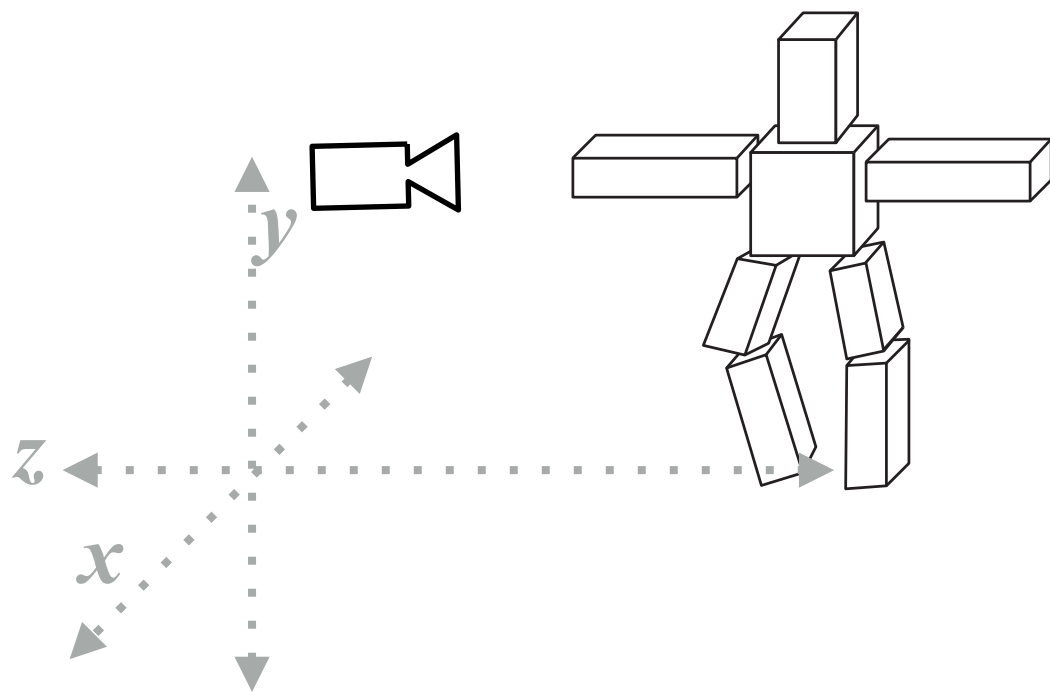


# Lecture 6: The Rasterization Pipeline

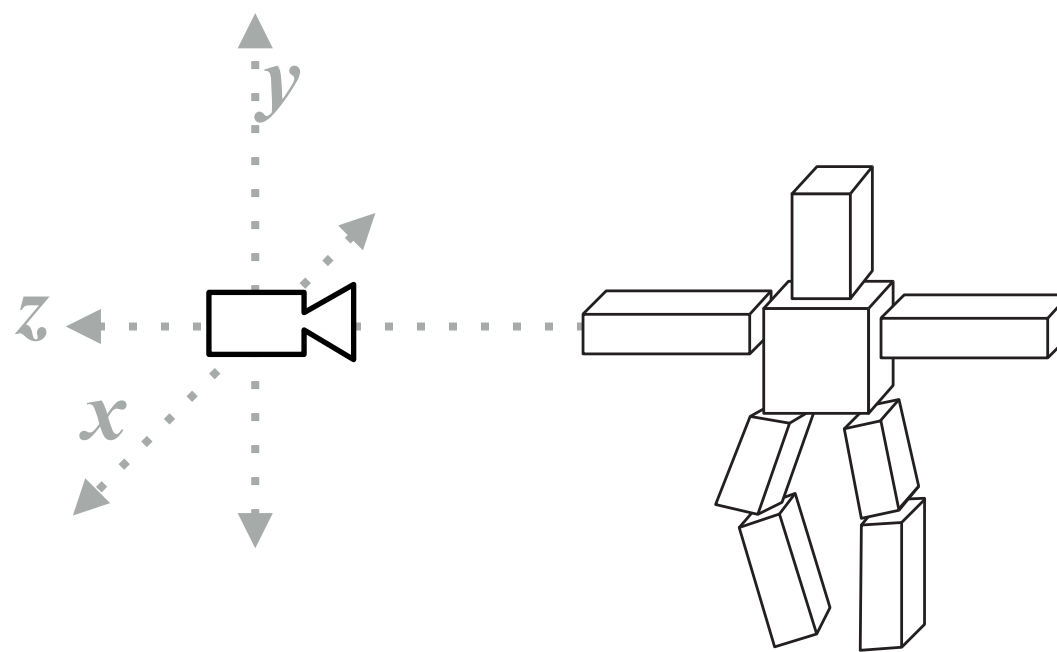


Computer Graphics and Imaging  
UC Berkeley CS184

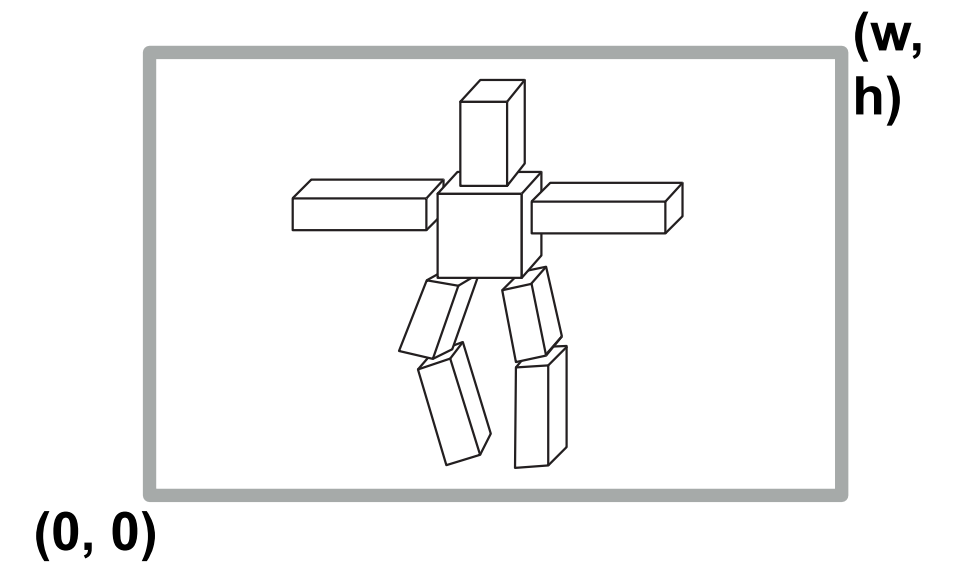
# What We've Covered So Far



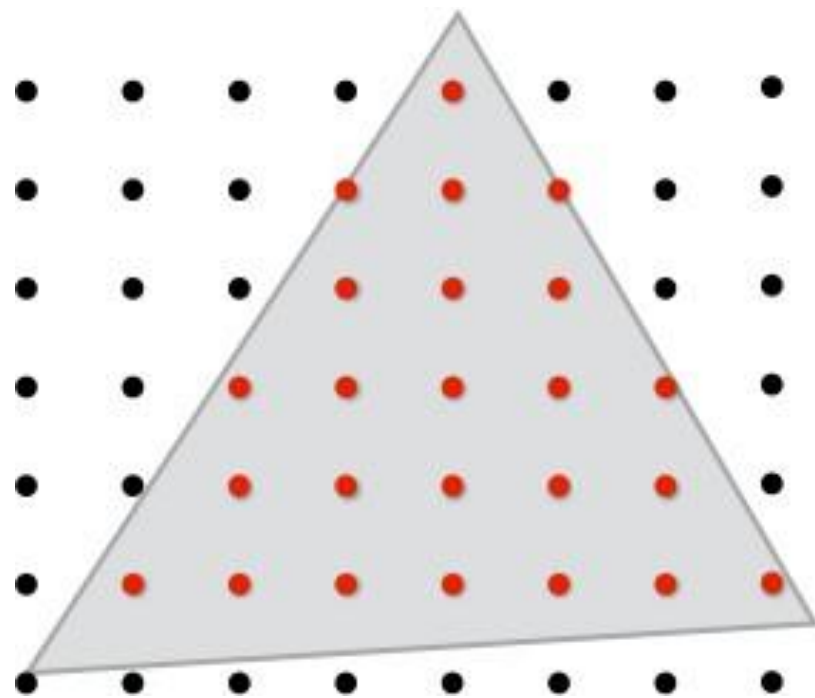
**Position objects and the camera in the world**



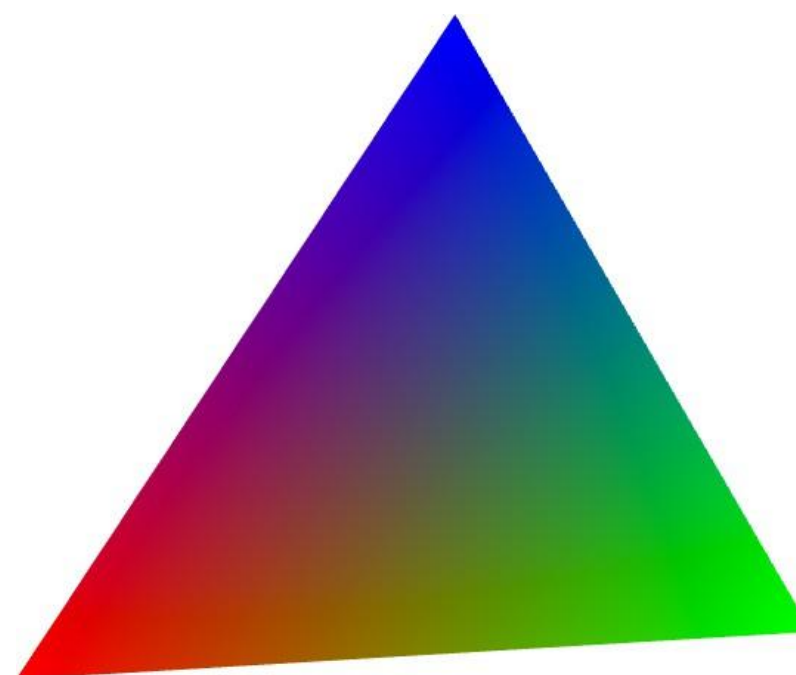
**Compute position of objects relative to the camera**



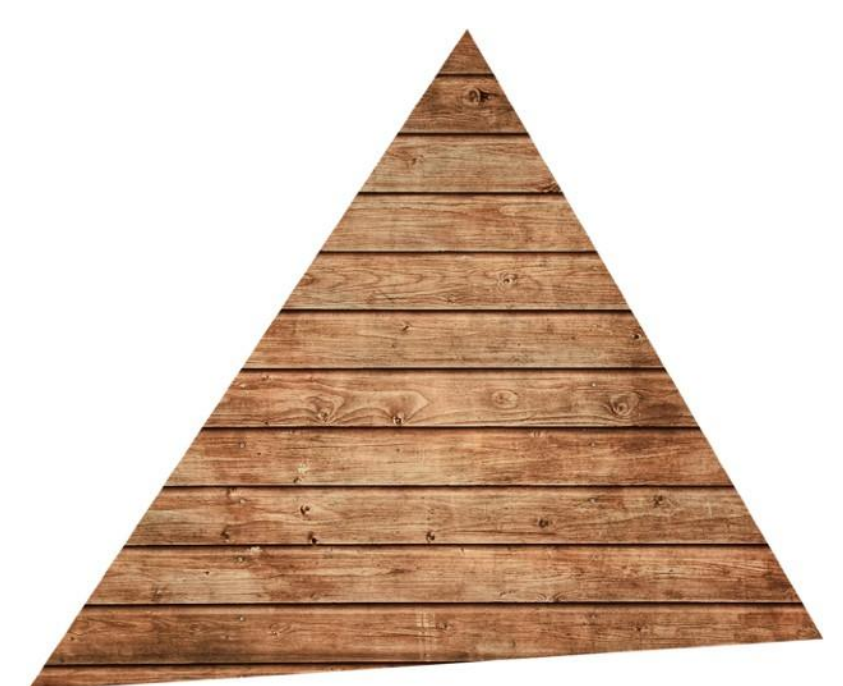
**Project objects onto the screen**



**Sample triangle coverage**

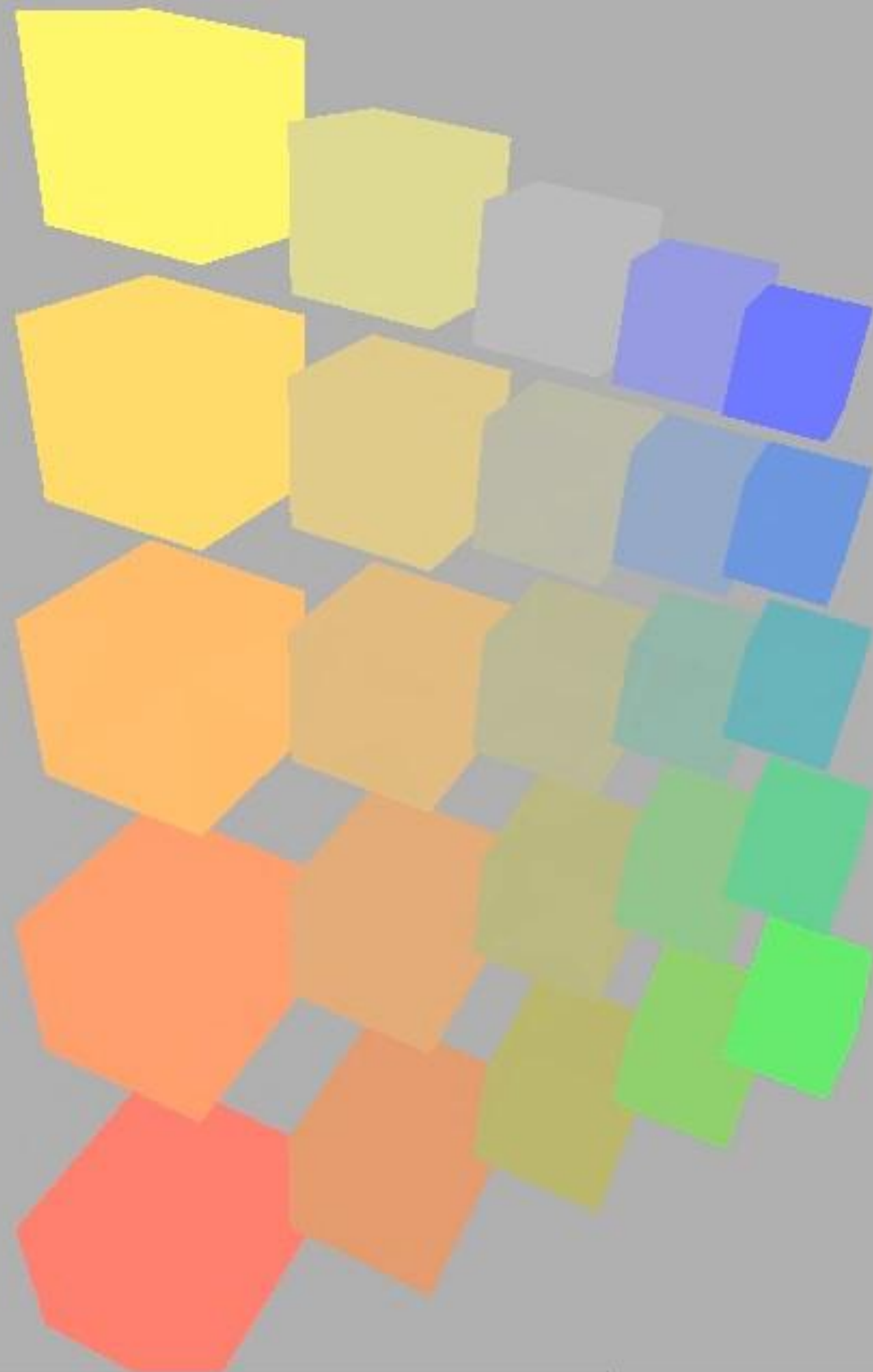


**Interpolate triangle attributes**

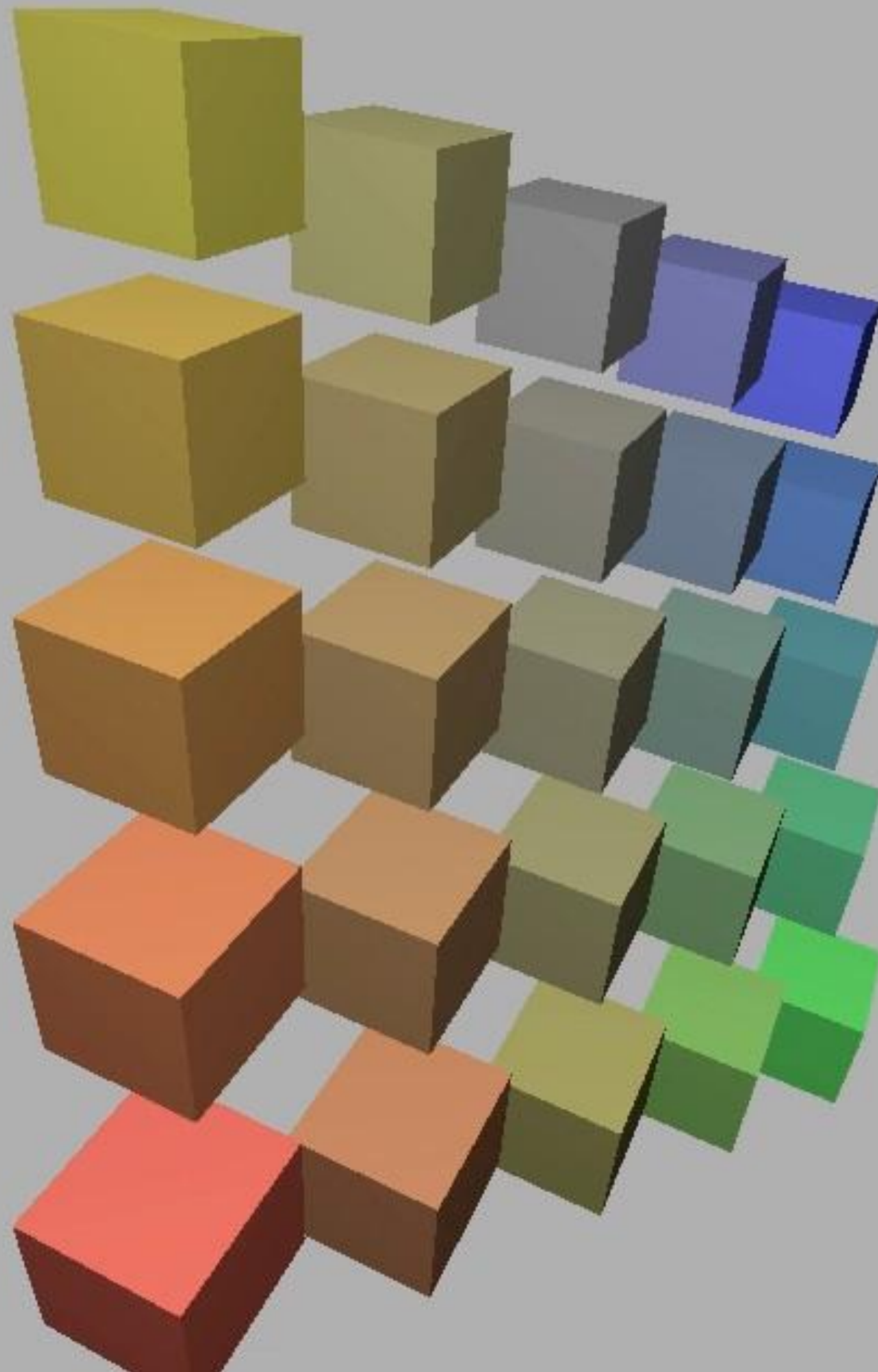


**Sample texture maps**

# Rotating Cubes in Perspective



# Rotating Cubes in Perspective





# What Else Are We Missing?



Credit: Bertrand Benoit. "Sweet Feast," 2009. [Blender /VRay]



# What Else Are We Missing?



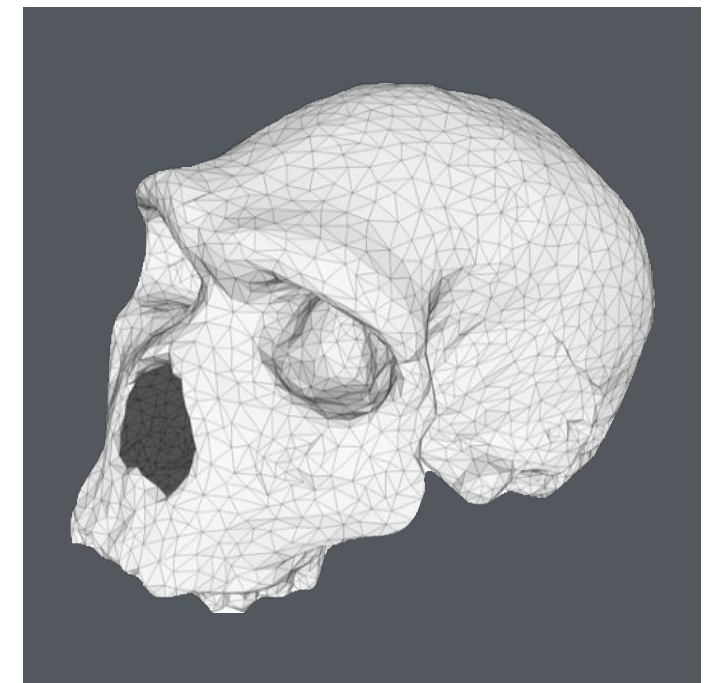
Credit: Giuseppe Albergo. "Colibri" [Blender]



# What Else Are We Missing?

## Surface representations

- Objects in the real world exhibit highly complex geometric details



## Lighting and materials

- Appearance is a result of how light sources reflect off complex materials



## Camera models

- Real lenses create images with focusing and other optical effects



# Course Roadmap

## Rasterization Pipeline

### Core Concepts

- Sampling
- Antialiasing
- Transforms

## Geometric Modeling

## Lighting & Materials

## Cameras & Imaging

Intro

Rasterization

Transforms & Projection

Texture Mapping

Today: Visibility, Shading, Overall Pipeline



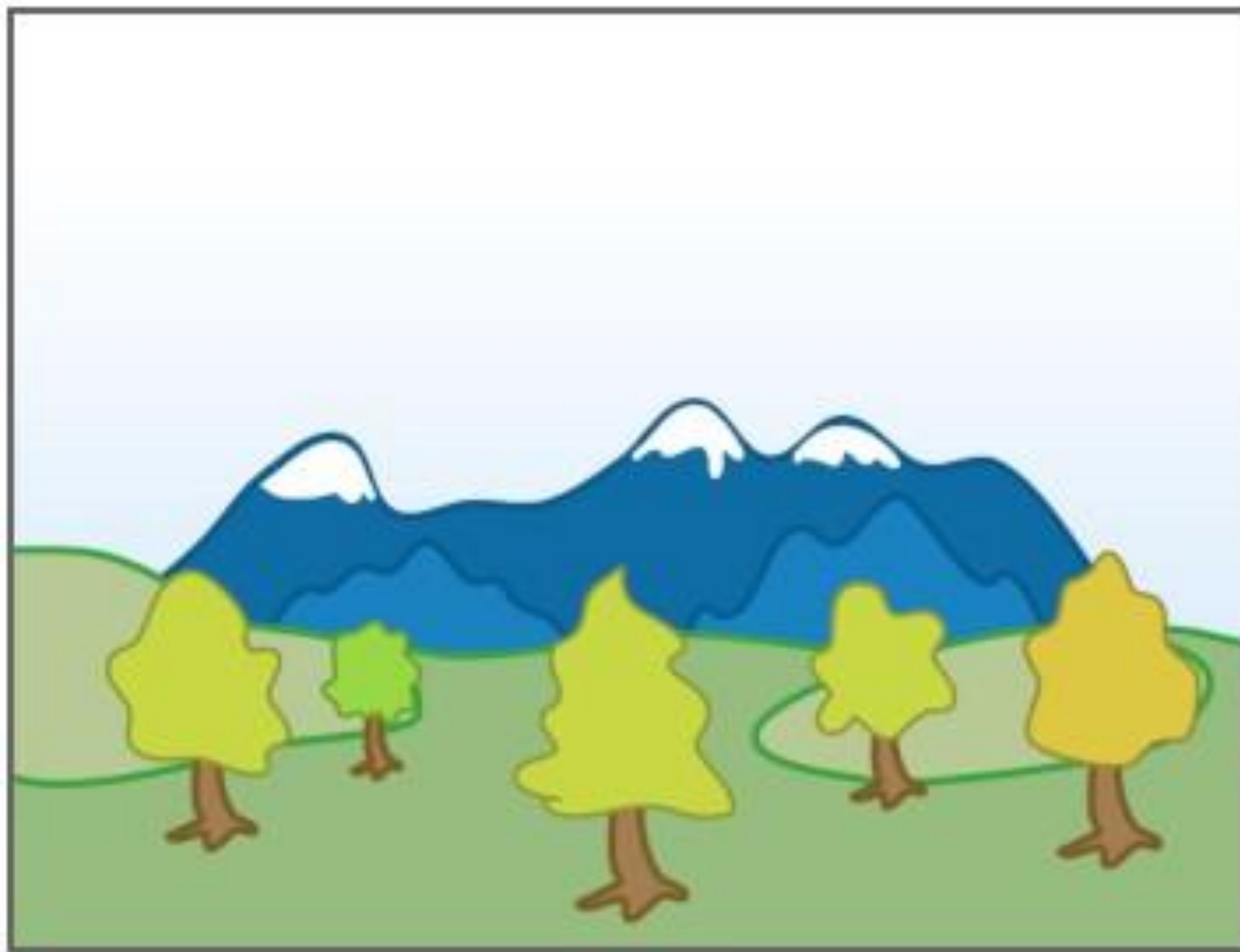


**Visibility**

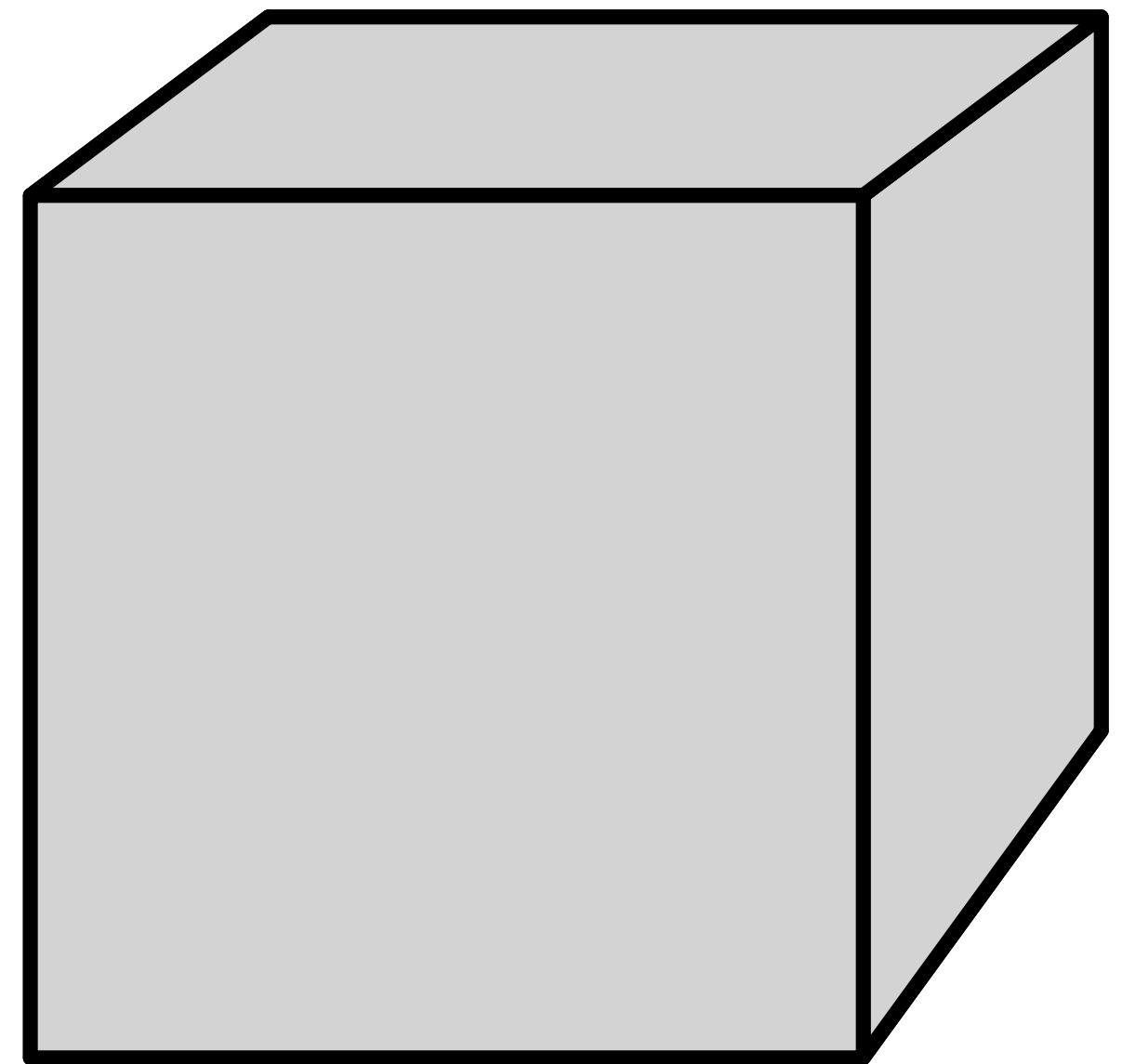
# Painter's Algorithm

Inspired by how painters paint

Paint from back to front, overwrite in the framebuffer



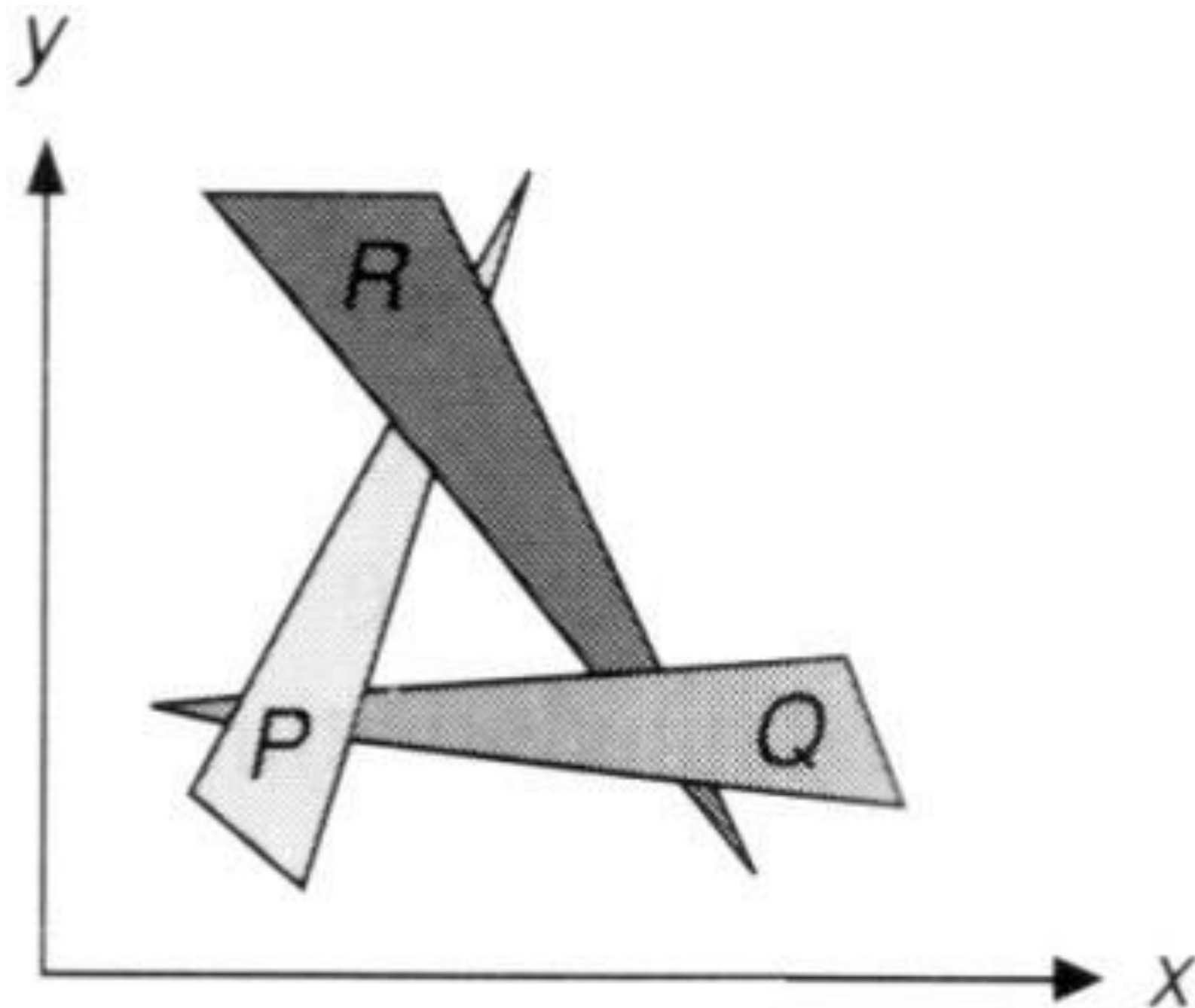
[Wikipedia]





# Painter's Algorithm

Requires sorting in depth ( $O(n \log n)$  for  $n$  triangles) Can have unresolvable depth order



[Foley et al.]

# Z-Buffer

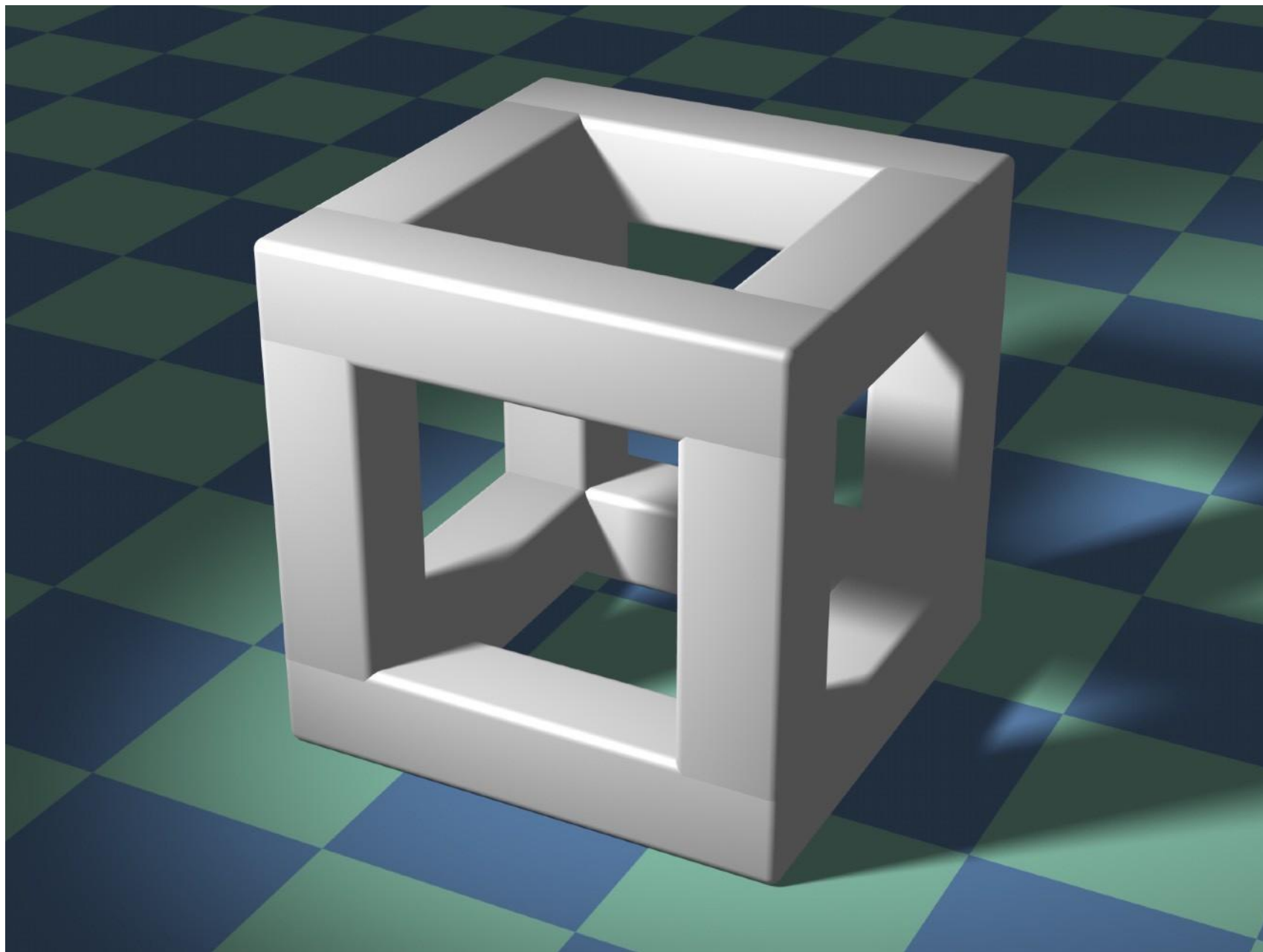
**This is the hidden-surface-removal algorithm that eventually won.**

## **Idea:**

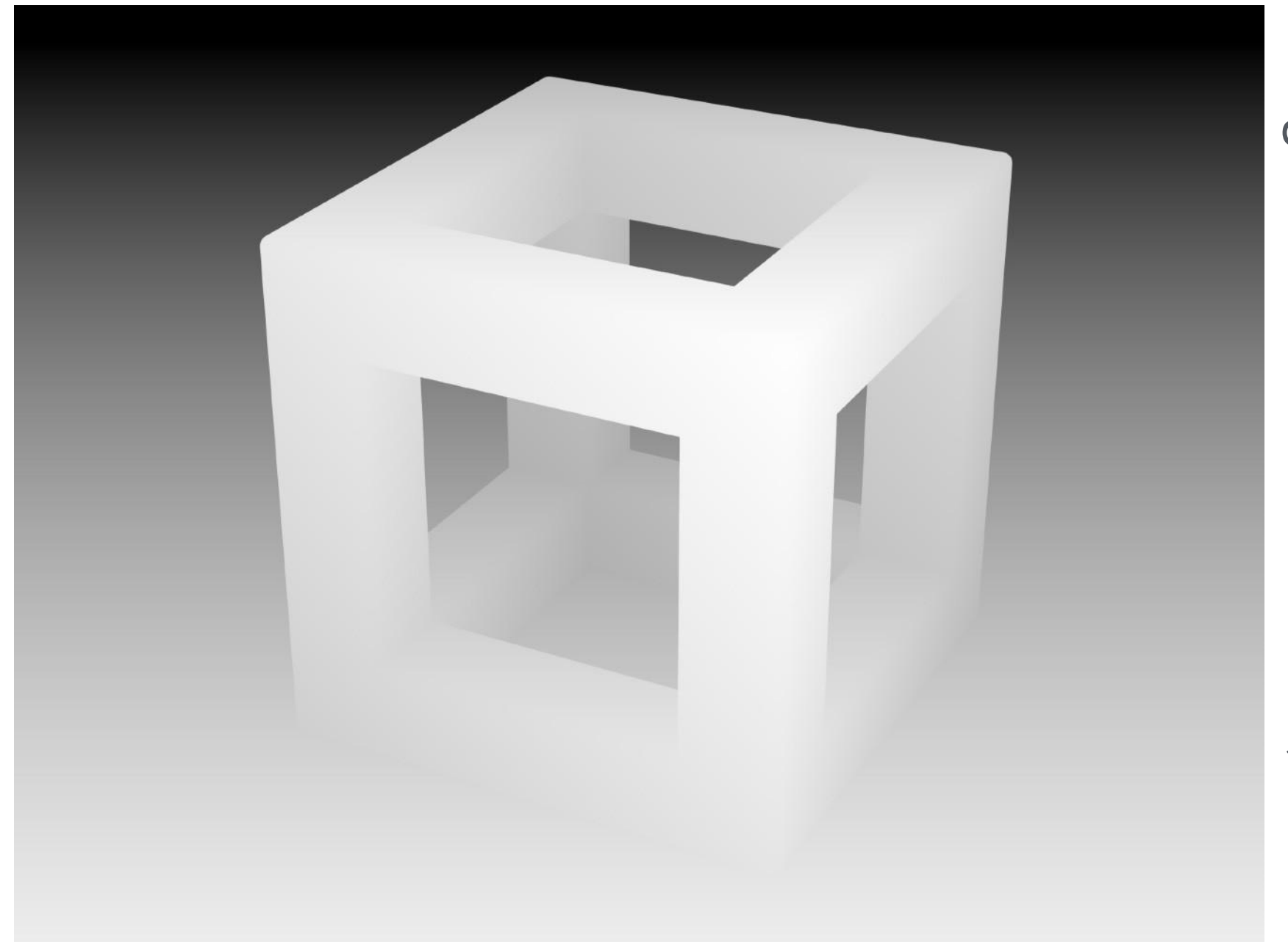
- **Store current min. z-value for each sample position**
- **Needs an additional buffer for depth values**
- **framebuffer stores RGB color values**
- **depth buffer (z-buffer) stores depth (16 to 32 bits)**



# Z-Buffer Example



**Rendering**



**Depth buffer**

# Z-Buffer Algorithm

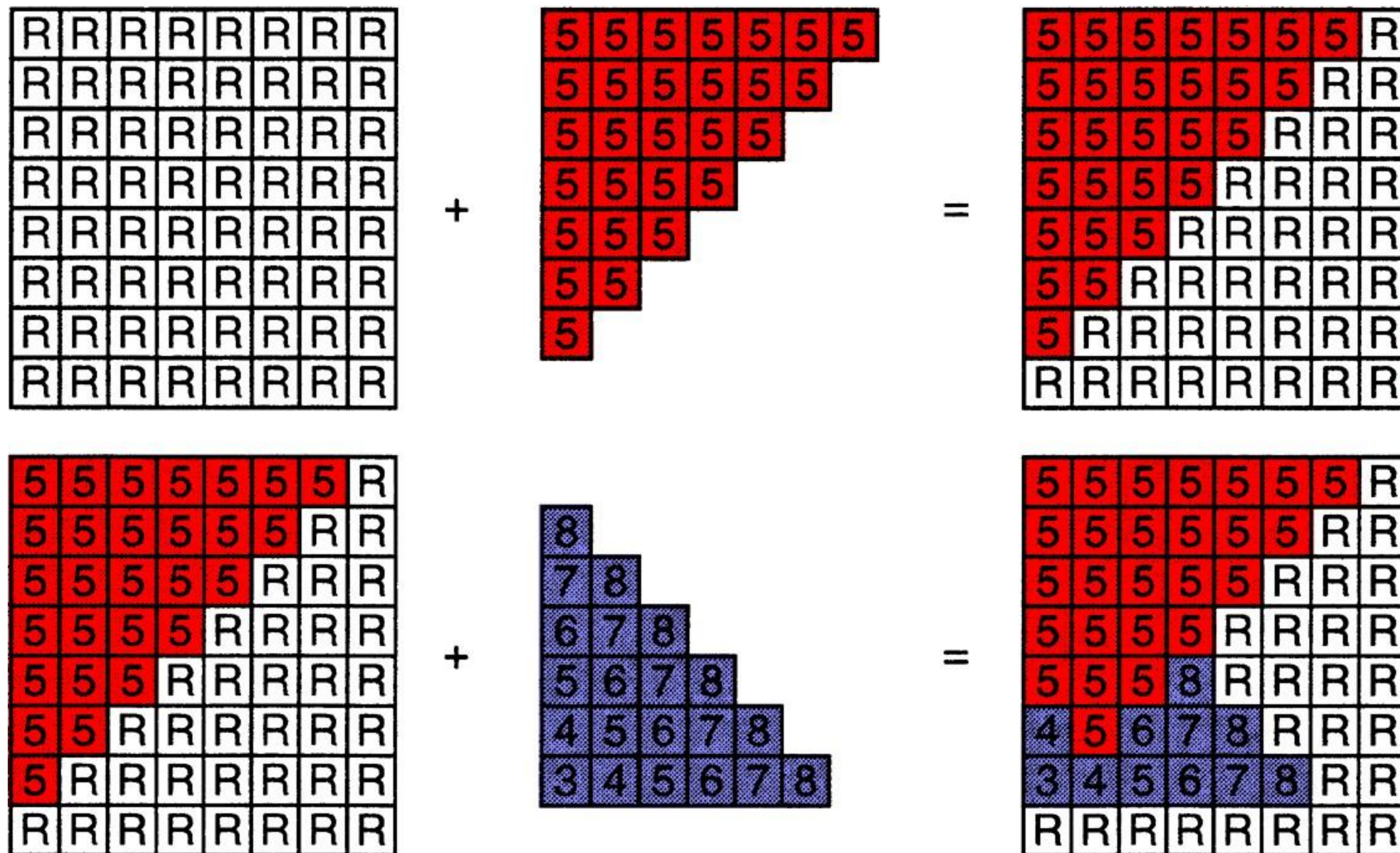
Initialize depth buffer to  $\infty$

During rasterization:

```
for(each triangle T)
  for (each sample(x,y,z) in T)
    if (z < zbuffer[x,y])           // closest sample so far
      framebuffer[x,y] = rgb;       // update color
      zbuffer[x,y]      = z;         // update z
    else
      ; // do nothing, this sample is not closest
```



# Z-Buffer Algorithm



# Z-Buffer Complexity

## Complexity

- $O(n)$  for  $n$  triangles
- Most important visibility algorithm
- Implemented in hardware for all GPUs
- Used by OpenGL



# **Simple Shading**

## **(Blinn-Phong Reflection Model)**

# **Simple Shading vs Realistic Lighting & Materials**

## **What we will cover today**

- **A local shading model: simple, per-pixel, fast**
- **Based on perceptual observations, not physics**

## **What we will cover later in the course**

- **Physics-based lighting and material representations**
- **Global light transport simulation**

**Shanghai**



# Perceptual Observations



**Specular highlights**

**Diffuse reflection**

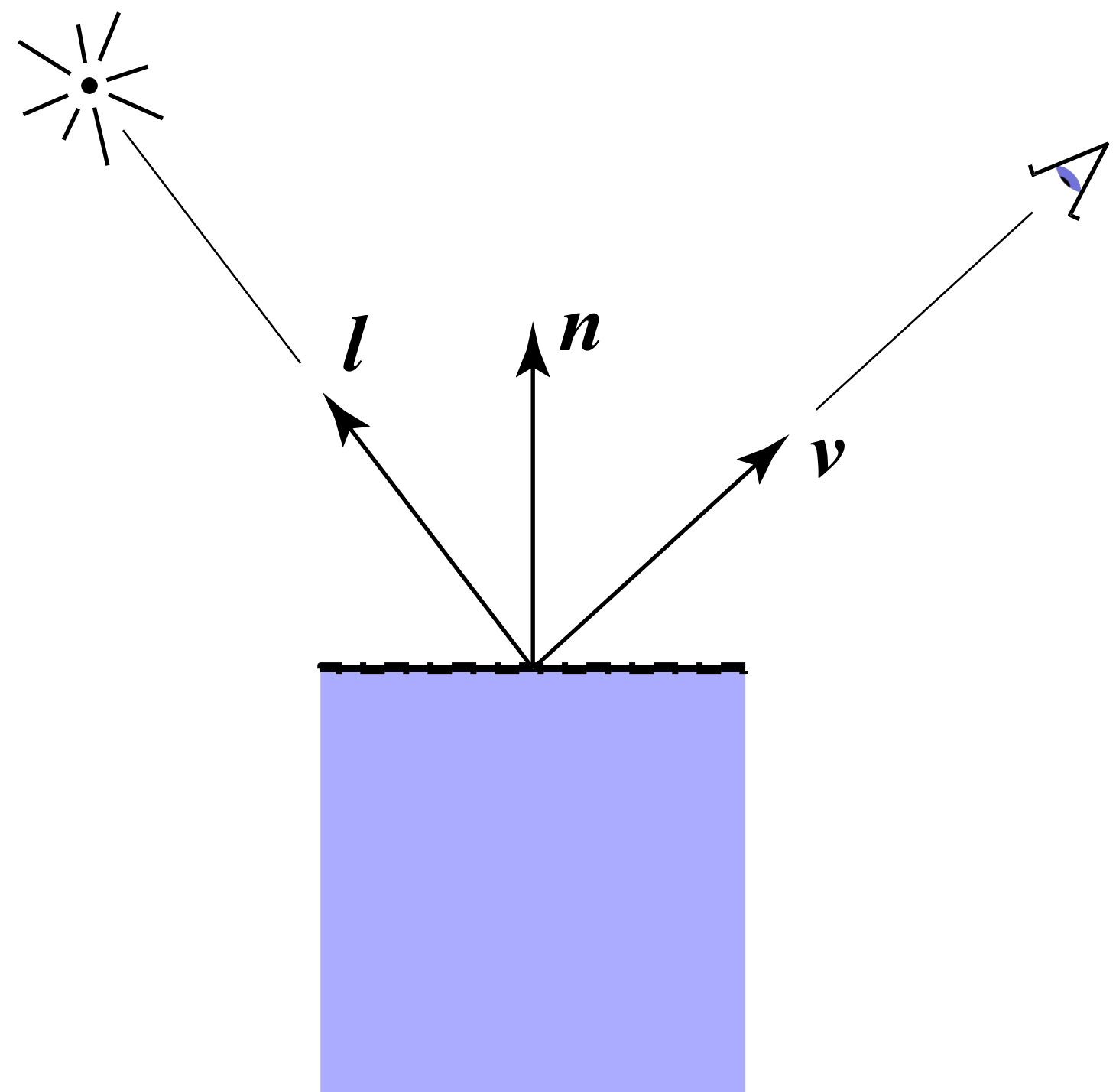
**Ambient lighting**

# Local Shading

Compute light reflected toward camera

## Inputs:

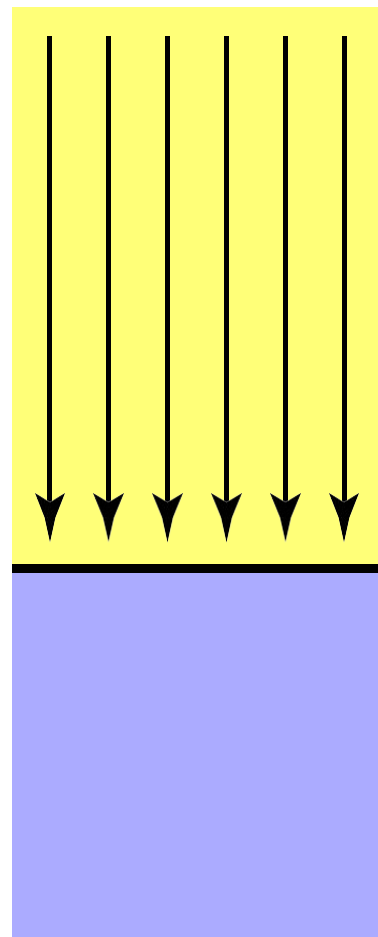
- Viewer direction,  $v$
- Surface normal,  $n$
- Light direction,  $l$   
(for each light source)
- Surface **parameters**  
(color, roughness, ...)



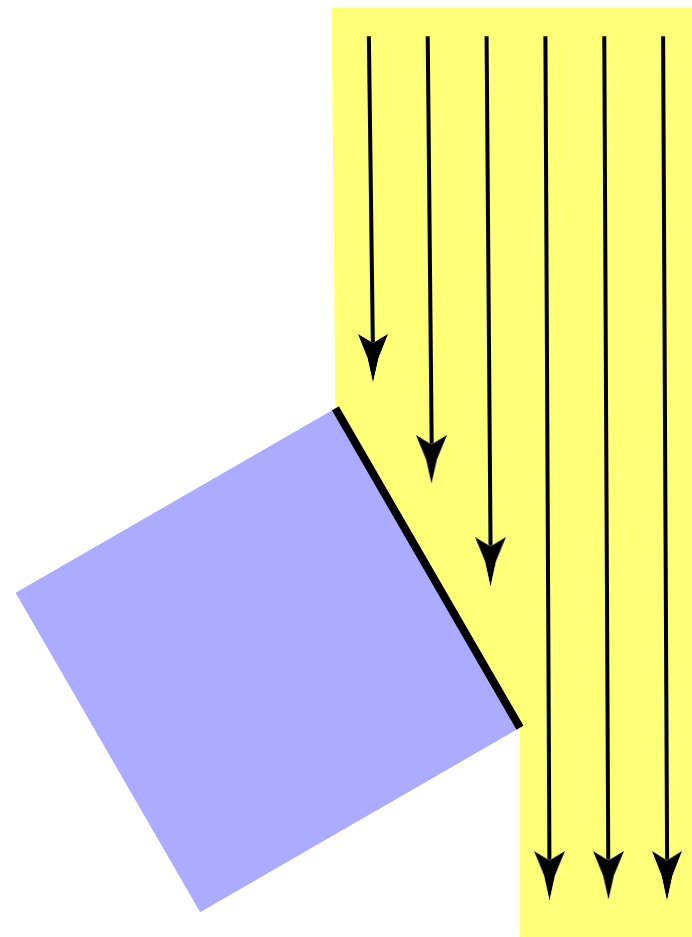
# Diffuse Reflection

Light is scattered uniformly in all directions

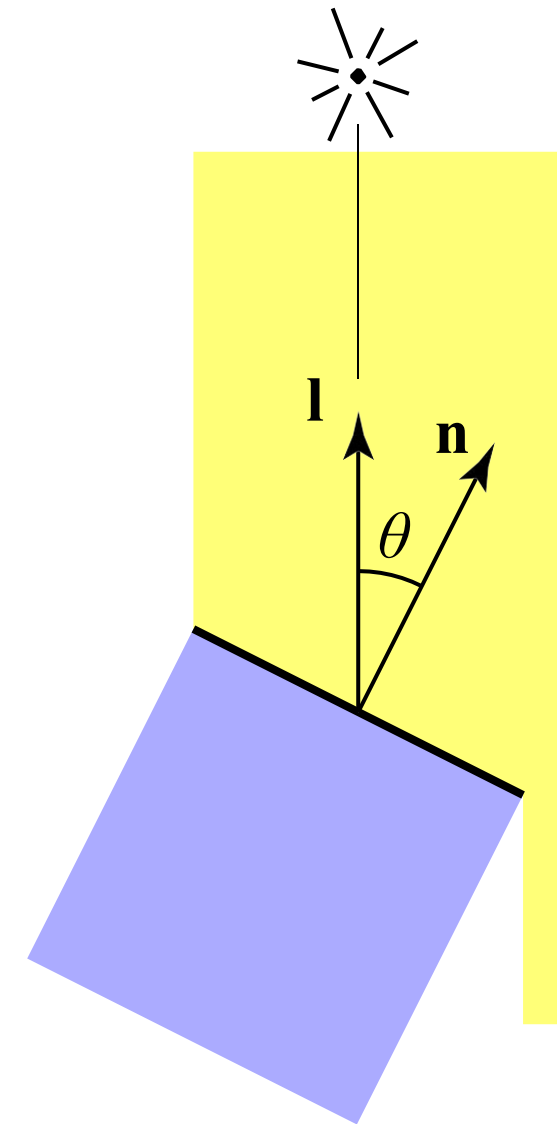
- Surface color is the same for all viewing directions  
(Lambert's cosine law)



Top face of cube  
receives a certain  
amount of light



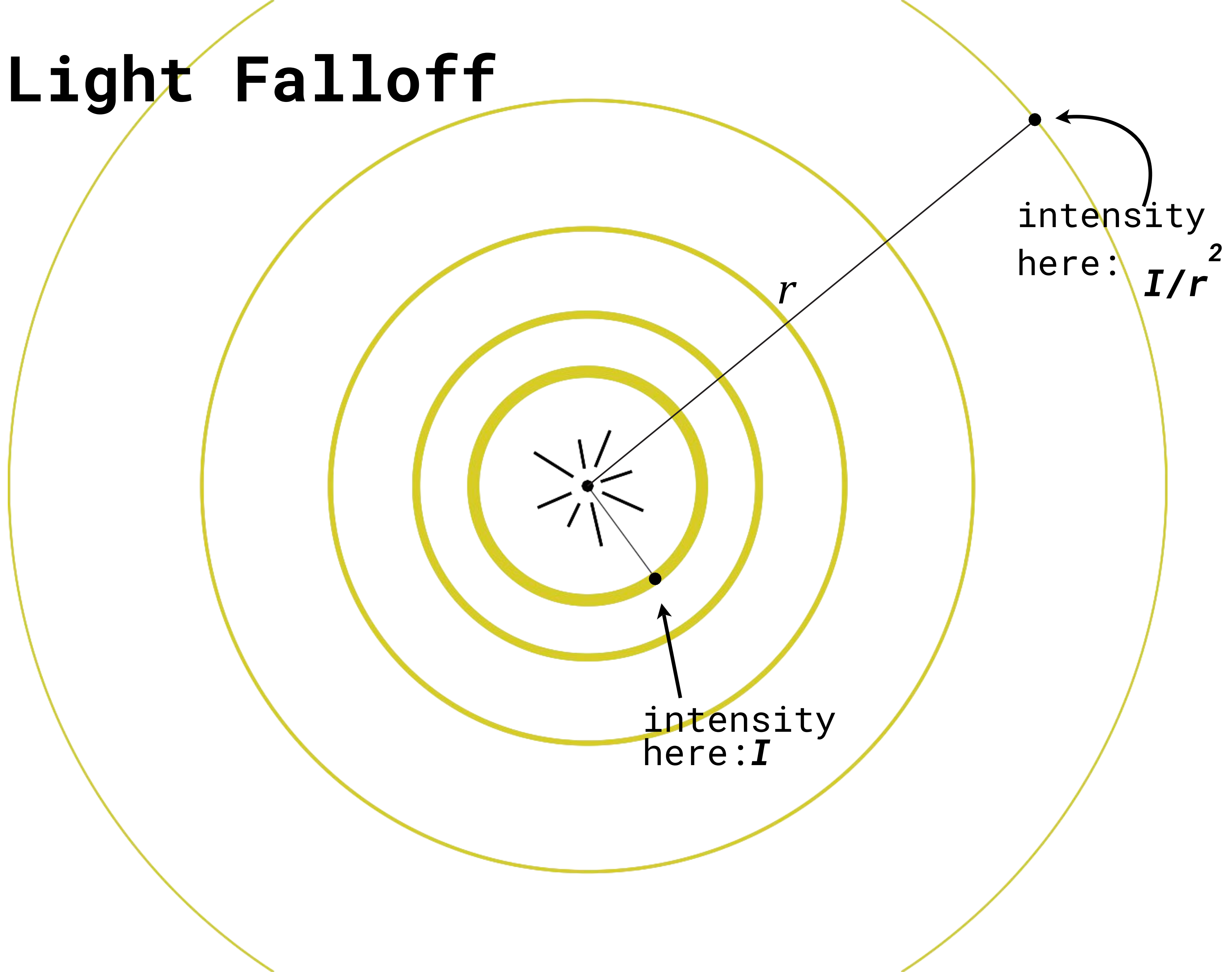
Top face of 60°  
rotated cube  
intercepts half the light



In general, light per unit  
area is proportional to  
 $\cos \theta = \mathbf{l} \cdot \mathbf{n}$

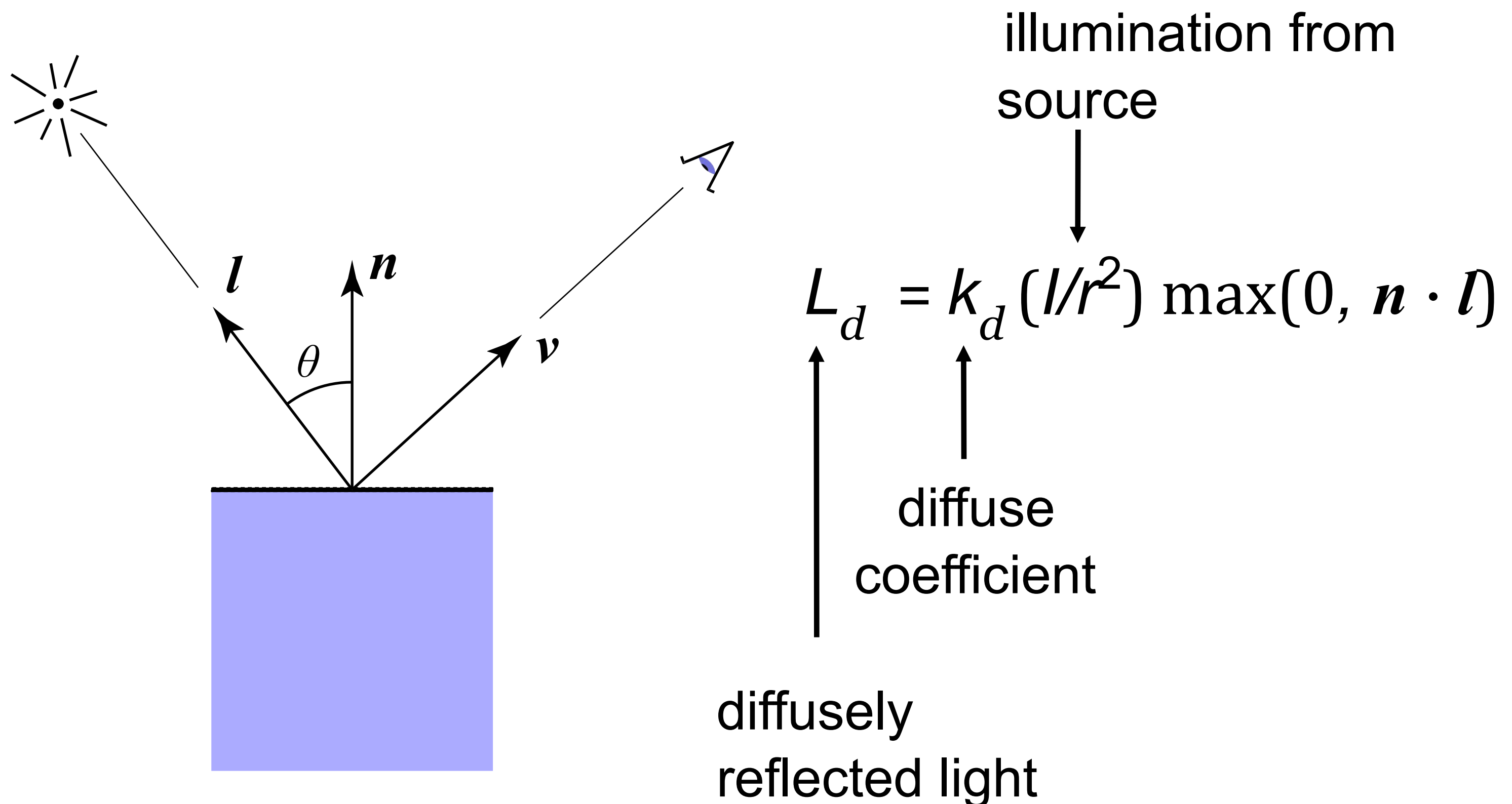


# Light Falloff



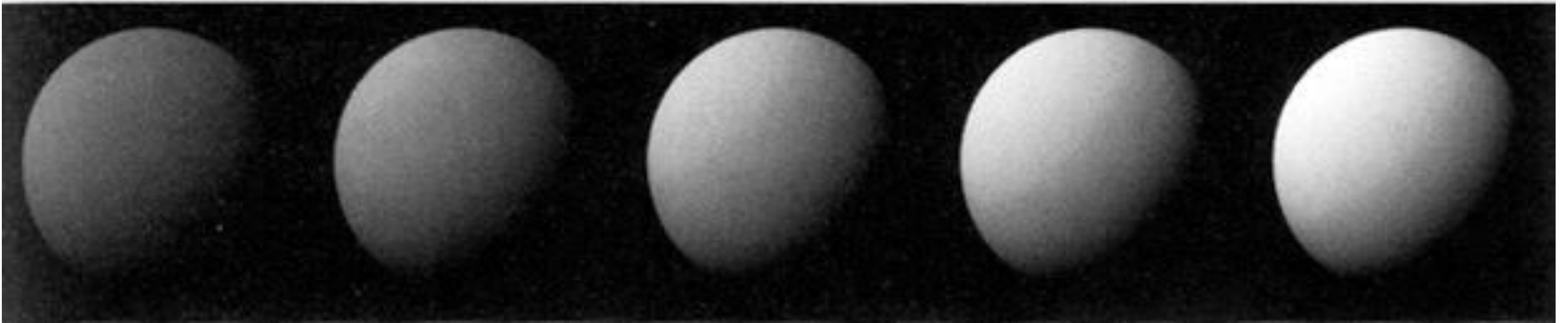
# Lambertian (Diffuse) Shading

Shading independent of view direction



# Lambertian (Diffuse) Shading

Produces matte appearance



$k_d \longrightarrow$



# Perceptual Observations



**Specular highlights**

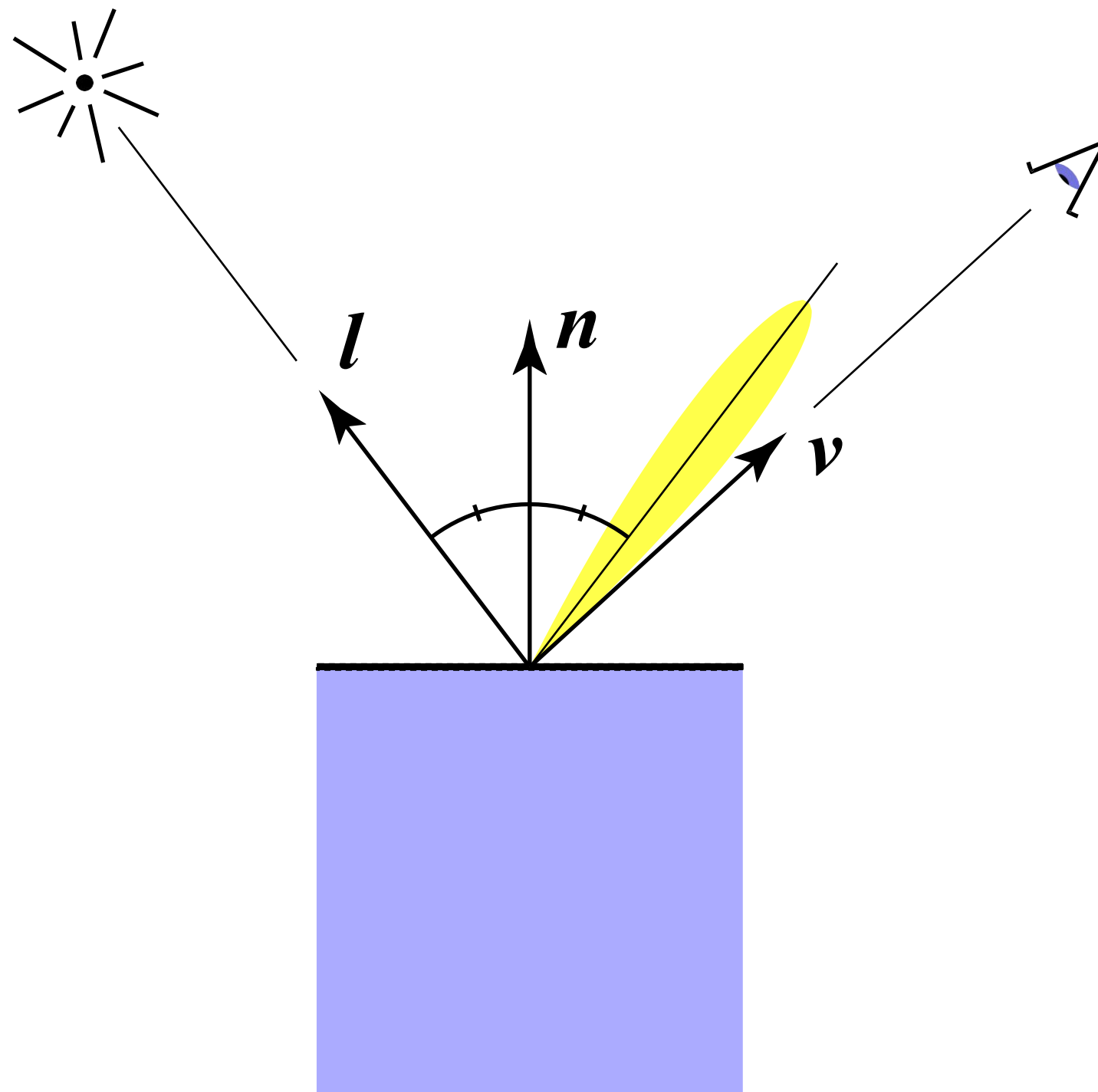
Diffuse reflection

Ambient lighting

# Specular Shading (Blinn-Phong)

Intensity depends on view direction

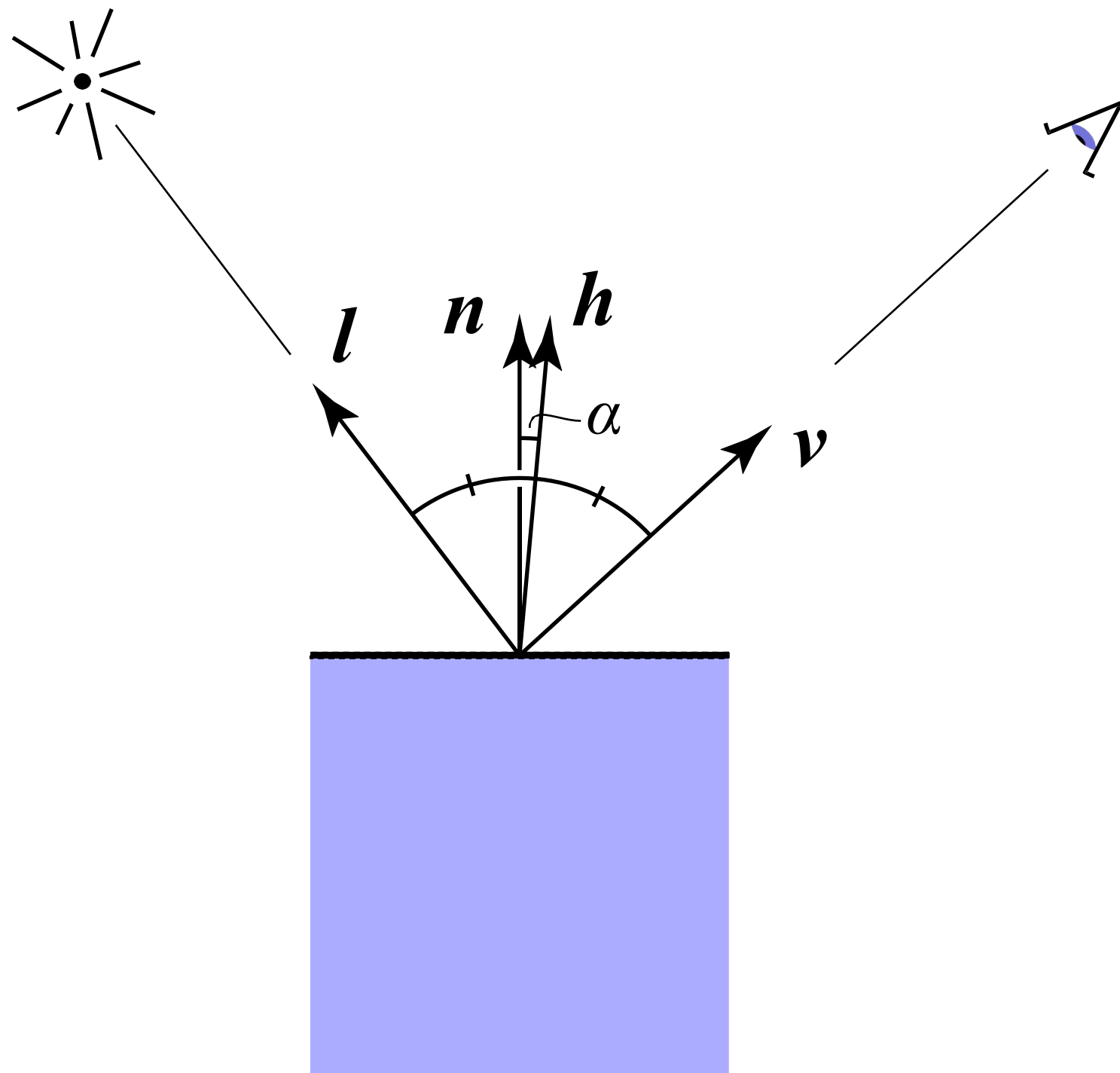
- Bright near mirror reflection direction



# Specular Shading (Blinn-Phong)

Close to mirror direction  $\Leftrightarrow$  half vector near normal

- (Measure “near” by dot product of unit vectors)



$$\begin{aligned} \mathbf{h} &= \text{bisector}(\mathbf{v}, \mathbf{l}) \\ &= \mathbf{v} + \mathbf{l} / \|\mathbf{v} + \mathbf{l}\| \end{aligned}$$

$$\begin{aligned} L_s &= k_s (I/r^2) \max(0, \cos \theta)^p \\ &= k_s (I/r^2) \max(0, \mathbf{n} \cdot \mathbf{h})^p \end{aligned}$$

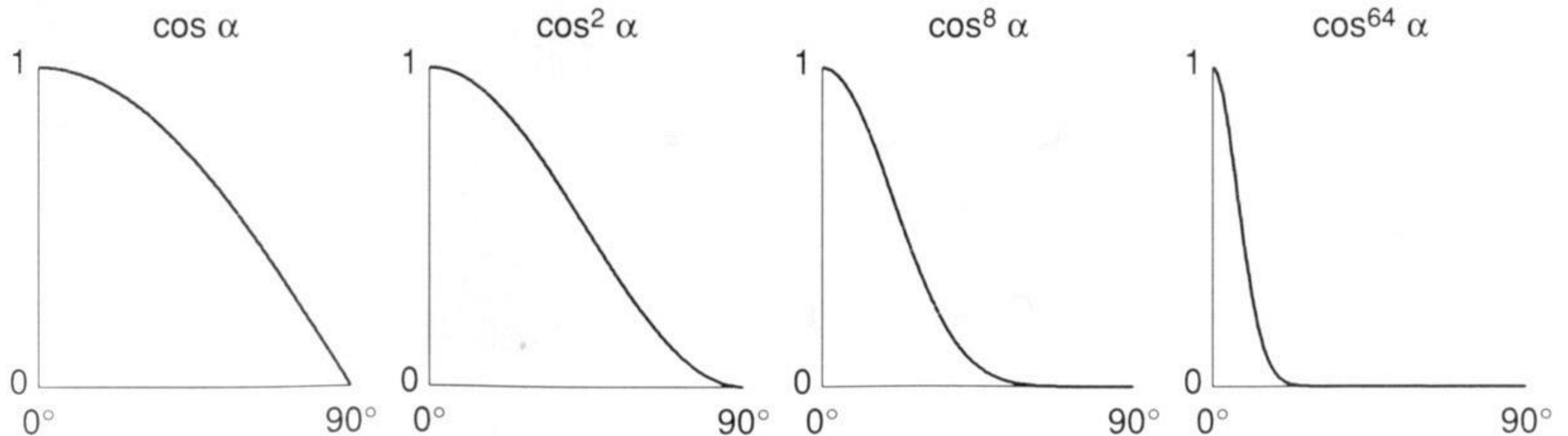
↑  
specularly  
reflected  
light

↑  
specular  
coefficient



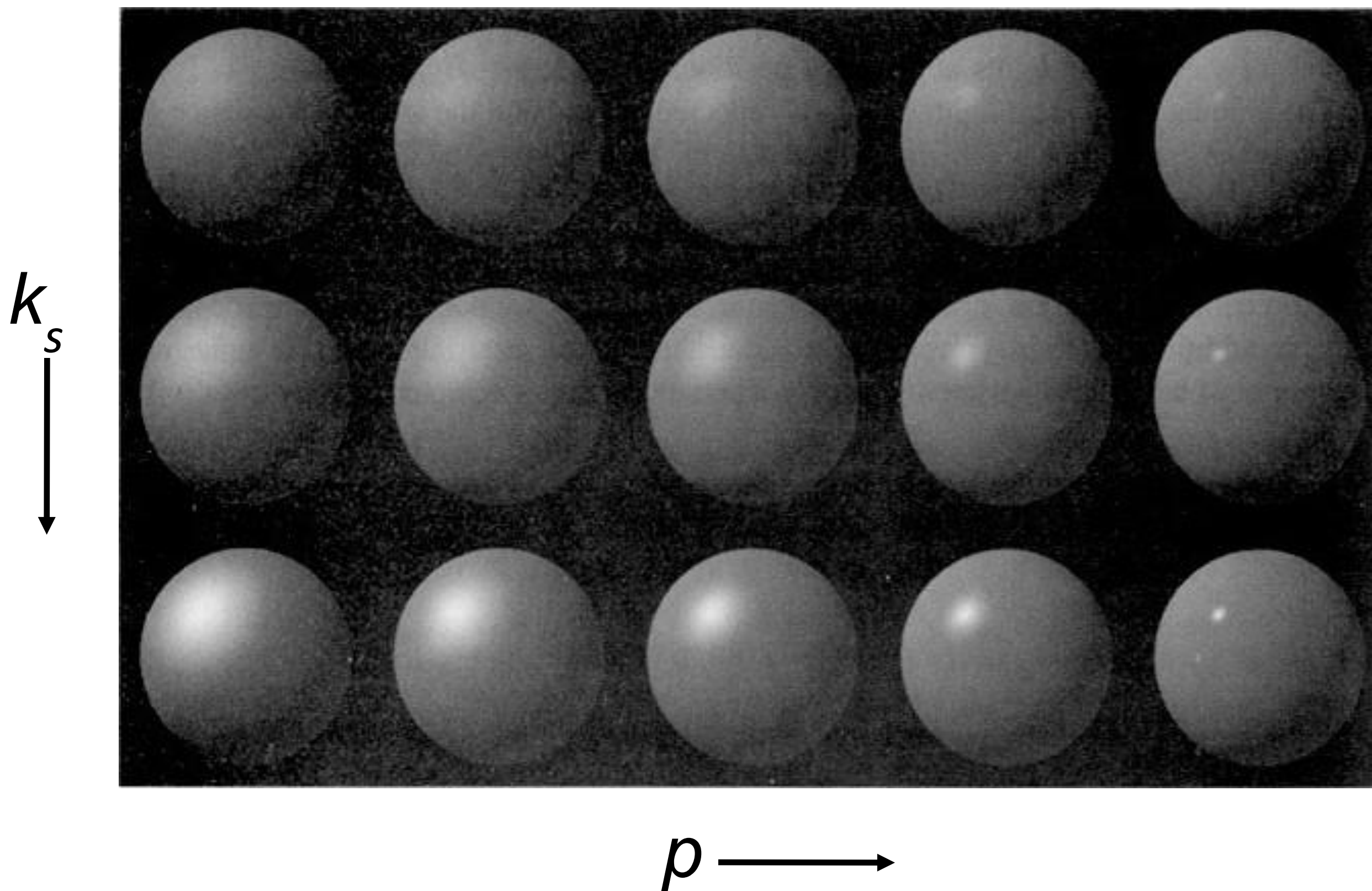
# Cosine Power Plots

Increasing  $p$  narrows the reflection lobe



# Specular Shading (Blinn-Phong)

$$L_s = k_s (I/r^2) \max(0, \mathbf{n} \cdot \mathbf{h})^p$$



# Perceptual Observations



Specular highlights

Diffuse reflection

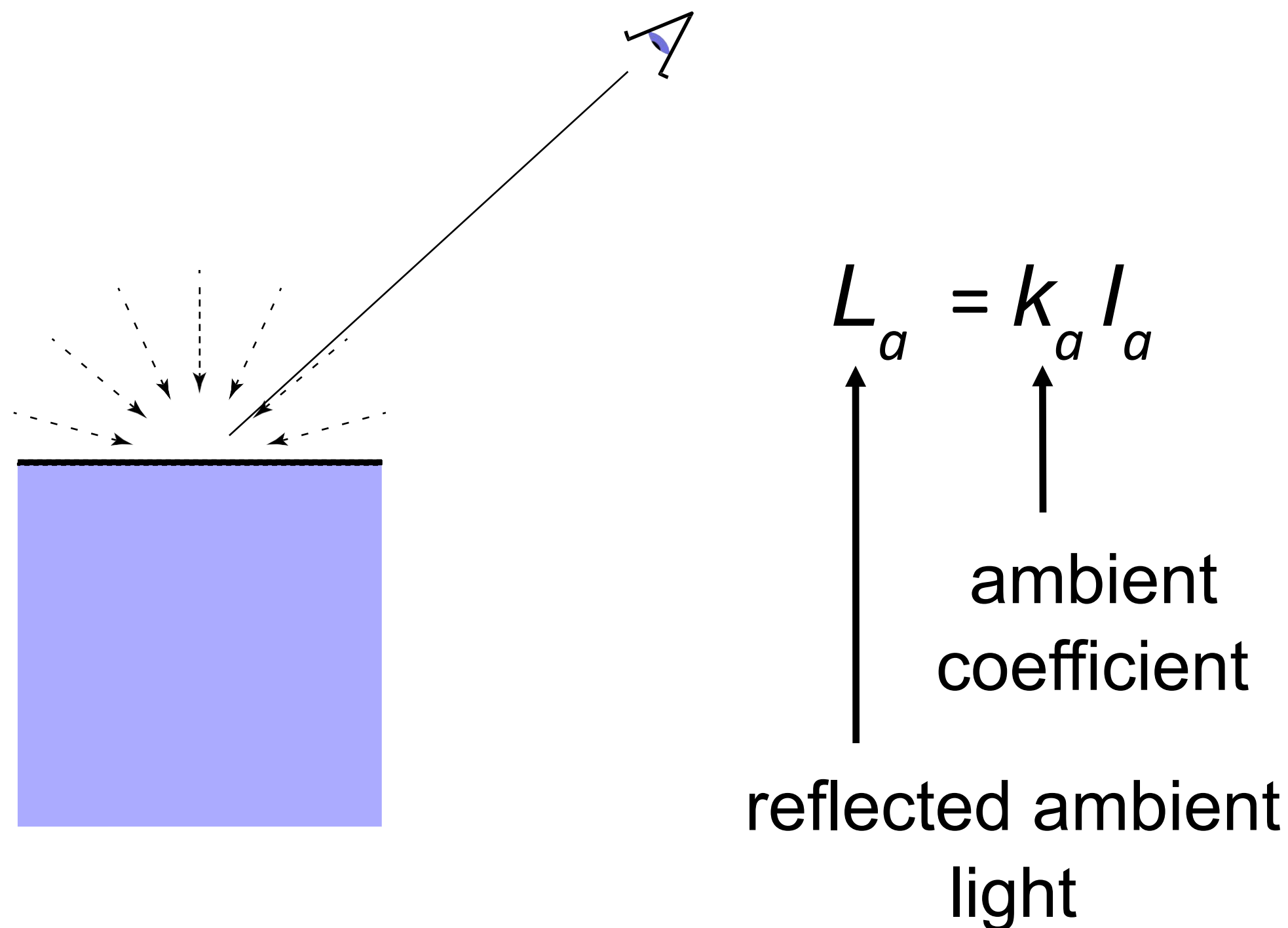
Ambient lighting



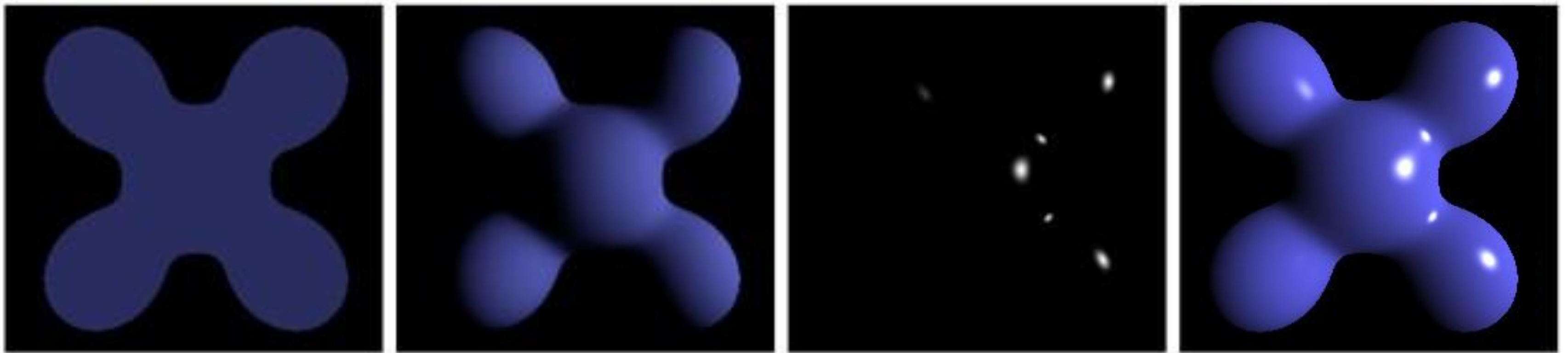
# Ambient Shading

Shading that does not depend on anything

- Add constant color to account for disregarded illumination and fill in black shadows



# Blinn-Phong Reflection Model



**Ambient    +    Diffuse    +    Specular    =   Phong Reflection**

$$L = L_a + L_d + L_s$$

$$= k_a I_a + k_d (I/r^2) \max(0, \mathbf{n} \cdot \mathbf{l}) + k_s (I/r^2) \max(0, \mathbf{n} \cdot \mathbf{h})^p$$

# Blinn-Phong Reflection Model

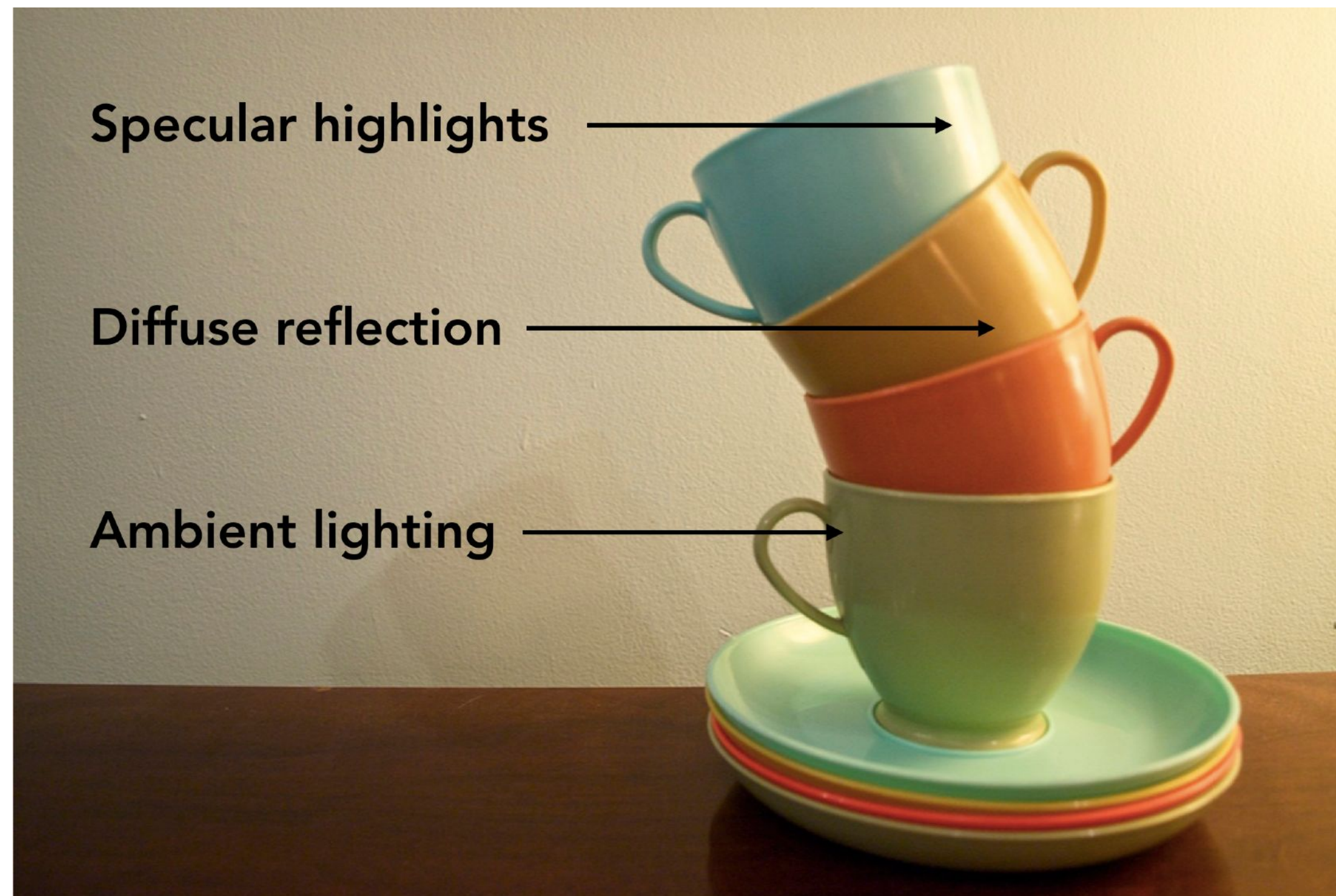


Photo credit: Jessica Andrews, flickr

$$L = L_a + L_d + L_s$$

$$= k_a I_a + k_d (I/r^2) \max(0, \mathbf{n} \cdot \mathbf{l}) + k_s (I/r^2) \max(0, \mathbf{n} \cdot \mathbf{h})^p$$



# Shading Triangle Meshes

# Shading Frequency: **Triangle**, **Vertex** or **Pixel**

## Shade each triangle (flat shading)

- Triangle face is flat — one normal vector
- Not good for smooth surfaces



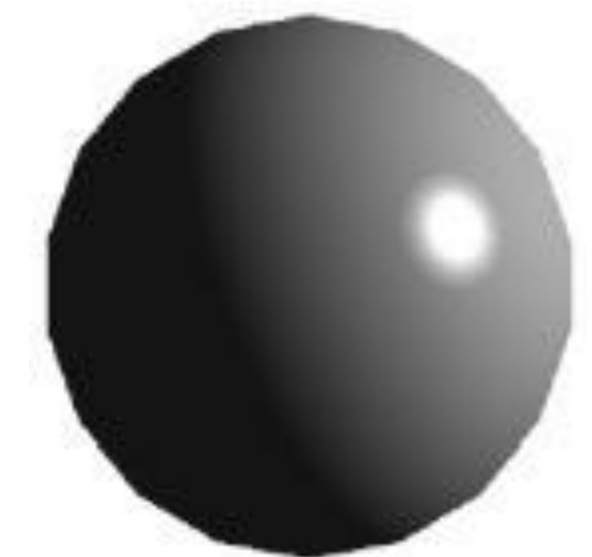
## Shade each vertex ("Gouraud" shading)

- Interpolate colors from vertices across triangle
- Each vertex has a normal vector

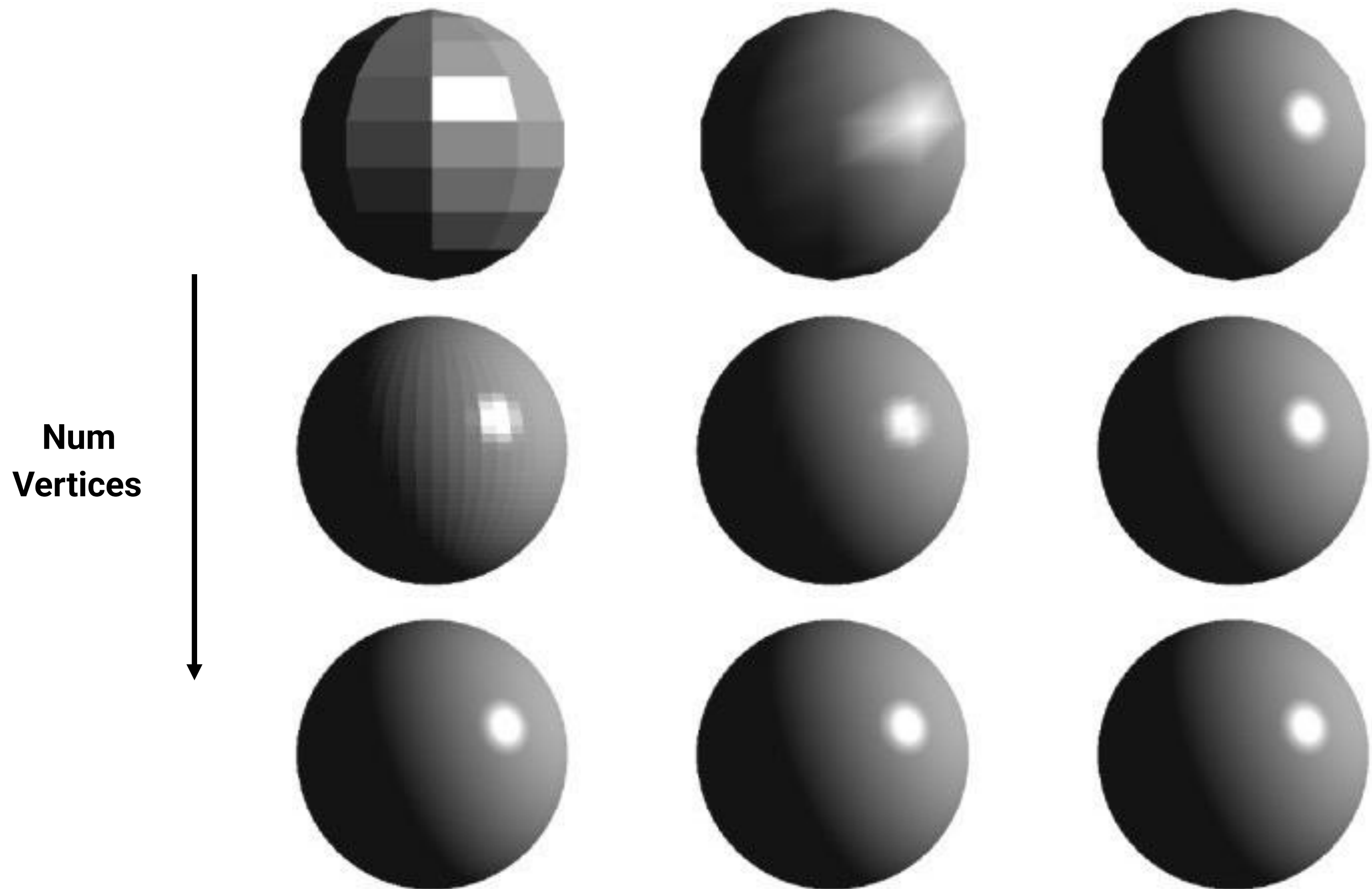


## Shade each pixel ("Phong" shading)

- Interpolate normal vectors across each triangle
- Compute full shading model at each pixel



# Shading Frequency: **Face**, **Vertex** or **Pixel**



Shading freq :  
Shading type :

**Face**  
**Flat**

**Vertex**  
**Gouraud**

**Pixel**  
**Phong (\*)**



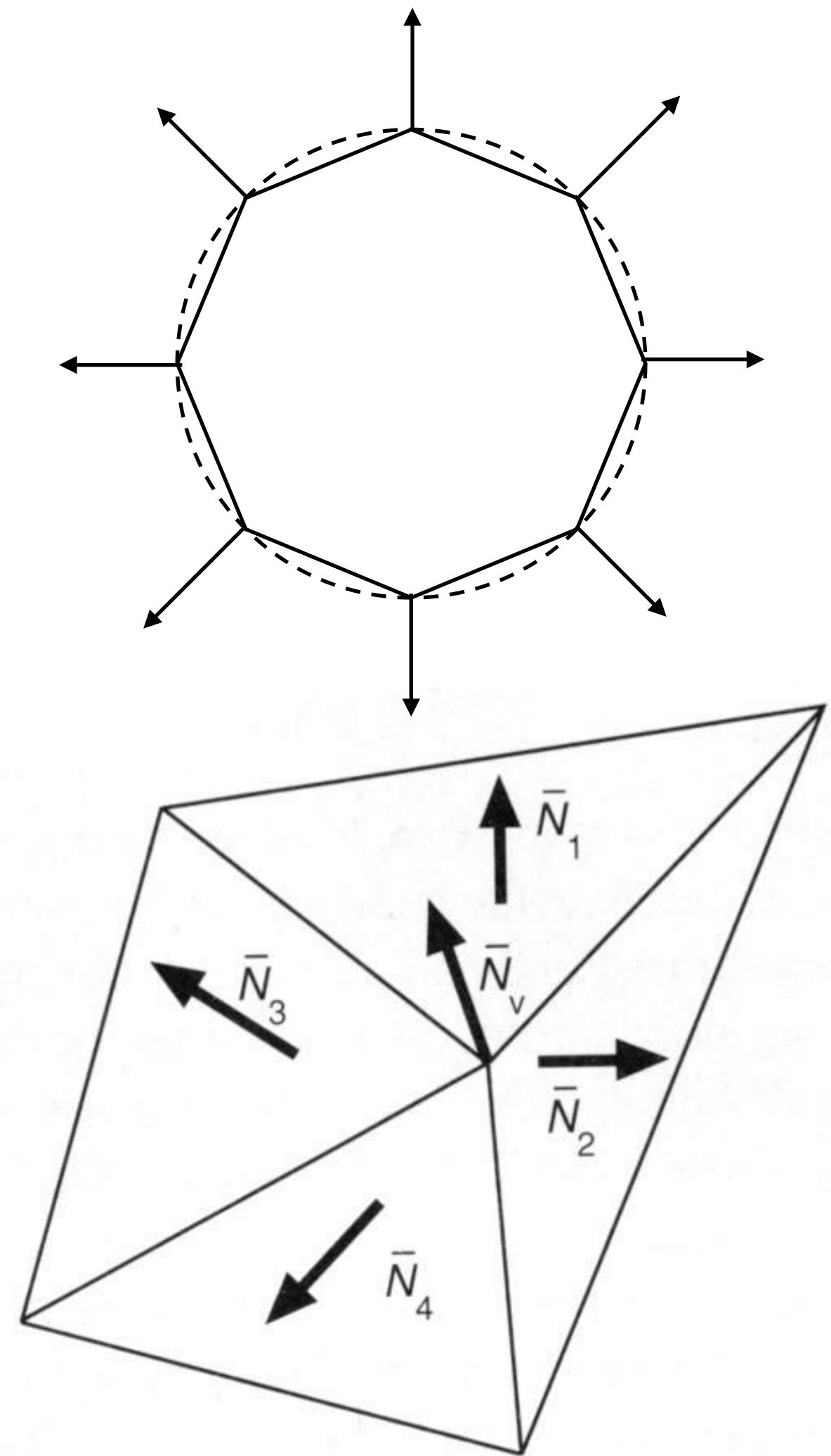
# Defining Per-Vertex Normal Vectors

**Get vertex normals from the underlying geometry (e.g. consider a sphere)**

**Otherwise have to infer vertex normals from triangle faces**

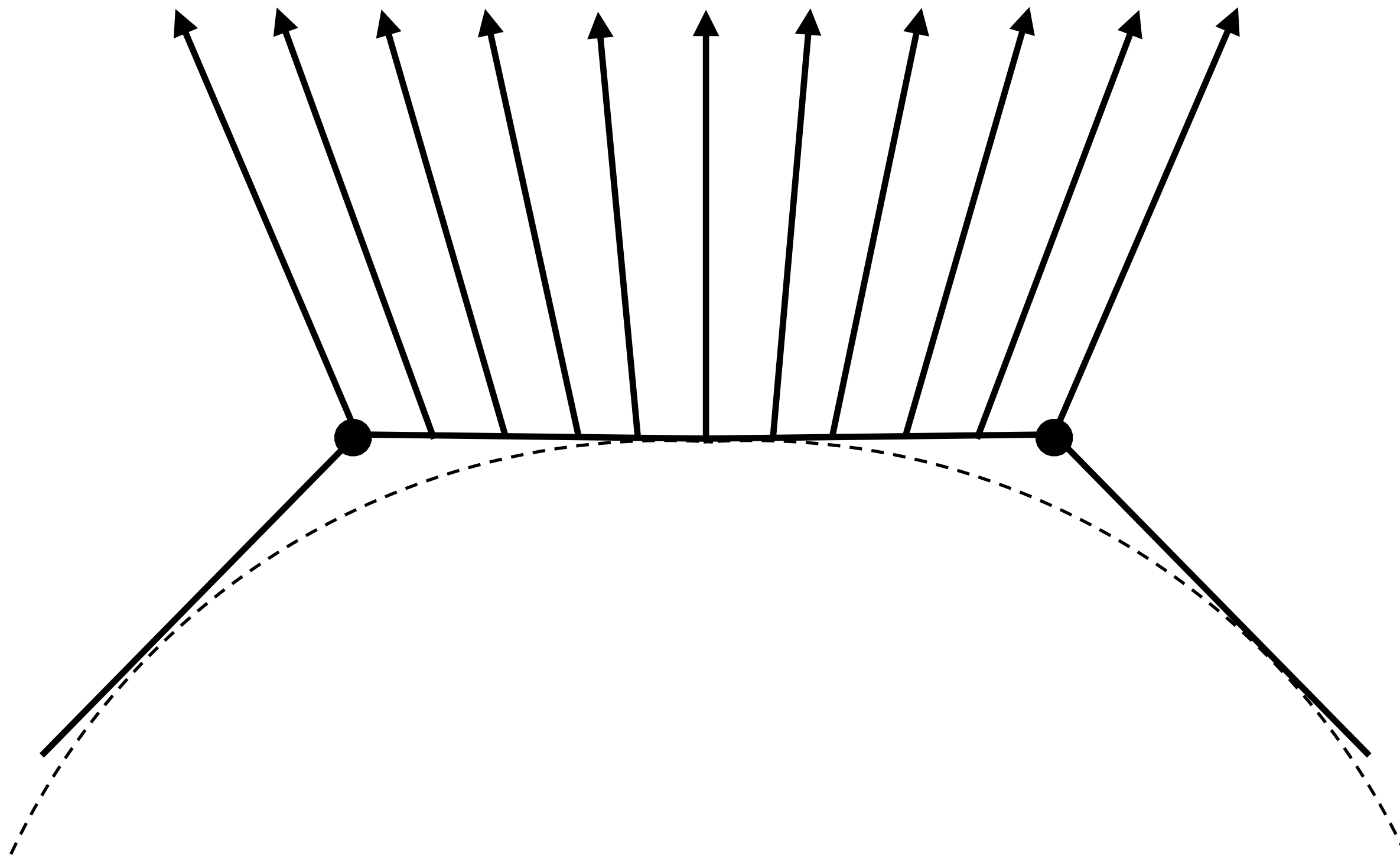
- **Simple scheme: average surrounding face normals**

$$N_v = \frac{\sum_i N_i}{\|\sum_i N_i\|}$$



# Defining Per-Pixel Normal Vectors

Barycentric interpolation of vertex normals

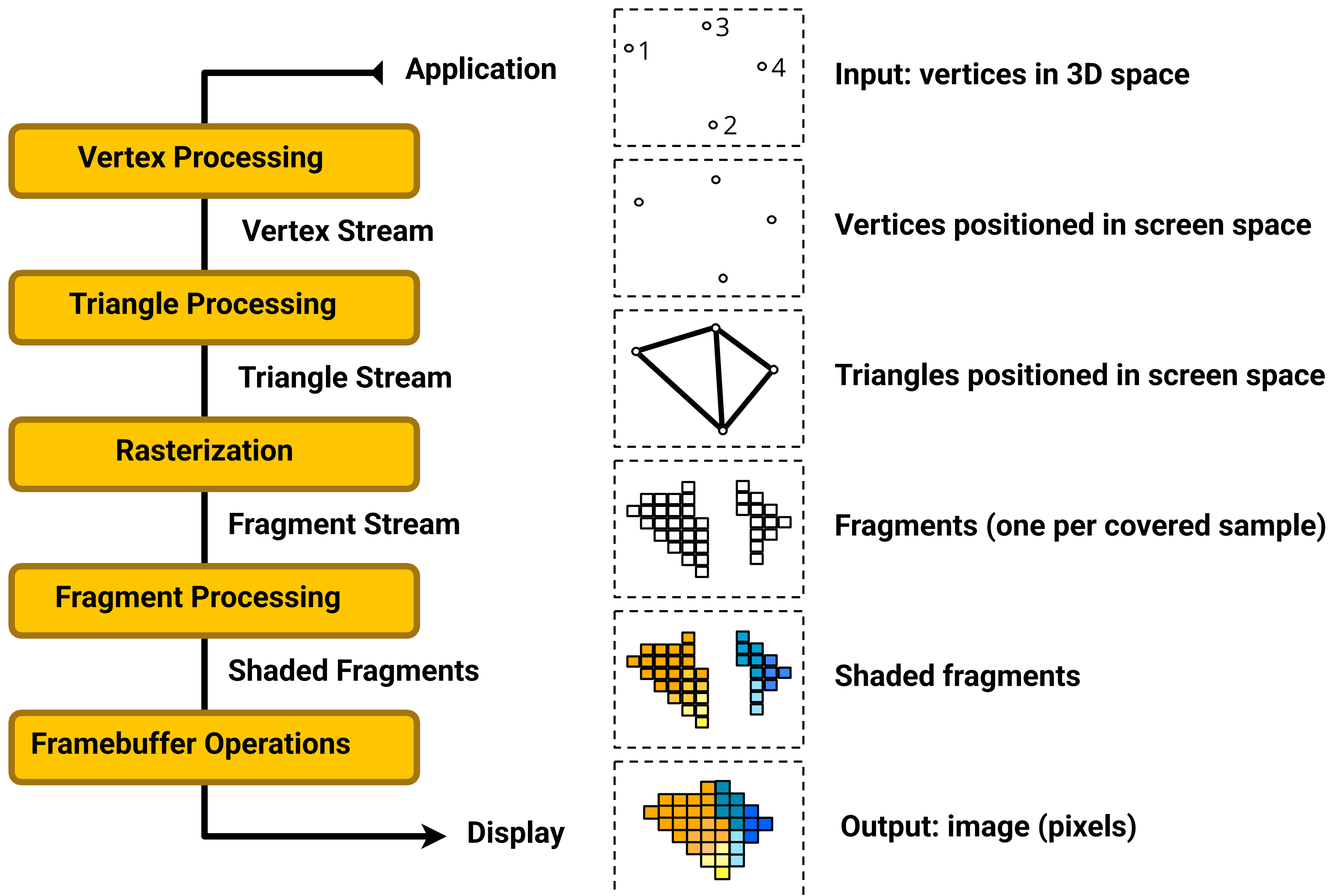


Problem: length of vectors?

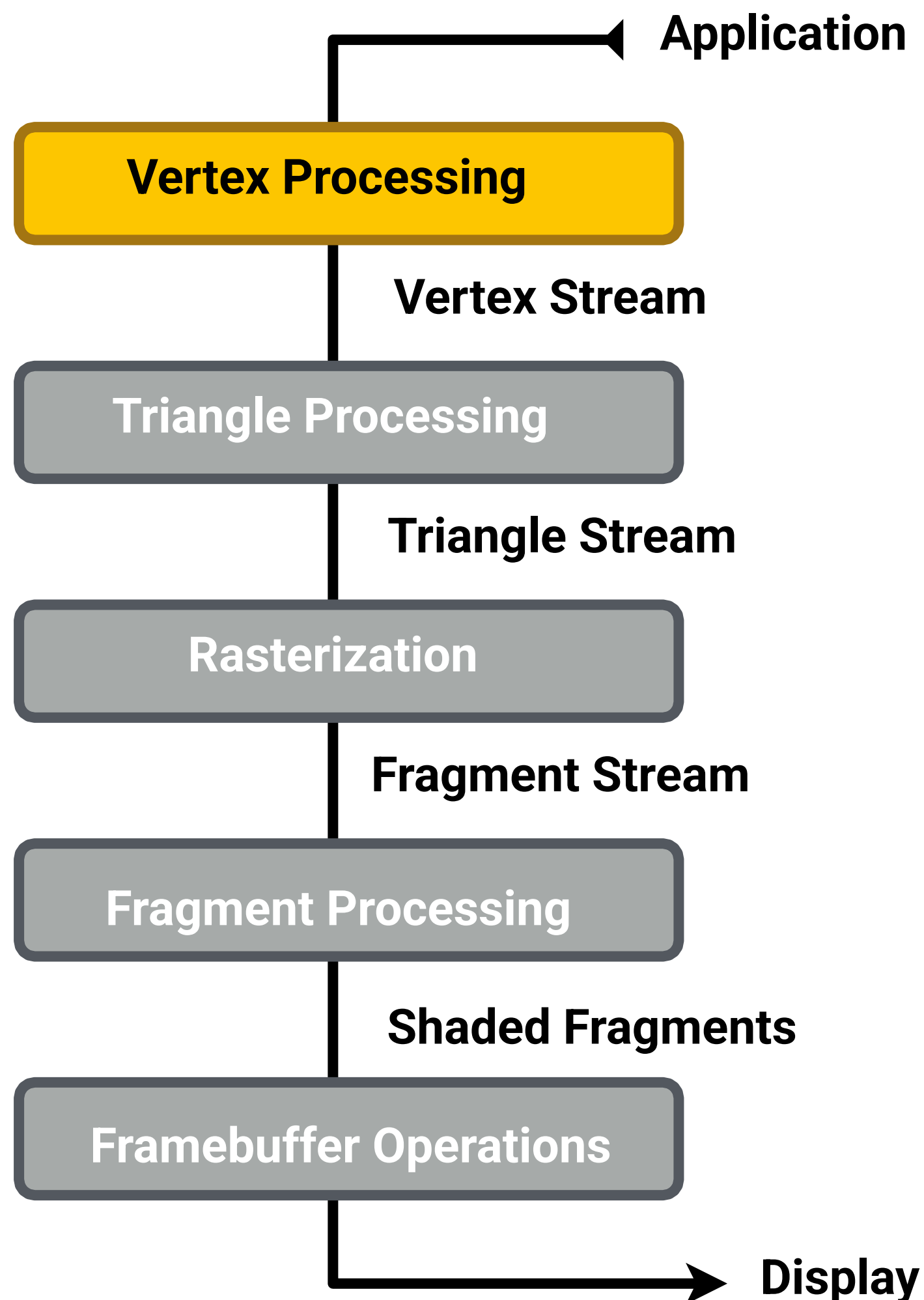
# **Rasterization Pipeline**



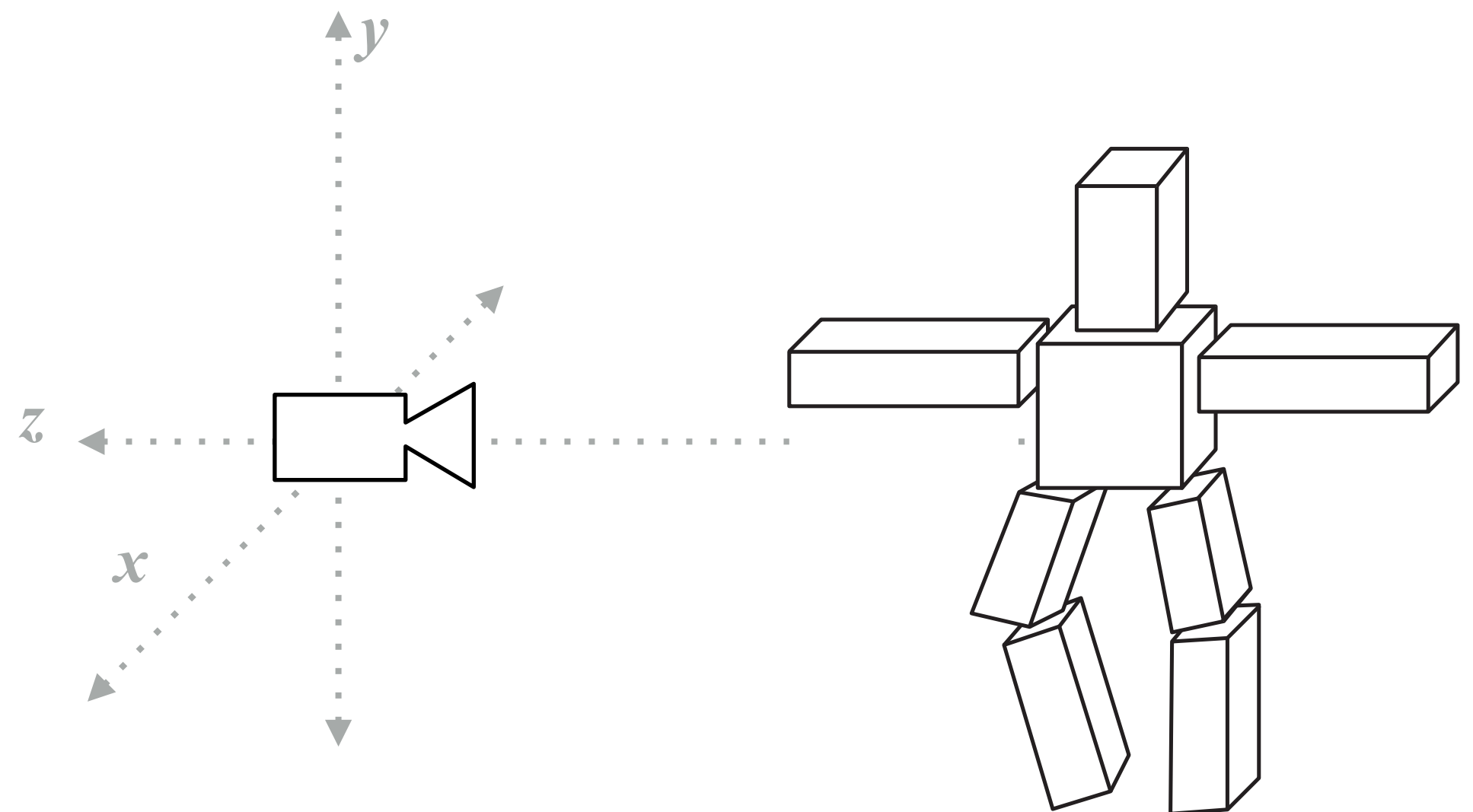
# Rasterization Pipeline



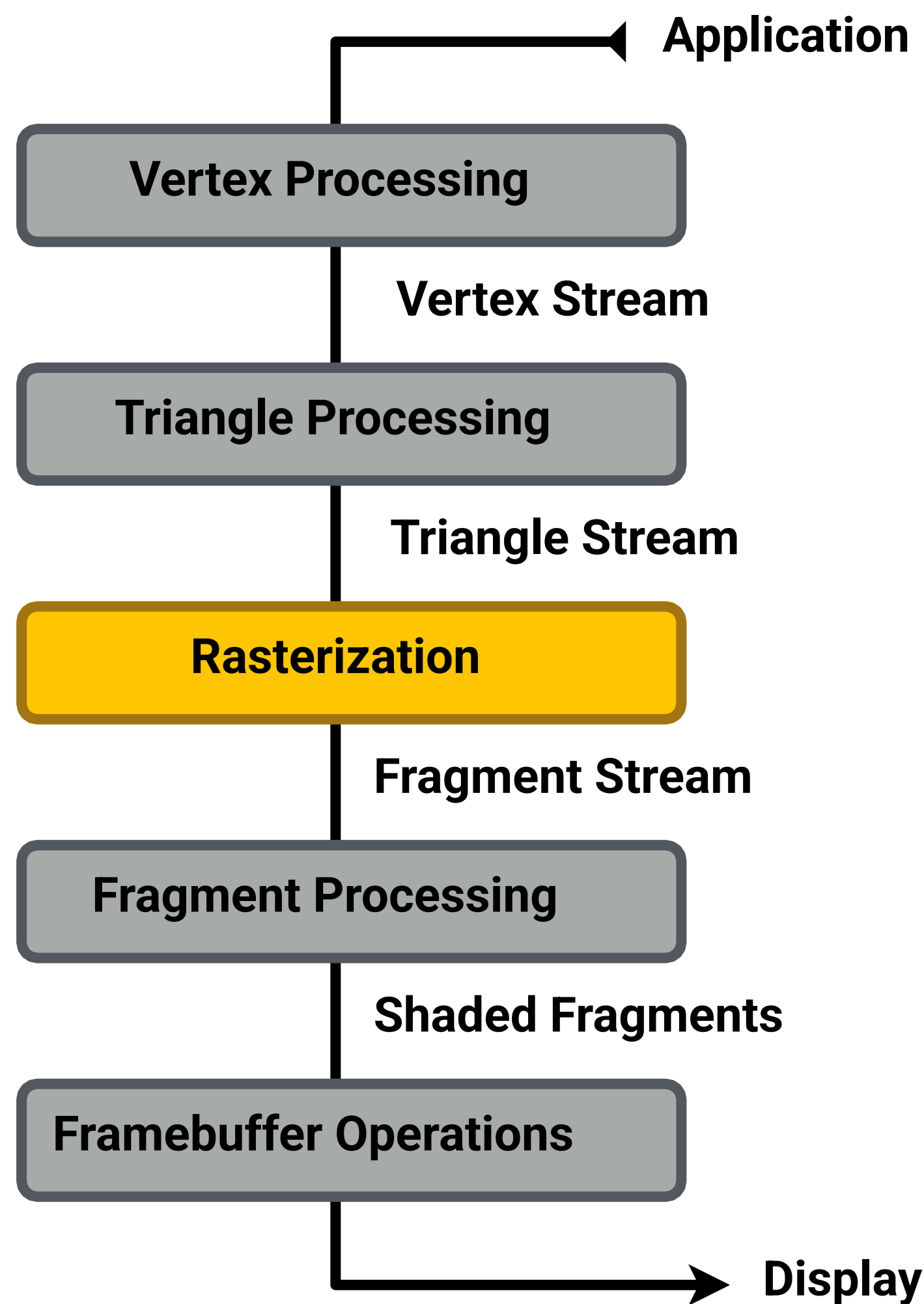
# Rasterization Pipeline



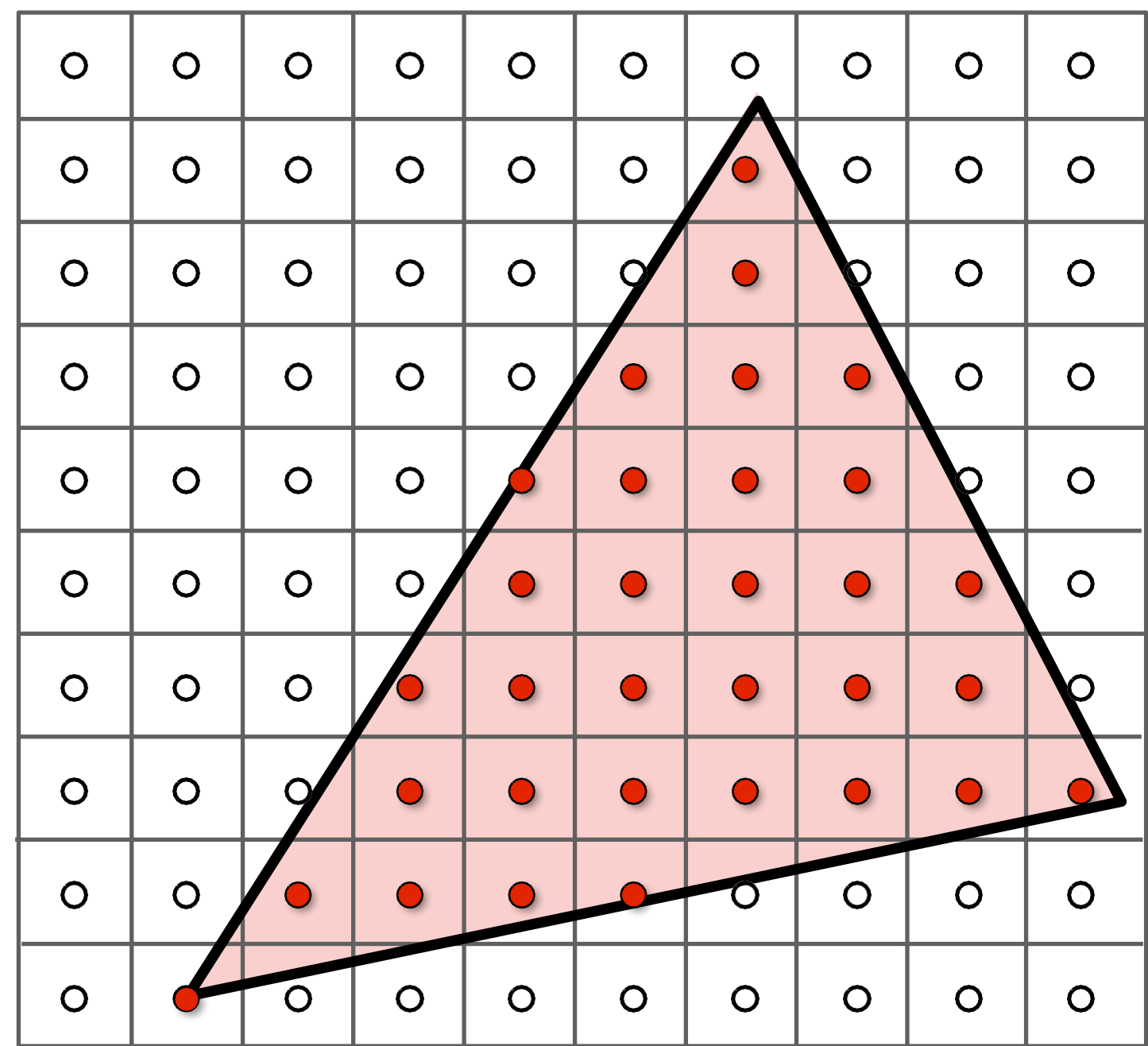
## Modeling & viewing transforms



# Rasterization Pipeline

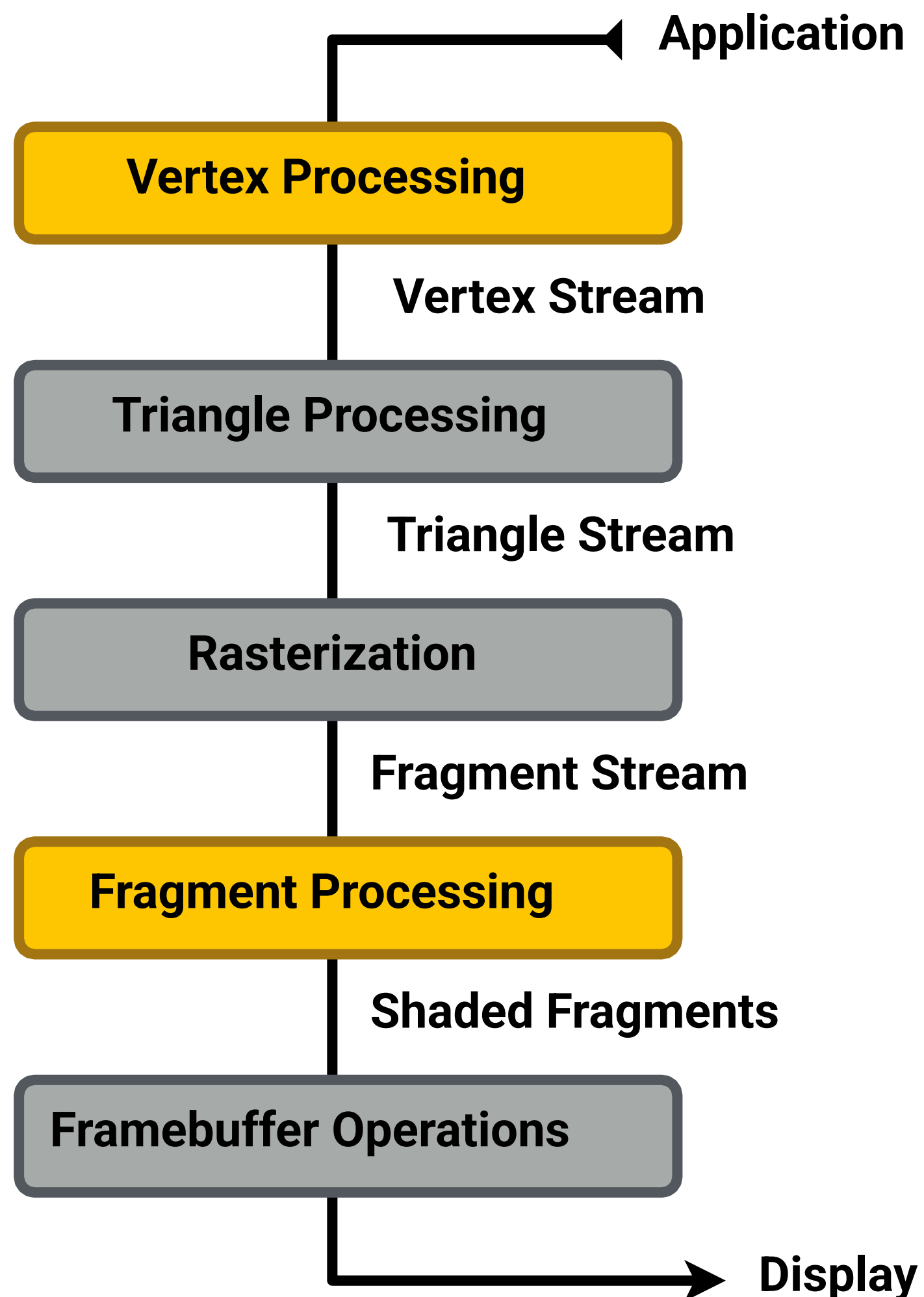


## Sampling triangle coverage

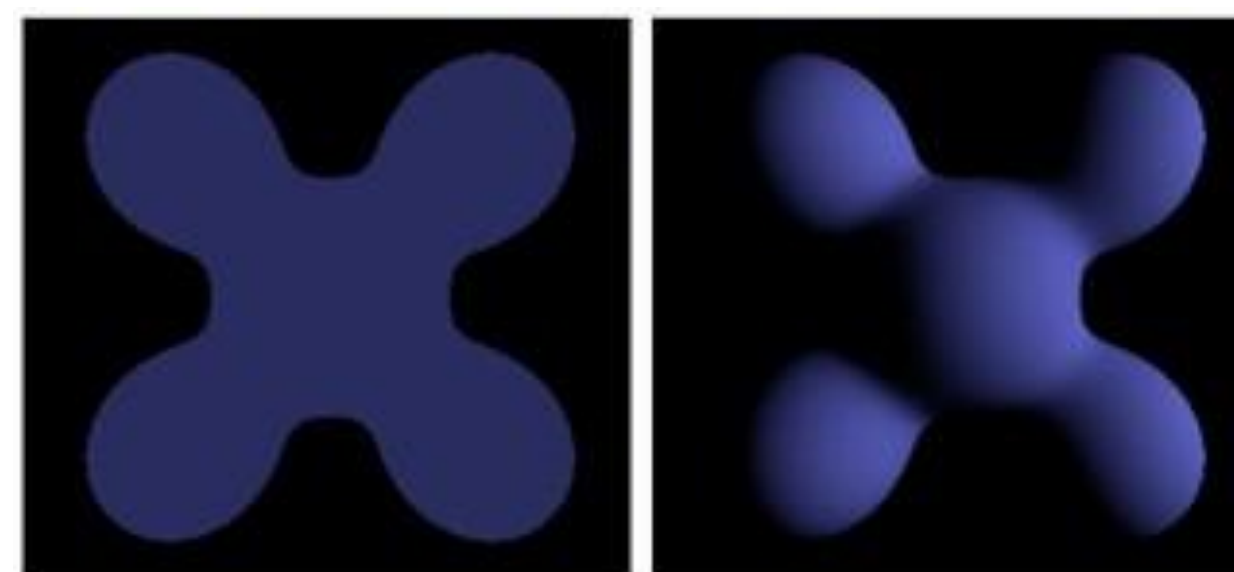




# Rasterization Pipeline

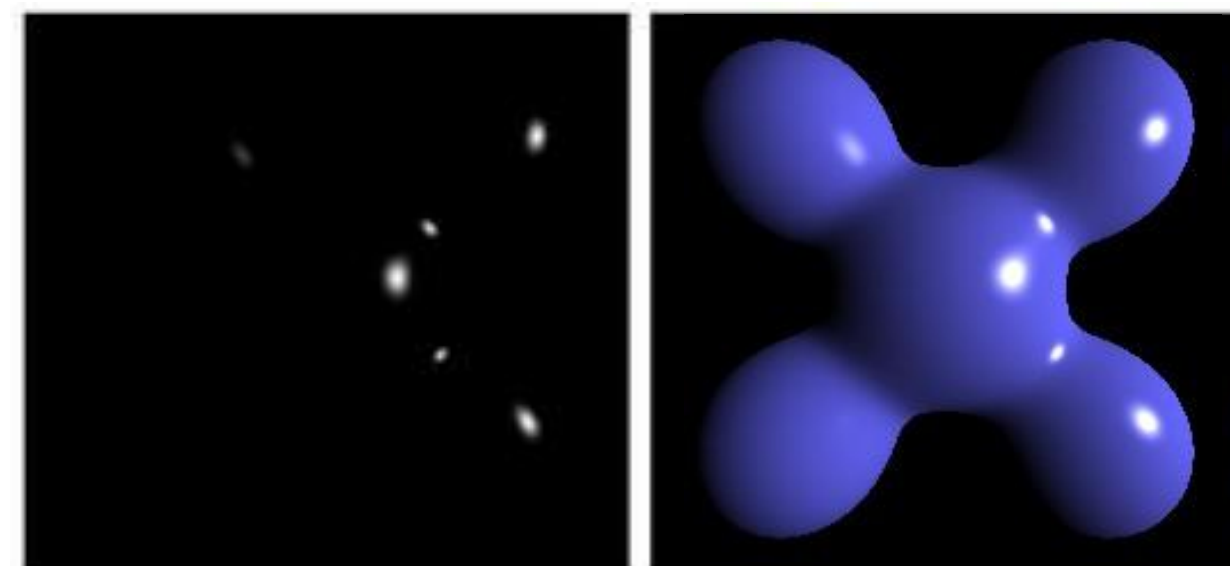


## Evaluating shading functions



Ambient +

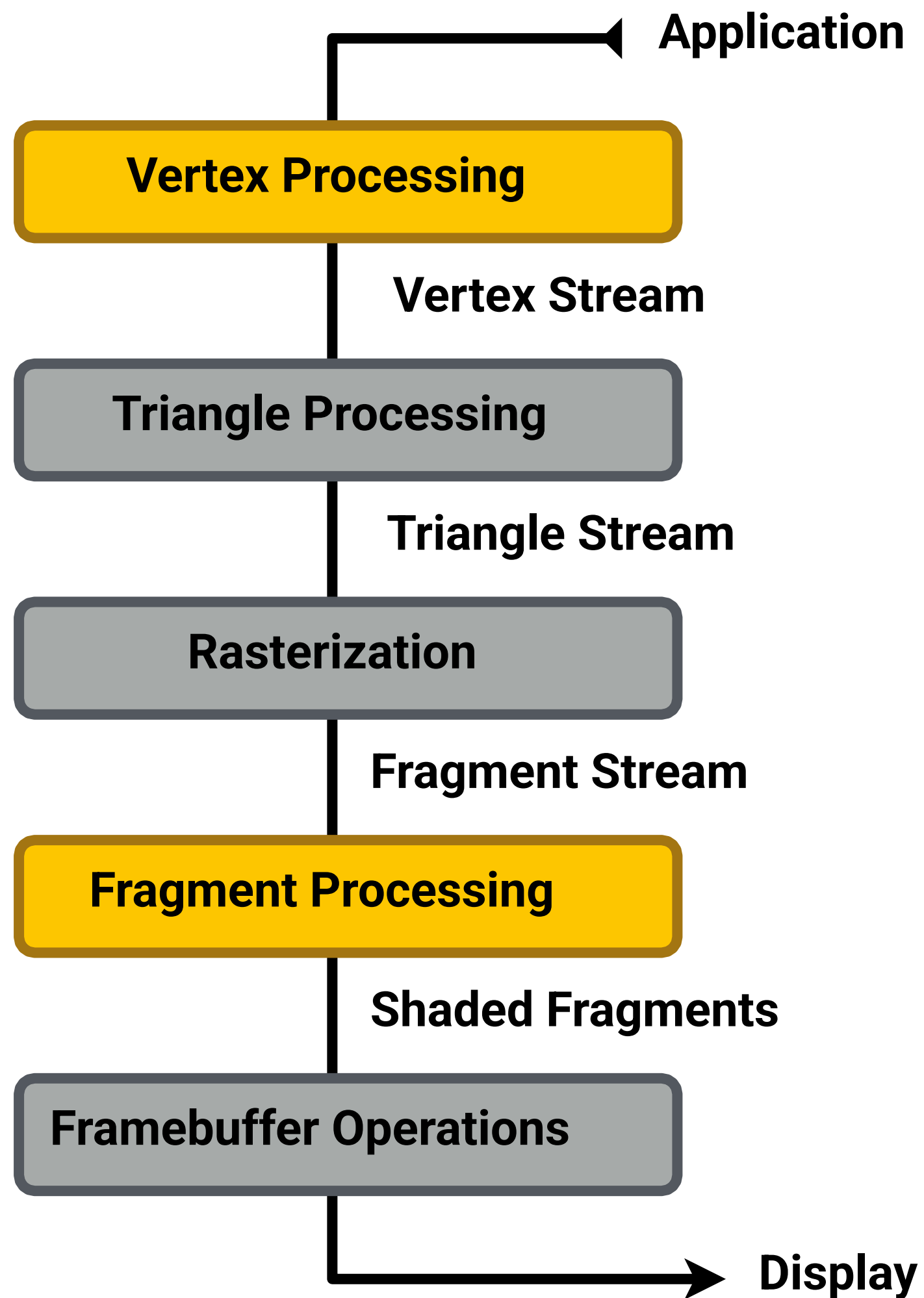
Diffuse



+ Specular

= Phong Reflection

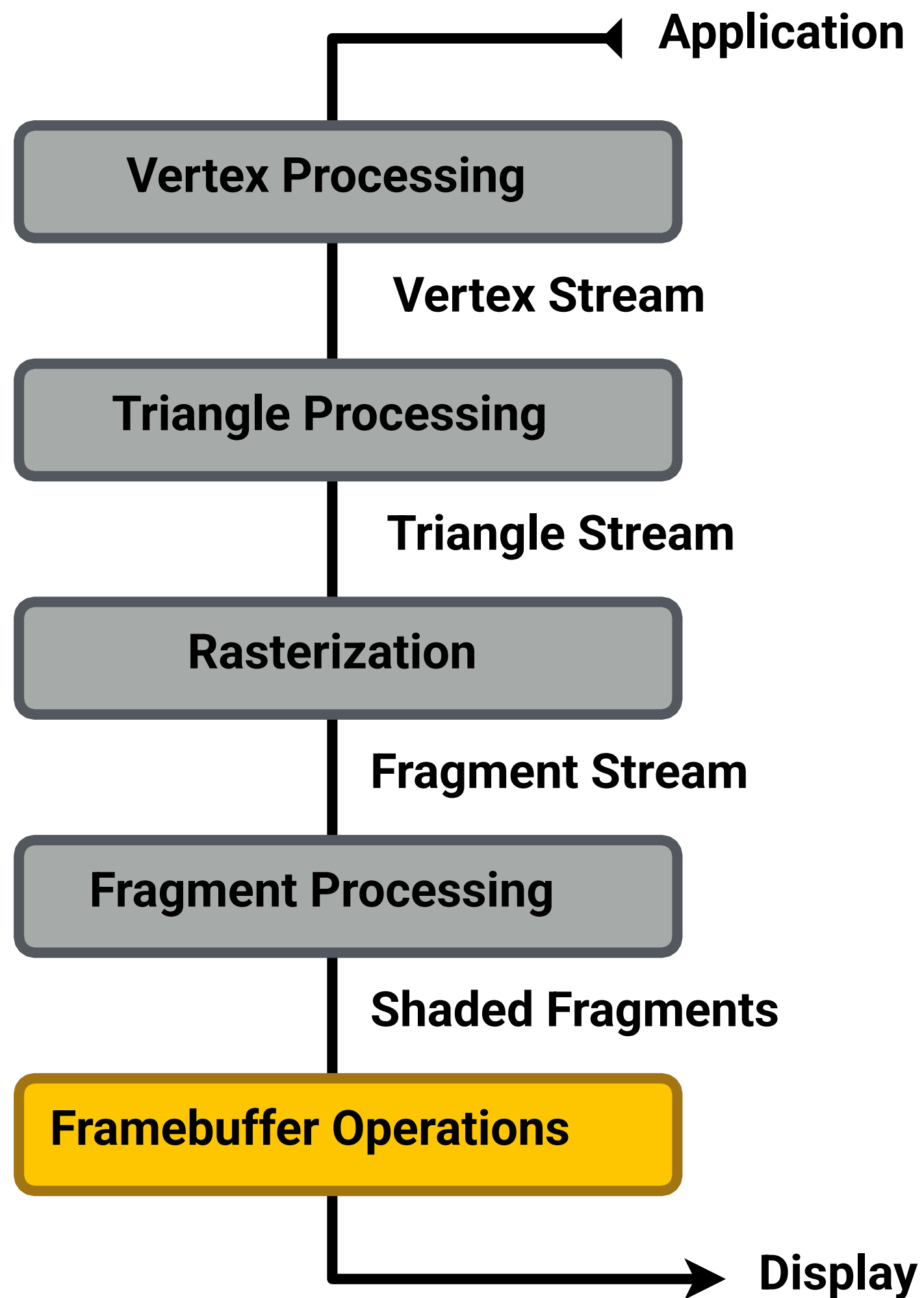
# Rasterization Pipeline



**Texture mapping**



# Rasterization Pipeline



## Z-Buffer Visibility Tests





# Shader Programs

- Program vertex and fragment processing stages
- Describe operation on a single vertex (or fragment)

## Example GLSL fragment shader program

```
uniform sampler2D myTexture;  
uniform vec3 lightDir;  
varying vec2 uv;  
varying vec3 norm;  
  
void diffuseShader()  
{  
  
    vec3 kd;  
  
    kd = texture2d(myTexture, uv);  
    kd *= clamp(dot(-lightDir, norm), 0.0, 1.0);  
    gl_FragColor = vec4(kd, 1.0);  
}
```

- Shader function executes **once per fragment**.
- **Outputs color** of surface at the current fragment's screen sample position.
- This shader performs a **texture lookup** to obtain the surface's material color at this point, then performs a **diffuse lighting calculation**.

# Shader Programs

- Program vertex and fragment processing stages
- Describe operation on a single vertex (or fragment)

## Example GLSL fragment shader program

```
uniform sampler2D myTexture; // program parameter
uniform vec3 lightDir;      // program parameter
varying vec2 uv;           // per fragment value (interp. by rasterizer)
varying vec3 norm;         // per fragment value (interp. by rasterizer)

void diffuseShader()
{
    vec3 kd;
    kd = texture2d(myTexture, uv); // material color from texture
    kd *= clamp(dot(-lightDir, norm), 0.0, 1.0); // Lambertian shading model
    gl_FragColor = vec4(kd, 1.0); // output fragment color
}
```

# Things to Remember

## Visibility

- Painter's algorithm and Z-Buffer algorithm

## Simple Shading Model

- Key geometry: lighting, viewing & normal vectors
- Ambient, diffuse & specular reflection functions
- Shading frequency: triangle, vertex or fragment

## Graphics Rasterization Pipeline

- Where do transforms, rasterization, shading, texturing and visibility computations occur?
- GPU = parallel processor implementing graphics pipeline



# Acknowledgments

**Thanks to Steve Marschner, Mark Pauly,  
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Kanazawa for presentation resources.**