<sup>3</sup>

Vincent Casser<sup>2</sup>  
Pratul P. Srinivasan<sup>3</sup>

Xinchen Yan<sup>2</sup>  
Jonathan T. Barron<sup>3</sup>

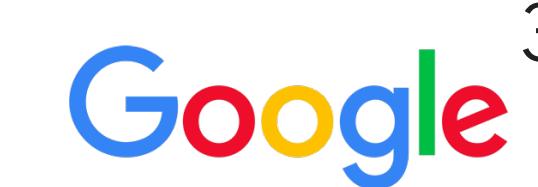
Sabeek Pradhan<sup>2</sup>  
Henrik Kretzschmar<sup>2</sup>



1



2

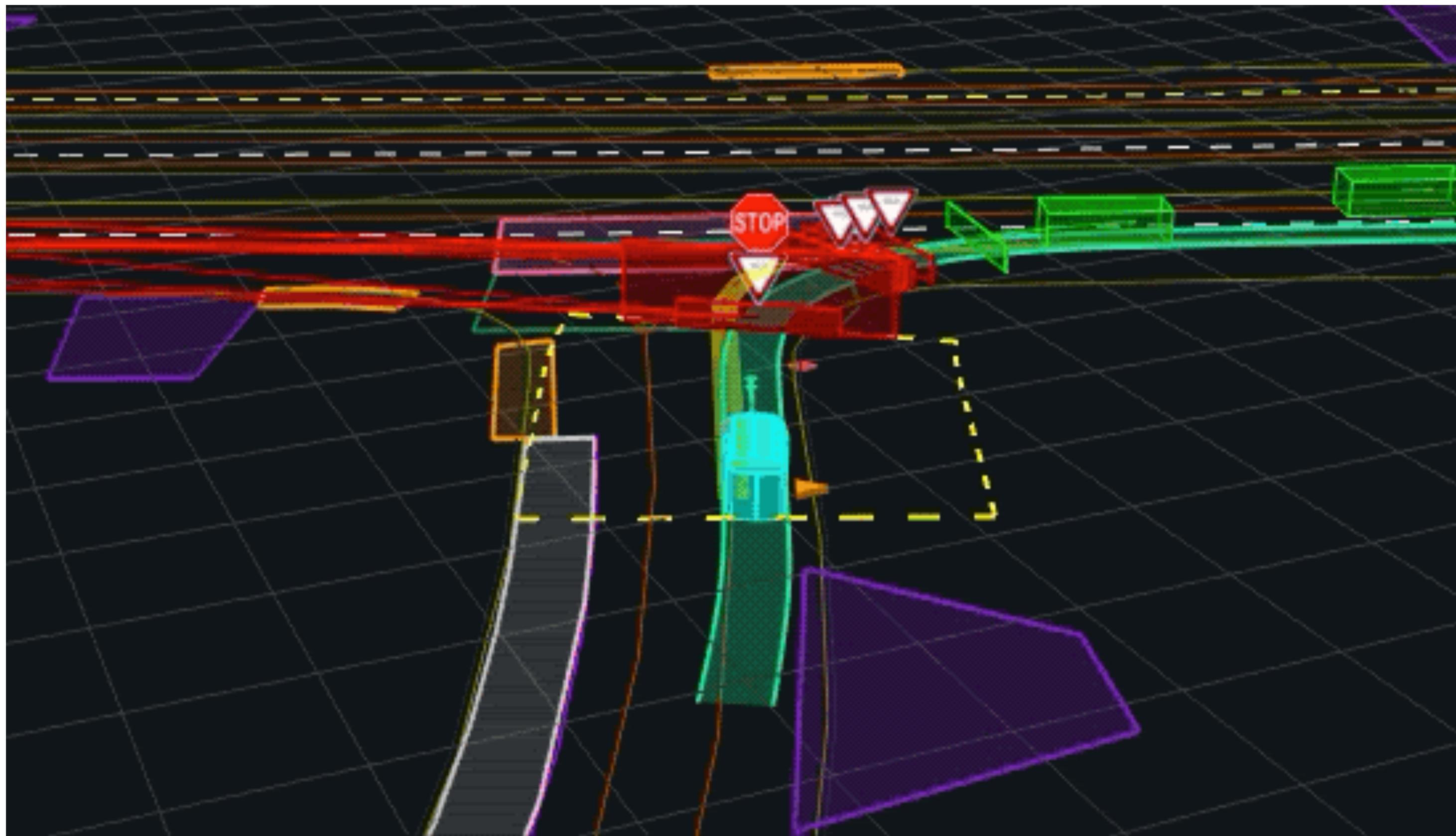


3

# Safety Testing



# Simulation is Essential for Scale



# Lidar Simulation



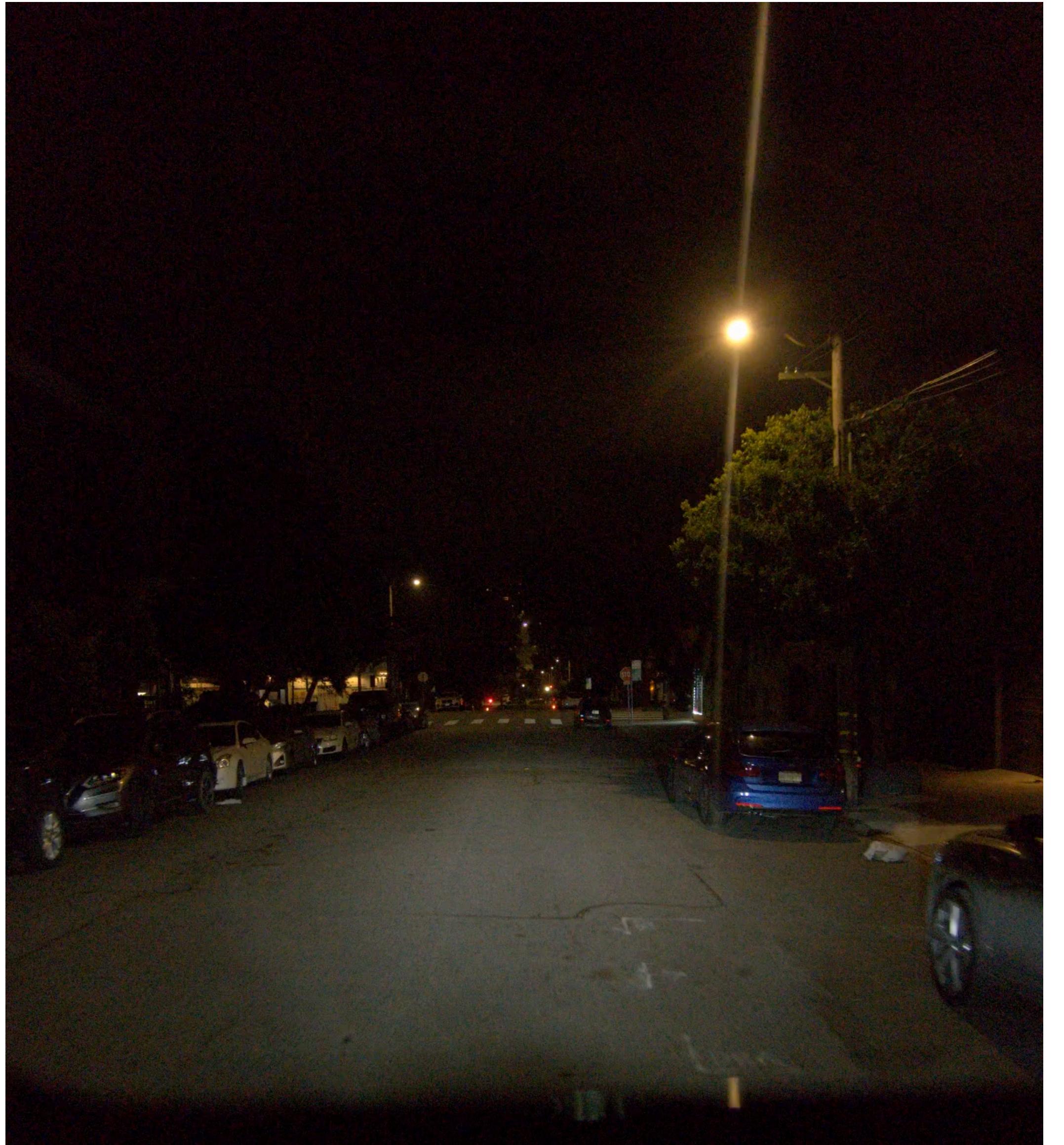
# Camera Simulation using Models



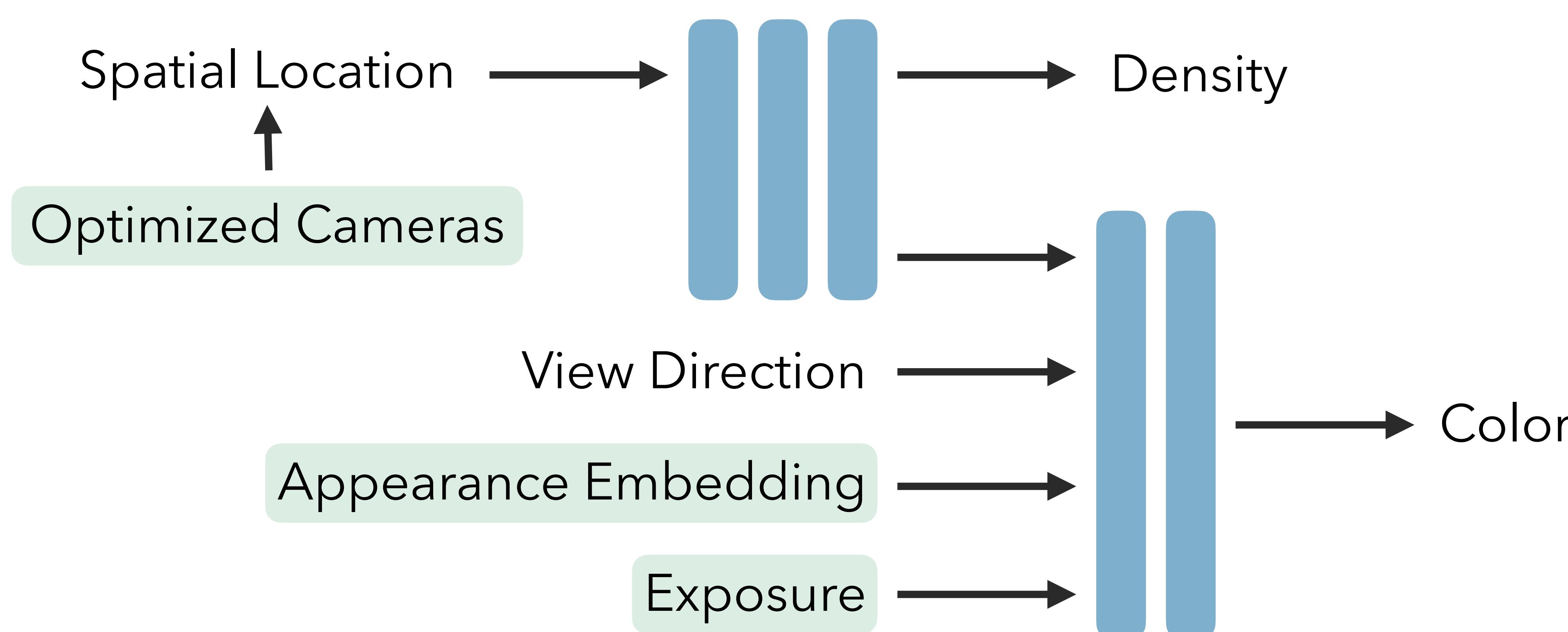
Access to lots of data

- + 360 degree view
- + Camera poses

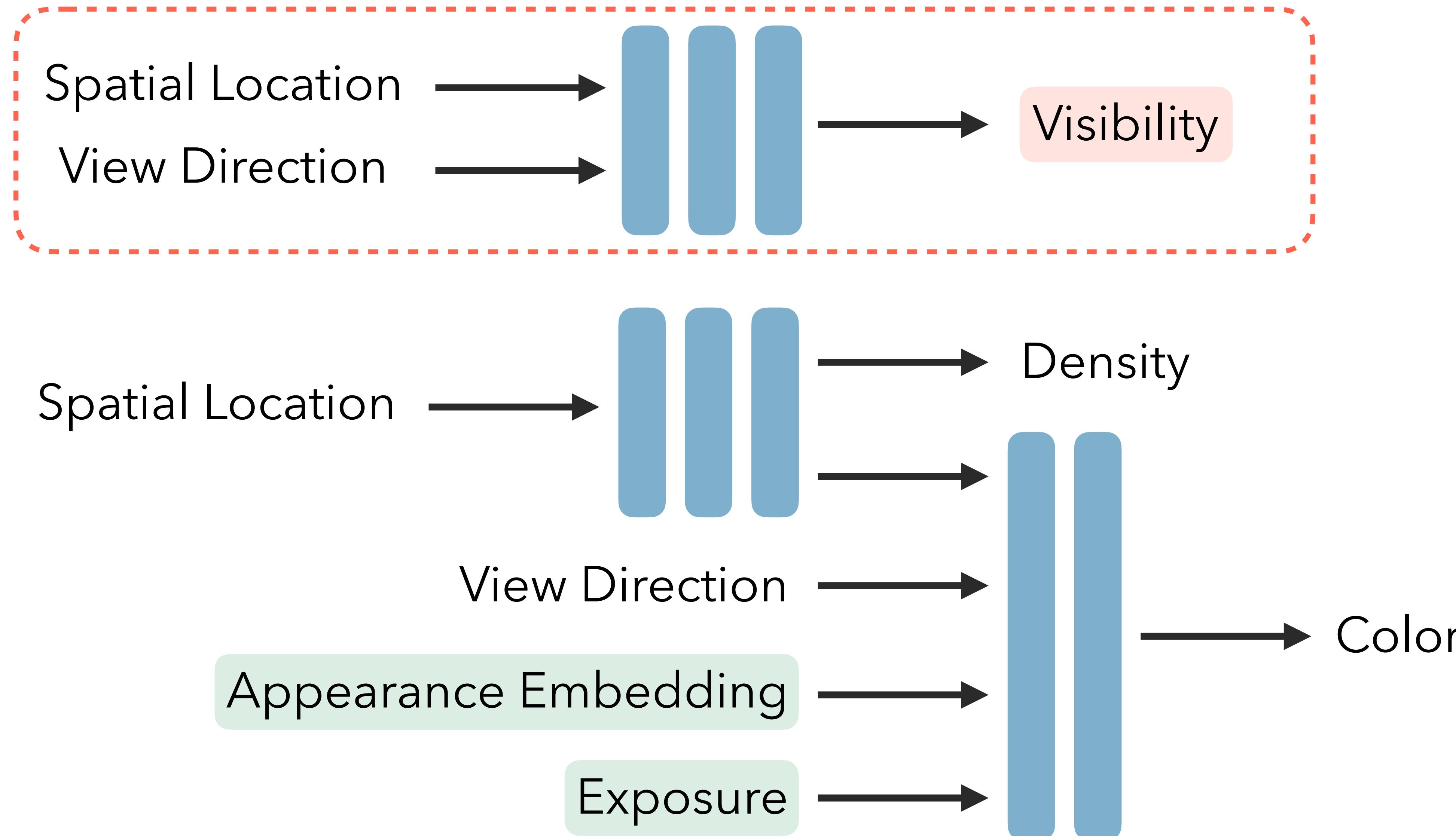
... but highly variable



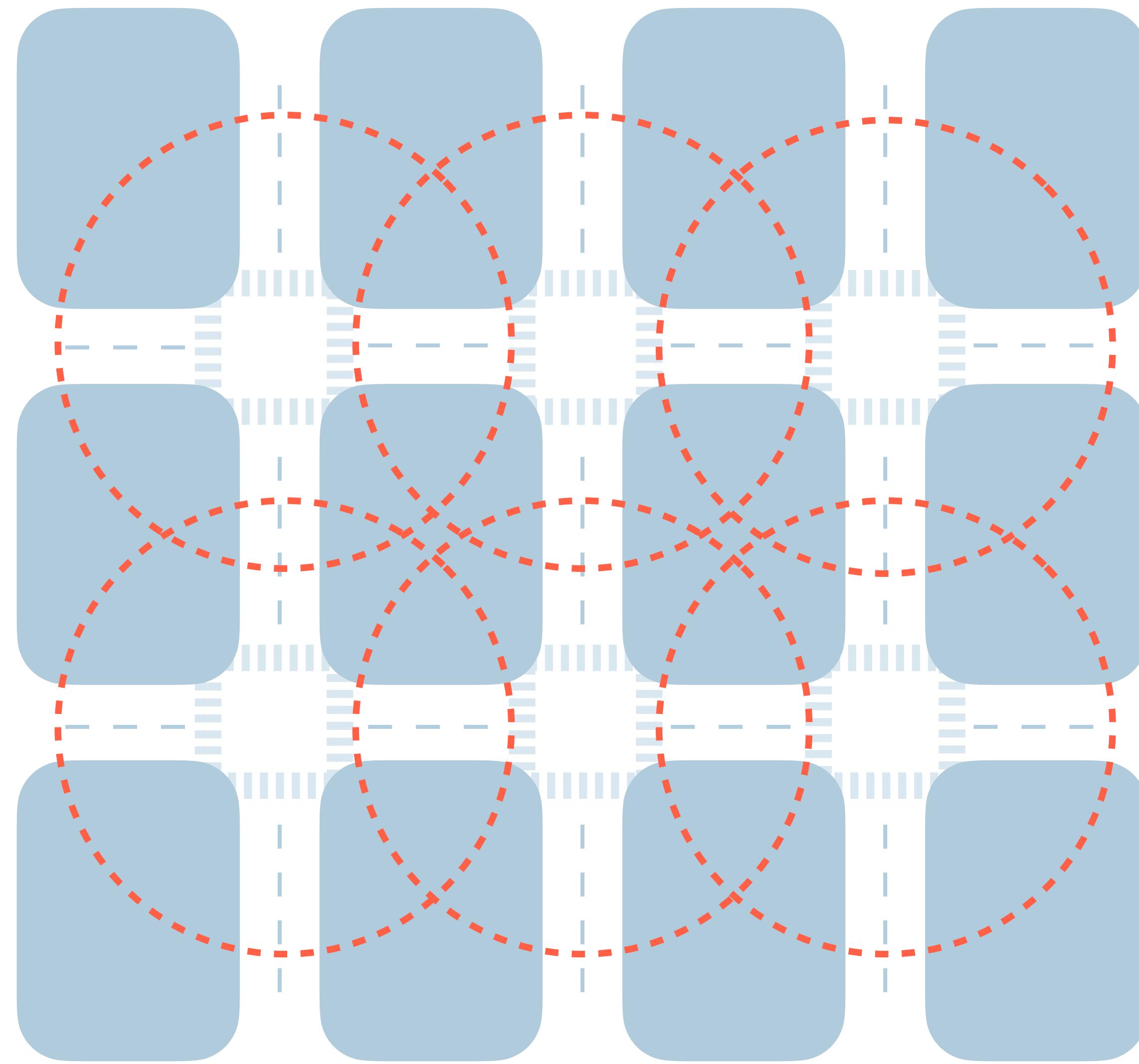
# Modifications to NeRF



# Modifications to NeRF

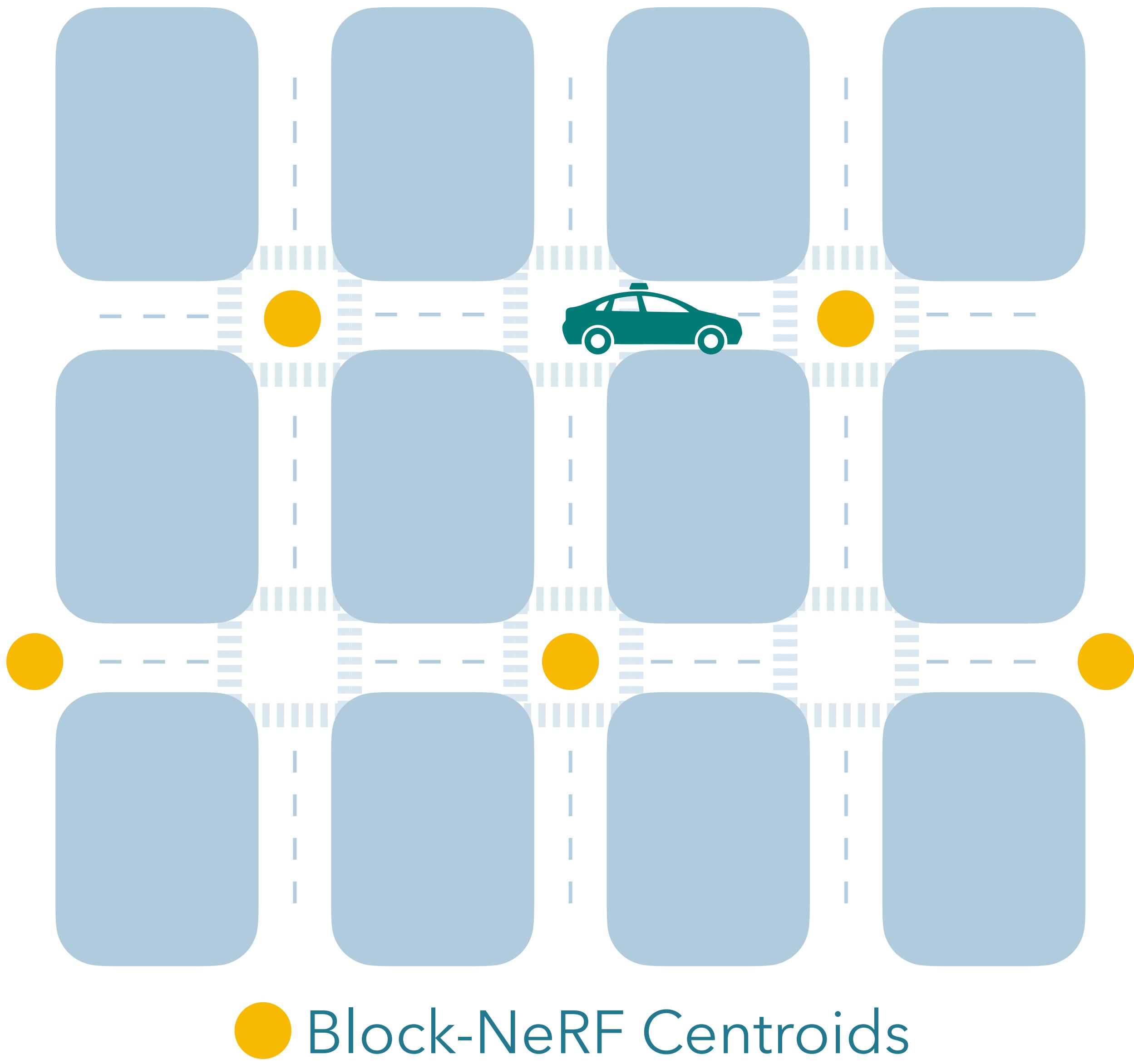


# Scaling to Large Scenes

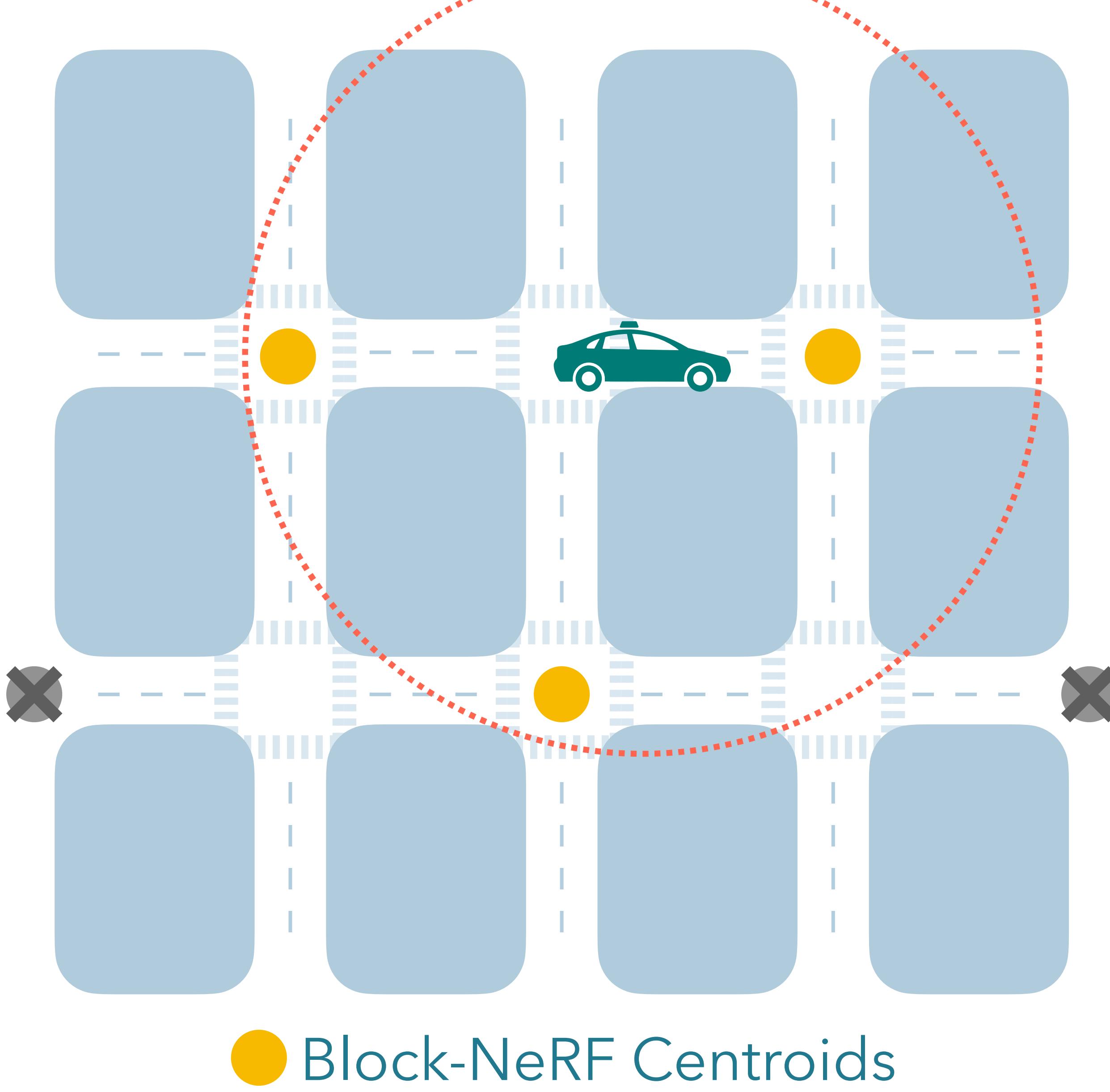


Block-NeRF

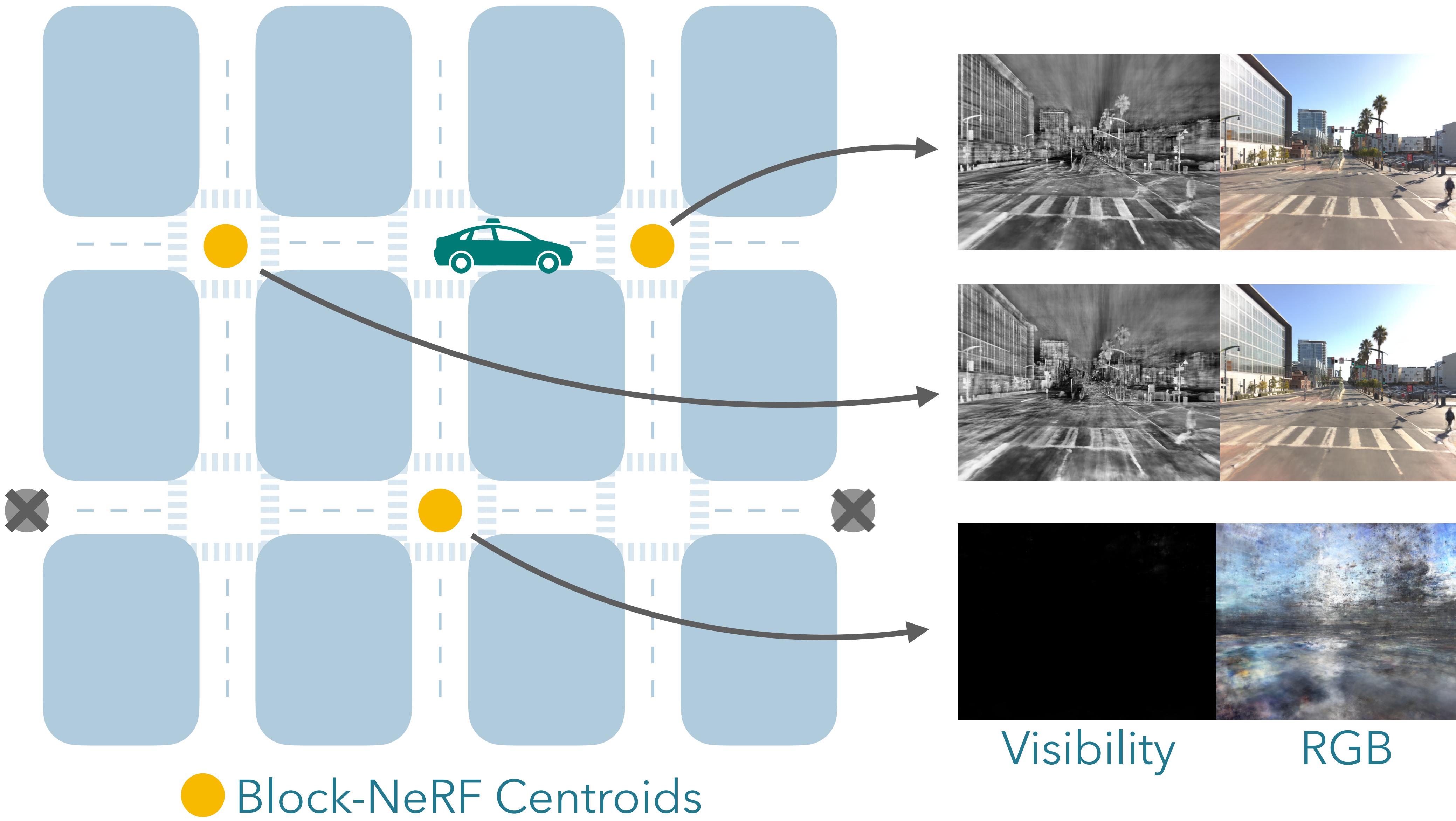
# Merging Block-NeRFs



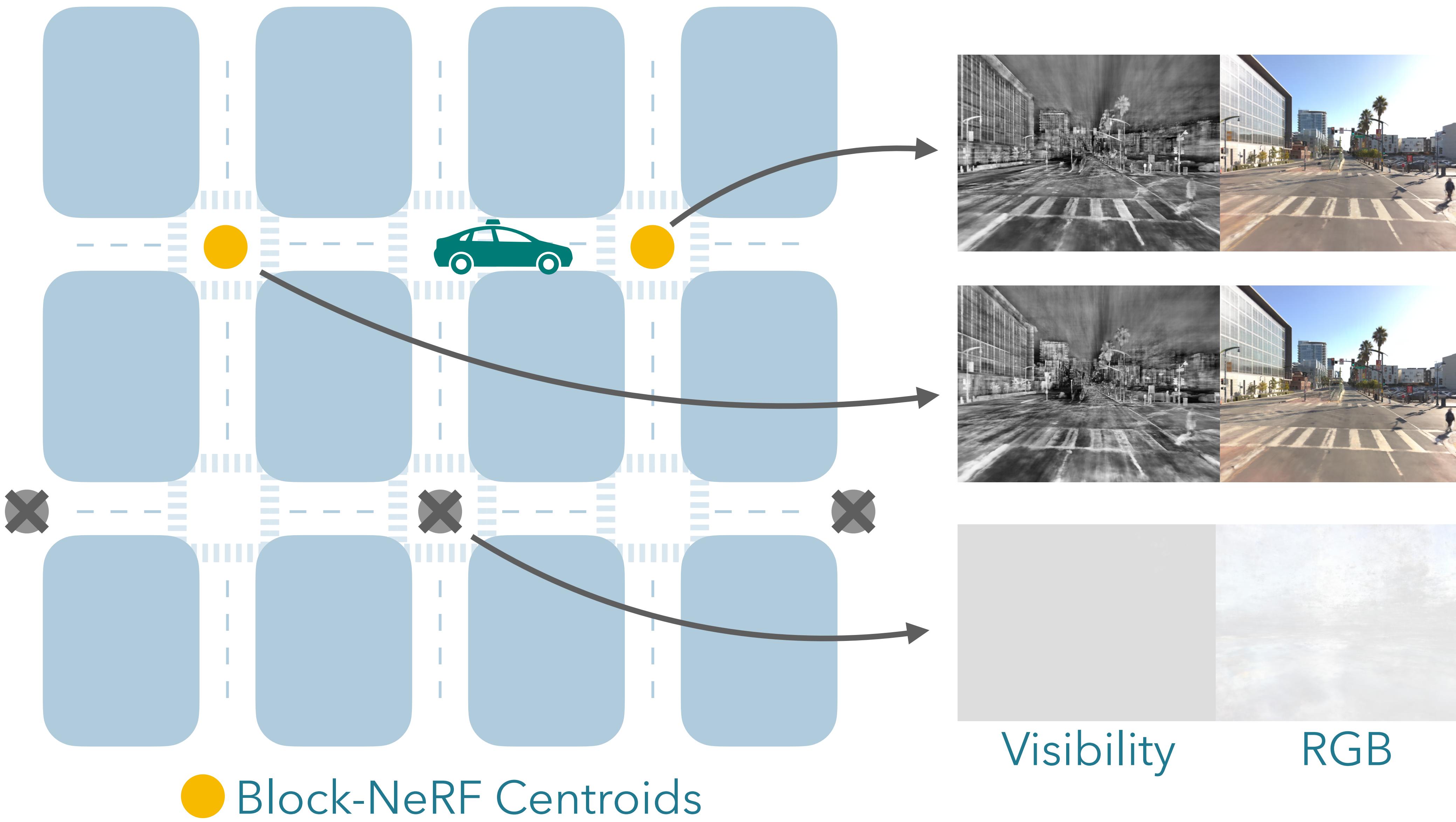
# Merging Block-NeRFs



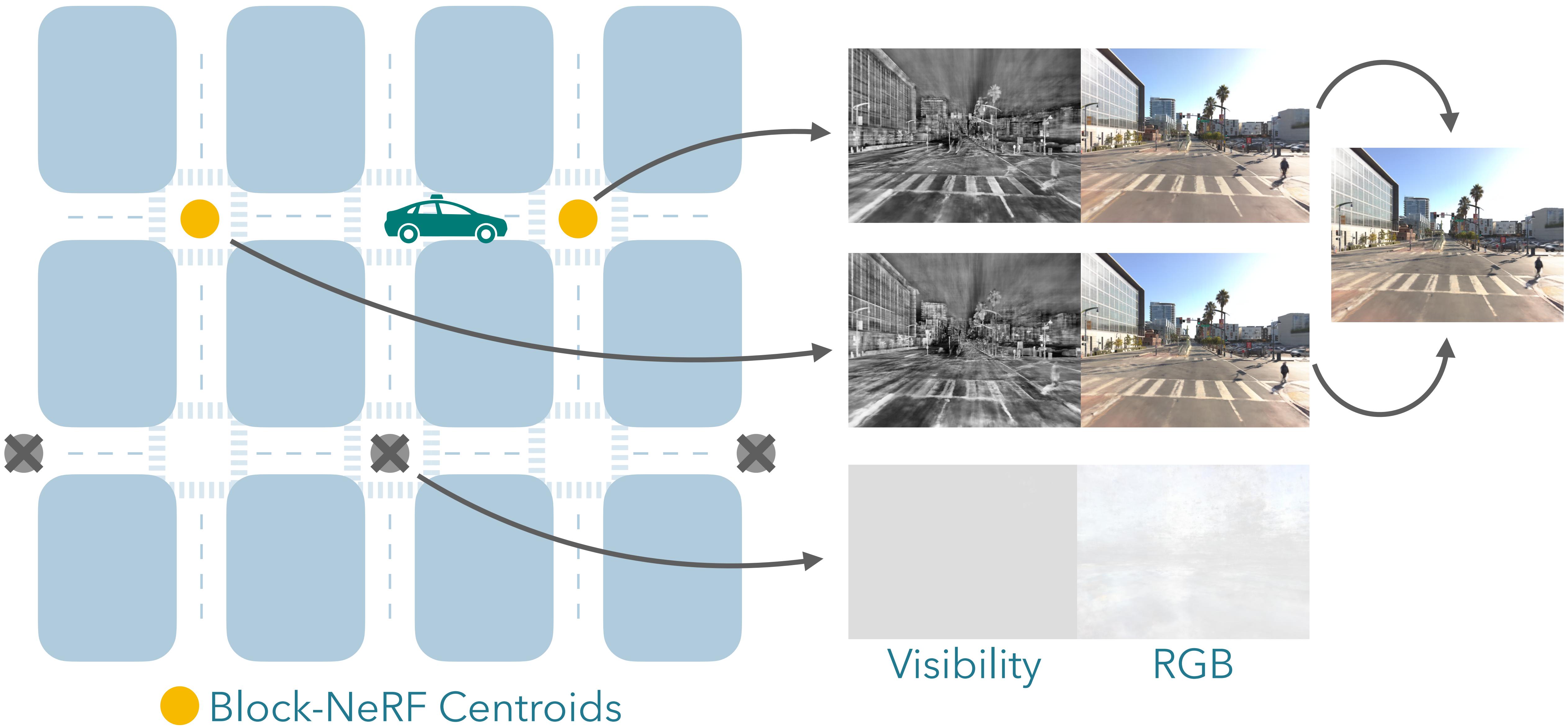
# Merging Block-NeRFs



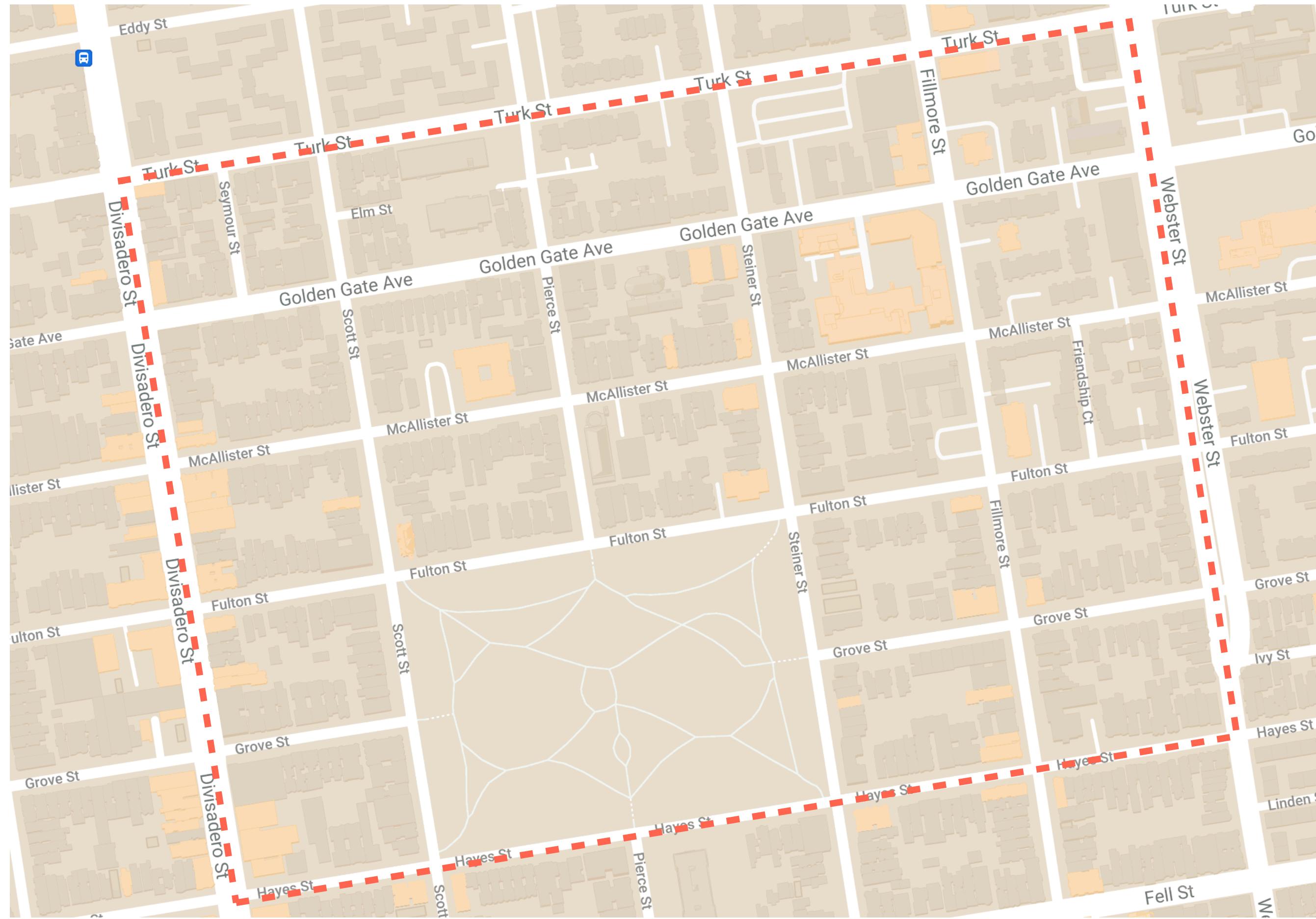
# Merging Block-NeRFs



# Merging Block-NeRFs



# Large Scene Reconstruction

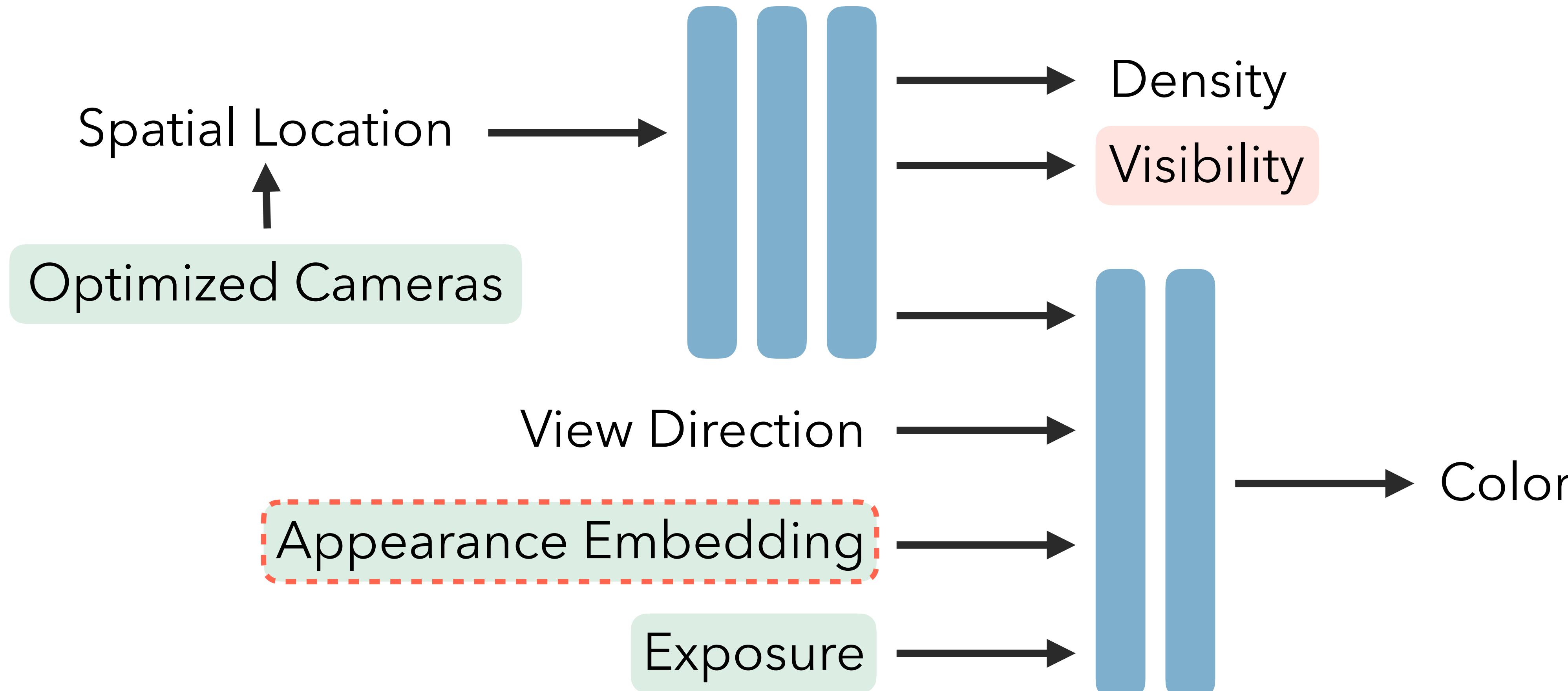


Alamo Square Neighborhood, San Francisco

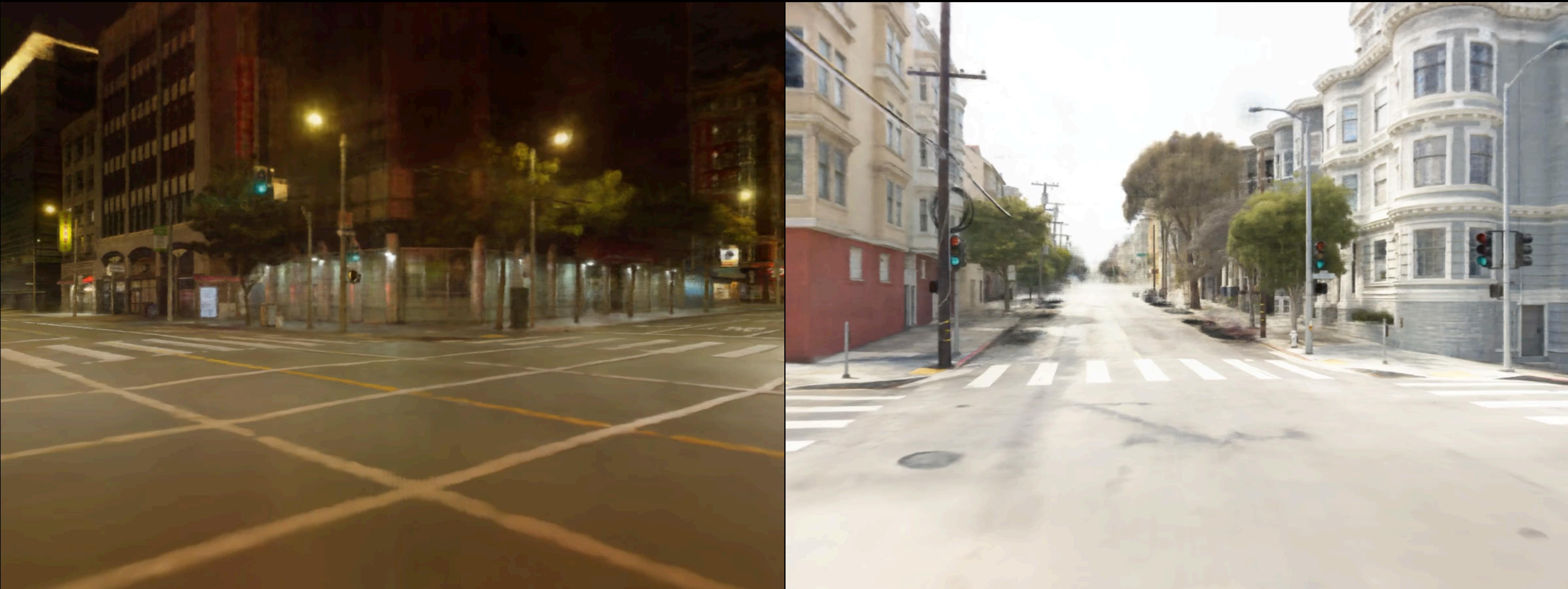
- ▶ 2.8 Million Images
- ▶ Captured over 3 months
- ▶ 1330 Data collection runs
- ▶ 13.4 Hours of driving
- ▶ 35 Block-NeRFs



# Modifications to NeRF



# Appearance Modulation



# Easy to locally update scene



During Construction



After Construction







# Instant NGP (train NeRF in seconds)



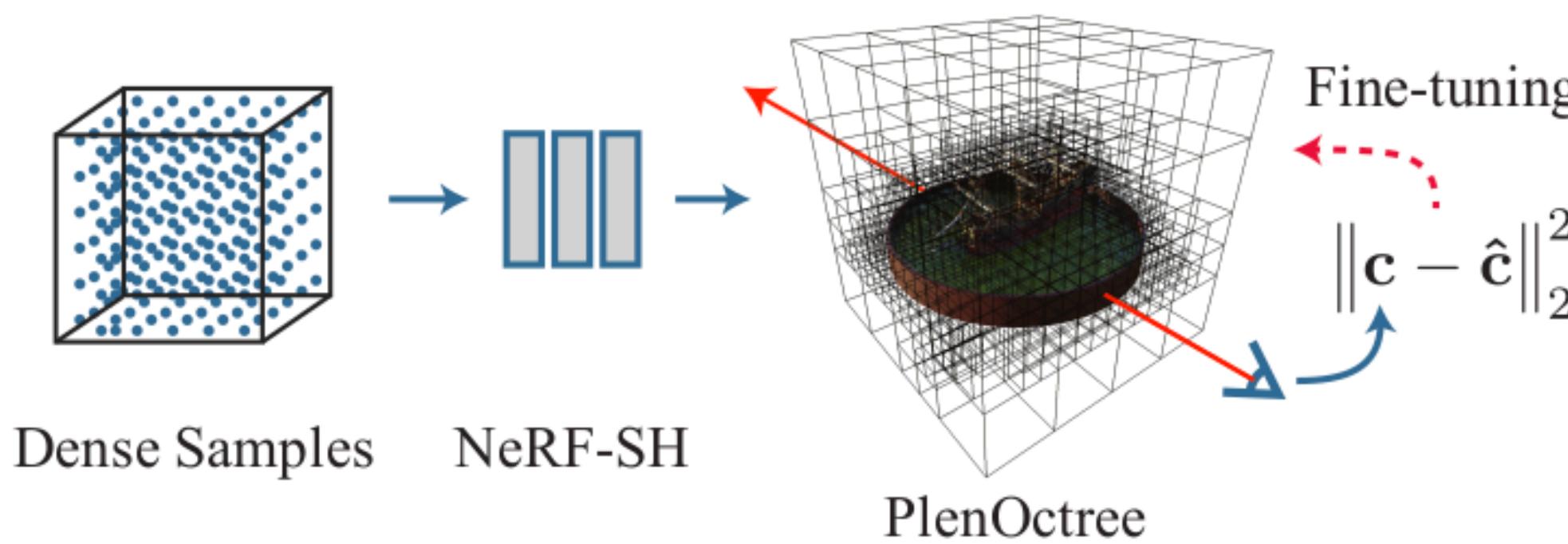
# Instant NGP (train NeRF in seconds)



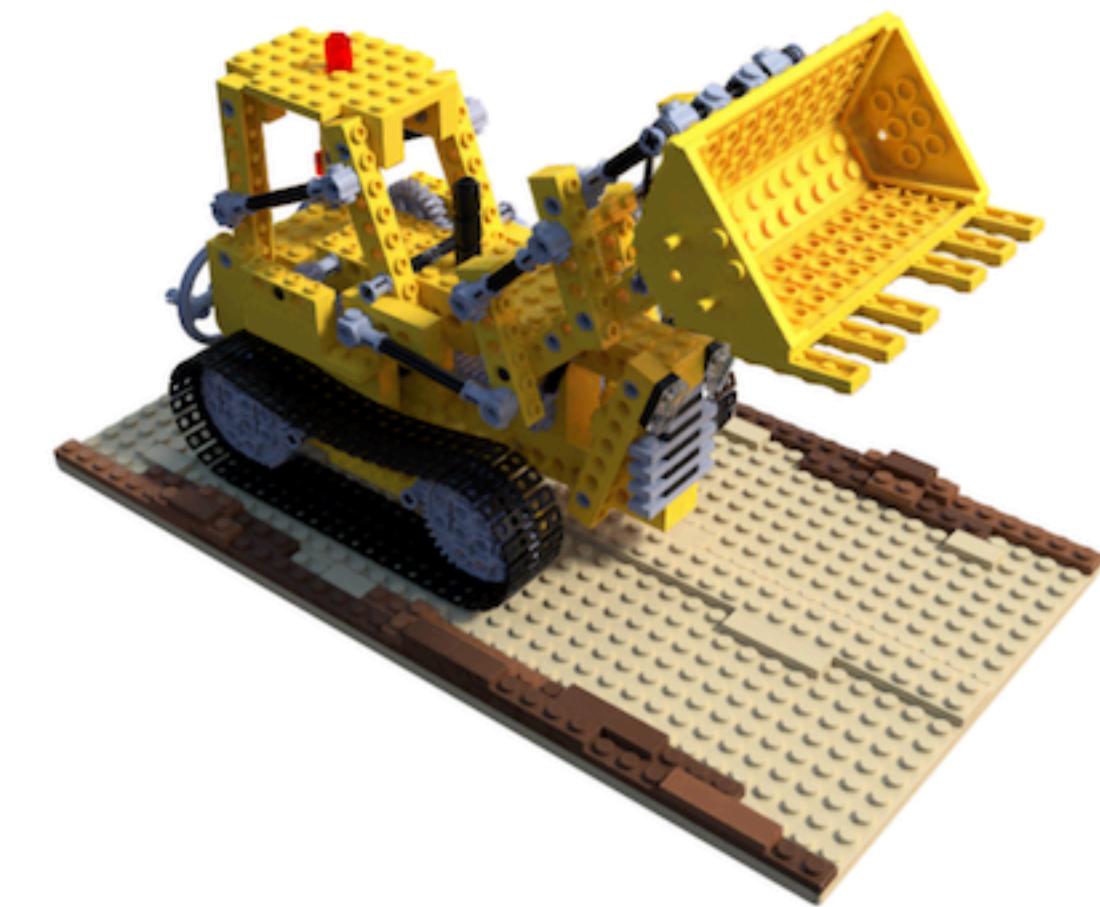
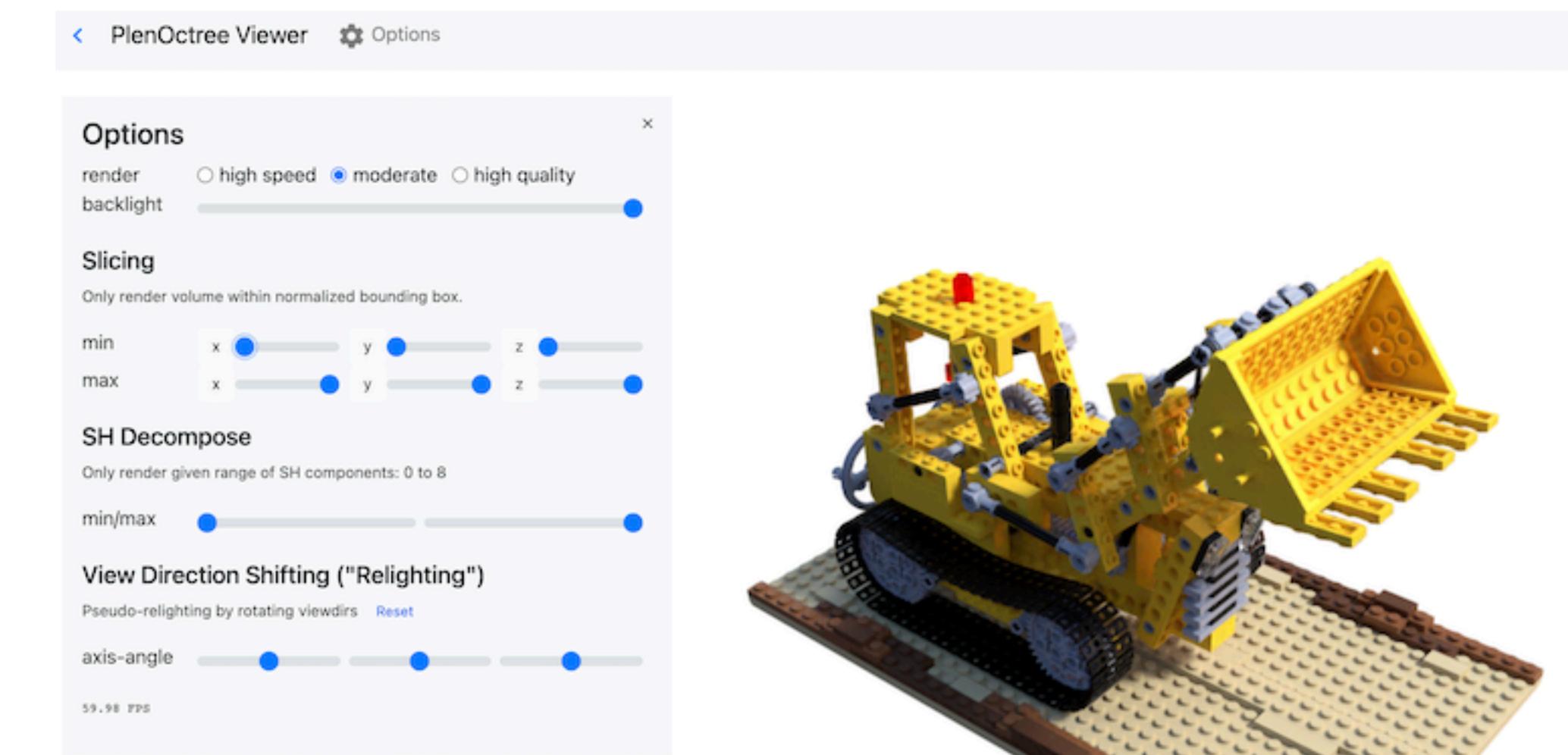
@smallfly

# PlenOctrees

Render a NeRF in your browser - [alexyu.net/plenoctrees/](http://alexyu.net/plenoctrees/)



Conversion to a PlenOctree



Real-time Rendering

# NeRFies



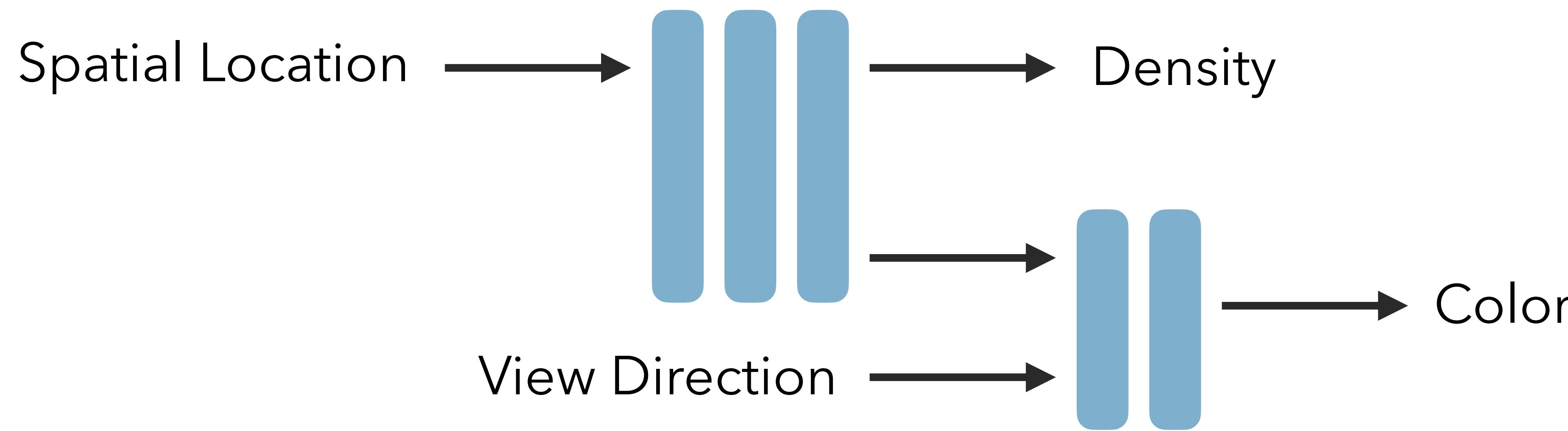
(a) Capture Process

(b) Input

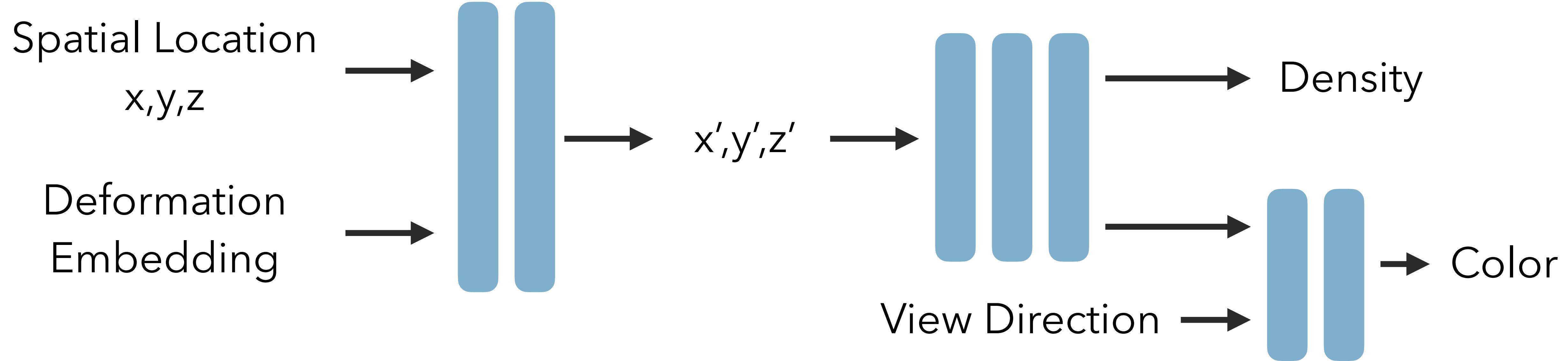
(c) Nerfie

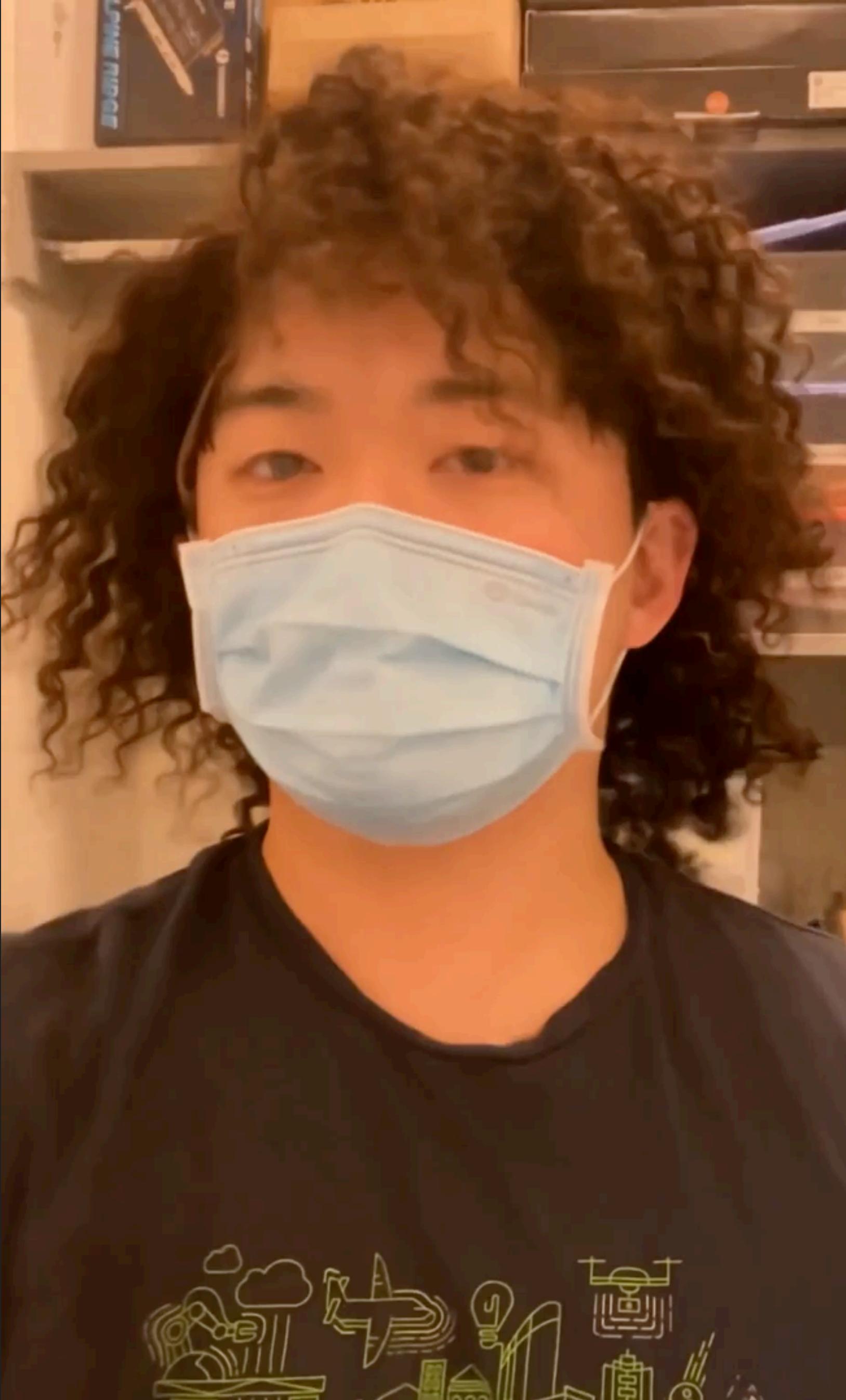
(d) Nerfie Depth

# Modifications to NeRF



# Modifications to NeRF





*Deformable Neural Radiance Fields*, Park et al. arXiv 2020

# Video NeRF

Input video



Fixed Time, View Interpolation



Fixed View, Time Interpolation



# Video NeRF



Input



# 3D GANs



*Efficient Geometry-aware 3D Generative Adversarial Networks, Chan et al. arXiv 2021*

# Dream Fields



An armchair in the shape of a \_\_\_\_.

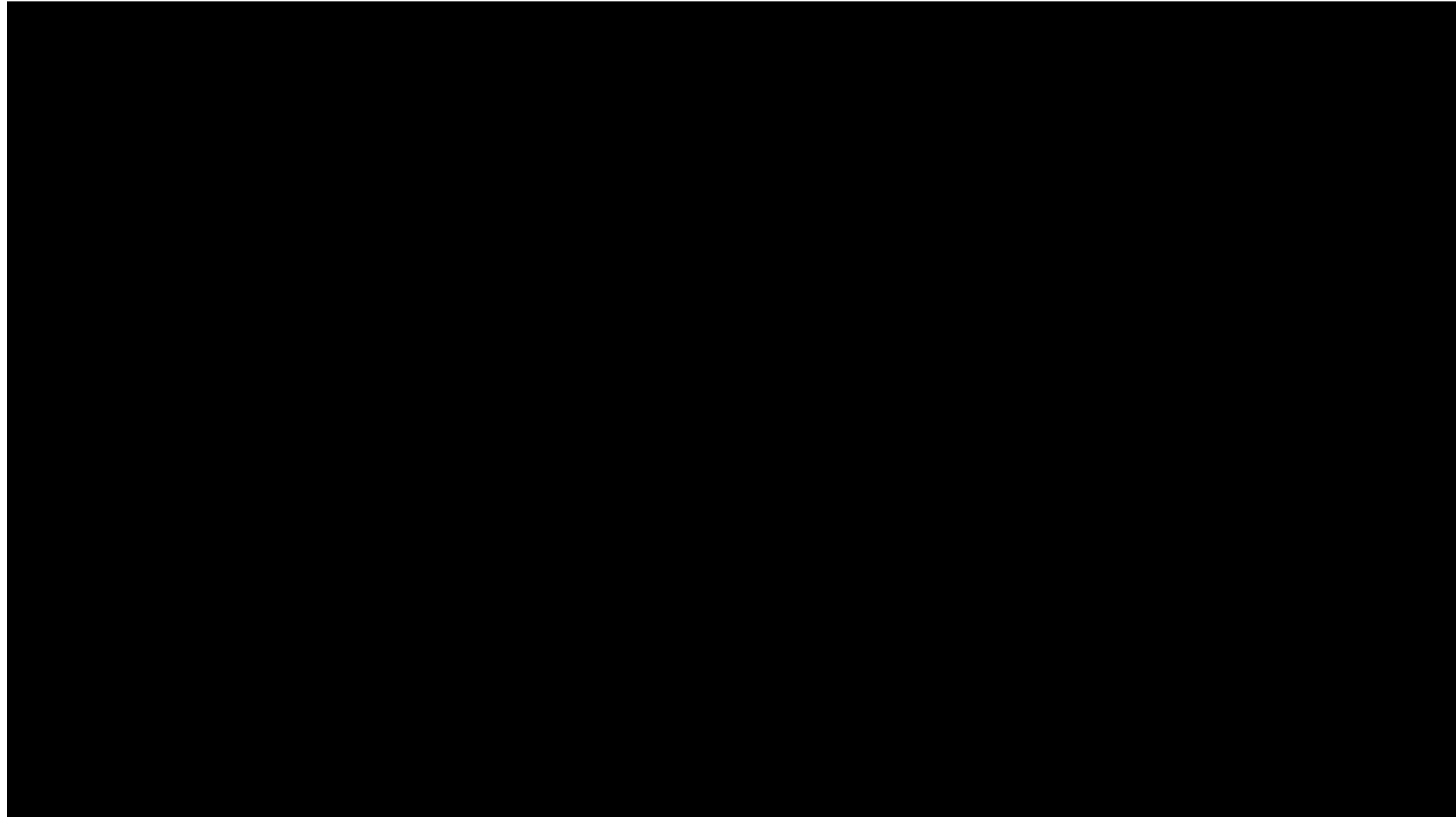
An armchair imitating a \_\_\_\_.

# HumanNeRF

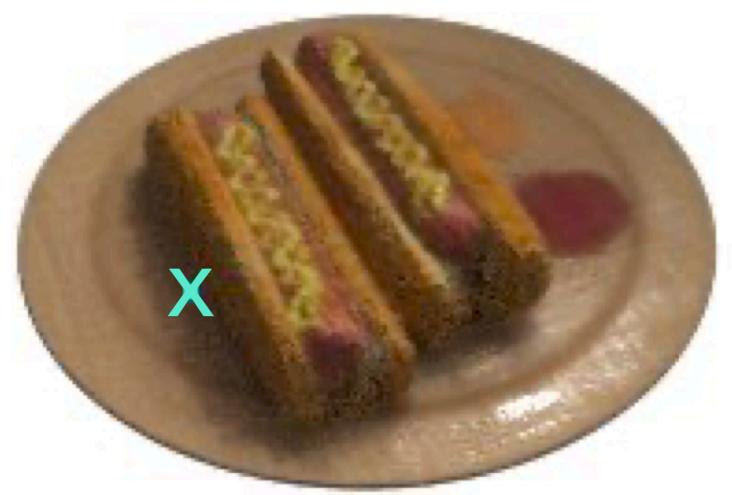


*HumanNeRF: Free-viewpoint Rendering of Moving People from Monocular Video, Weng et al. arXiv 2022*

# NeRF in the Dark

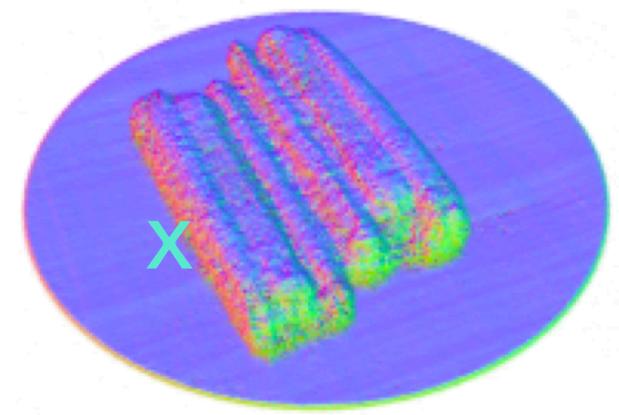


# Decompose Lighting and Materials

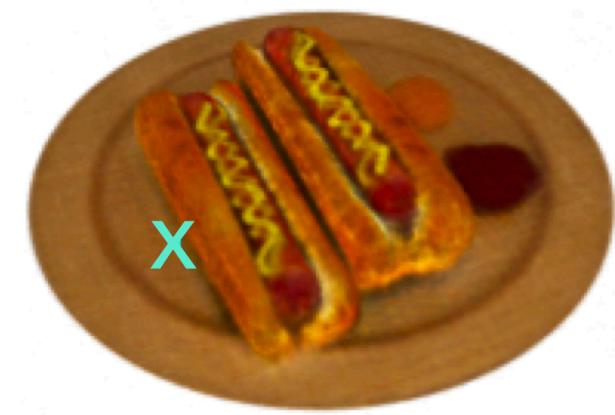


(a) Our Rendered Image  
(Novel View and Lighting)

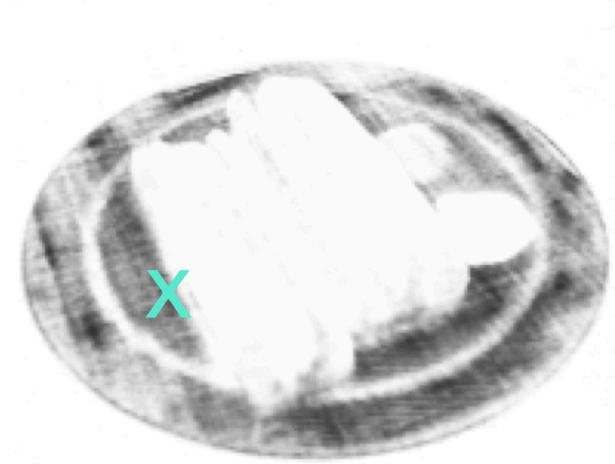
$$= \int_S \left( (\text{b) Light Visibility} \times \text{c) Direct Illumination} + \text{d) Indirect Illumination} \right) \times \text{e) BRDF} d\omega_i$$
The equation illustrates the decomposition of the rendered image into its components. It shows the rendered image (a) as a sum of direct and indirect illumination terms. Each term is multiplied by the BRDF (e) and weighted by light visibility (b). The direct illumination term (c) includes a color swatch, while the indirect illumination term (d) is grayscale.



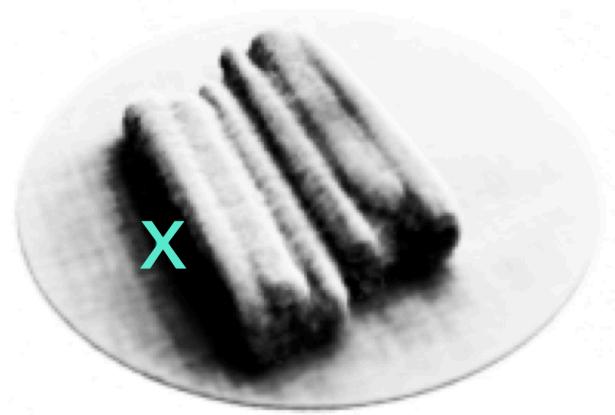
(f) Normals



(g) Albedo



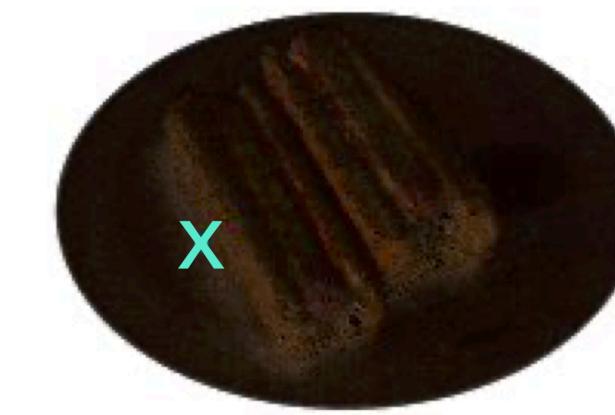
(h) Roughness



(i) Shadow Map



(j) Direct



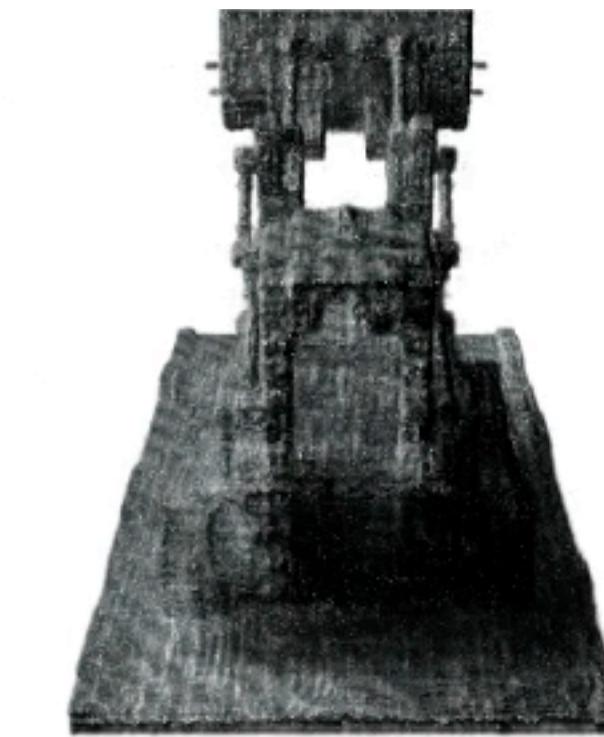
(k) Indirect

# Decompose Lighting and Materials

Edit Lighting



Edit Lighting and Materials



# iMap (NeRF SLAM)



*iMAP: Implicit Mapping and Positioning in Real-Time*, Sucar et al. arXiv 2021

# ObjectNeRF

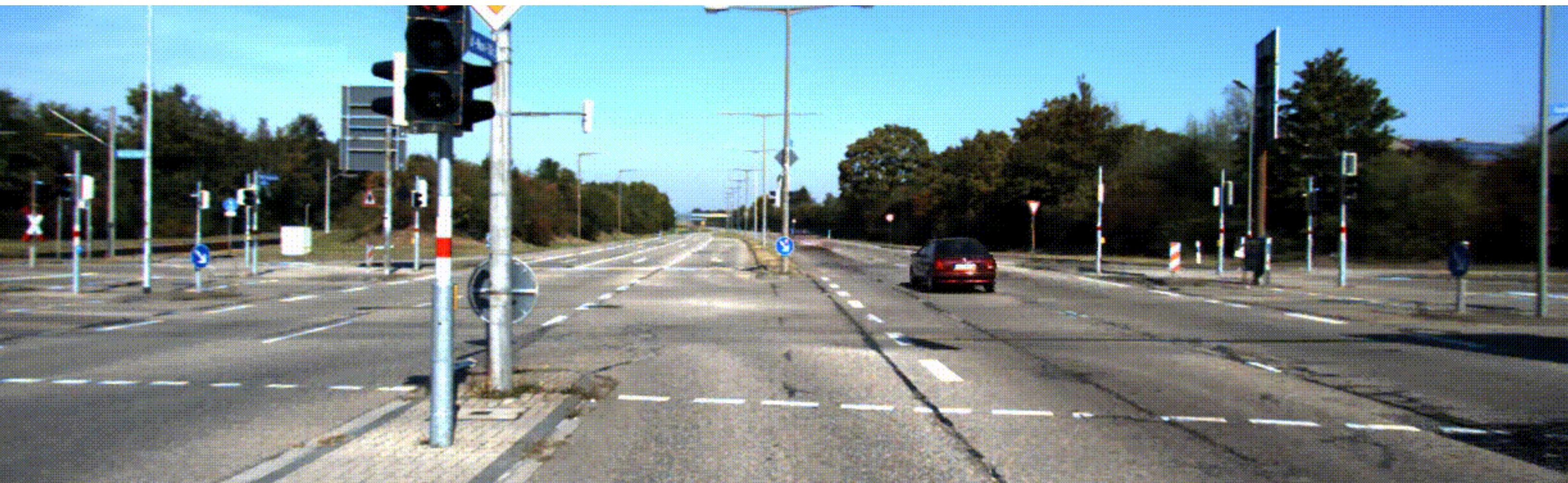
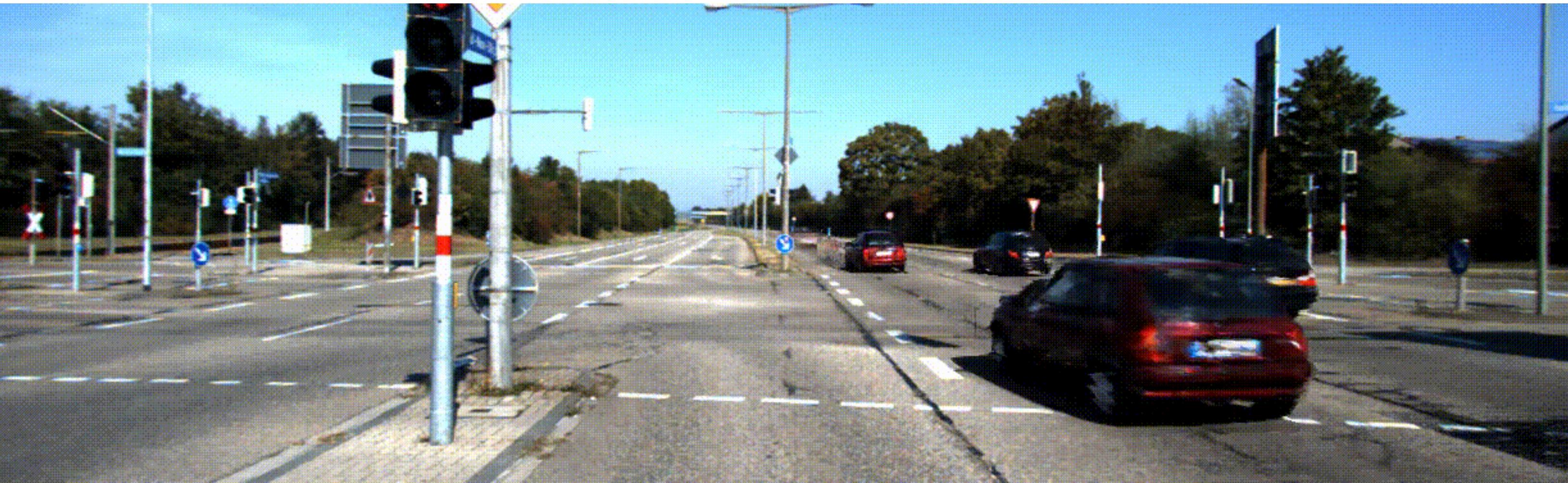


Novel View Synthesis



Editable Scene Rendering

# Neural Scene Graphs for Dynamic Scenes



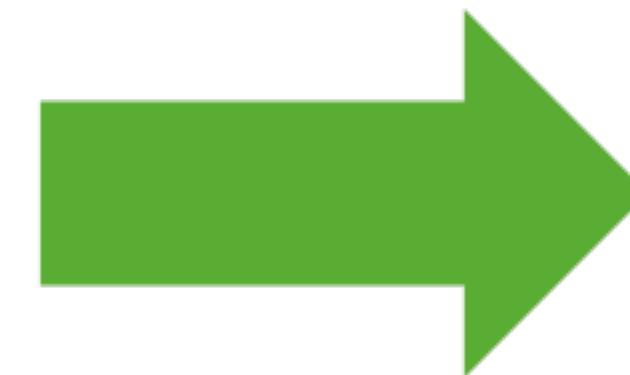
# Neural Scene Graphs for Dynamic Scenes



# GANcraft

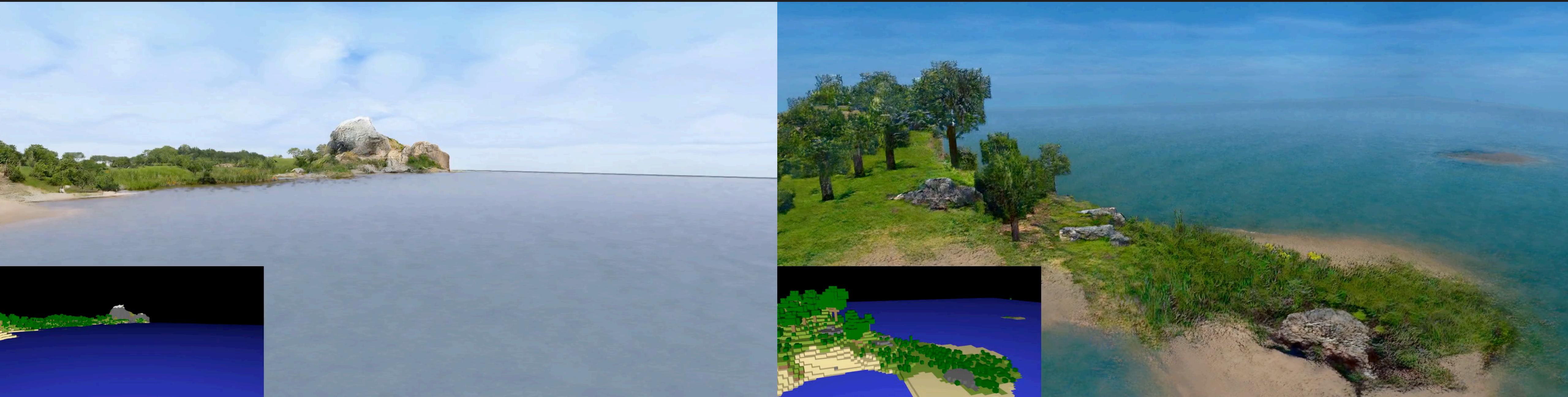


Minecraft



GANcraft

# GANcraft





*GANcraft: Unsupervised 3D Neural Rendering of Minecraft Worlds*, Hao et al. arXiv 2021