

Lecture 19:

Introduction to Color Science



Computer Graphics and Imaging

UC Berkeley CS184



**Color
defines our
visual
perception**



We Render for the human observer







Johannes Vermeer *The Music Lesson*





Wassily Kandinsky, Color Study. Squares with Concentric Circles, 1913 Munich, The Städtische Galerie im Lenbachhaus



Mark Rothko
No. 61. Rust and Blue
1953,
Museum of Contemporary Art, Los Angeles







SIGN IN

Search...

SHOP NOW ▾

OUR TECHNOLOGY

REVIEWS

BLOG

HELP

 CART

Discover What Color Feels Like

Bring greater vibrancy and color to your world with EnChroma high-performance glasses for color blindness.

SHOP NOW

Color-Blind Reactions to Perceiving New Colors



Simulation of Color Blind Perception ***(Color Vision Deficiency)***



Normal







Simulation of Color Blind Perception



Normal



Protan



Deutan



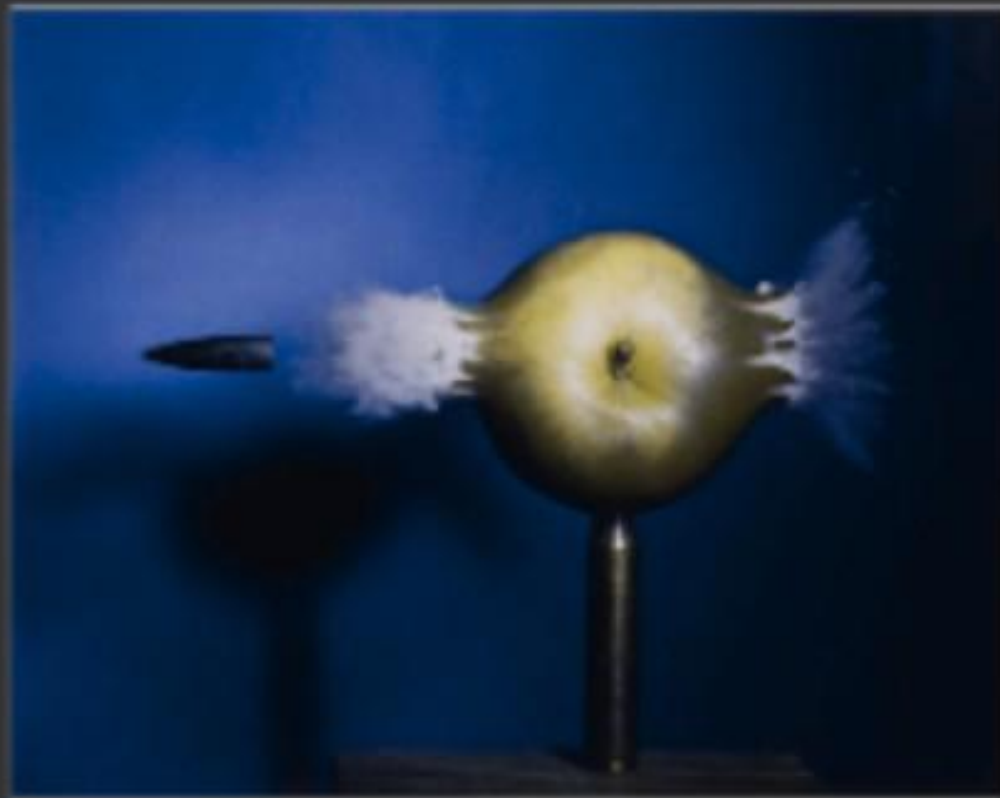
Tritan

Color is Core to Our Human Visual Sense



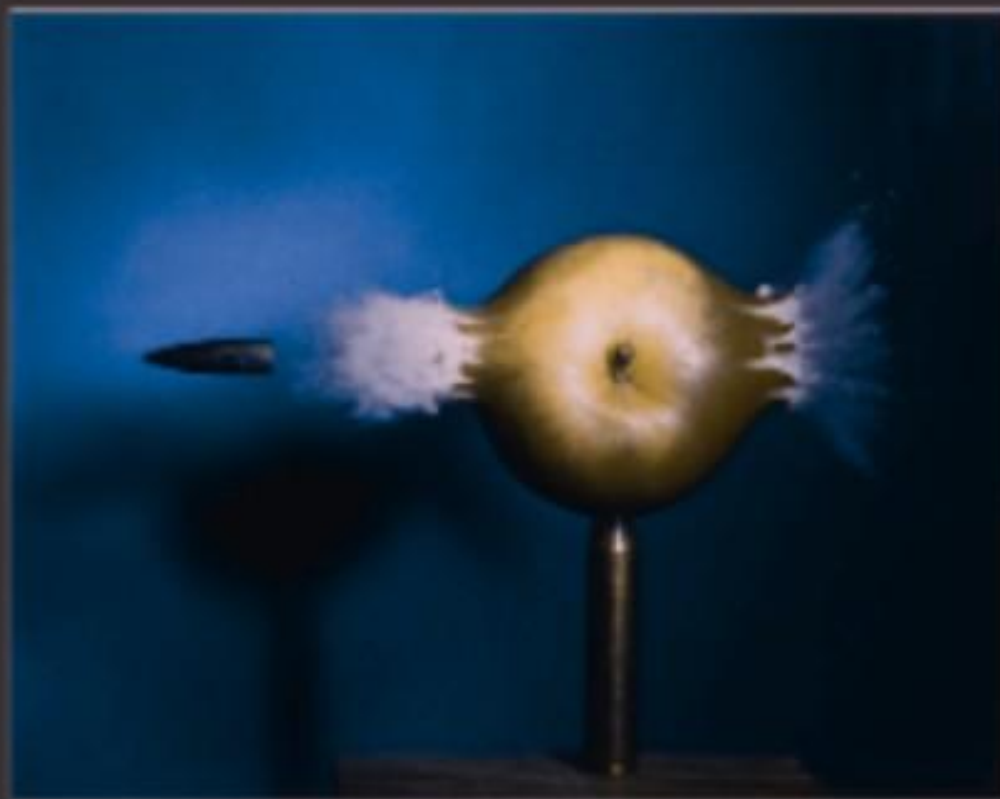
Steve McCurry | Reza | Walter looss | Steve McCurry
Harold Edgerton | NASA | National Geographic

Color is Core to Our Human Visual Sense



Steve McCurry | Reza | Walter Iooss | Steve McCurry
Harold Edgerton | NASA | National Geographic

Color is Core to Our Human Visual Sense



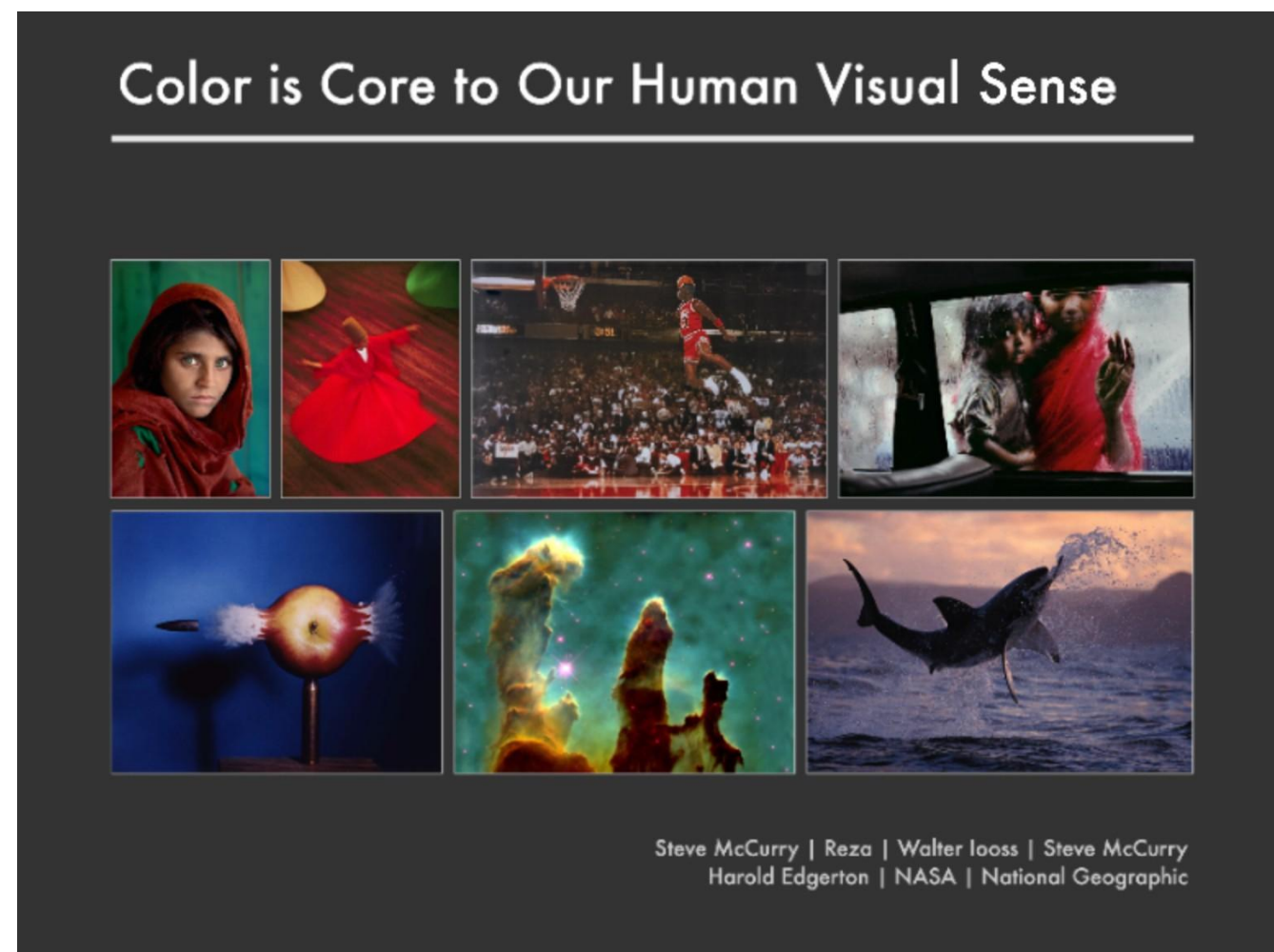
Steve McCurry | Reza | Walter looss | Steve McCurry
Harold Edgerton | NASA | National Geographic

Color is Core to Our Human Visual Sense

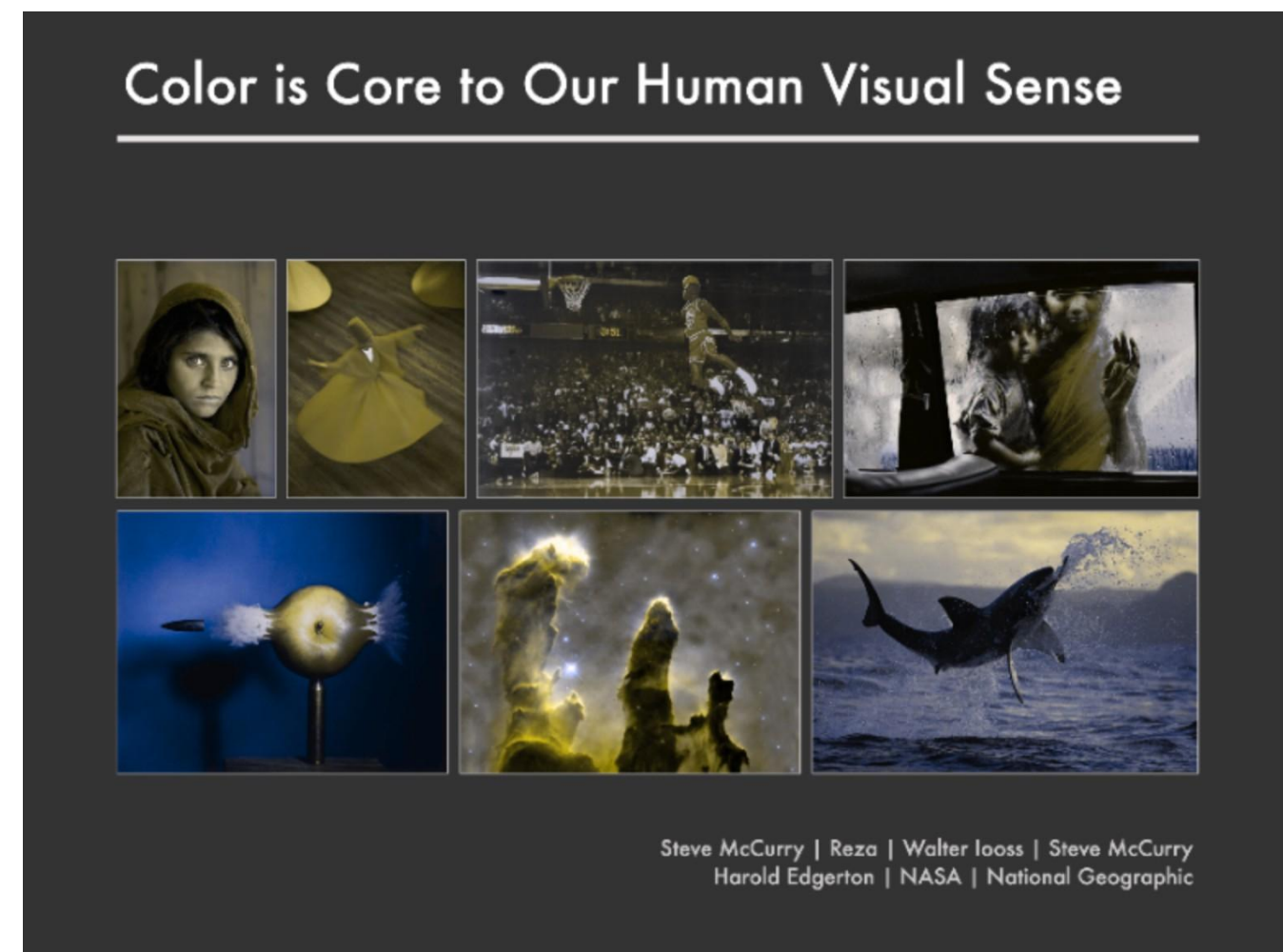


Steve McCurry | Reza | Walter looss | Steve McCurry
Harold Edgerton | NASA | National Geographic

Simulation of Color Blind Perception



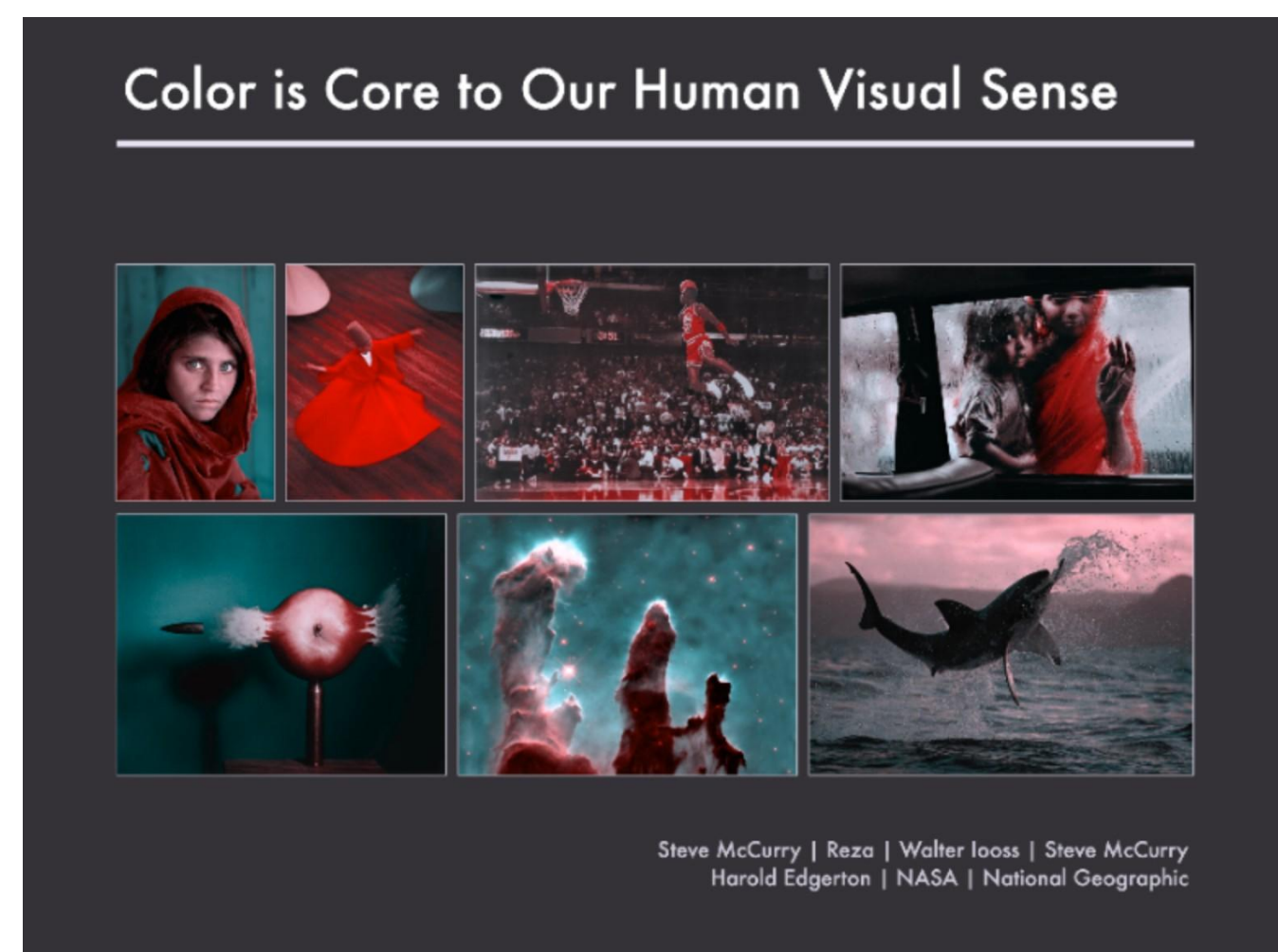
Normal



Protan



Deutan Tritan



Chromatic Adaptation

A Person With One Trichromatic Eye and One Deuteranopic Eye

Graham and Hsia, 1959.
"A unilaterally dichromatic subject".

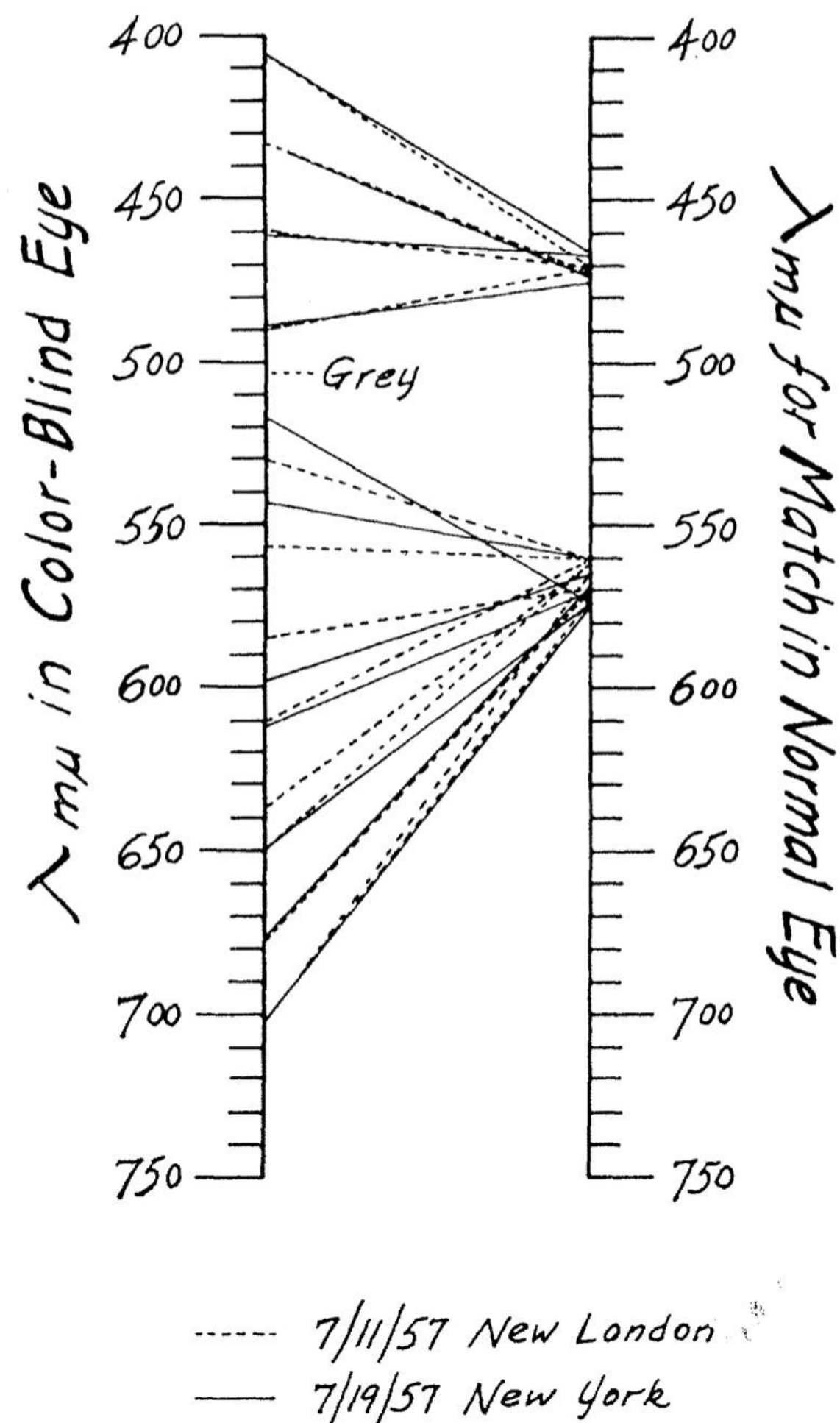


FIG. 2.—Results of the experiment on binocular matching

Studying Chromatic Adaptation



Slide credit: Mark Fairchild



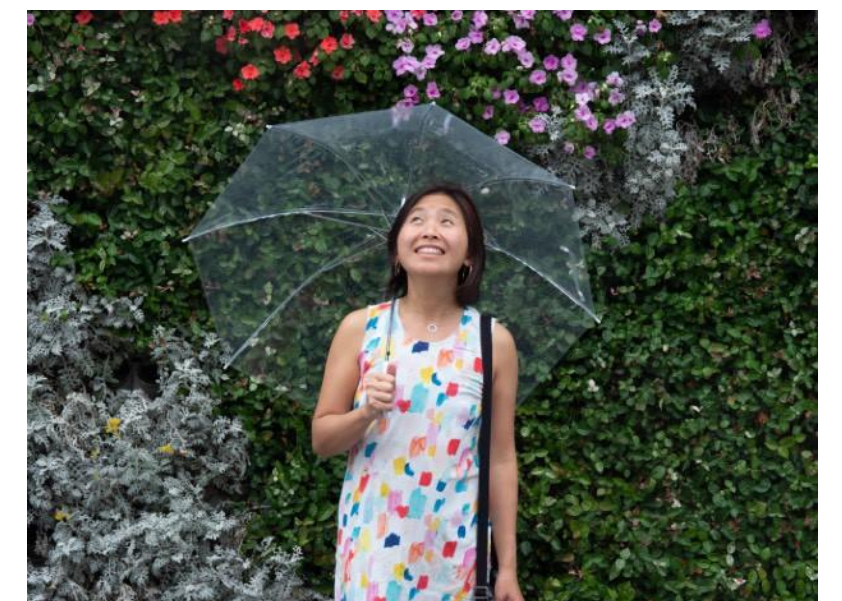
Slide credit: Mark Fairchild



Slide credit: Mark
Fairchild

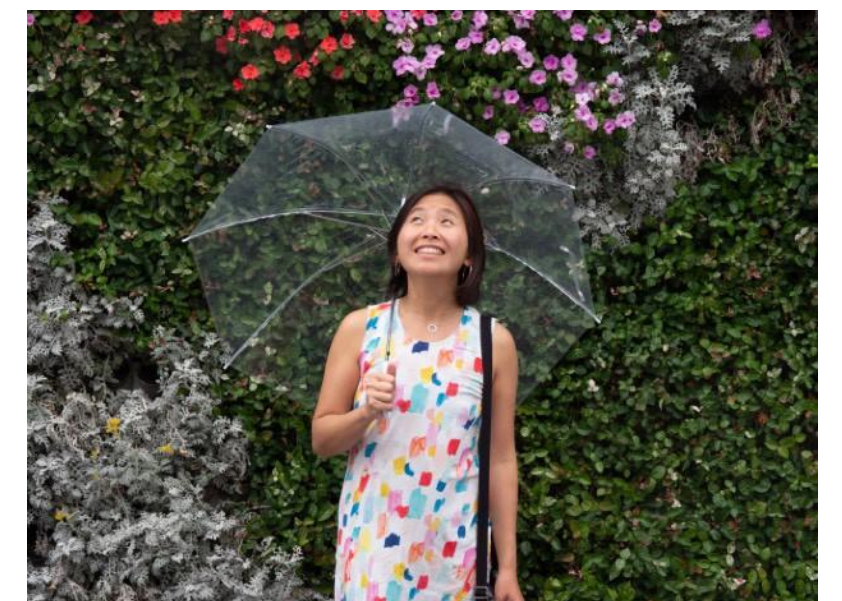


Automatic White Balance - Examples



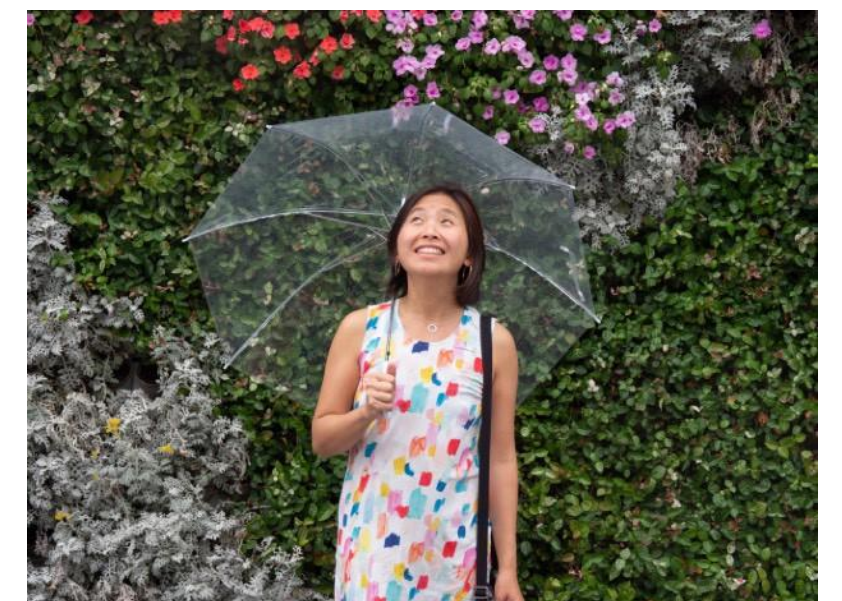
No white balance (all processed as “daylight”)

Automatic White Balance - Examples



Automatic white balance applied (Lightroom implementation)

Automatic White Balance - Examples



AWB + light manual editing

Automatic White Balance

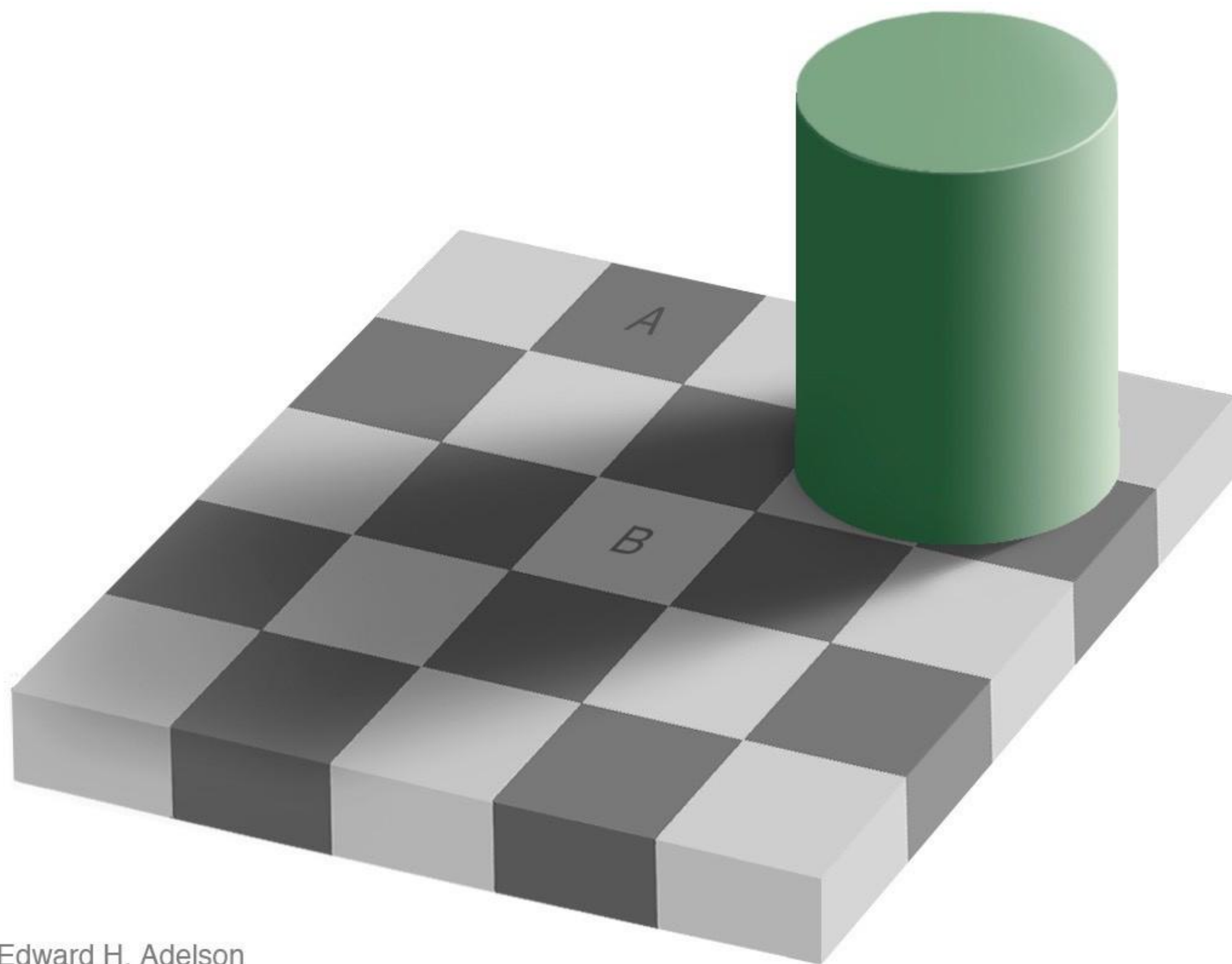
$$\begin{bmatrix} R \\ G \\ B \end{bmatrix} = \begin{bmatrix} \frac{1}{R'_W} & 0 & 0 \\ 0 & \frac{1}{G'_W} & 0 \\ 0 & 0 & \frac{1}{B'_W} \end{bmatrix} \begin{bmatrix} R' \\ G' \\ B' \end{bmatrix}$$

R, G, B - automatic white balanced output

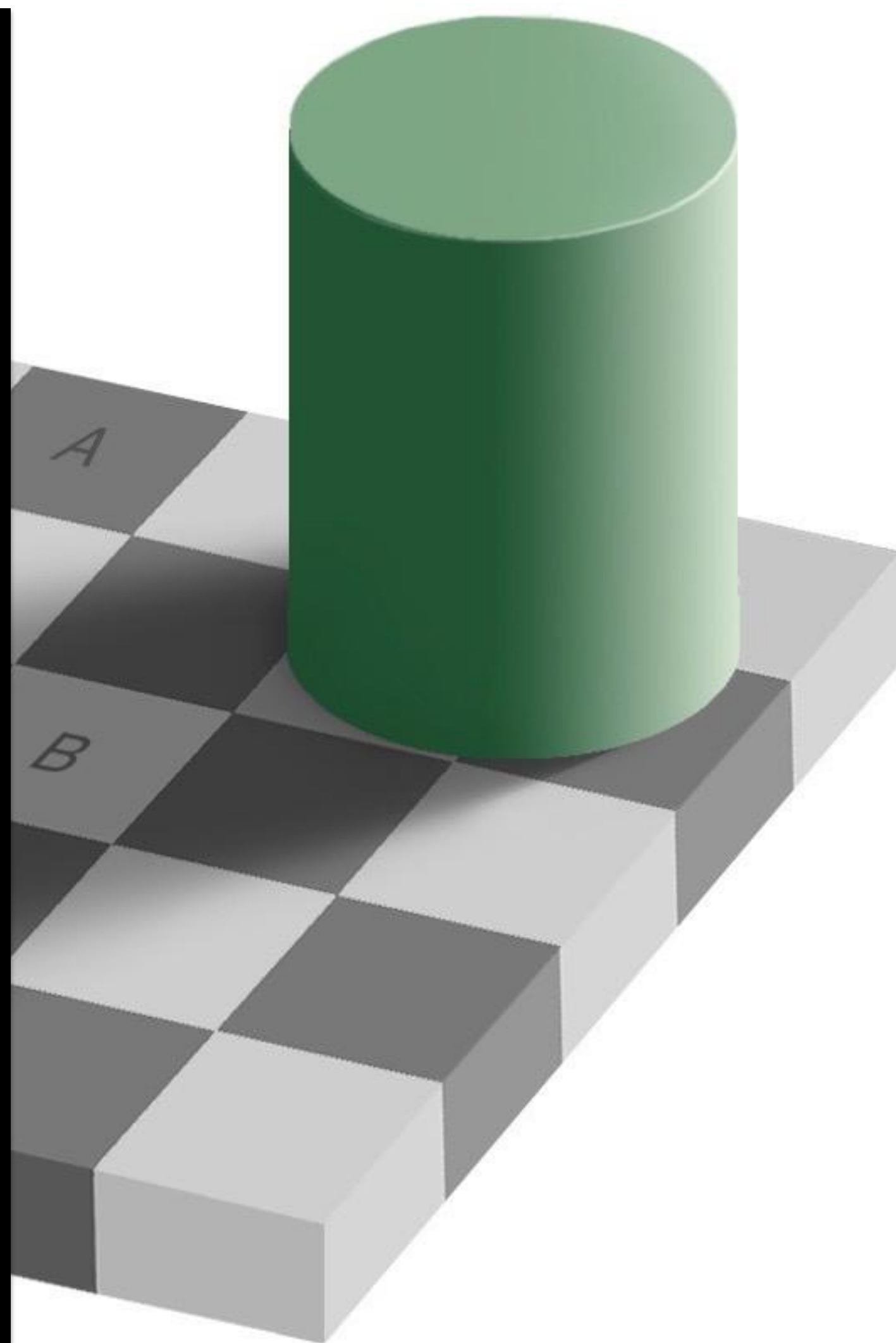
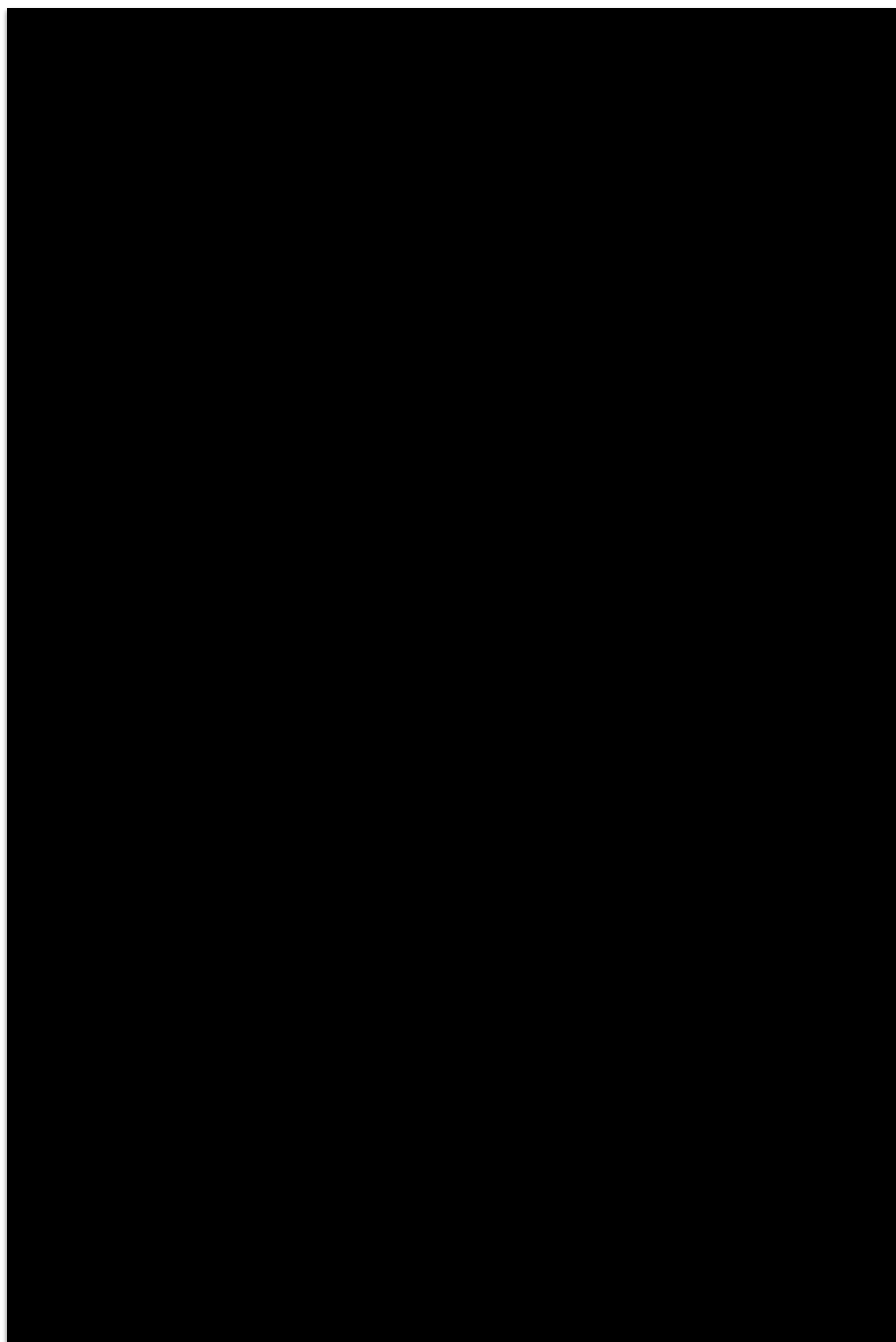
R'_W, G'_W, B'_W - raw input of white object

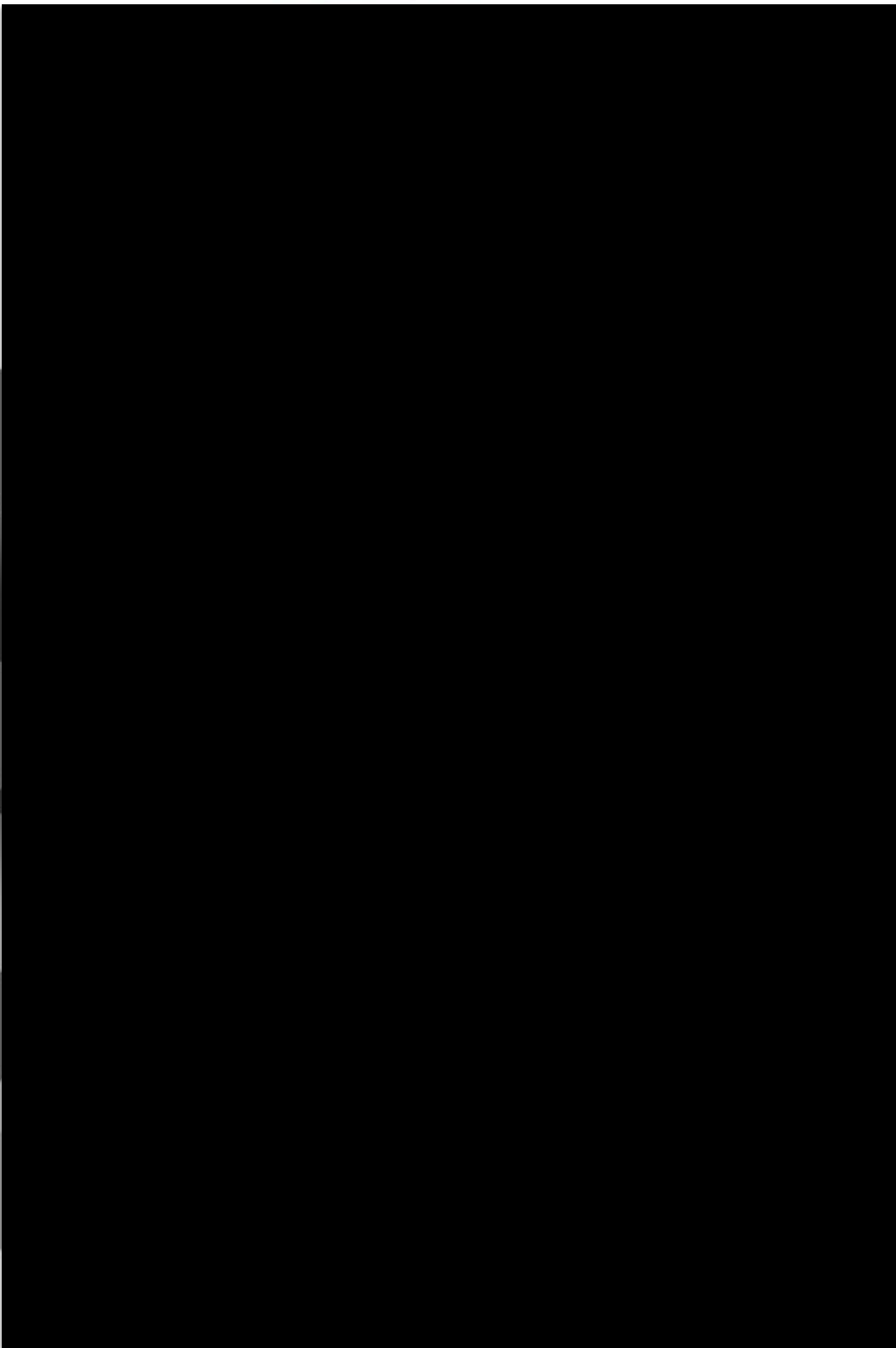
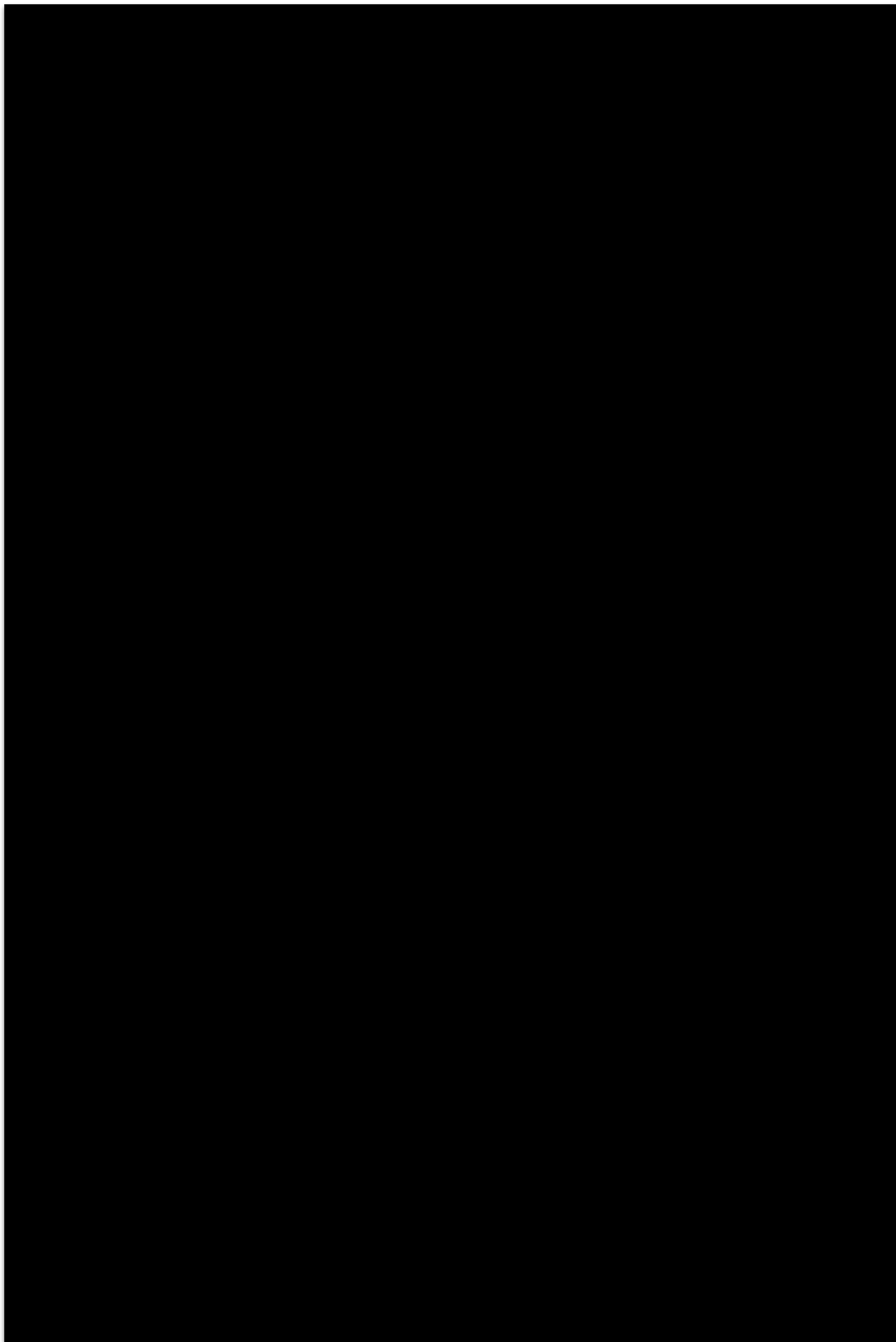
R', G', B' - raw input

**Color Perception is
Highly Adaptive**



Edward H. Adelson



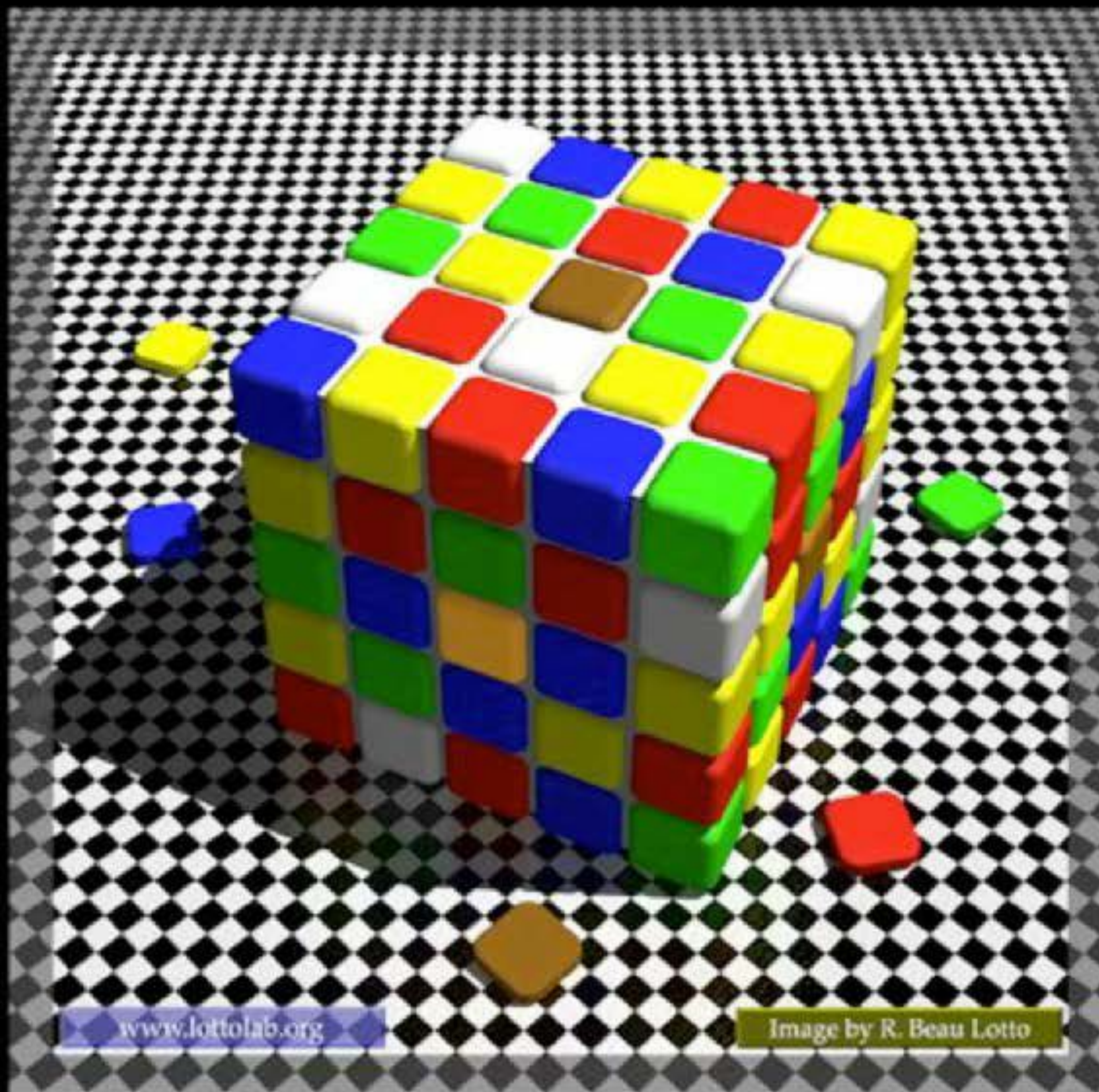






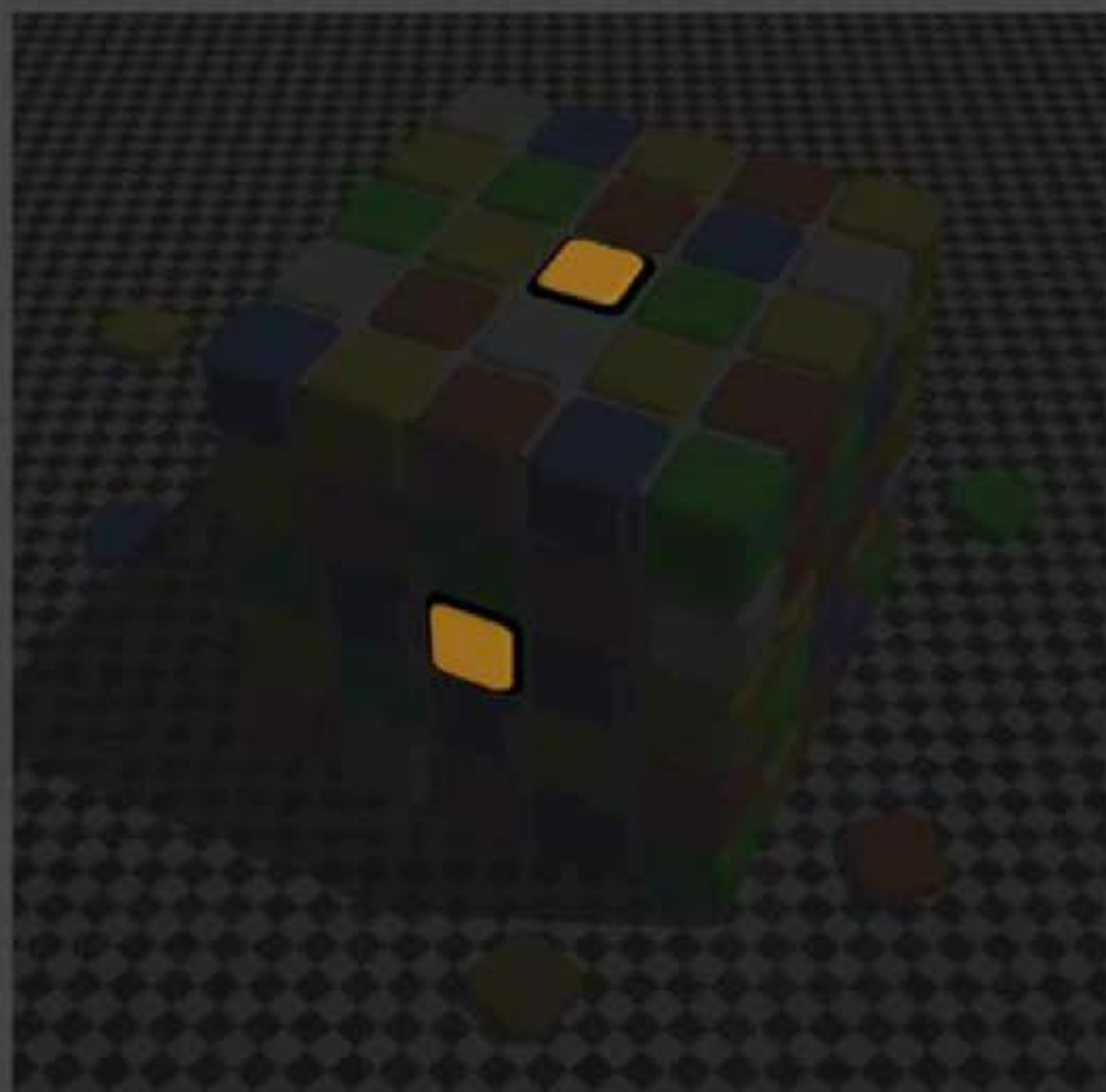
A

B

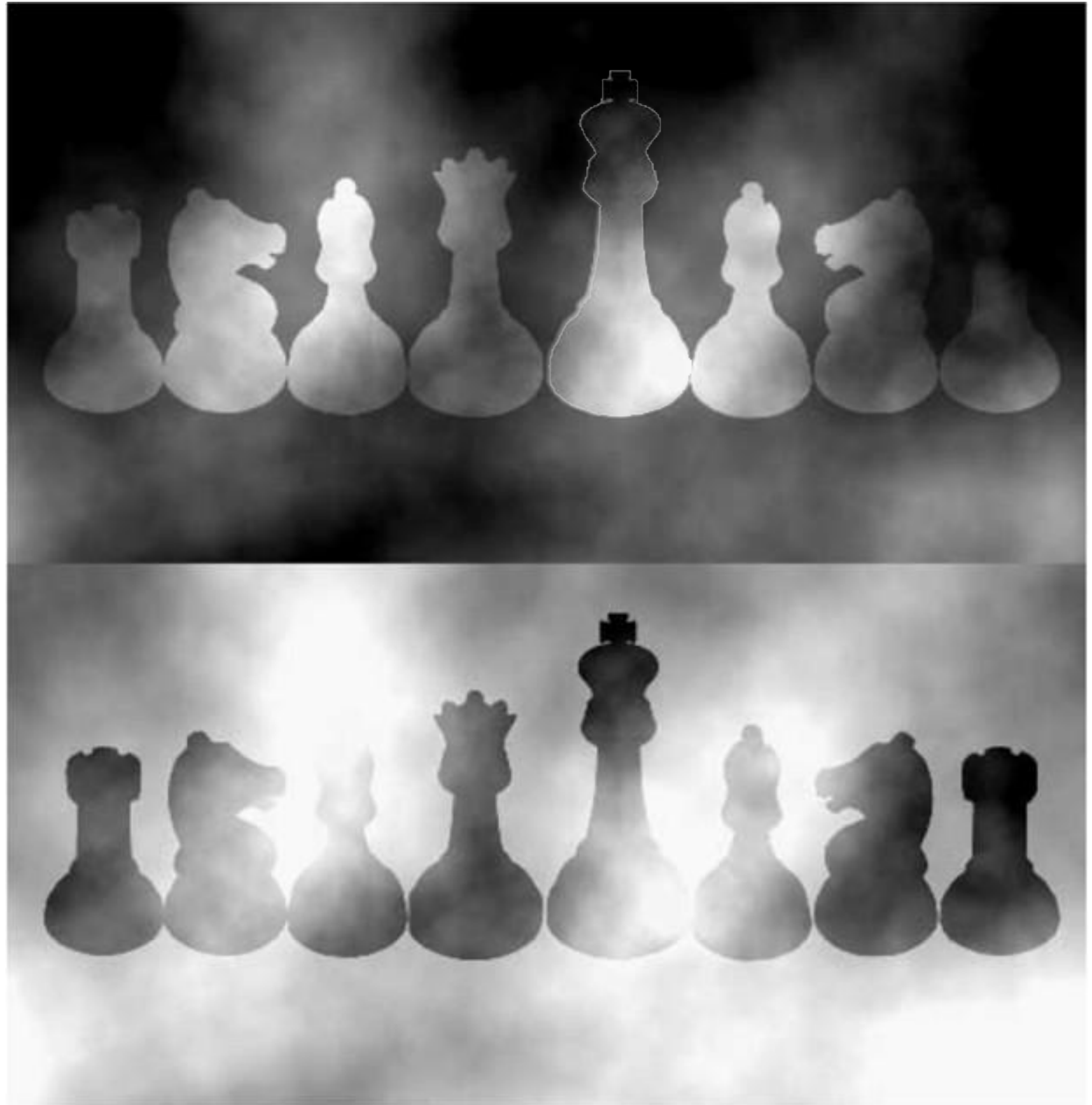


www.lottolab.org

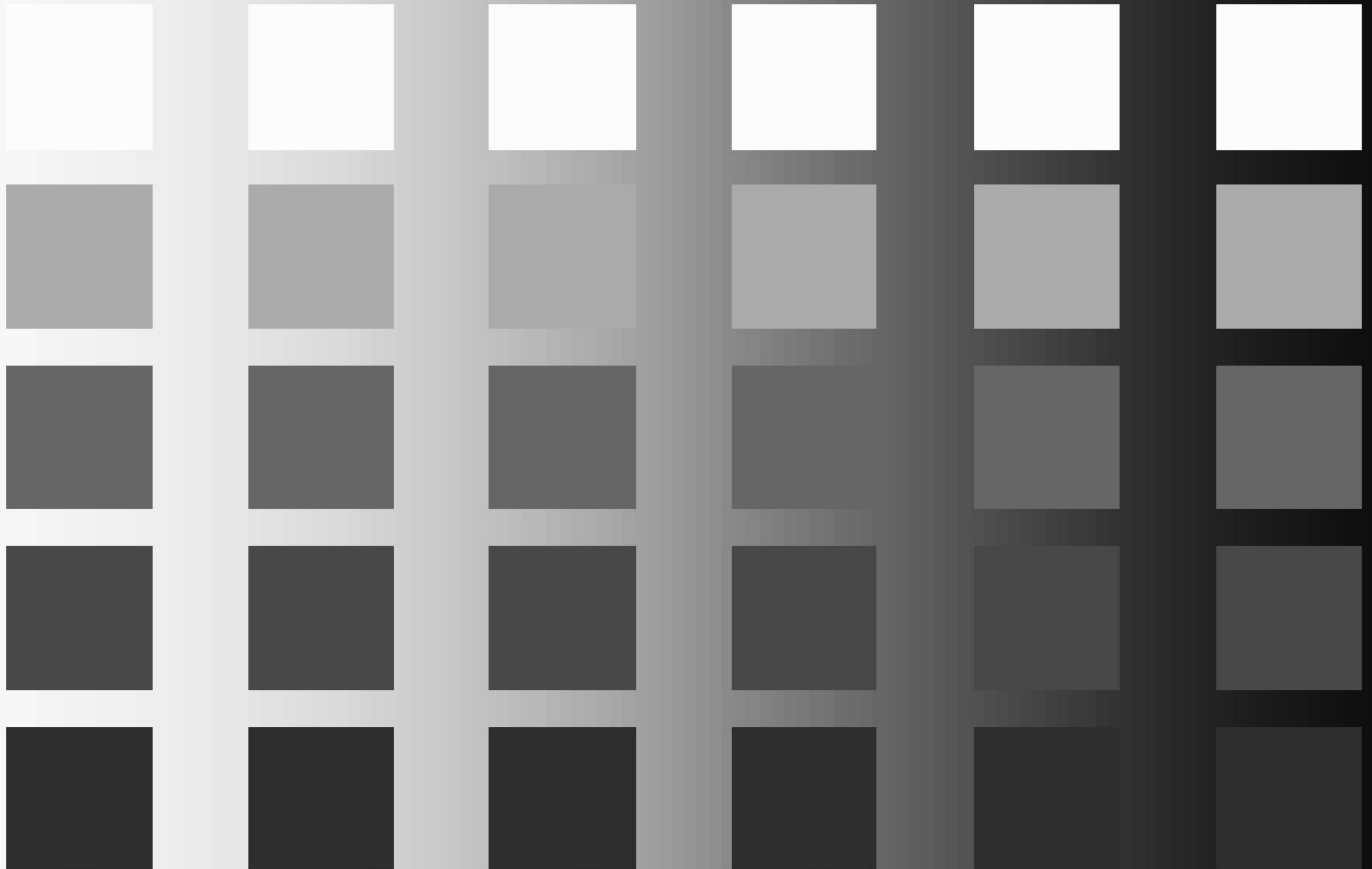
Image by R. Beau Lotto



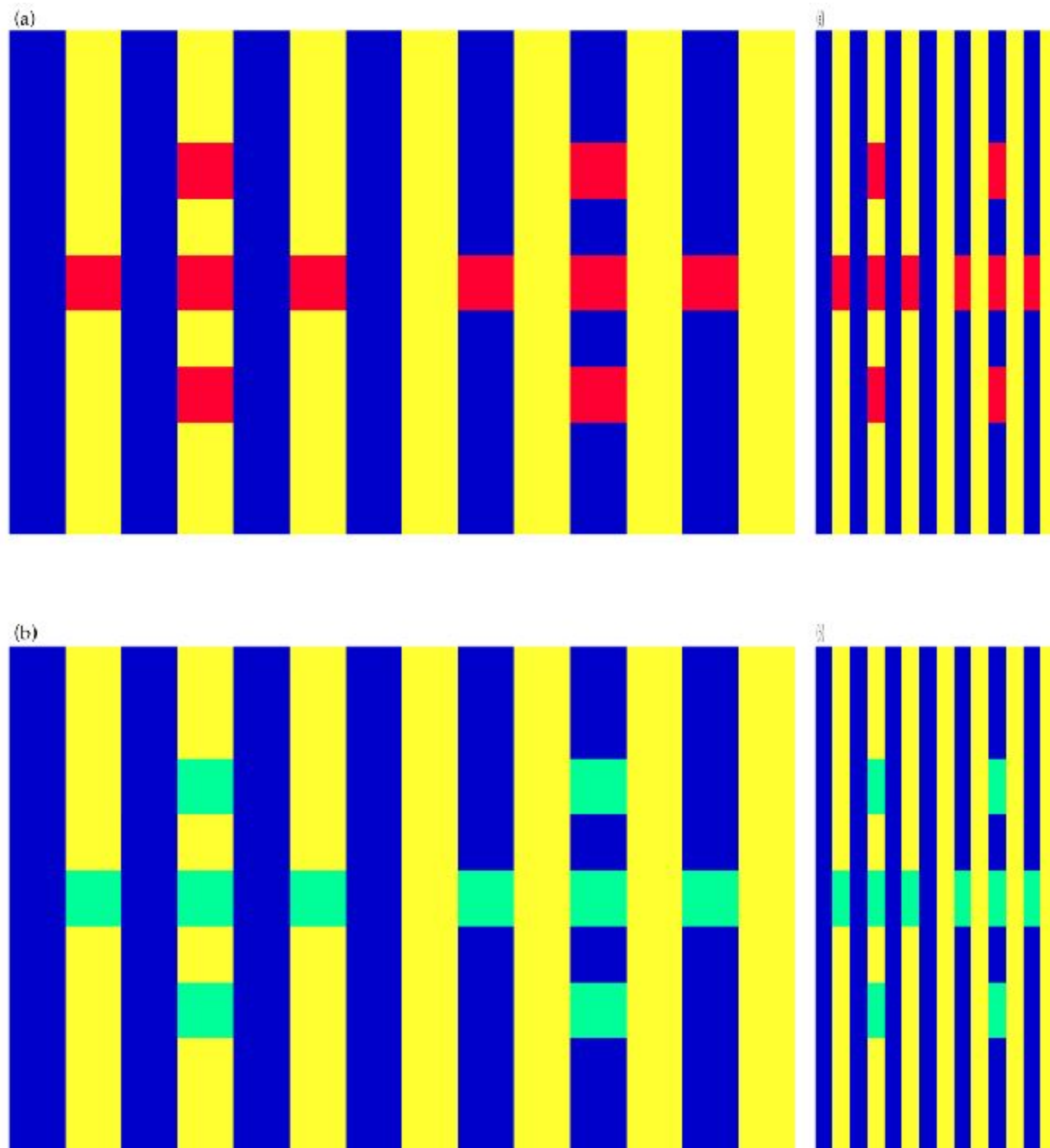
Even simple judgment,
such as lightness, depend
on brain processing
(Anderson and Winawer, Nature, 2005)



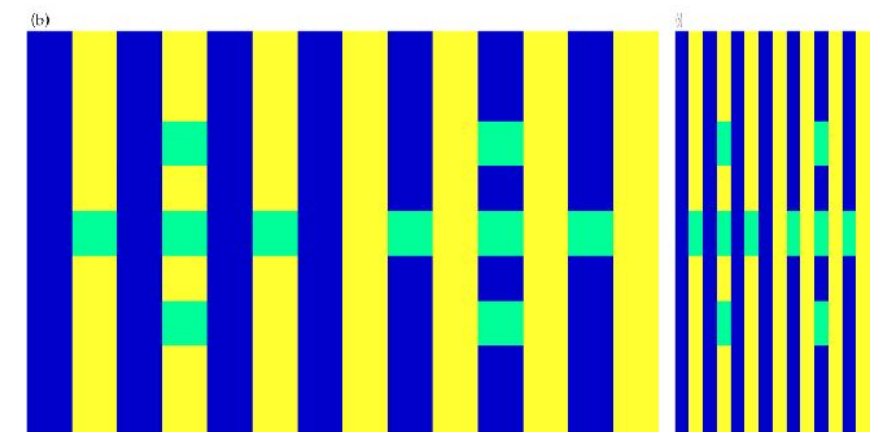
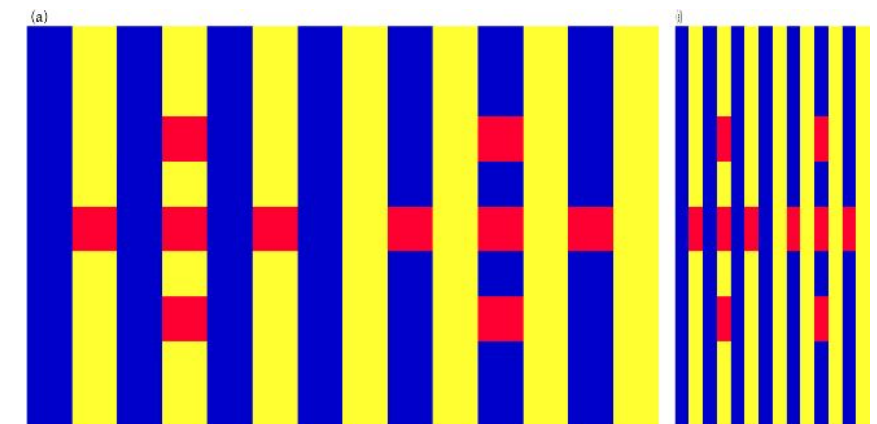
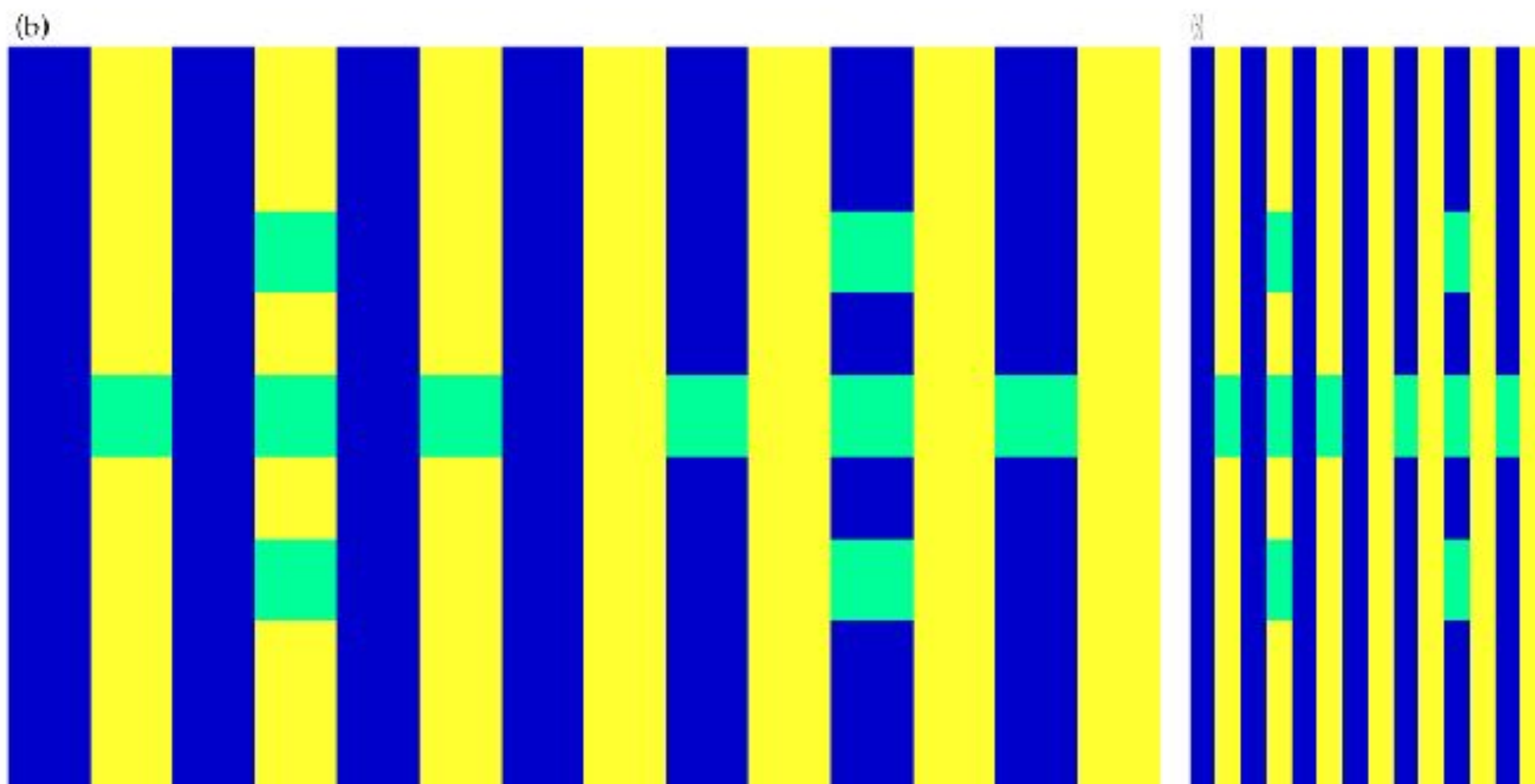
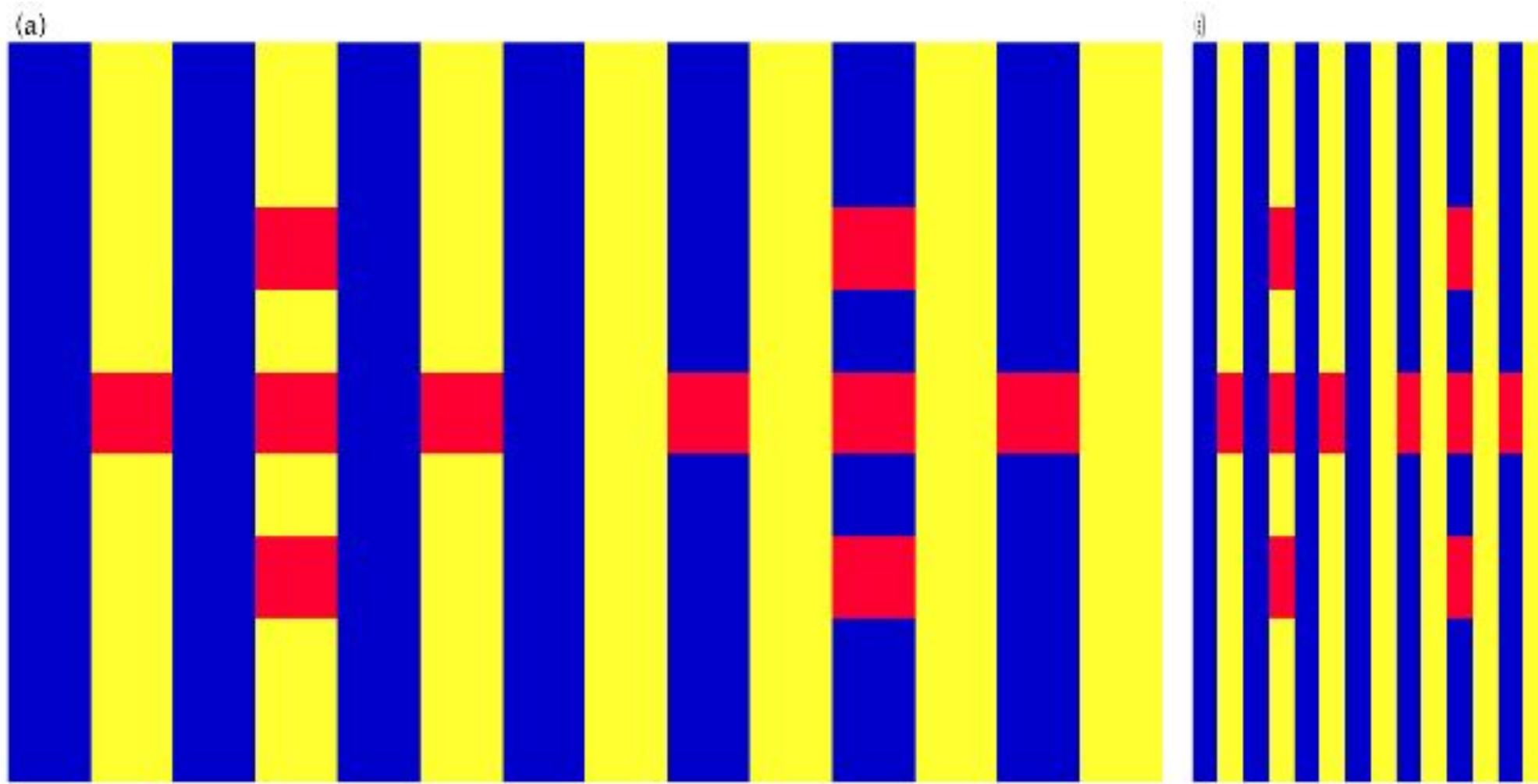
Simultaneous Contrast and Surround Effect



Surround Effects

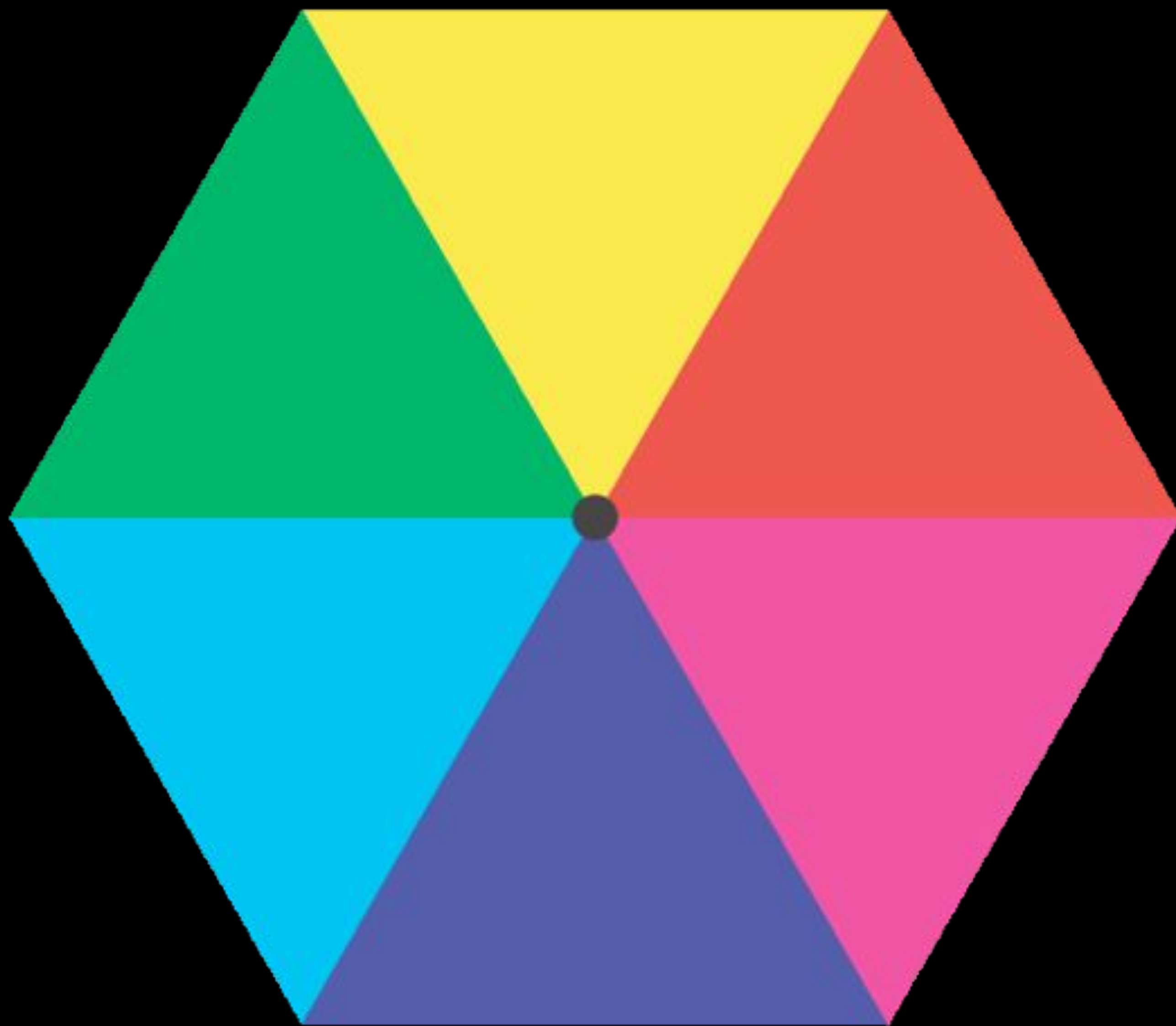


Surround Effects

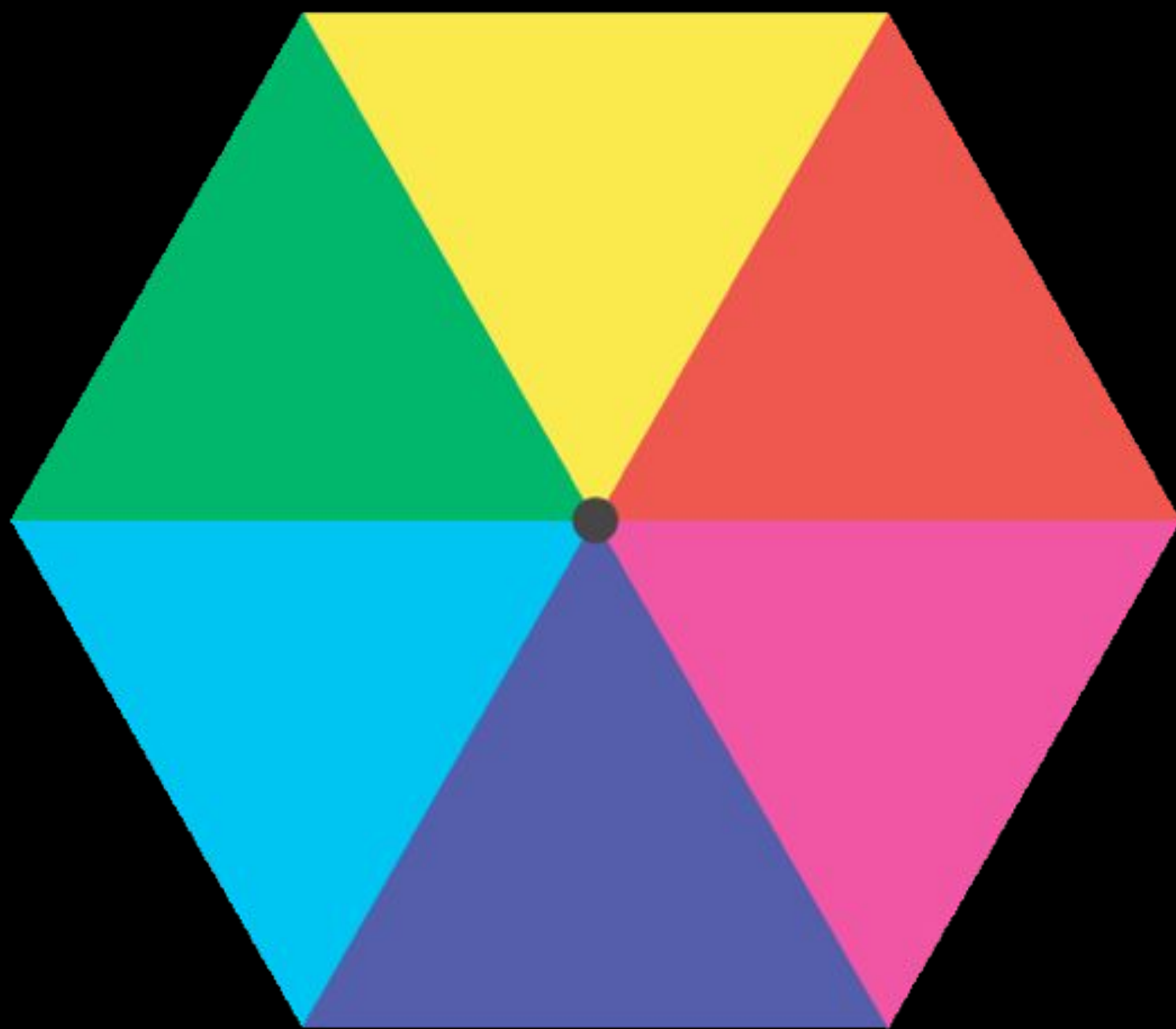


AfterImages:

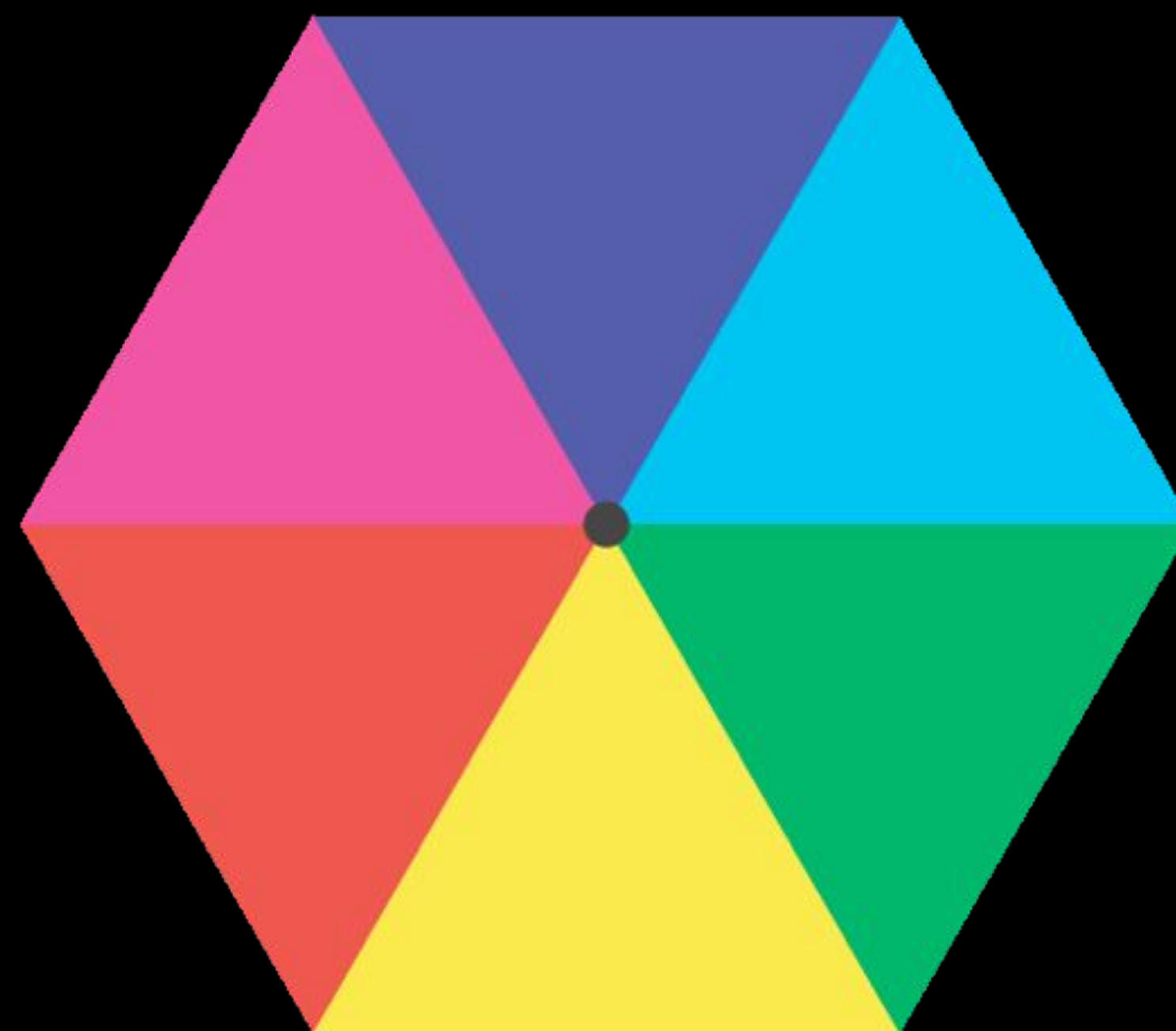
Perception Operates on “Opponent” Color Axes



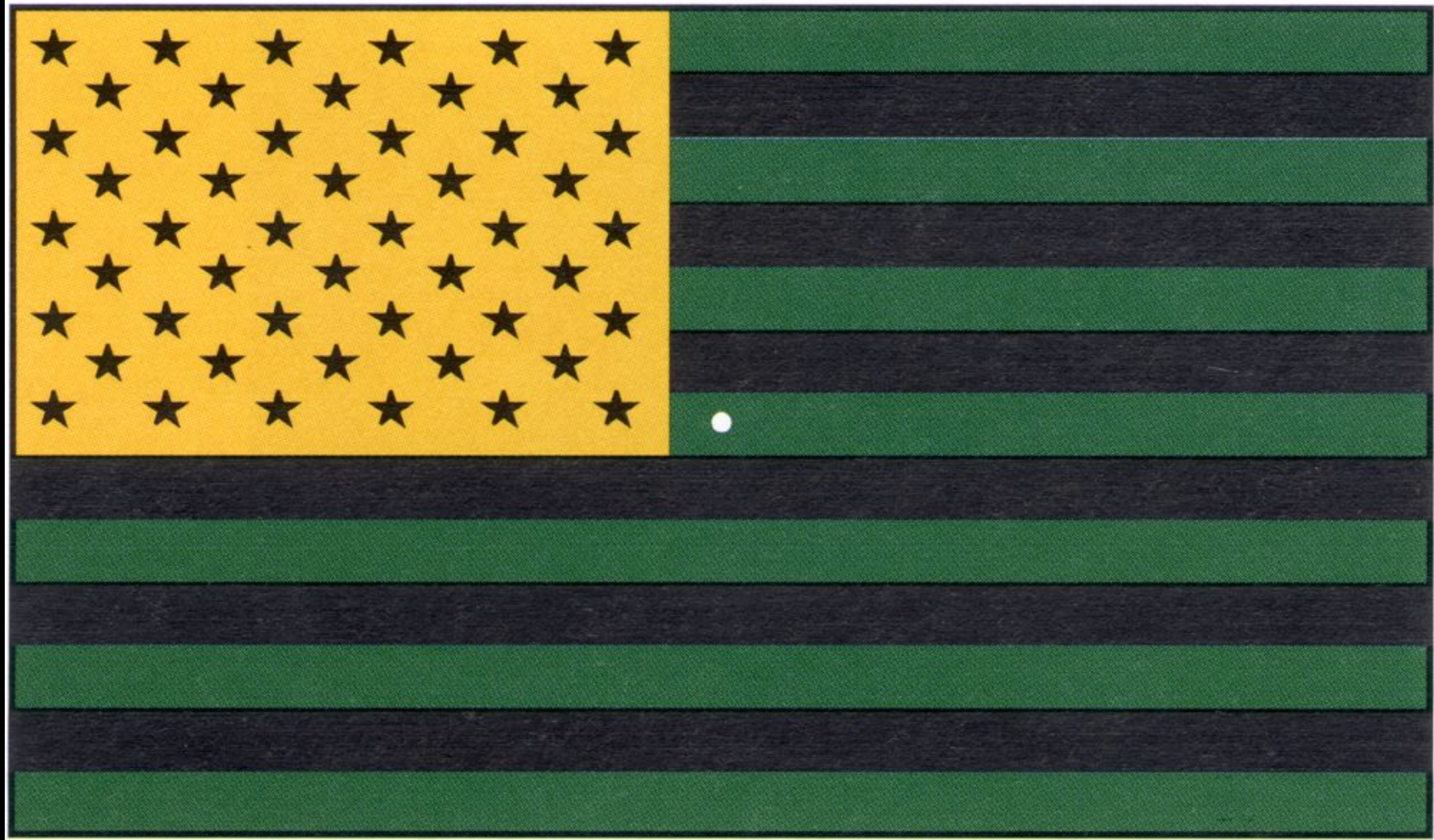




Image



Afterimage









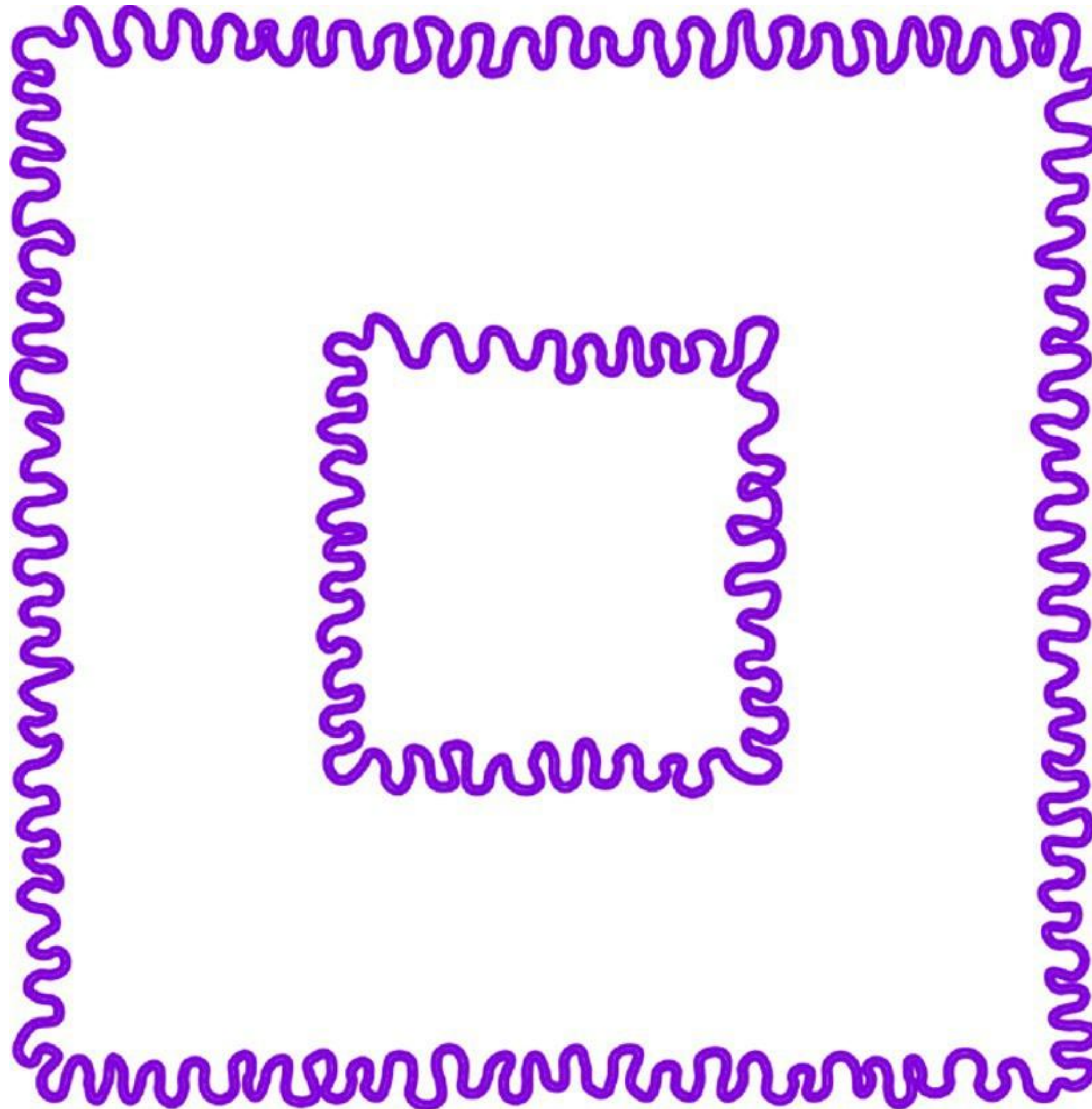
keep staring at the black dot.



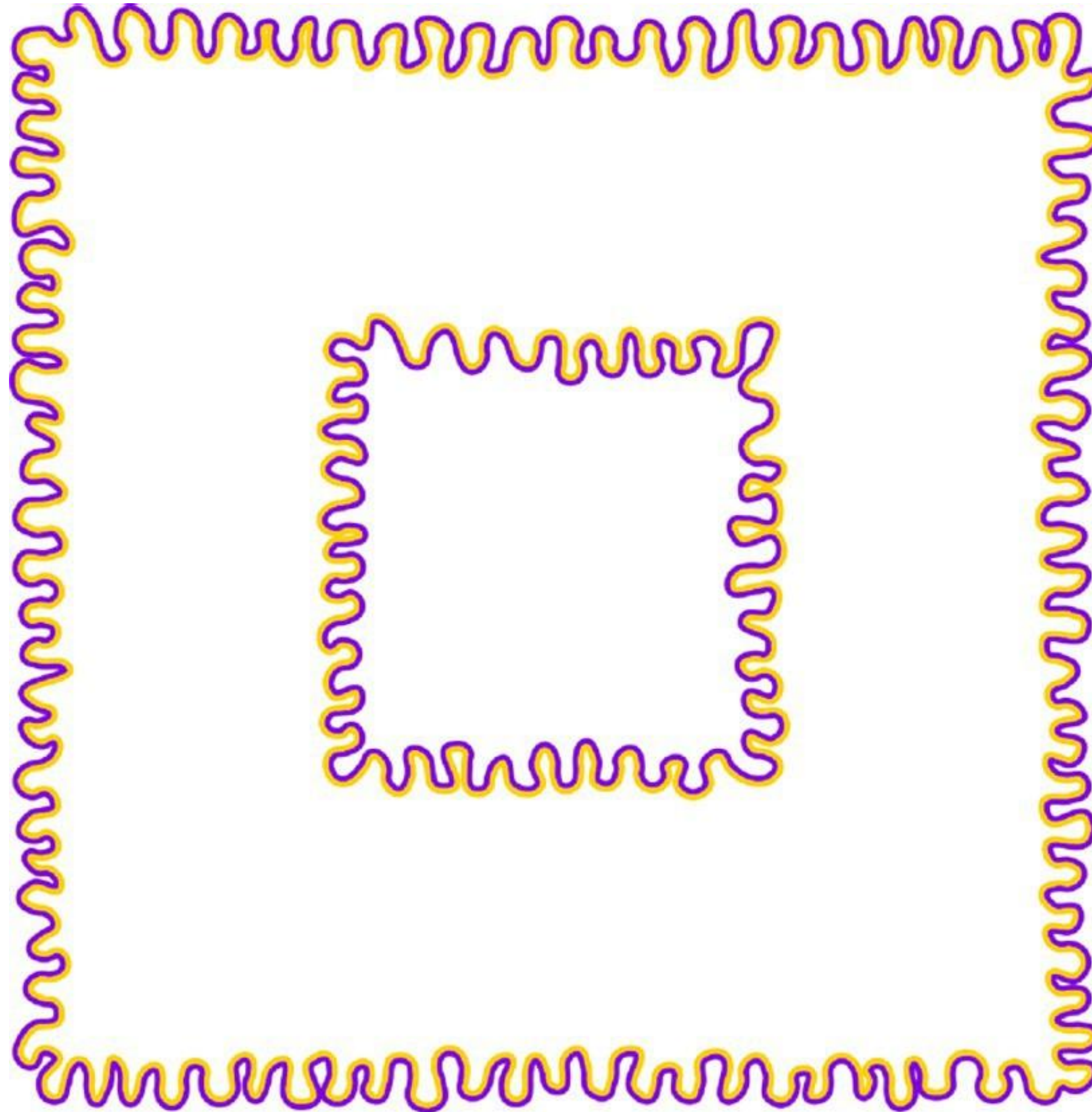
johnsadowski.com

**Color Perception is
Complex and Surprising**

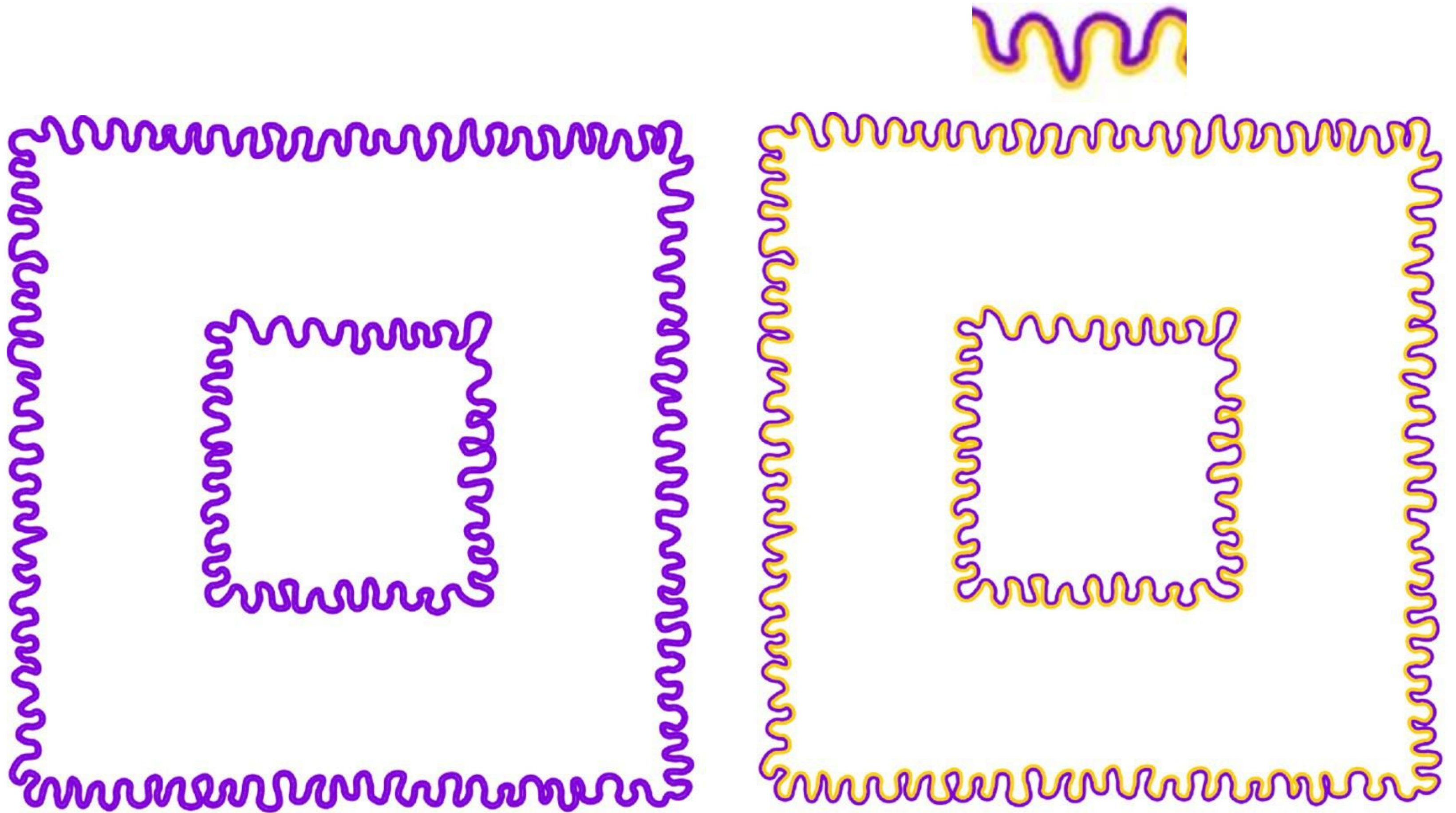
Watercolor Illusion



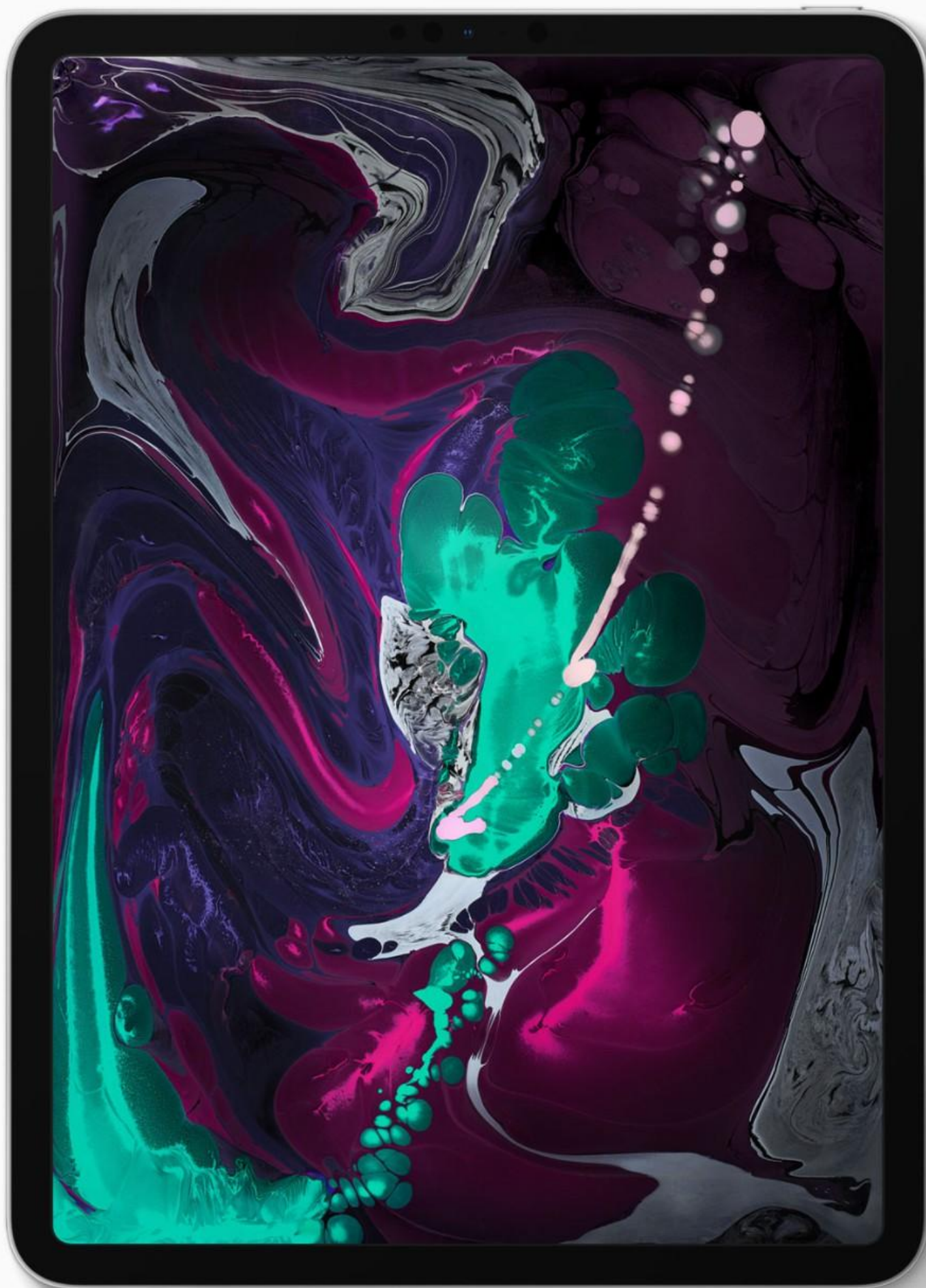
Watercolor Illusion



Watercolor Illusion



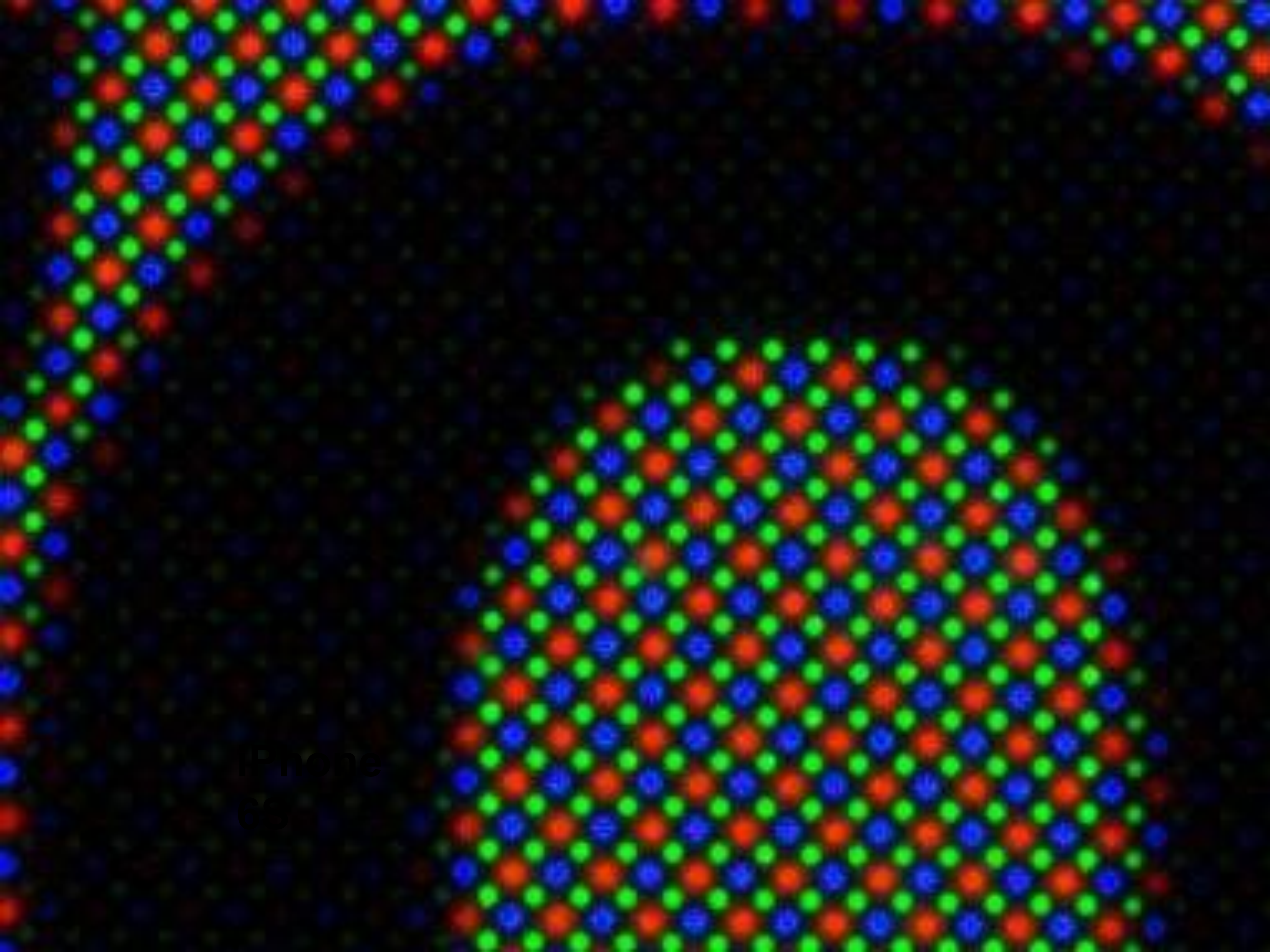
**Yet, we understand color reproduction
as a quantitative science...**



11"



12.9"



iPhone
6S

Cancel

Send to Lightroom

lavender-73_Original-Edit-Edit ▾

56%

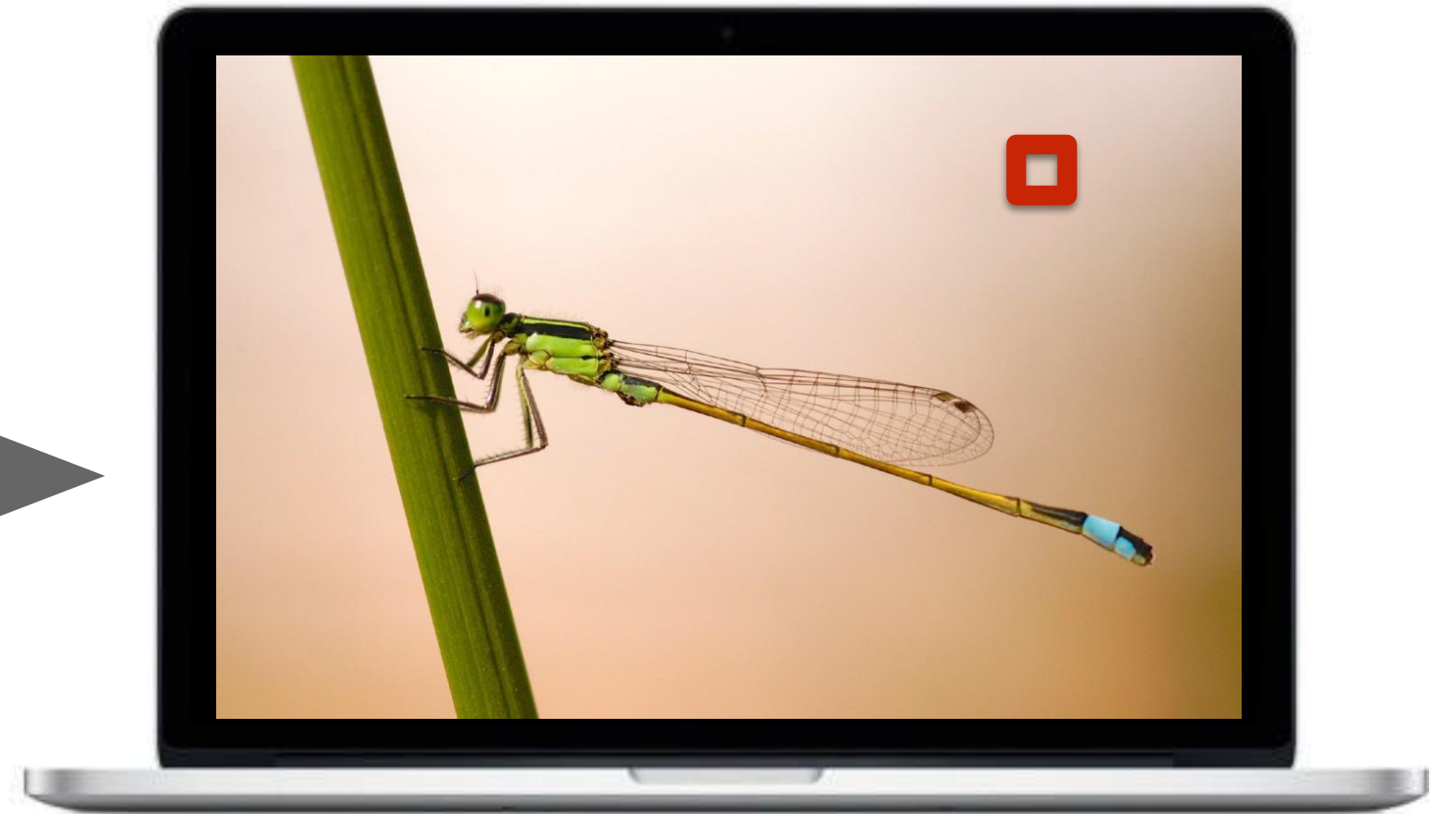


30

Color Reproduction Problem



Real world damselfly



Display image of damselfly
on computer screen

Lagos

What is Color?

What is Color?



- **Color** is a phenomenon of the human visual perception - it is not a universal property of light (photons).
- **Colors** are the visual sensation that we see from light of different **spectral power distributions**

Color Science

Sources of Optical Radiation: PHYSICS Characterization of Objects:
PHYSICS, CHEMISTRY Perception: ANATOMY, PHYSIOLOGY,
PSYCHOLOGY

Physical Basis of Color



credit: Science Media Group.

Isaac Newton's Experimentum Crucis



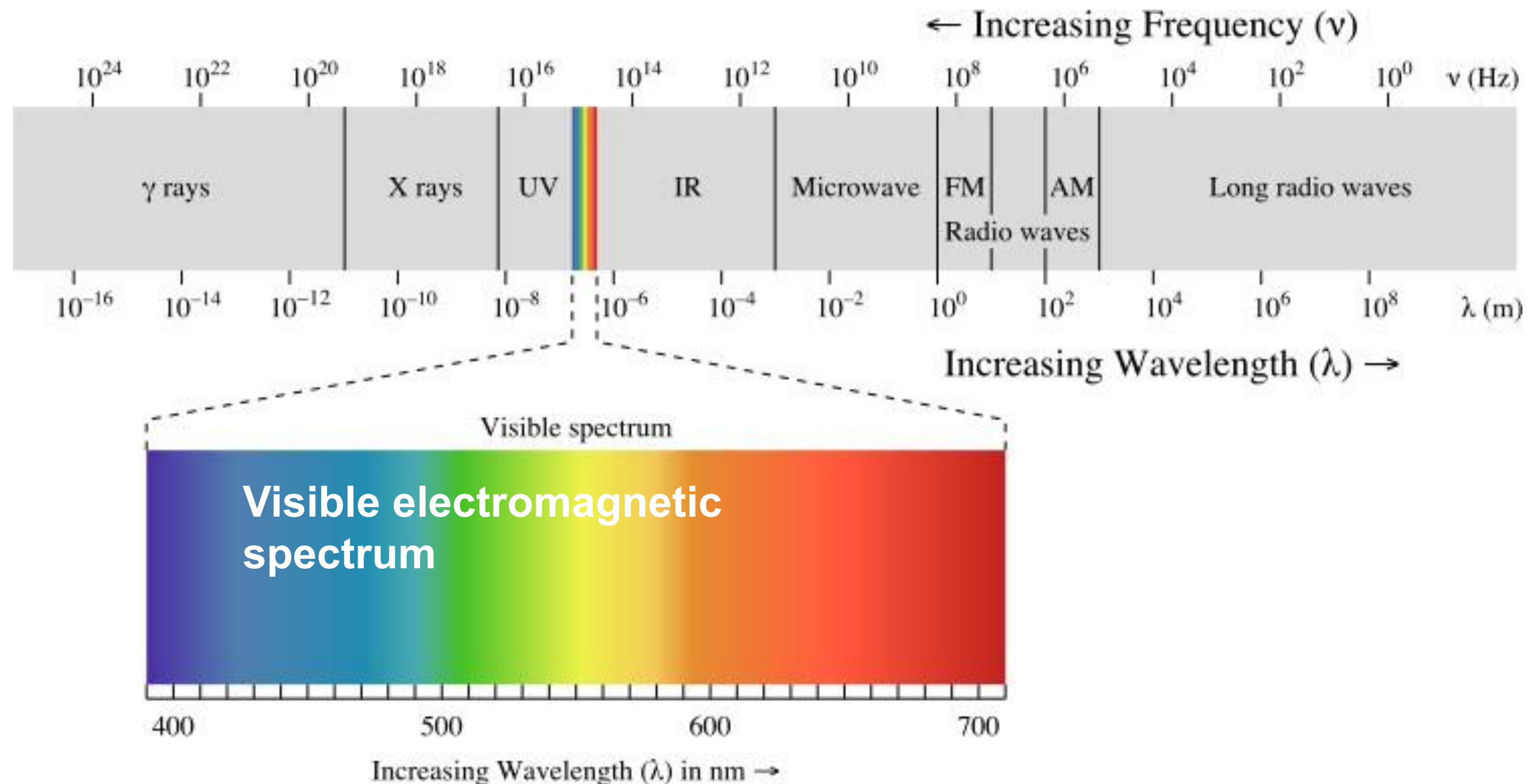
The 'experimentum crucis' – in his Woolsthorpe Manor bedroom. Acrylic painting by Sascha Grusche (17 Dec 2015)

- Newton showed sunlight can be subdivided into a rainbow with a prism
- Resulting light cannot be further subdivided with a second prism

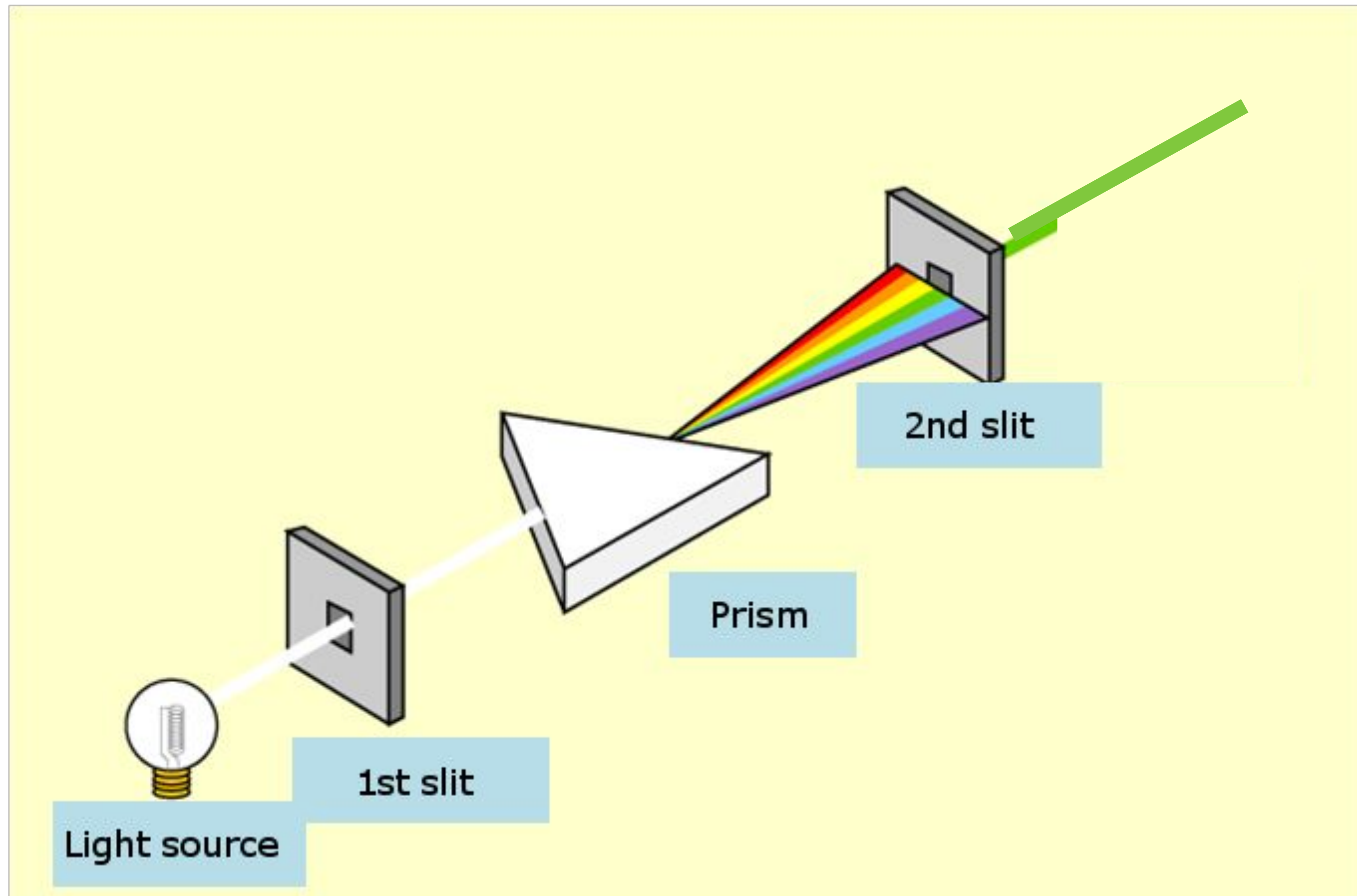
The Visible Spectrum of Light

Electromagnetic radiation

- Oscillations of different frequencies (wavelengths)

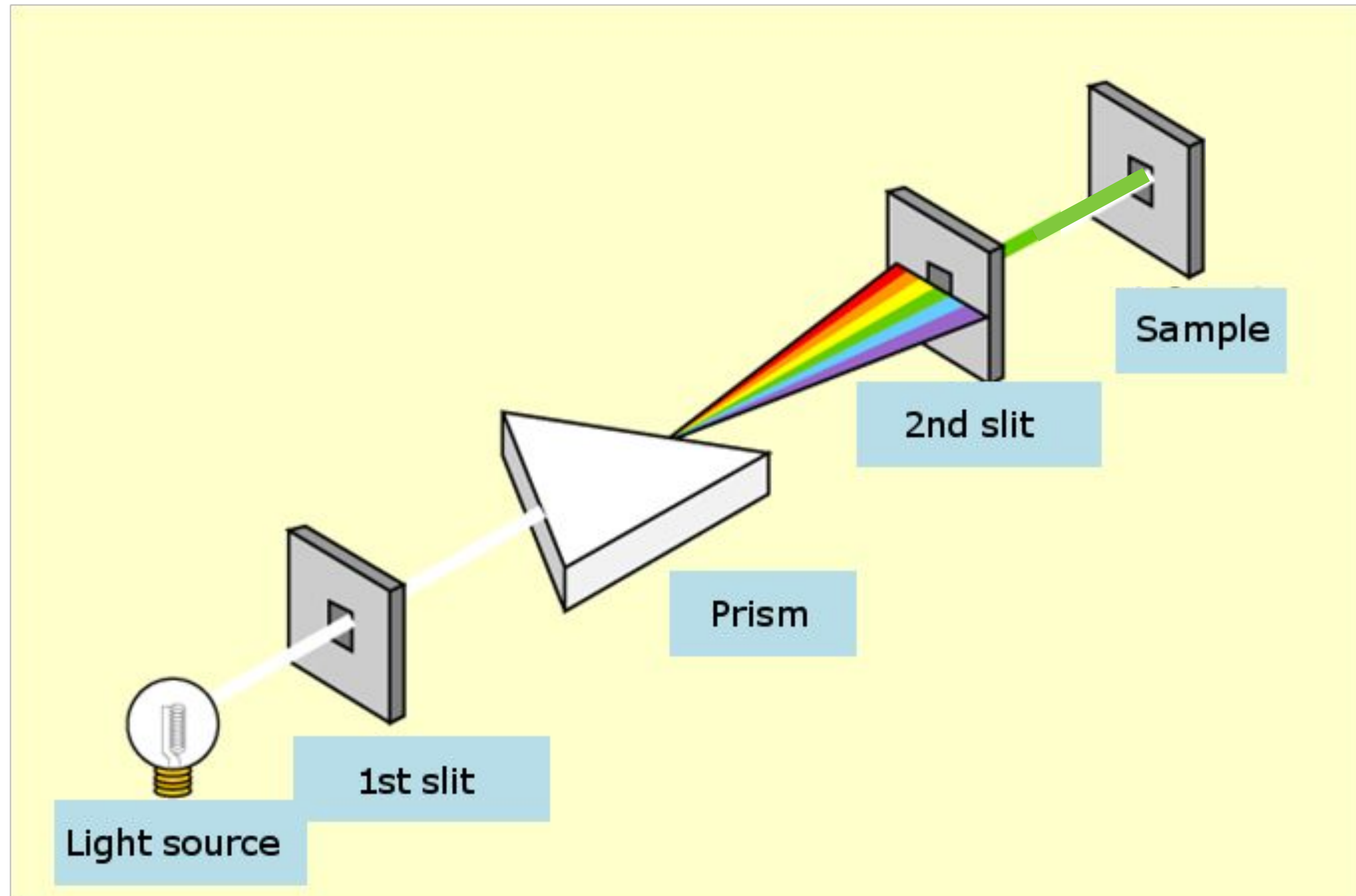


Monochromator



A monochromator delivers light of a single wavelength from a light source with broad spectrum. Control which wavelength by angle of prism.

Spectrometer



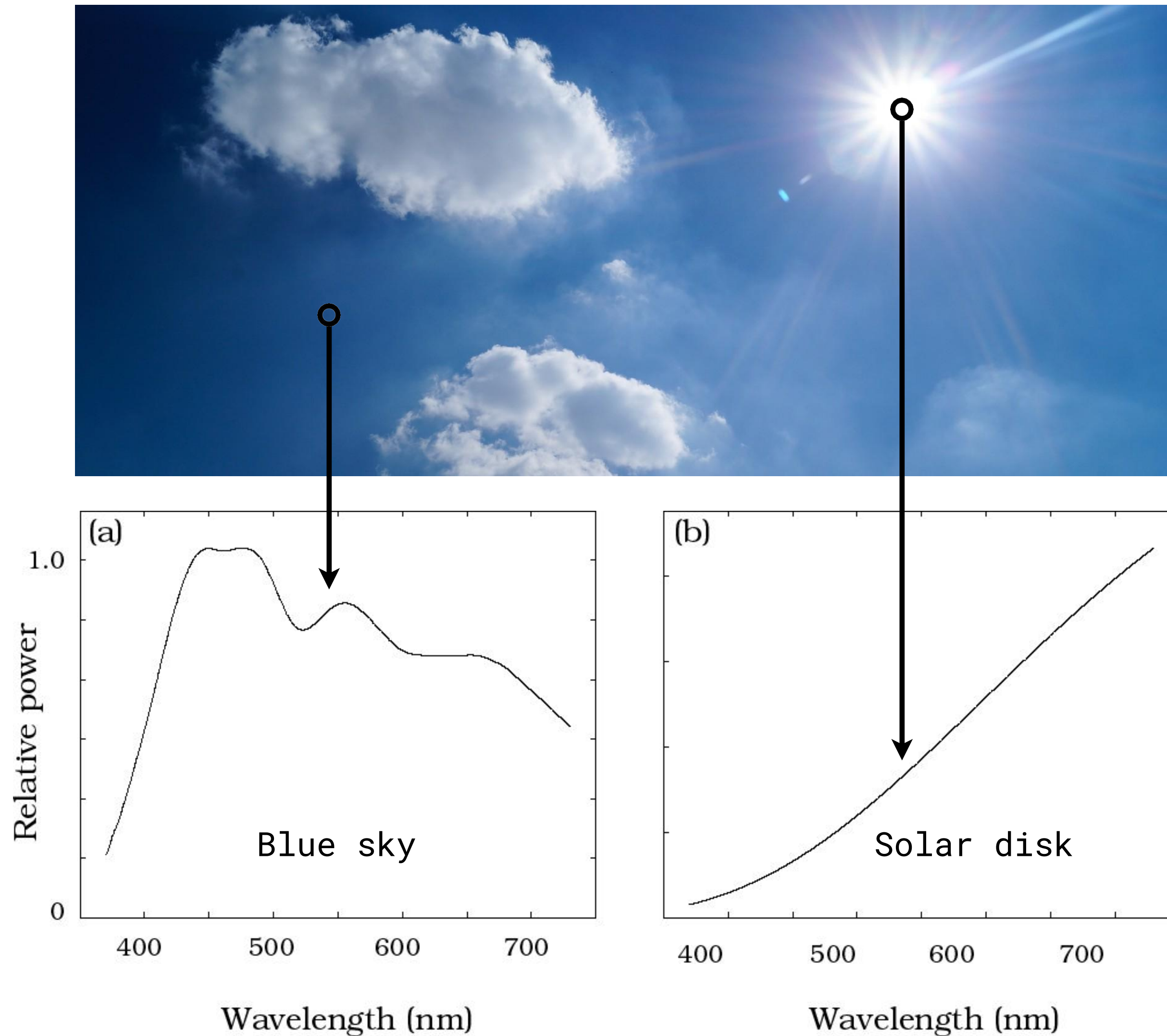
For an unknown light source, use a monochromator to isolate each wavelength of light for measurement.

Spectral Power Distribution (SPD)

Salient property in measuring light

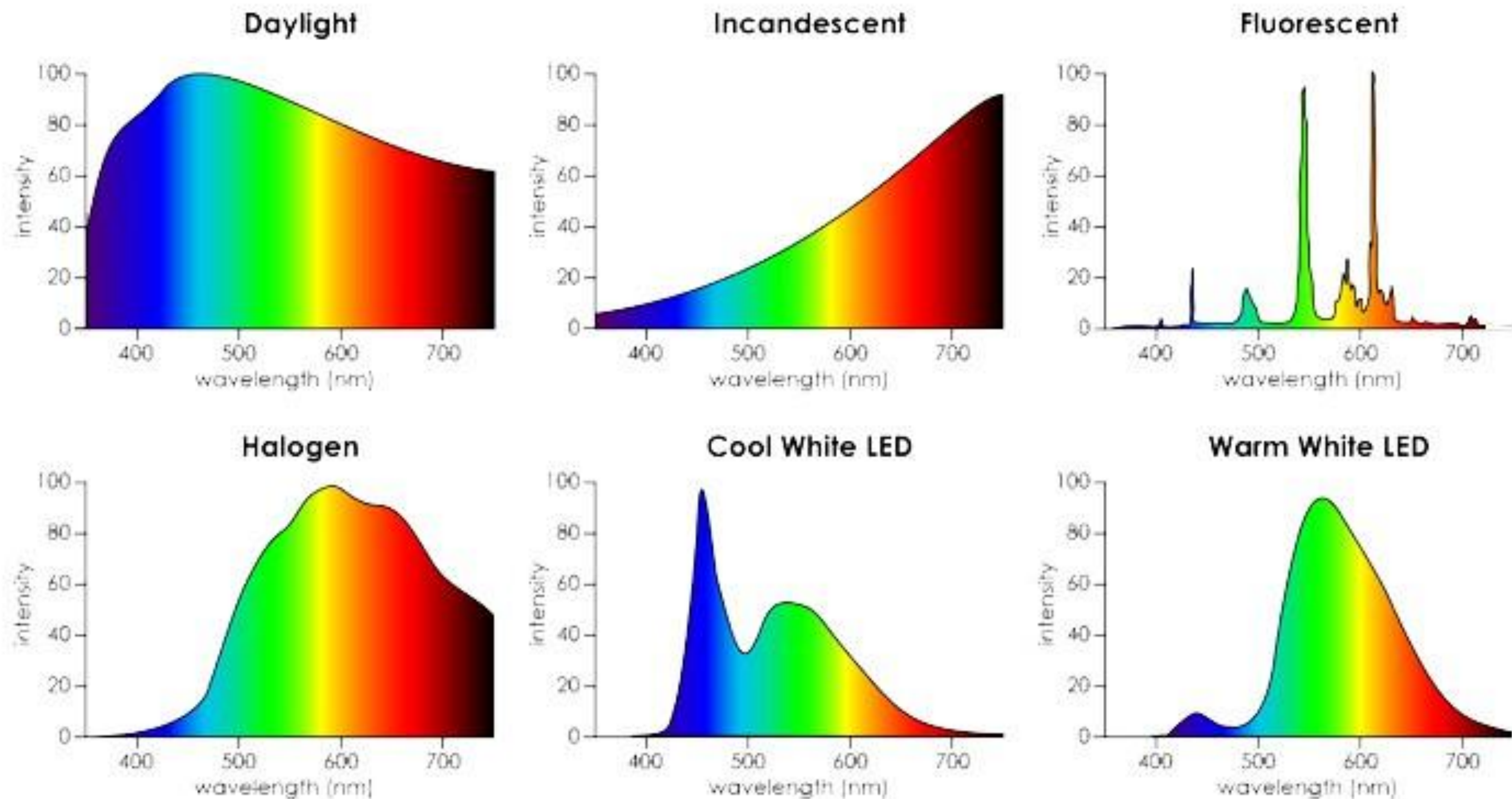
- The amount of light present at each wavelength

Daylight Spectral Power Distributions

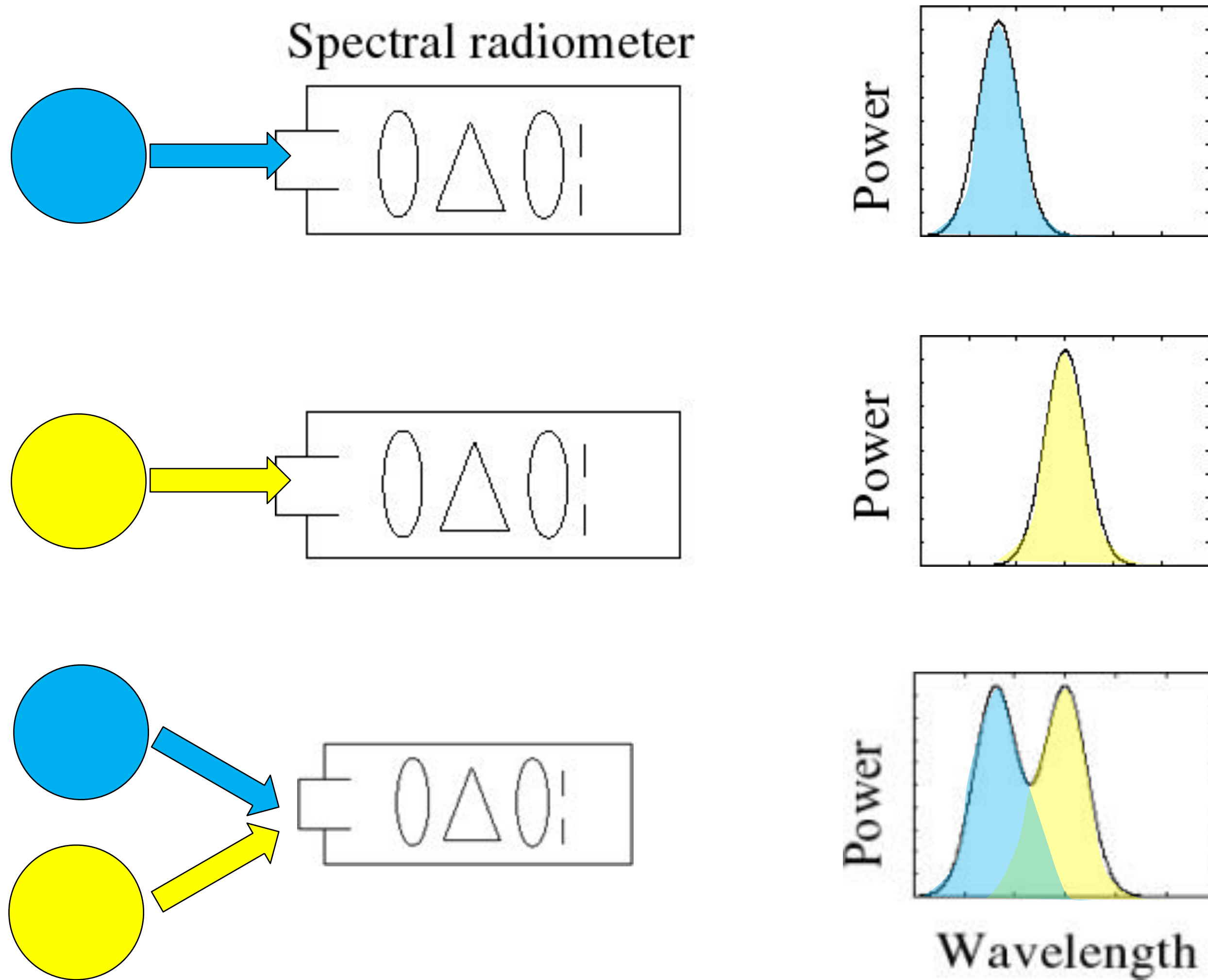


Spectral Power Distribution of Light Sources

Distribution of energy by wavelength



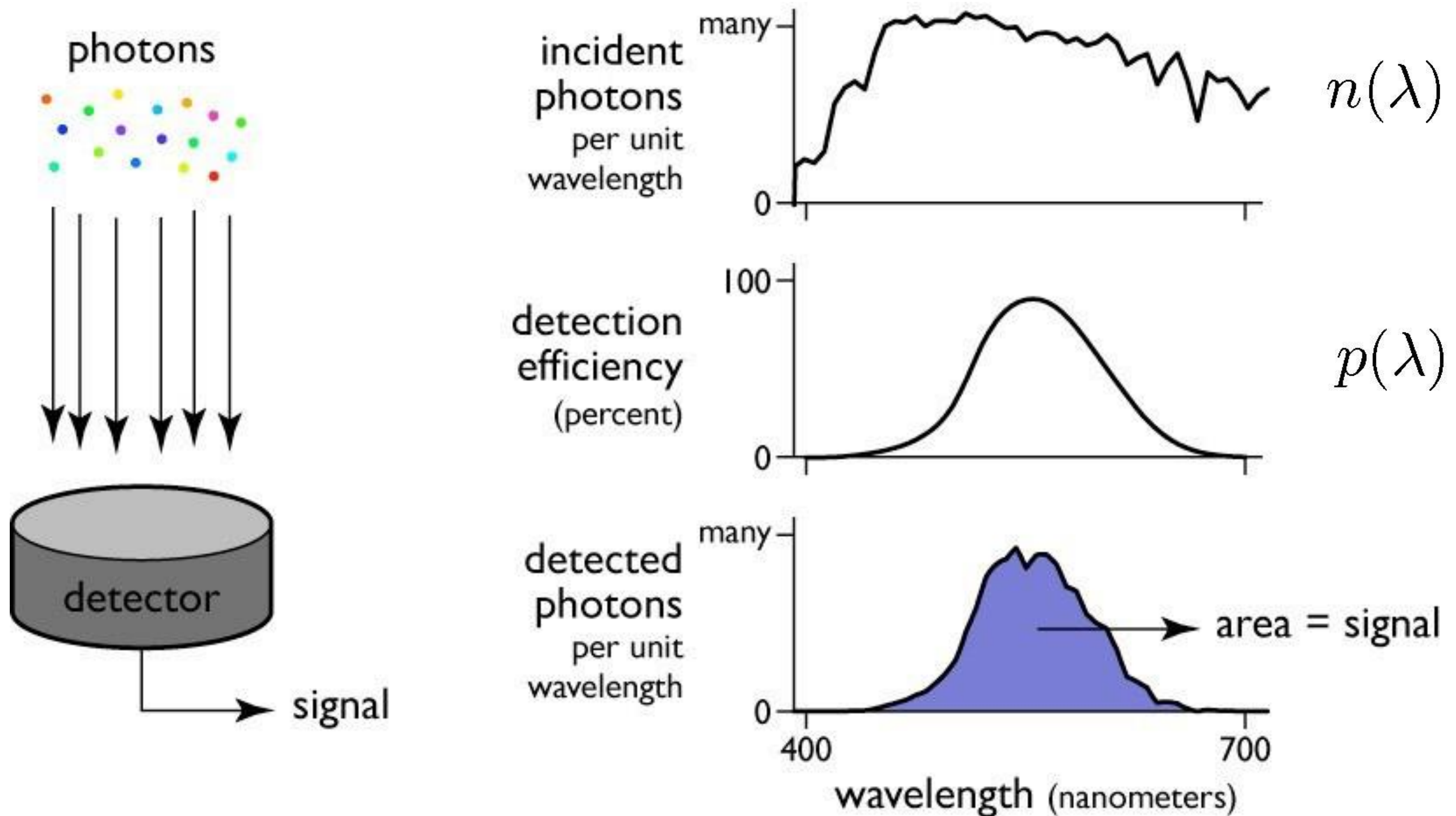
Superposition (Linearity) of Spectral Power Distributions



Measuring Light

A Simple Model of a Light Detector

A Simple Model of a Light Detector



$$X = \int n(\lambda)p(\lambda) d\lambda$$

Mathematics of Light Detection

Same math carries over to spectral power distributions

- Light entering the detector has its spectral power distribution, $s(\lambda)$
- Detector has its spectral sensitivity or spectral response, $r(\lambda)$

$$X = \int s(\lambda) r(\lambda) d\lambda$$

measured signal

input spectrum

detector's sensitivity

Mathematics of Light Detection

If we think of s and r as discrete, sampled representations (vectors) rather than continuous functions, this integral operation is a dot product:

$$X = s \cdot r$$

We can also write this in matrix form:

$$X = \begin{bmatrix} \text{---} & s & \text{---} \end{bmatrix} \begin{bmatrix} | \\ r \\ | \end{bmatrix}$$

Dimensionality Reduction From ∞ to 1

At the detector:

- **SPD is a function of wavelength** (∞ dimensional signal)
- **Detector result is a scalar value** (1 dimensional signal)

Tristimulus Theory of Color

Searching for a Linear Systems Basis for Colors: *The Color Matching Experiment*

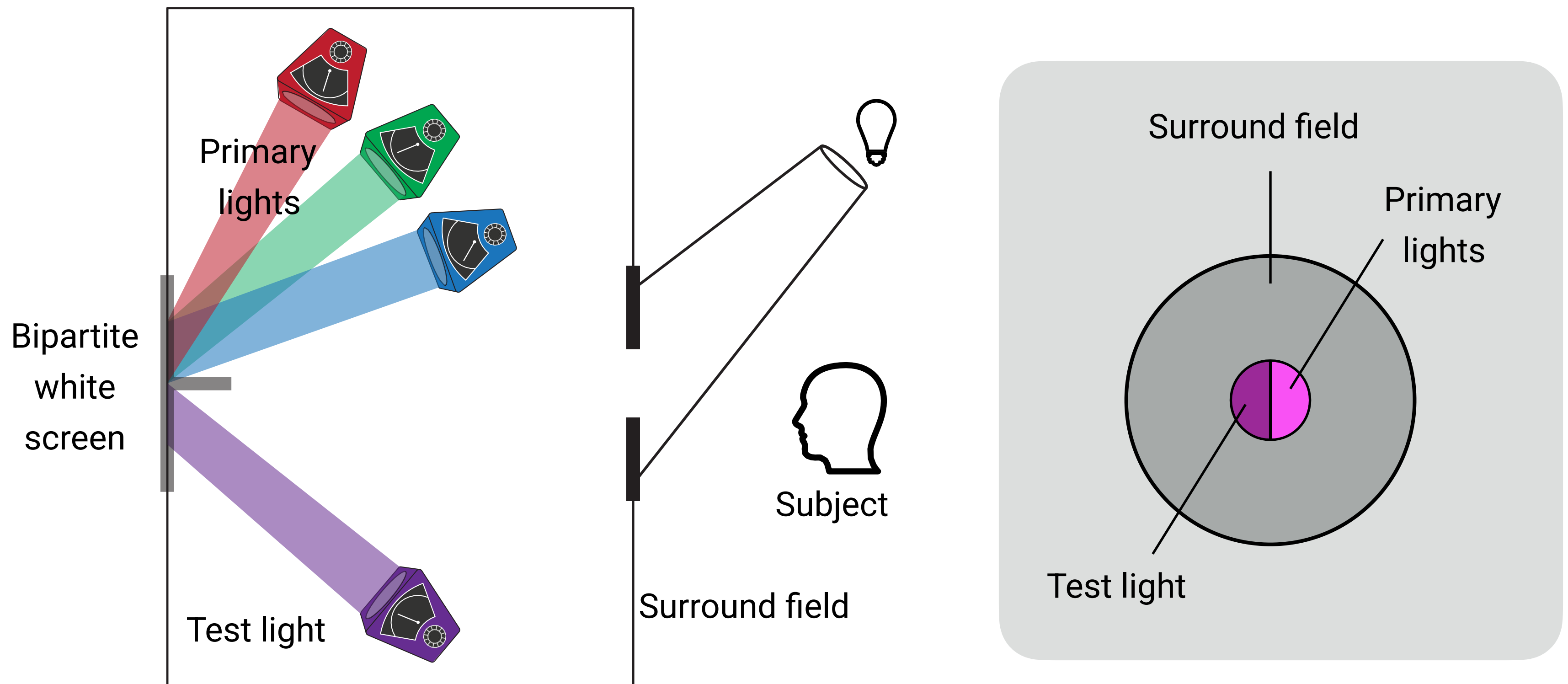
Maxwell's Crucial Color Matching Experiment



<http://designblog.rietveldacademie.nl/?p=68422>

Portrait: <http://rsta.royalsocietypublishing.org/content/366/1871/1685>

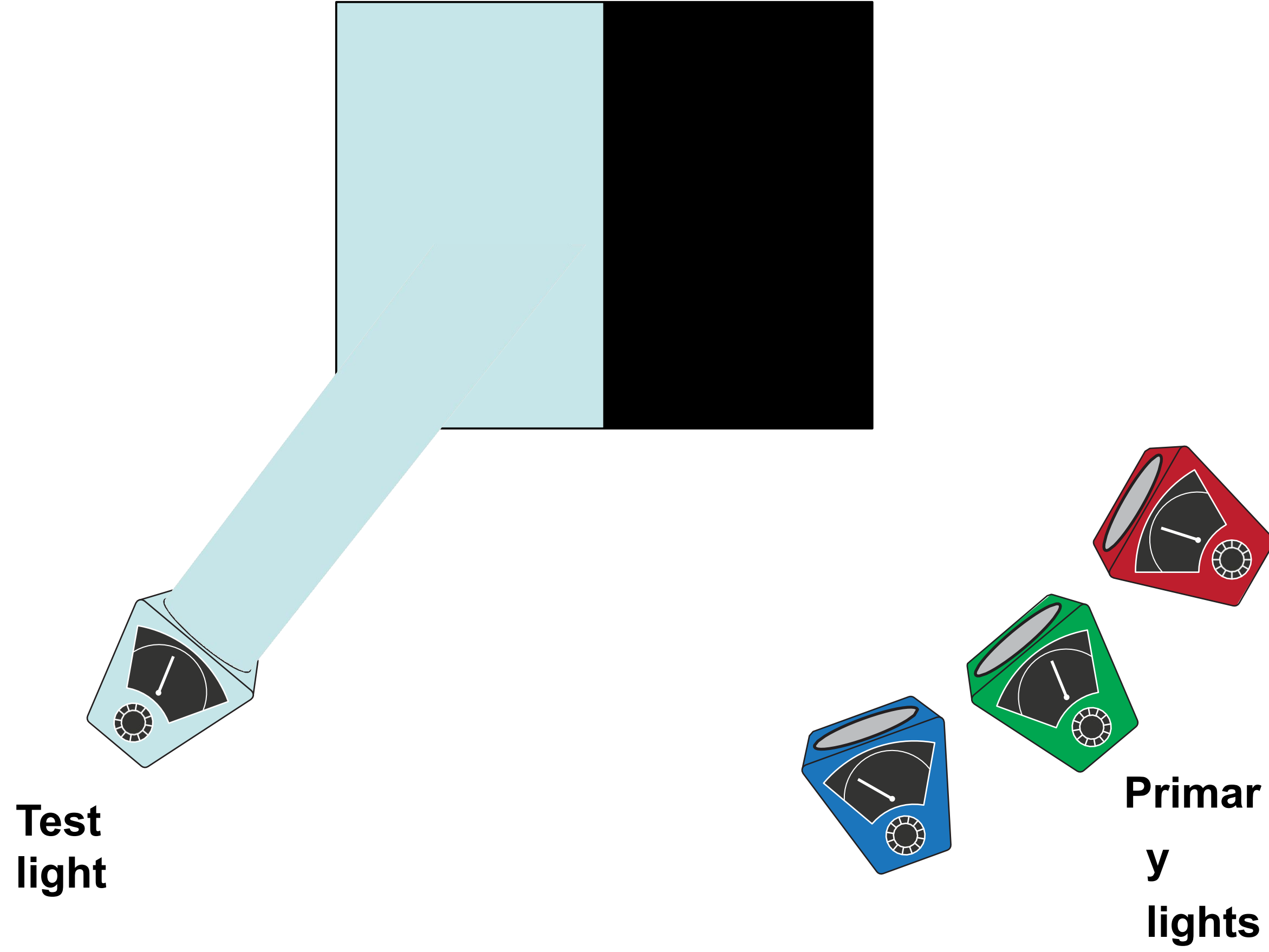
Color Matching Experiment



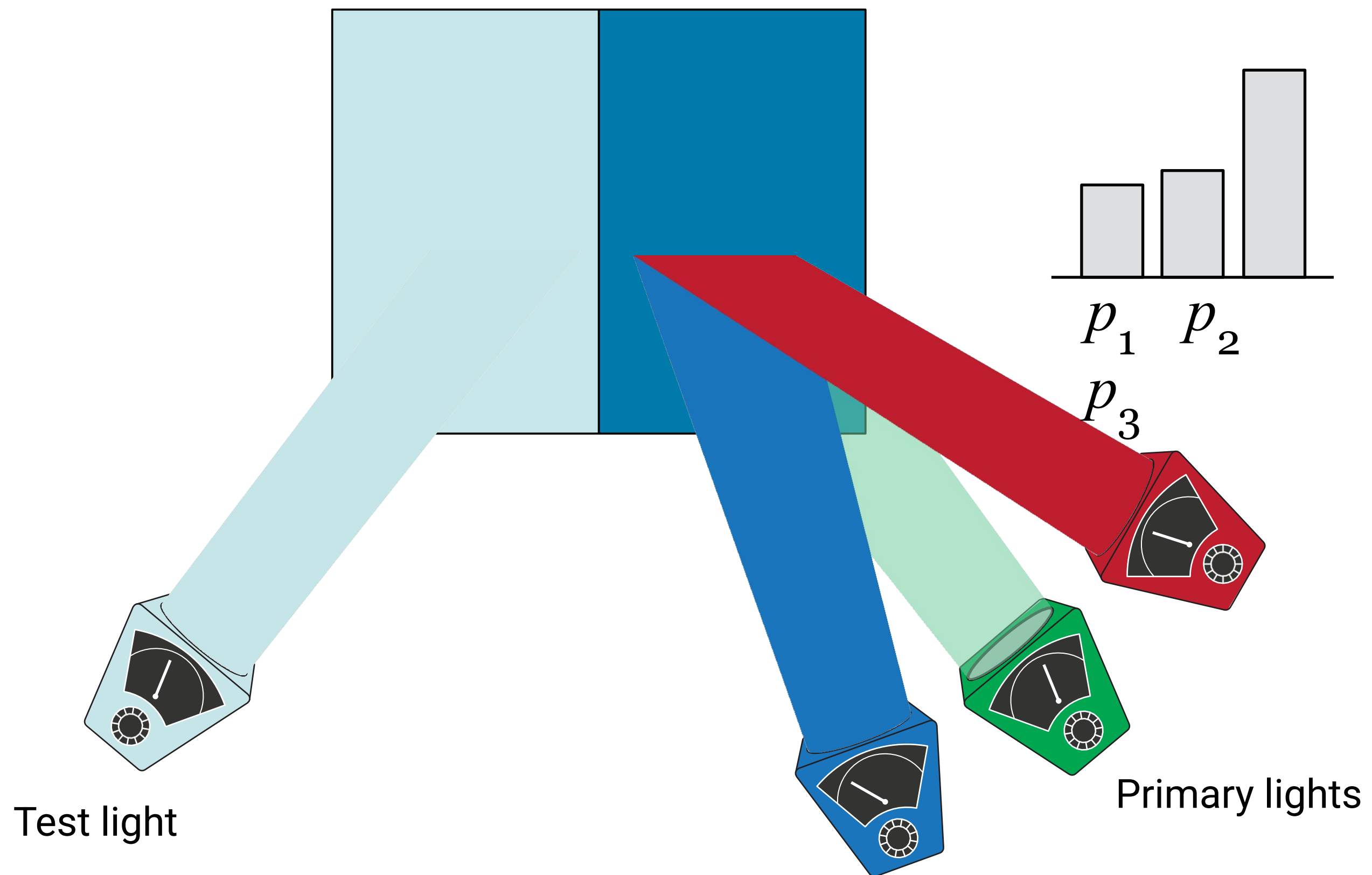
Same idea as spinning top, fancier implementation (Maxwell did this too)

1. Show test light spectrum on left
2. Mix “primaries” on right until they match
3. The primaries need not be RGB

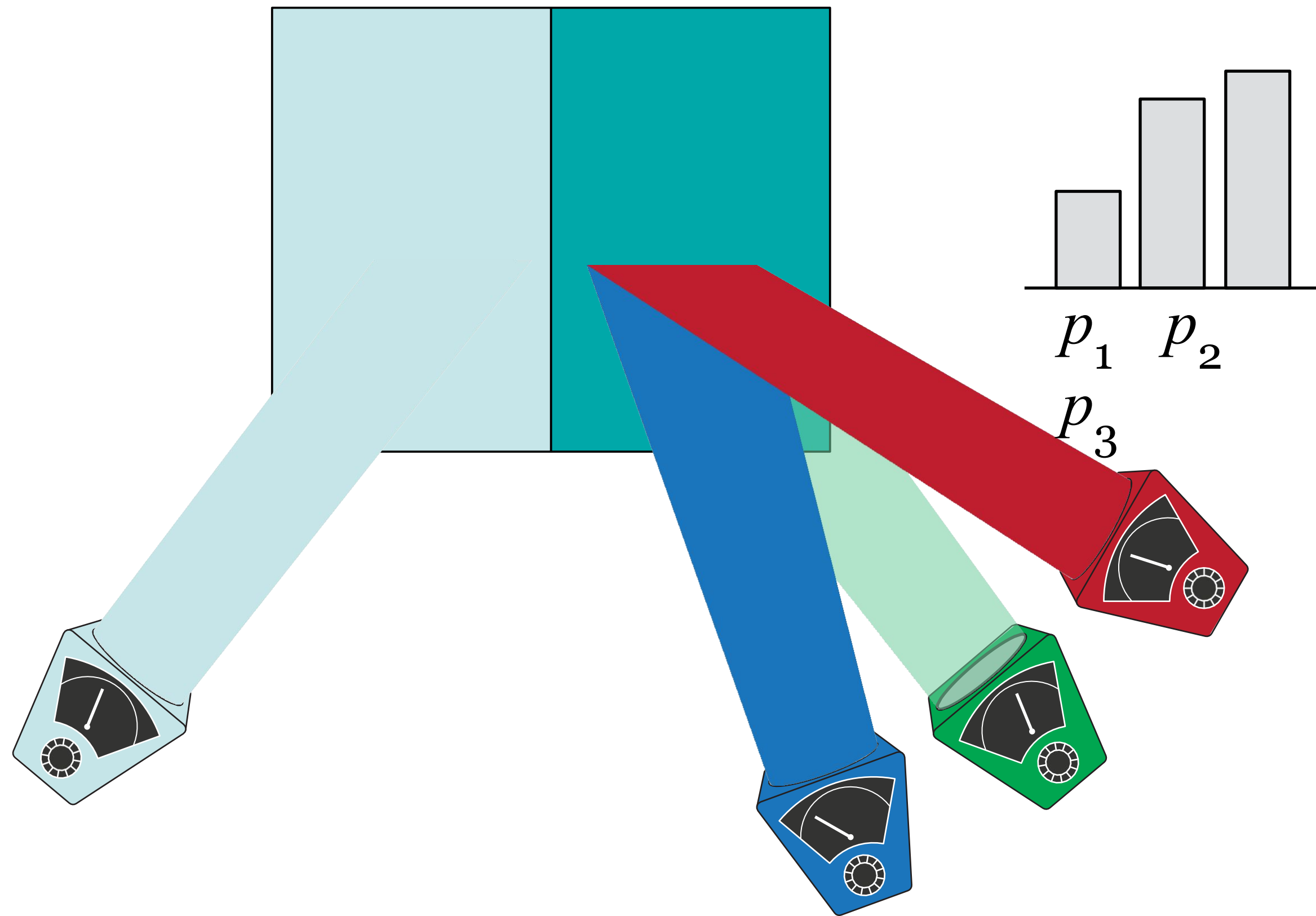
Example Experiment



Example Experiment

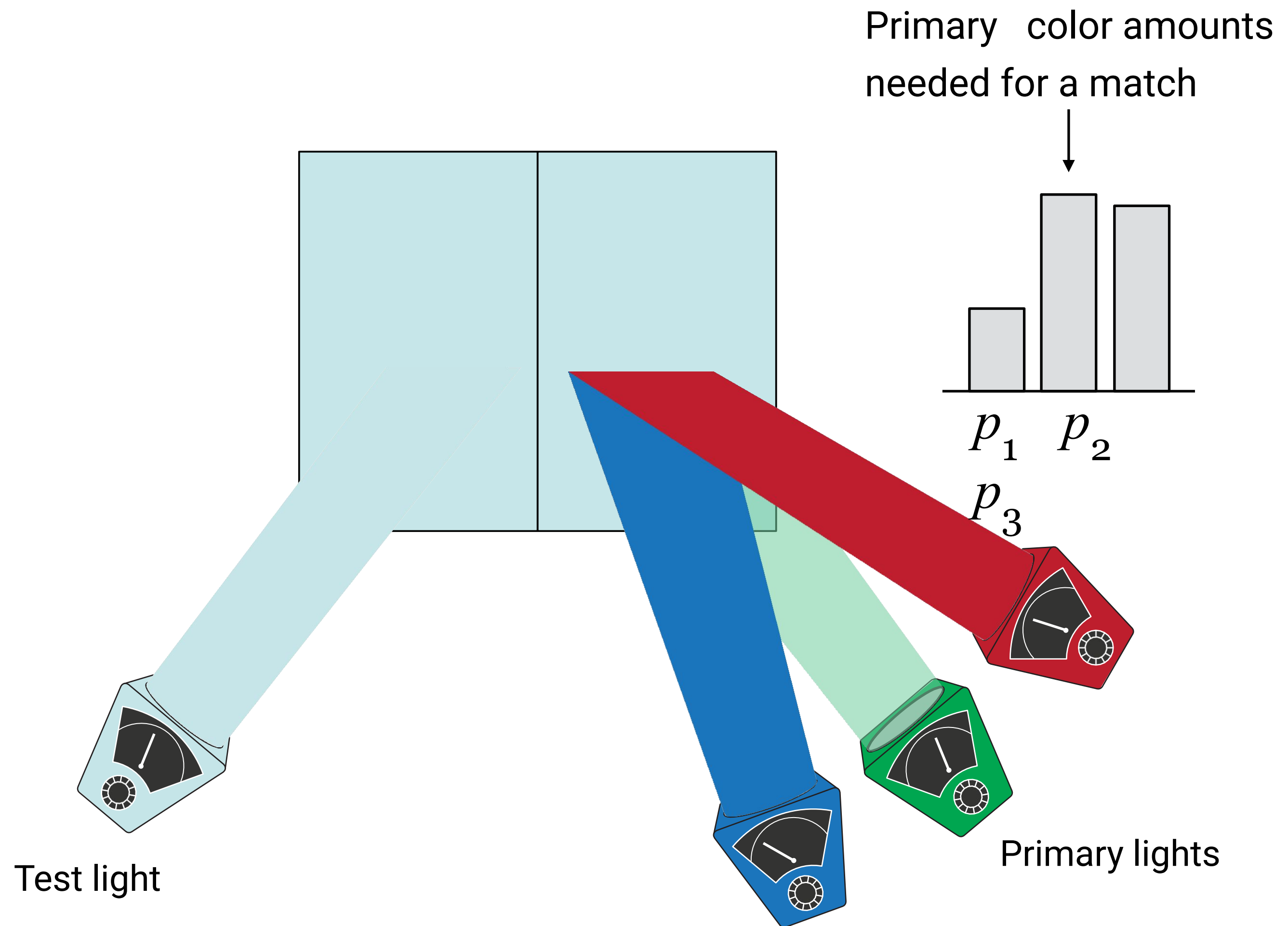


Example Experiment

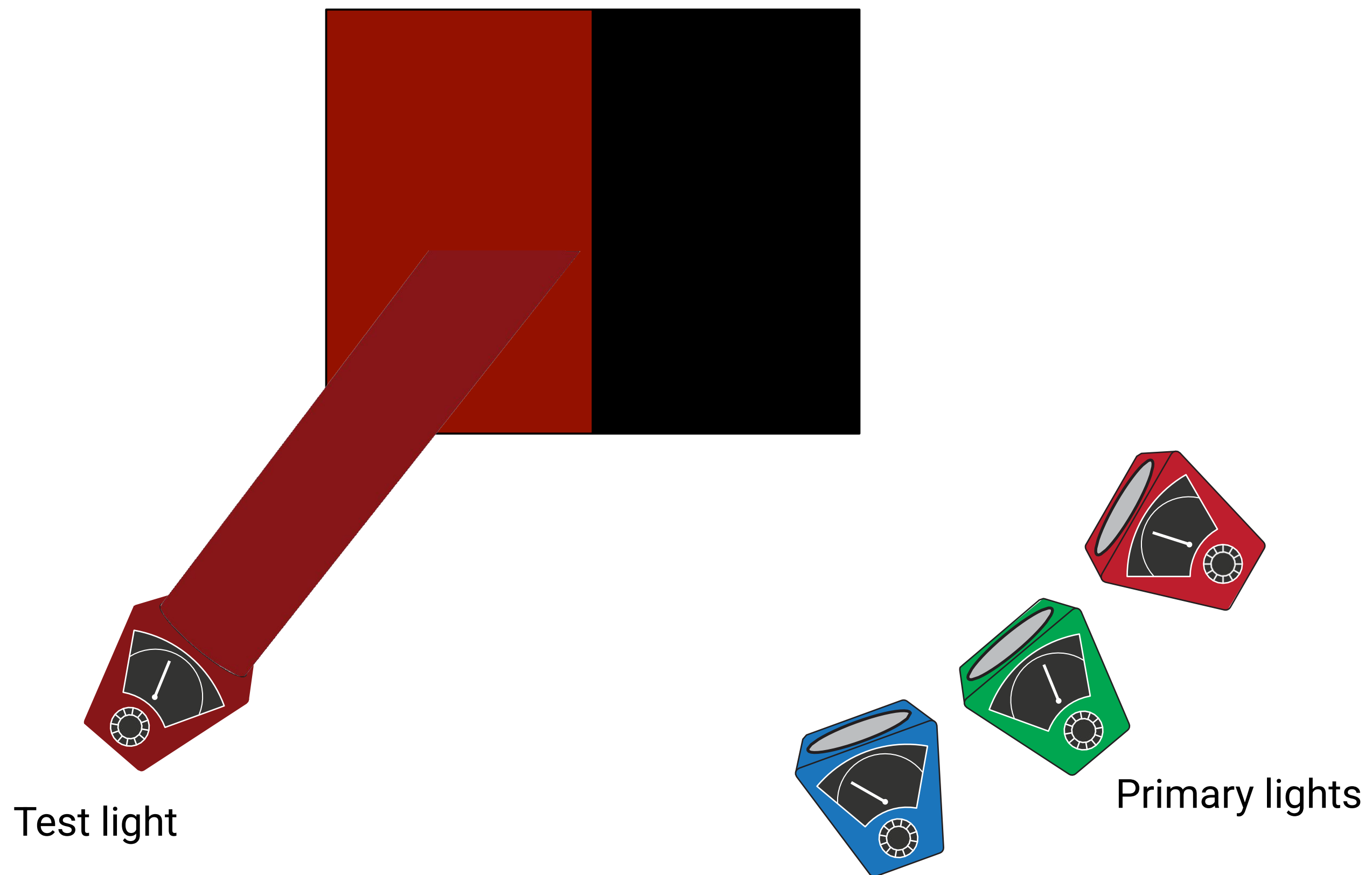


Slide credit: Kotani, Durand, Freeman

Example Experiment

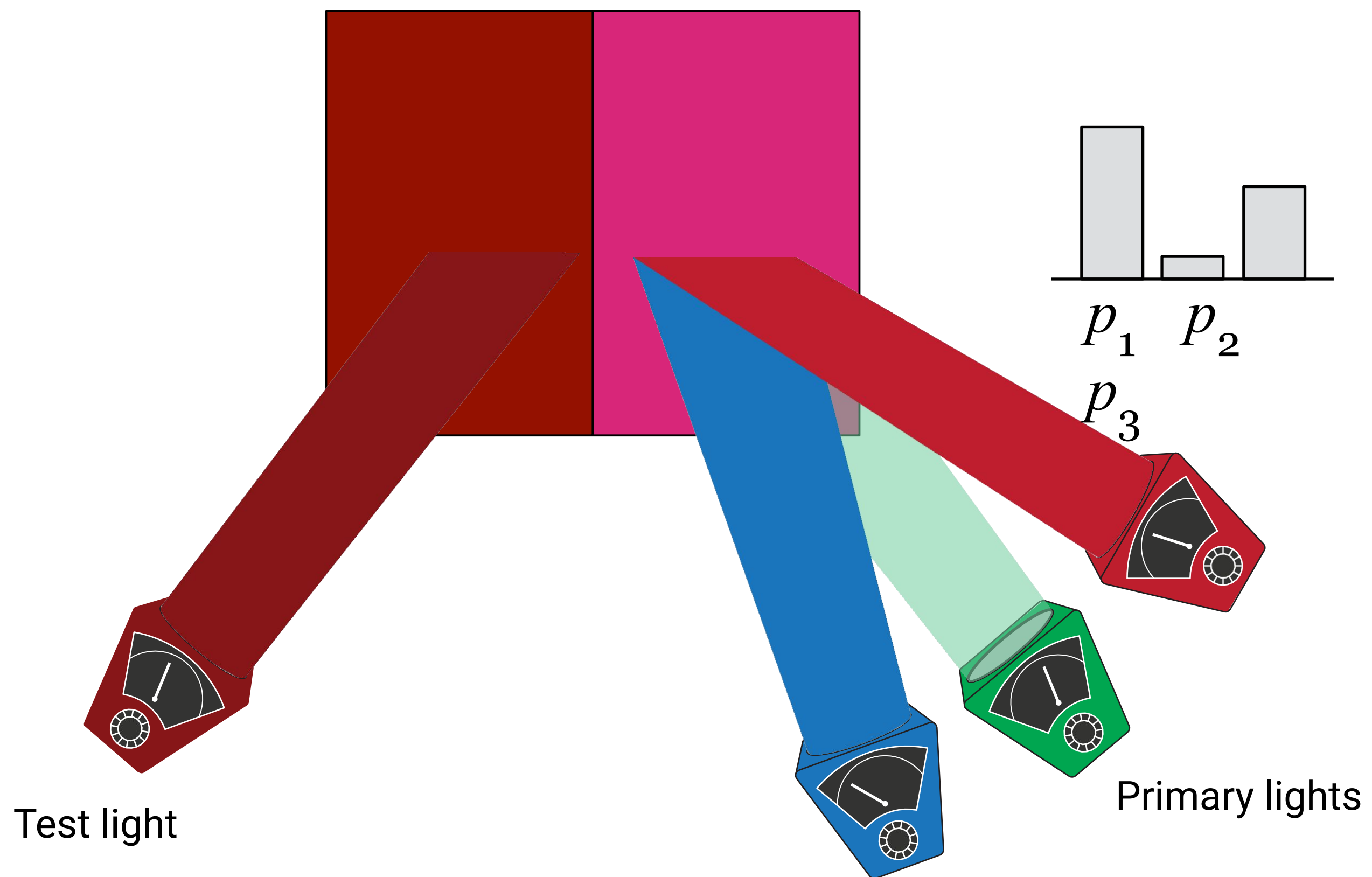


Experiment 2: Out of Gamut



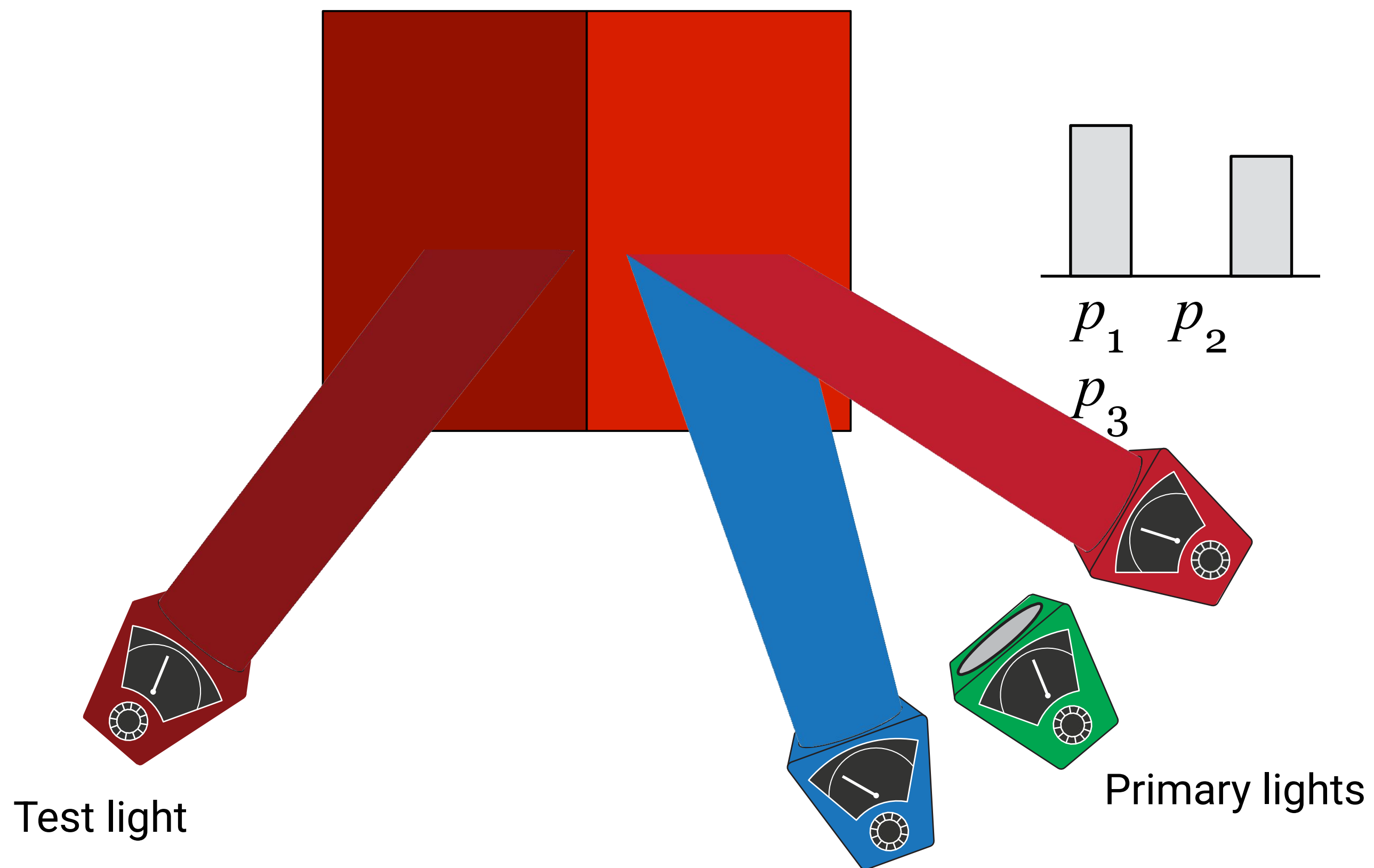
Slide credit: Kotani, Durand, Freeman

Experiment 2: Out of Gamut



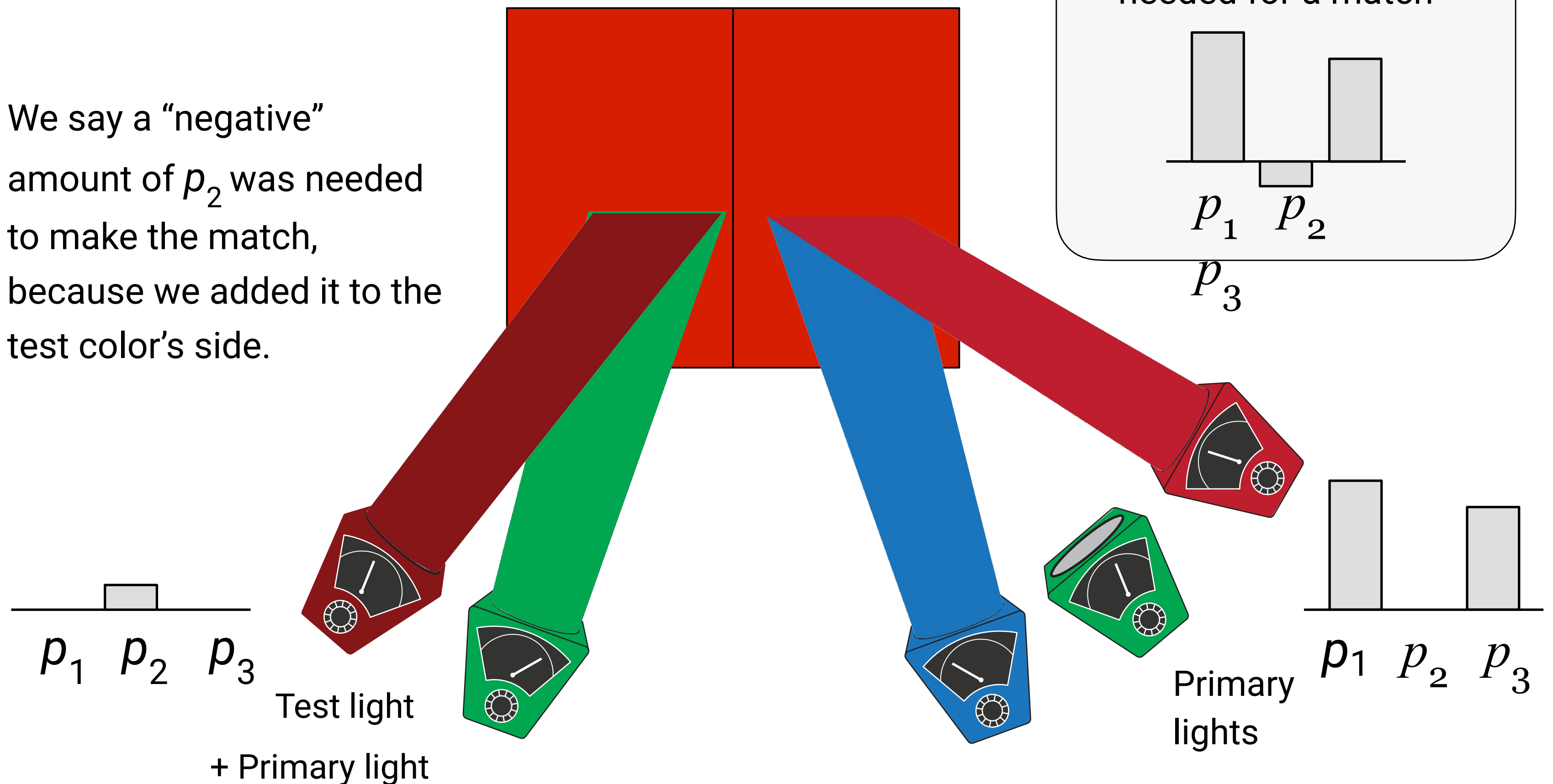
Slide credit: Kotani, Durand, Freeman

Experiment 2: Out of Gamut



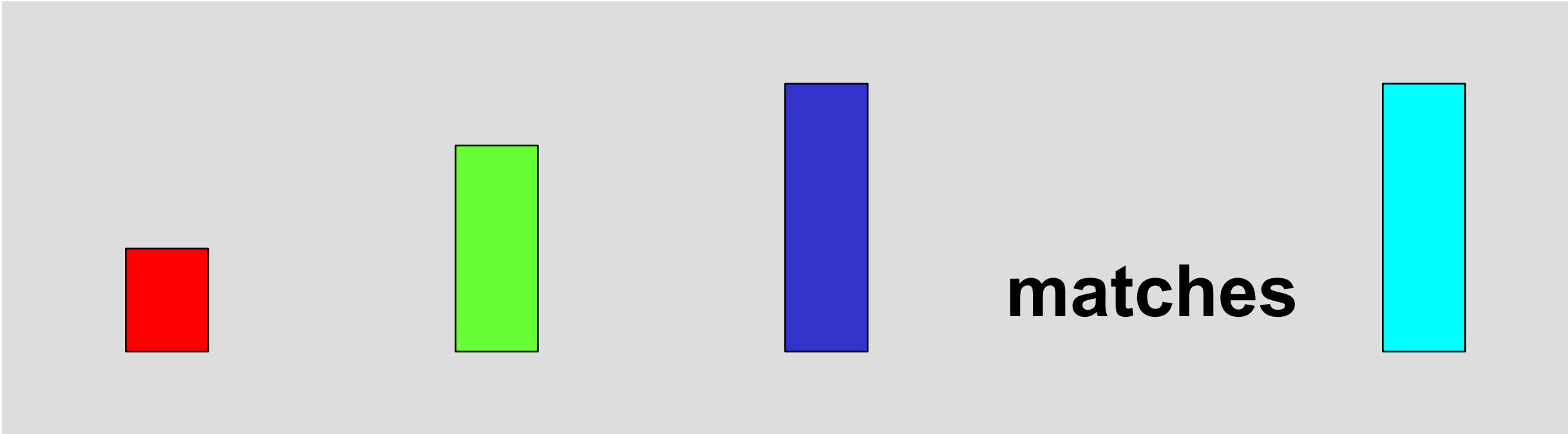
Experiment 2: Out of Gamut

We say a “negative” amount of p_2 was needed to make the match, because we added it to the test color’s side.

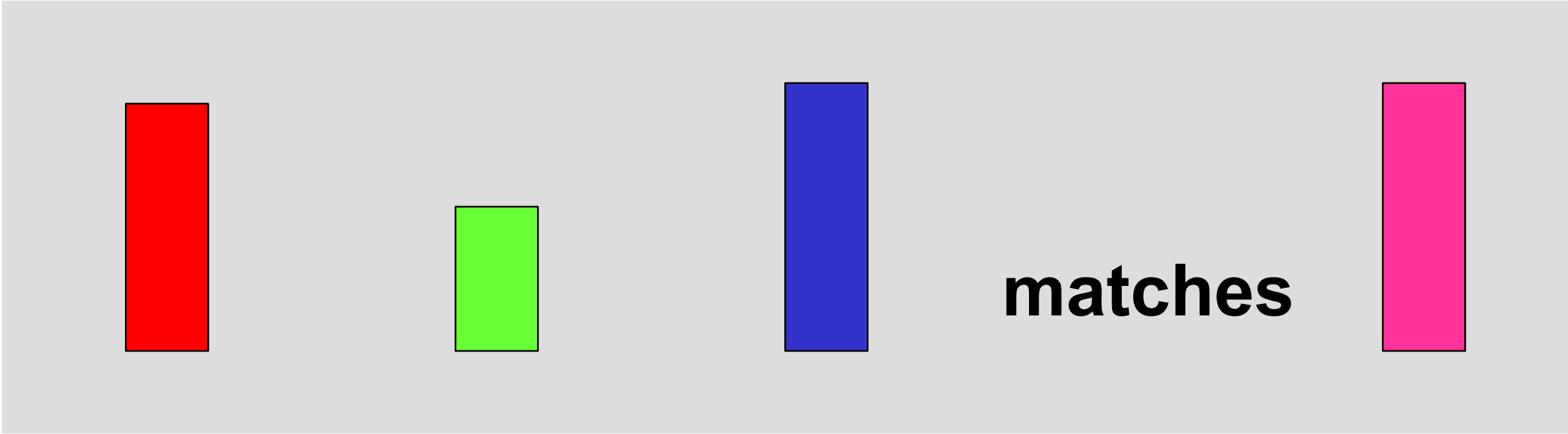


The Color Matching Experiment is Linear

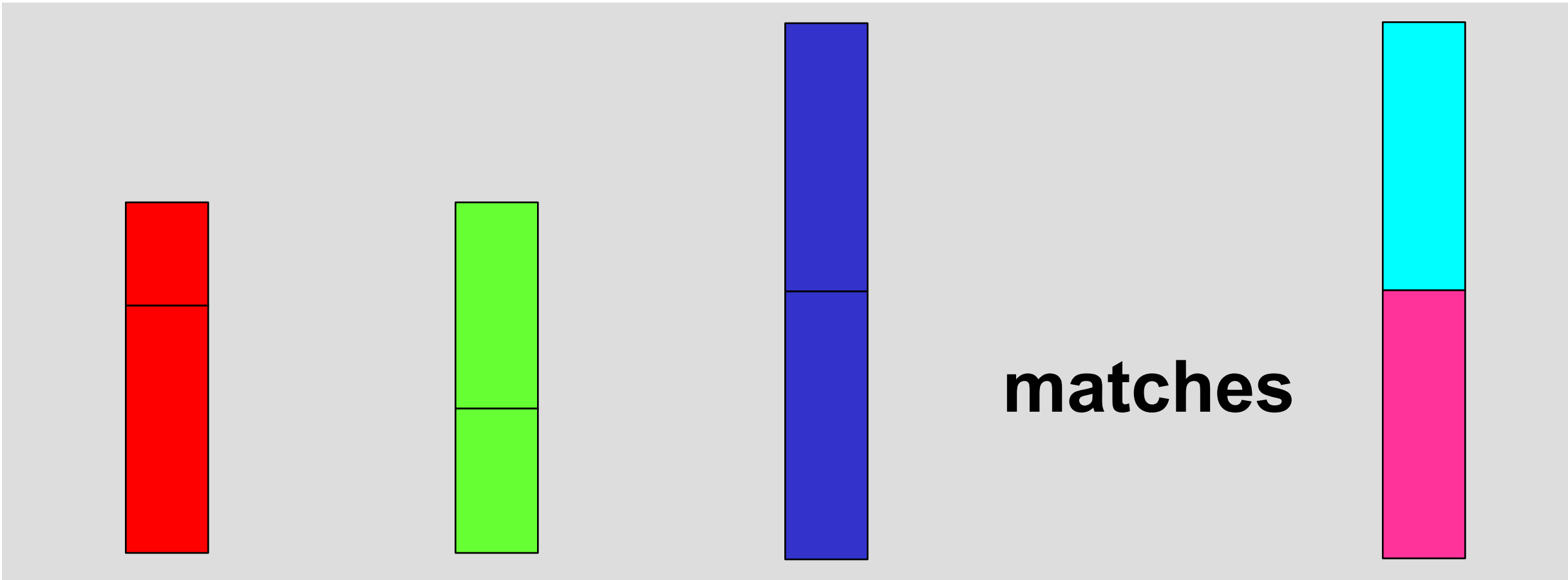
If



and



then



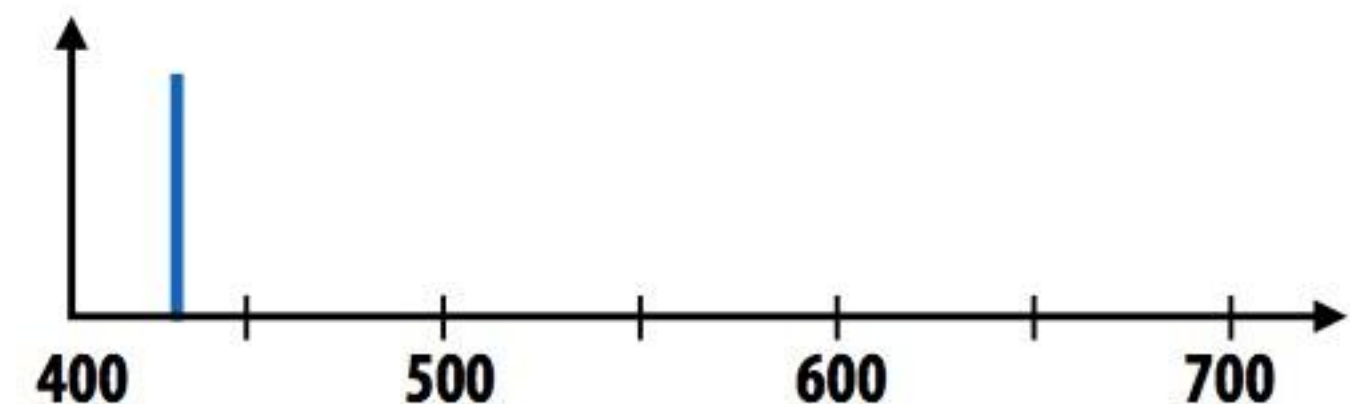
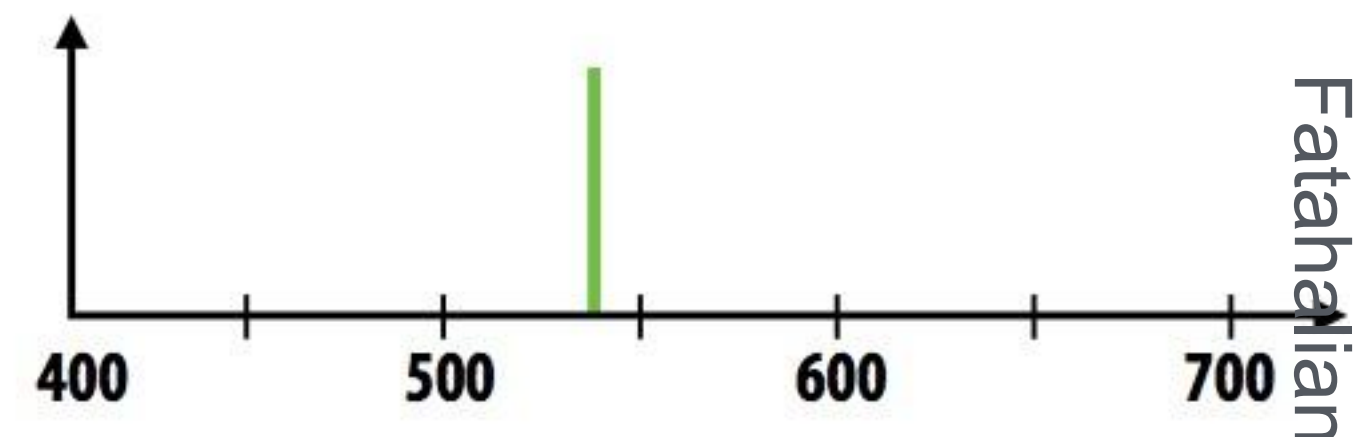
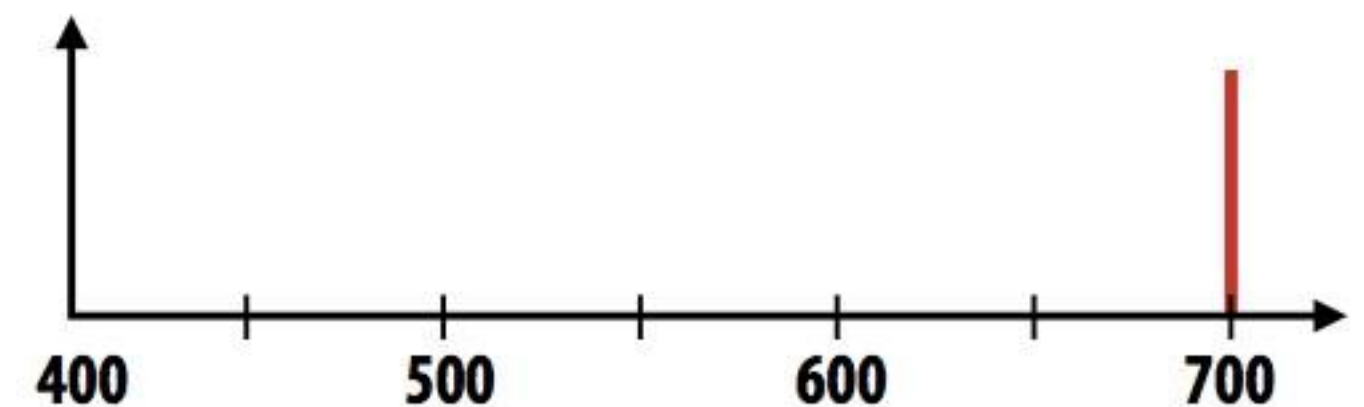
What is the Dimensionality of Human Color Perception?

What is the definition of “dimension” here?

- We can appeal to linear systems theory, where “dimension” equals the rank of a basis for the linear space.

CIE RGB Color Matching Experiment

Same setup as additive color matching before, but primaries are monochromatic light (single wavelength) of the following wavelengths defined by CIE RGB standard



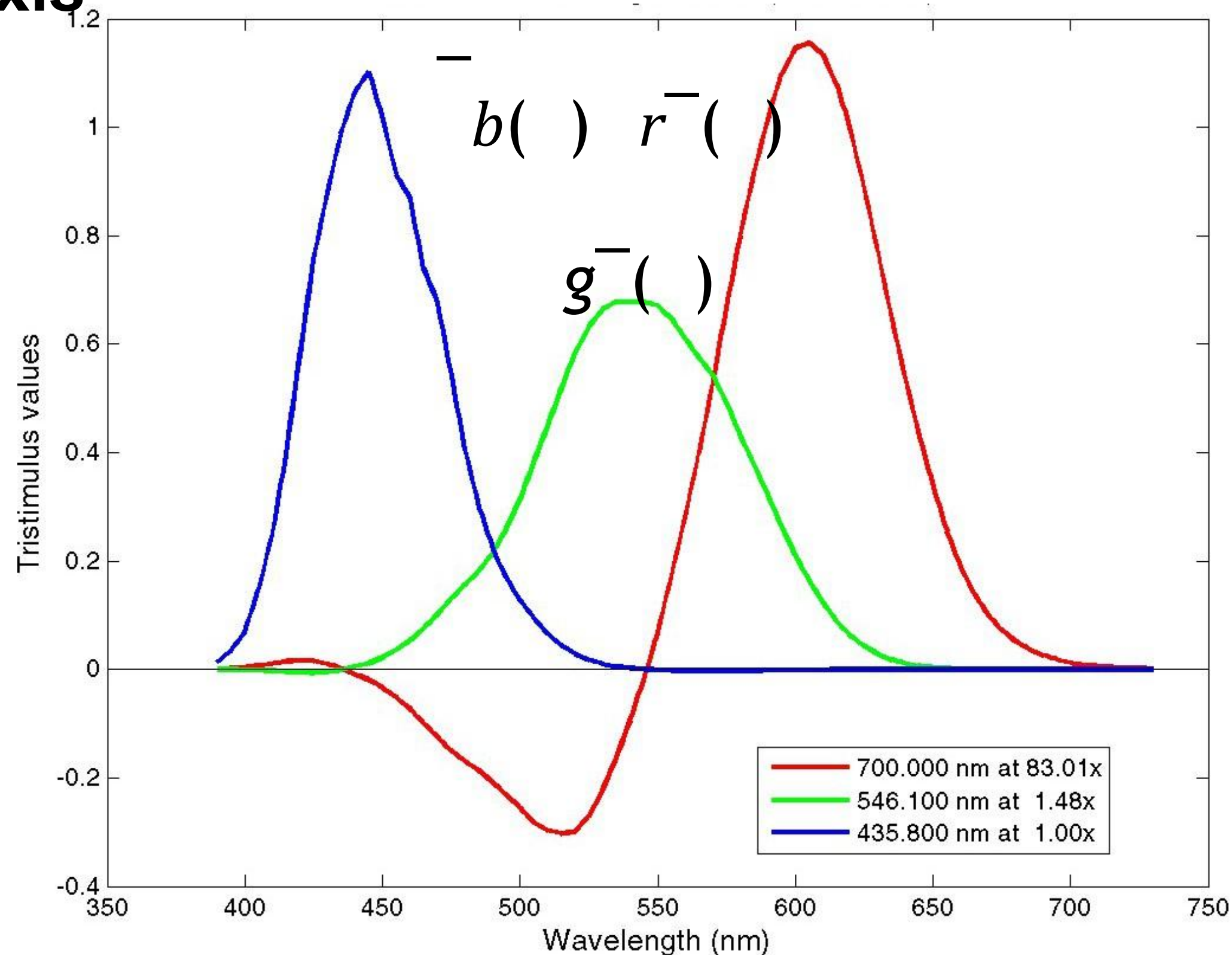
The test light is also a monochromatic light



Kayvon
Fatahian

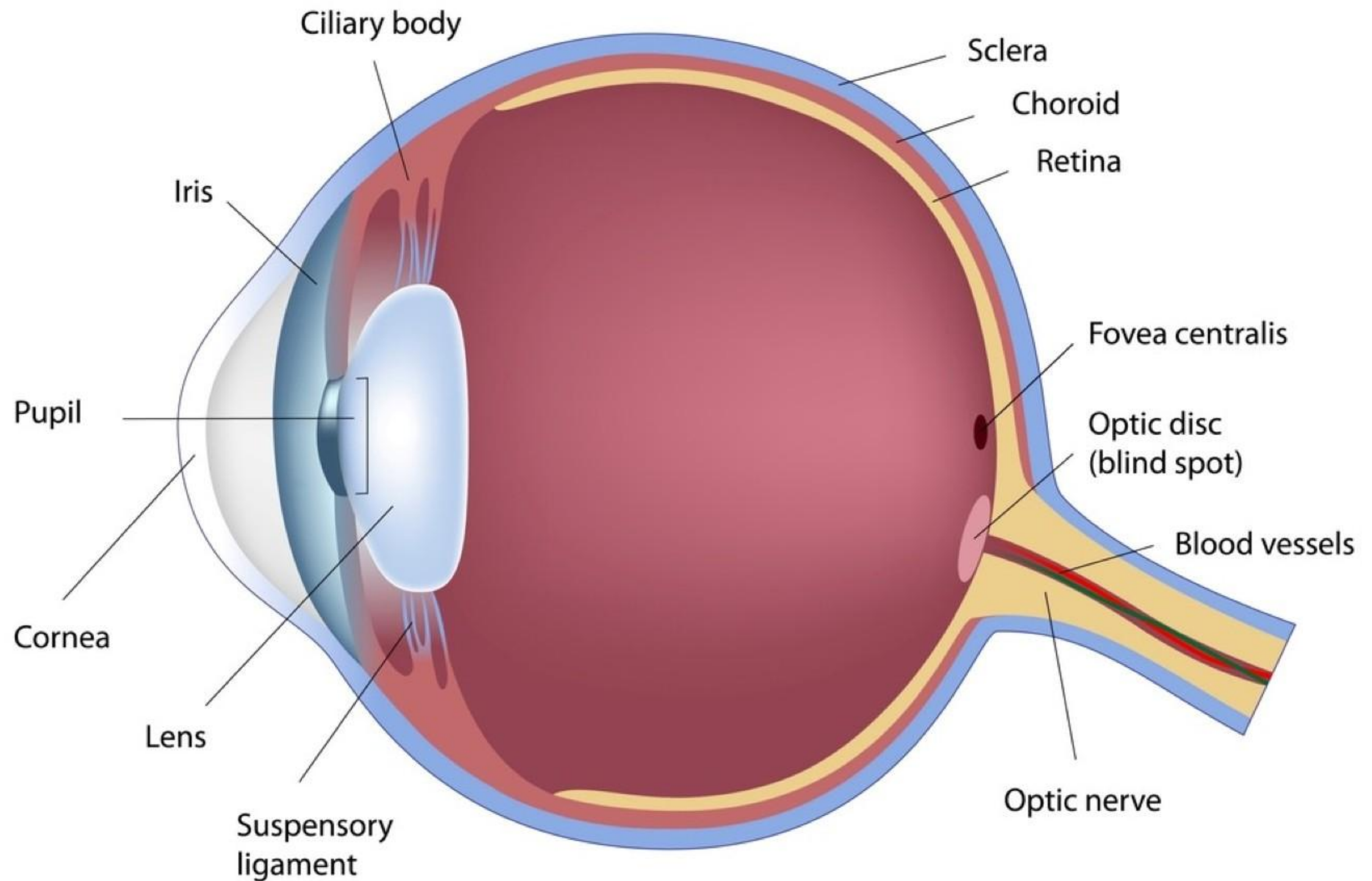
CIE RGB Color Matching Functions

Graph plots how much of each CIE RGB primary light must be combined to match a monochromatic light of wavelength given on x-axis



Biological Basis of Color

Anatomy of The Human Eye



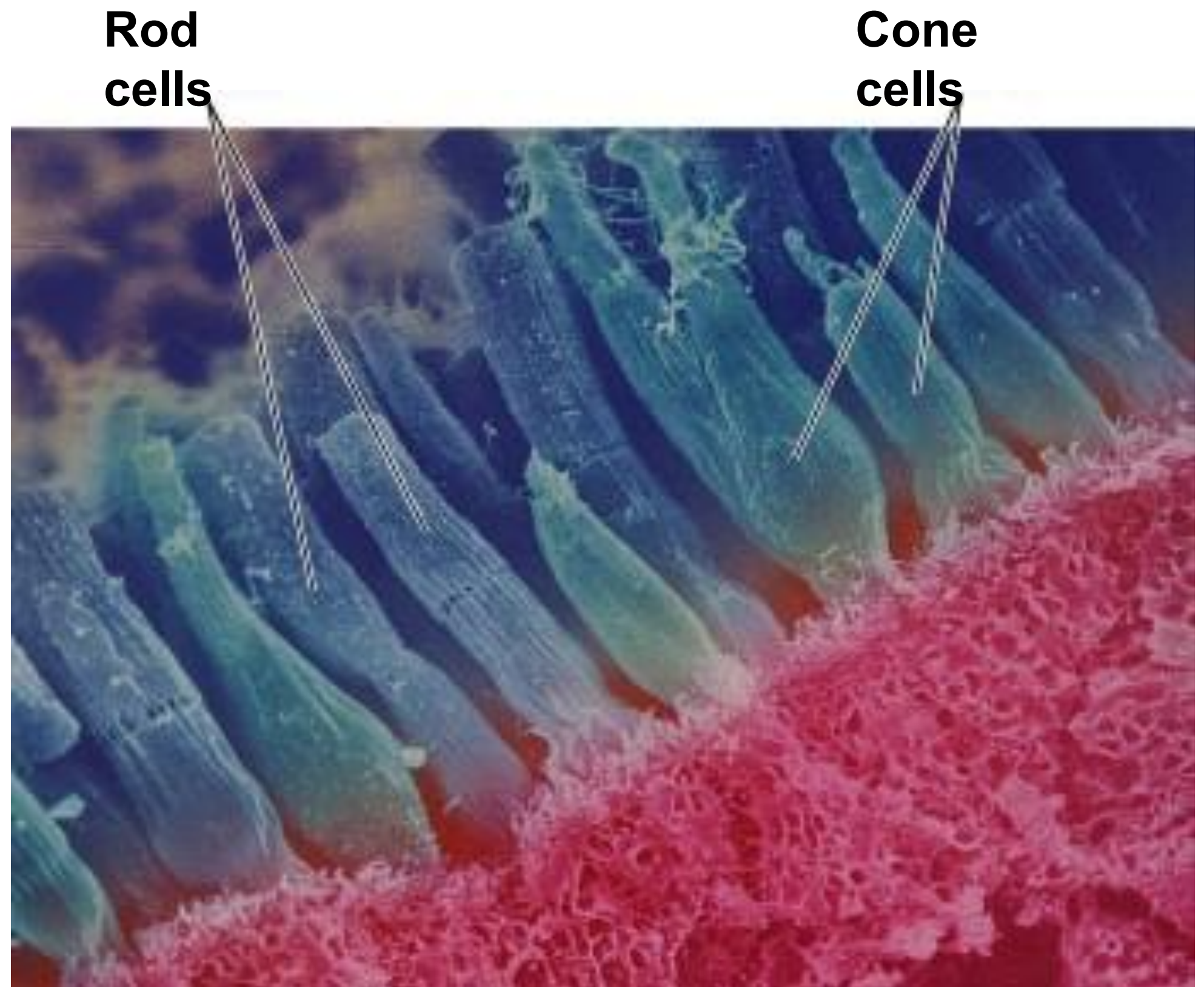
Retinal Photoreceptor Cells: Rods and Cones

Rods are primary receptors in very low light (“scotopic” conditions), e.g. dim moonlight

- ~120 million rods in eye
- Perceive only shades of gray, no color

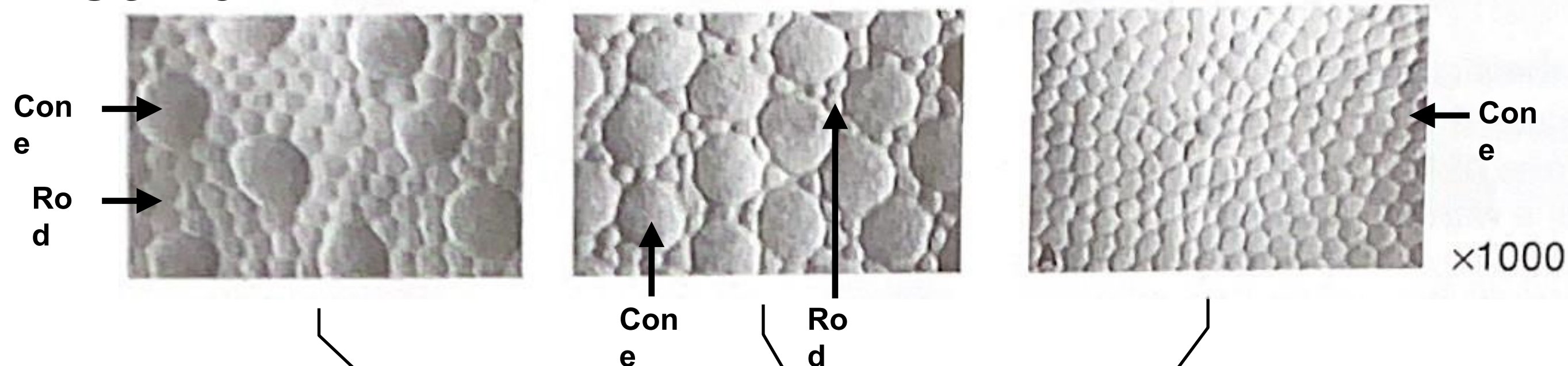
Cones are primary receptors in typical light levels (“photopic”)

- ~6-7 million cones in eye
- Three types of cones, each with different spectral sensitivity

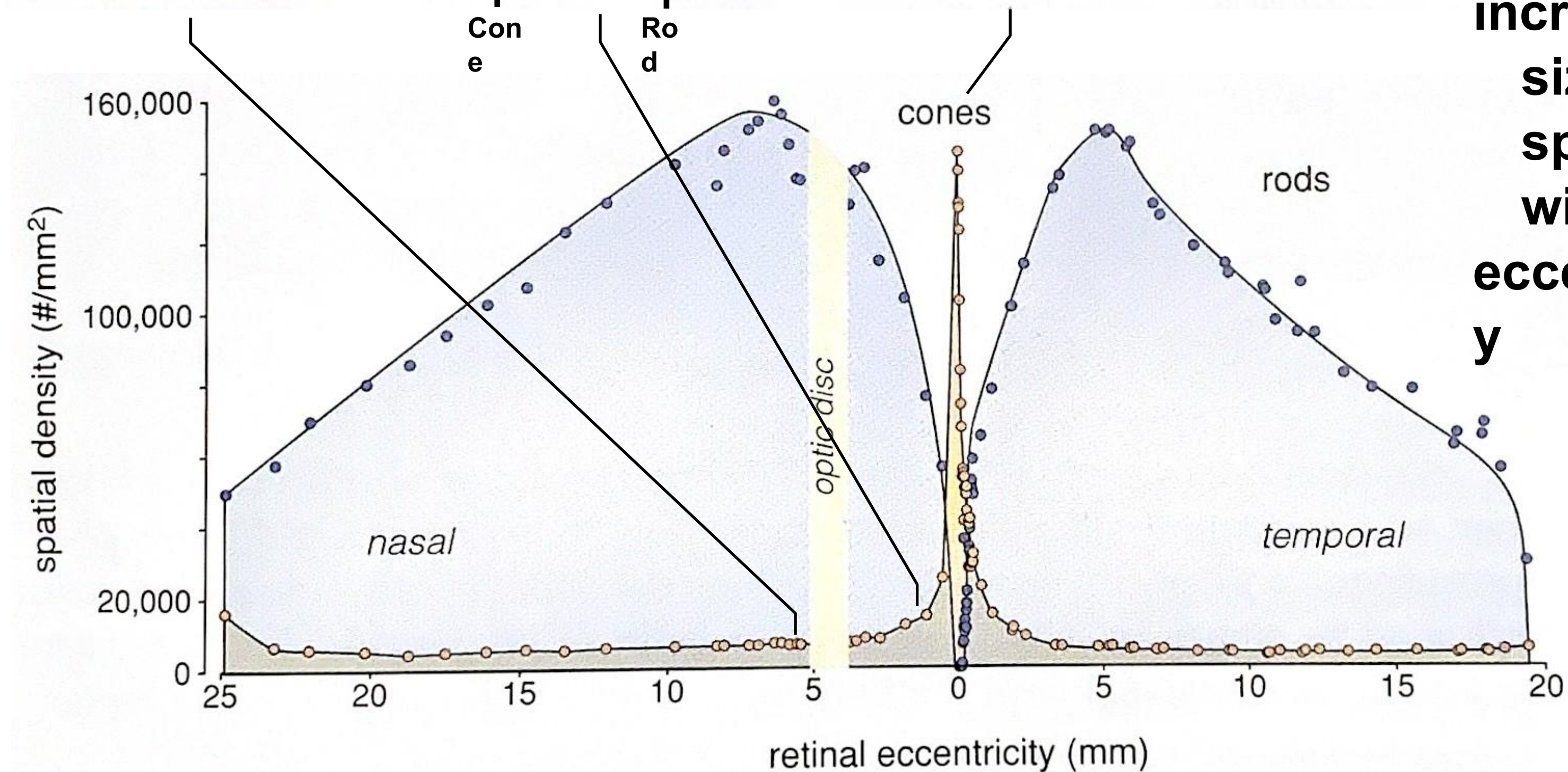


<http://ebooks.bfwpub.com/life.php> Figure 45.18

Photoreceptor Size and Distribution Vary Across Retina

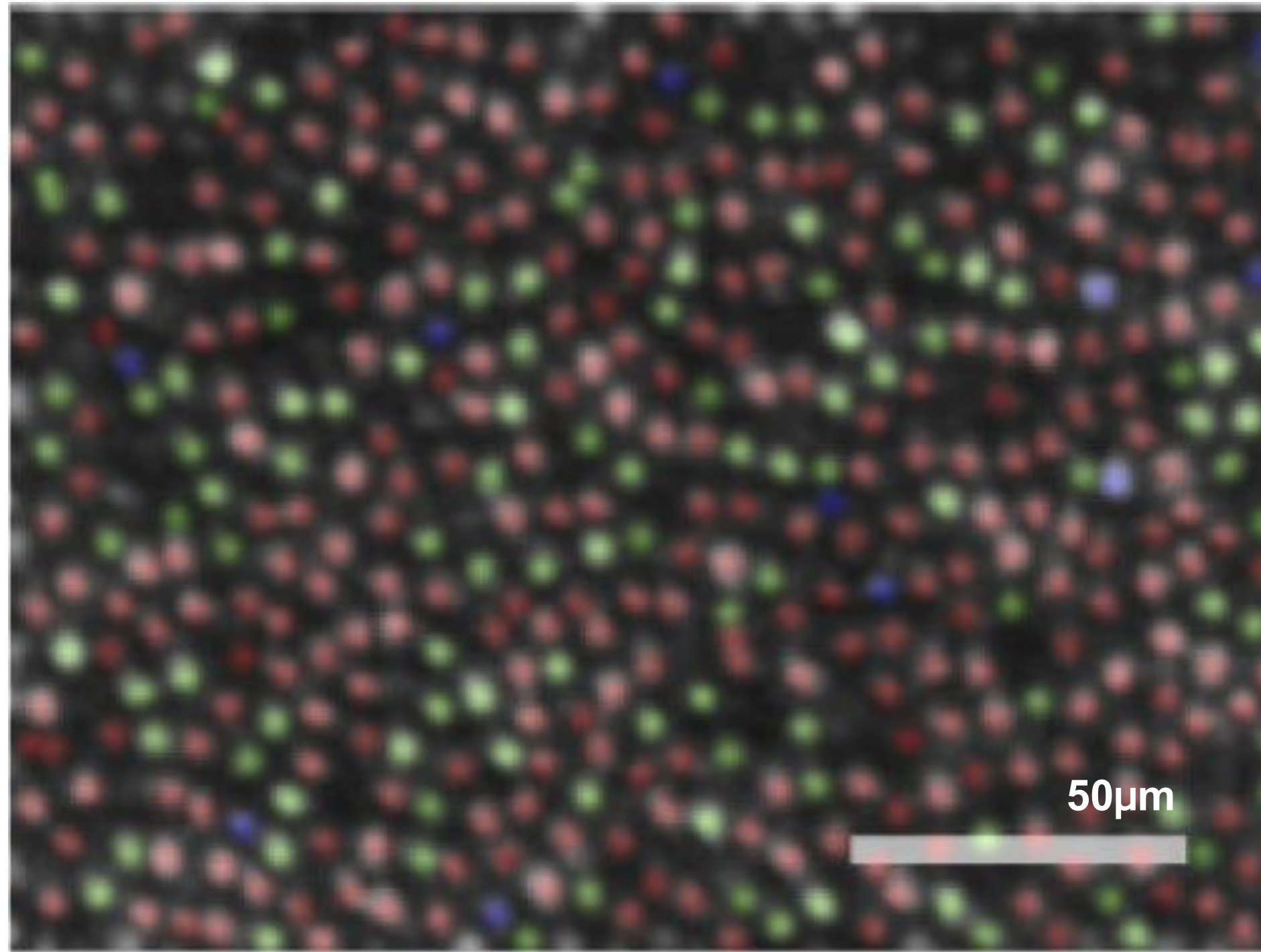


- No rods in fovea
- Cones increase in size and spacing with eccentricity



after Østerberg, 1935; as modified by Rodieck, 1988

On the Retina, Three Types of Cone Cells



Sabesan Lab, UW. Pandiyan et al.
2020.

Three types of cone cells: S, M, and L (corresponding to peak response at short, medium, and long wavelengths)

Ren Ng

Credit:

<http://depts.washington.edu/sabaolab/>

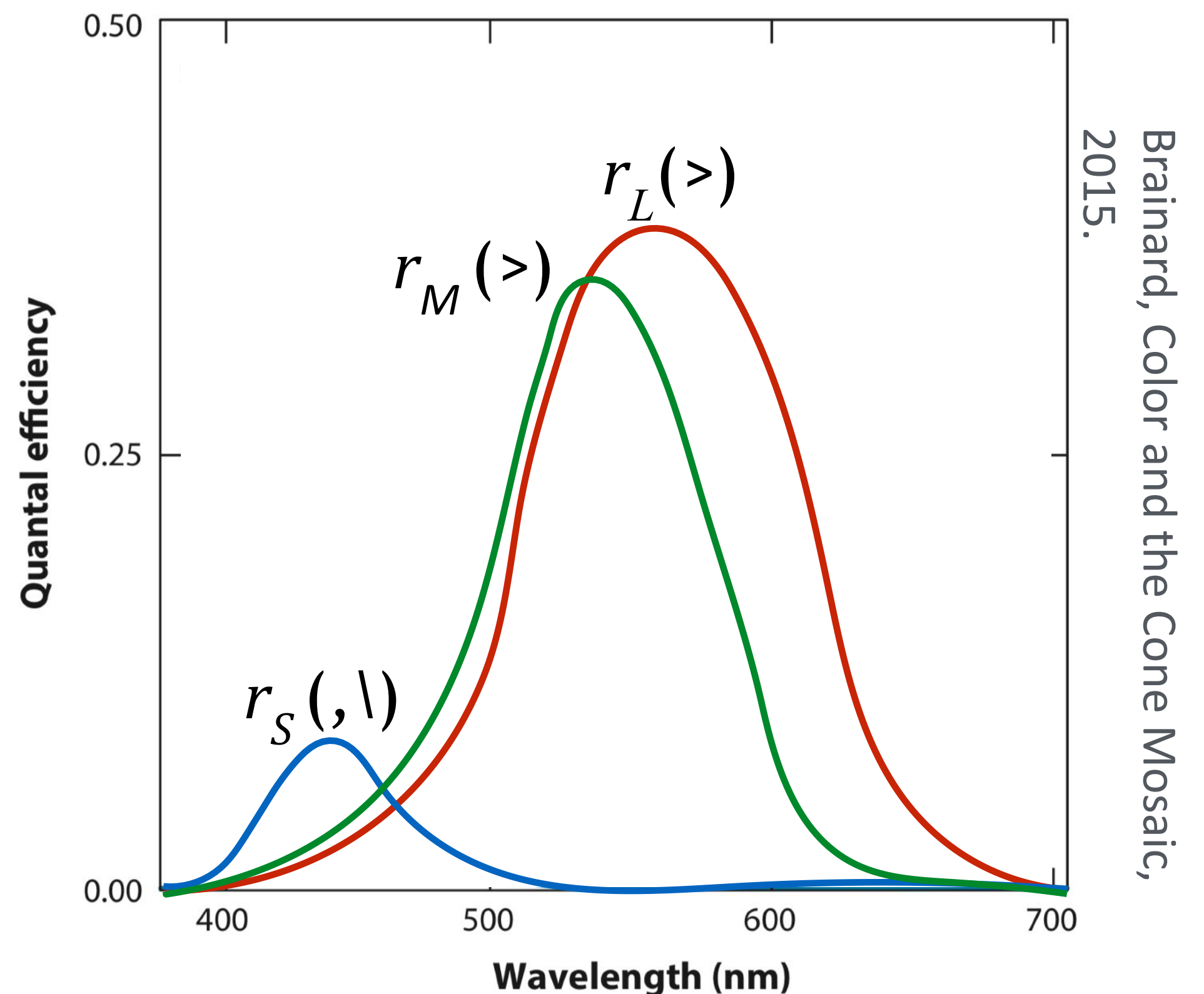
Spectral Response of Human Cone Cells

Instead of one detector as before, now we have three detectors (S, M, L cone cells), each with a different spectral response curve

$$S = \int r_S(\lambda) s(\lambda) d\lambda$$

$$M = \int r_M(\lambda) s(\lambda) d\lambda$$

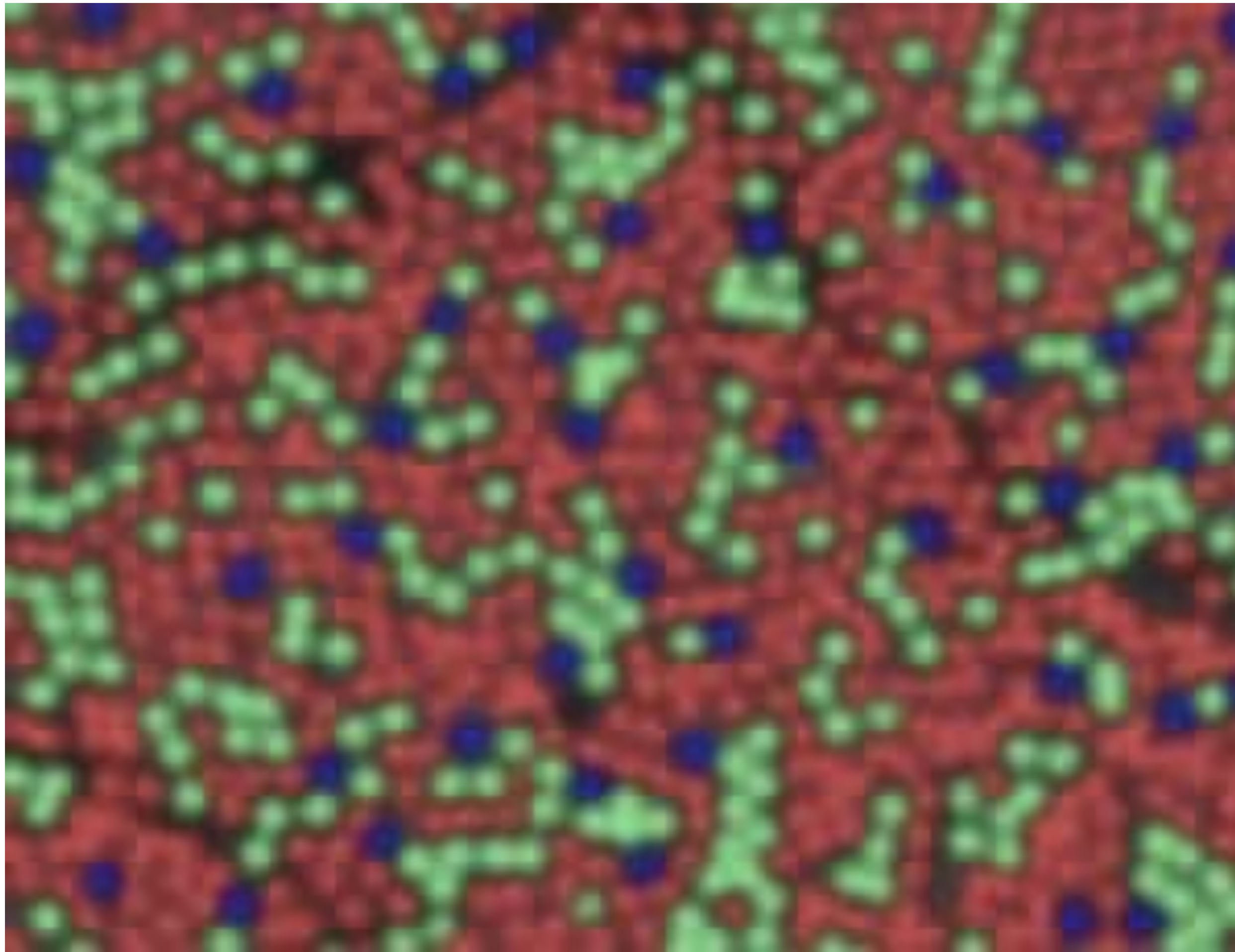
$$L = \int r_L(\lambda) s(\lambda) d\lambda$$



Example: Spectral Response of Human Cone Cells

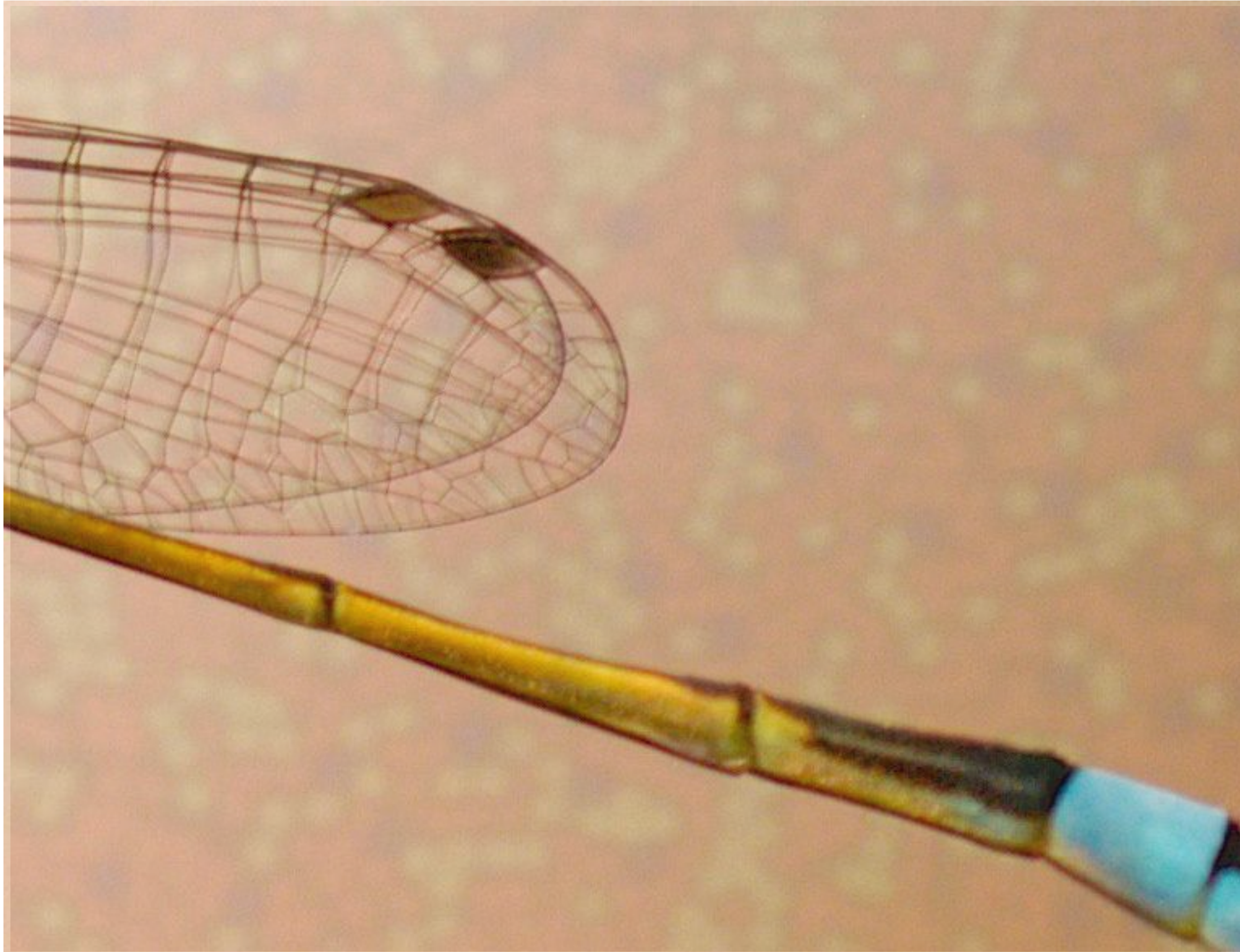


Example: Spectral Response of Human Cone Cells



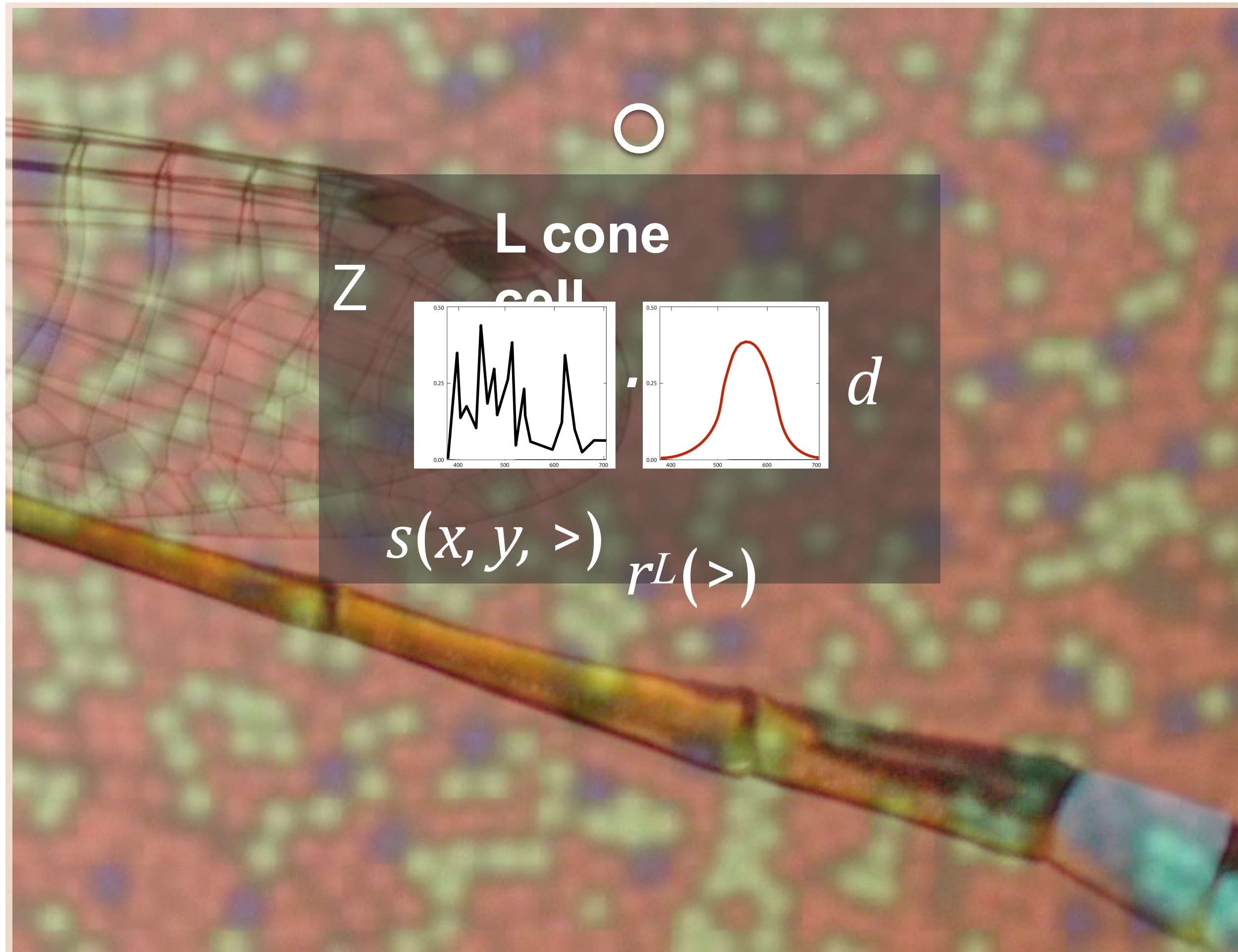
Credit: Sabesan,
<http://depts.washington.edu/sabaolab/>

Example: Spectral Response of Human Cone Cells



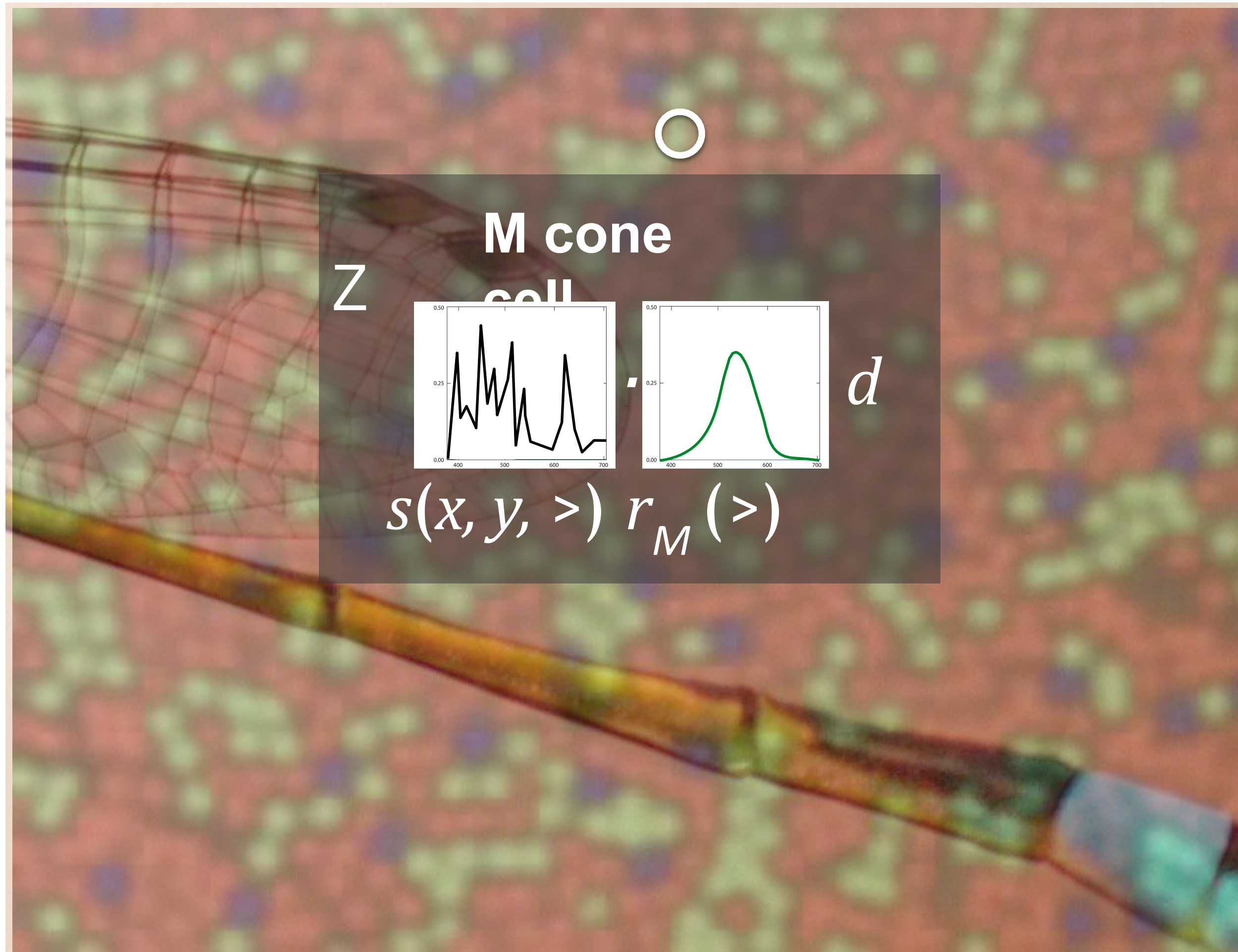
Credit: Sabesan,
<http://depts.washington.edu/sabaolab/>

Example: Spectral Response of Human Cone Cells



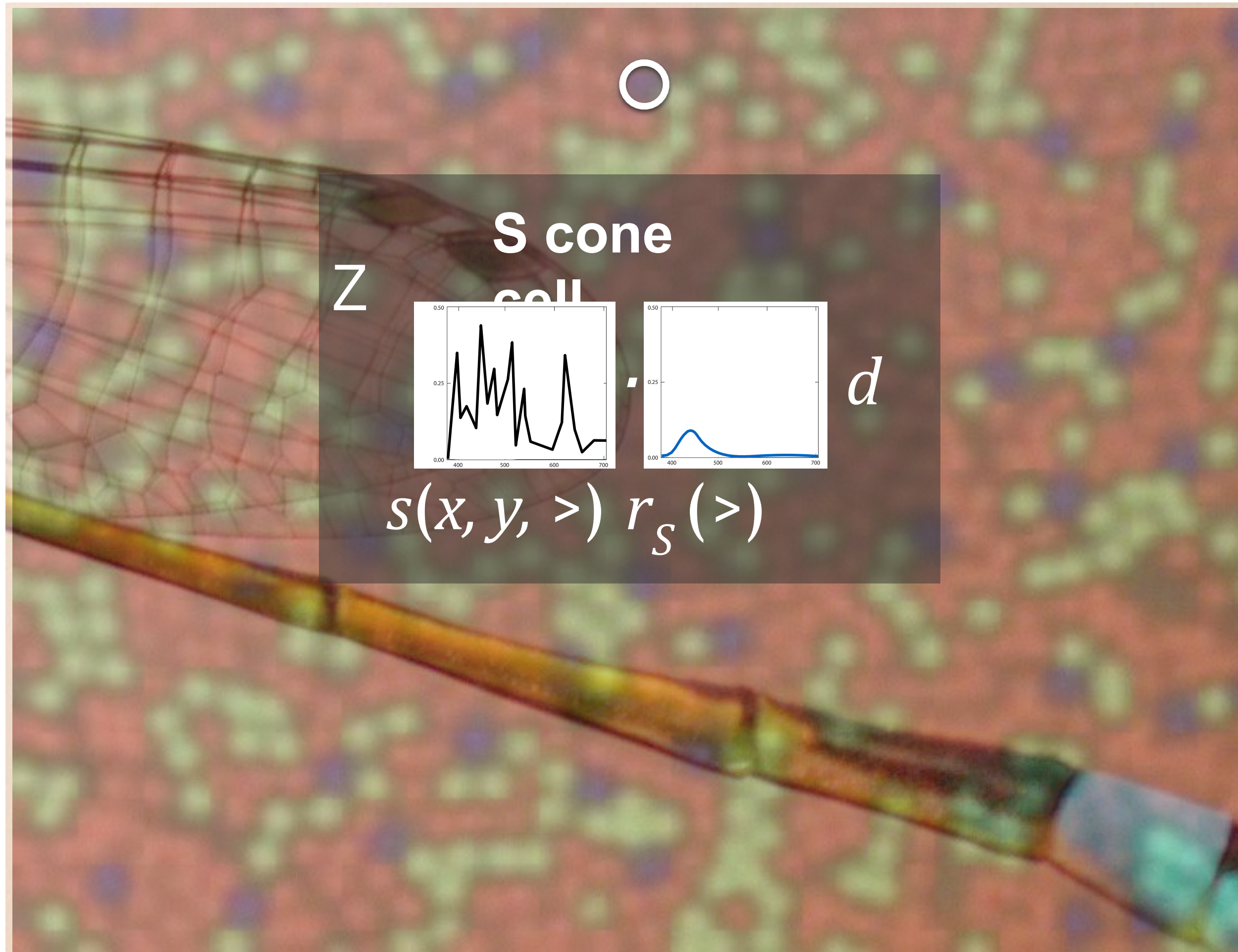
Credit: Sabesan,
<http://depts.washington.edu/sabaolab/>

Example: Spectral Response of Human Cone Cells



Credit: Sabesan,
<http://depts.washington.edu/sabaolab/>

Example: Spectral Response of Human Cone Cells



Credit: Sabesan,
<http://depts.washington.edu/sabaolab/>

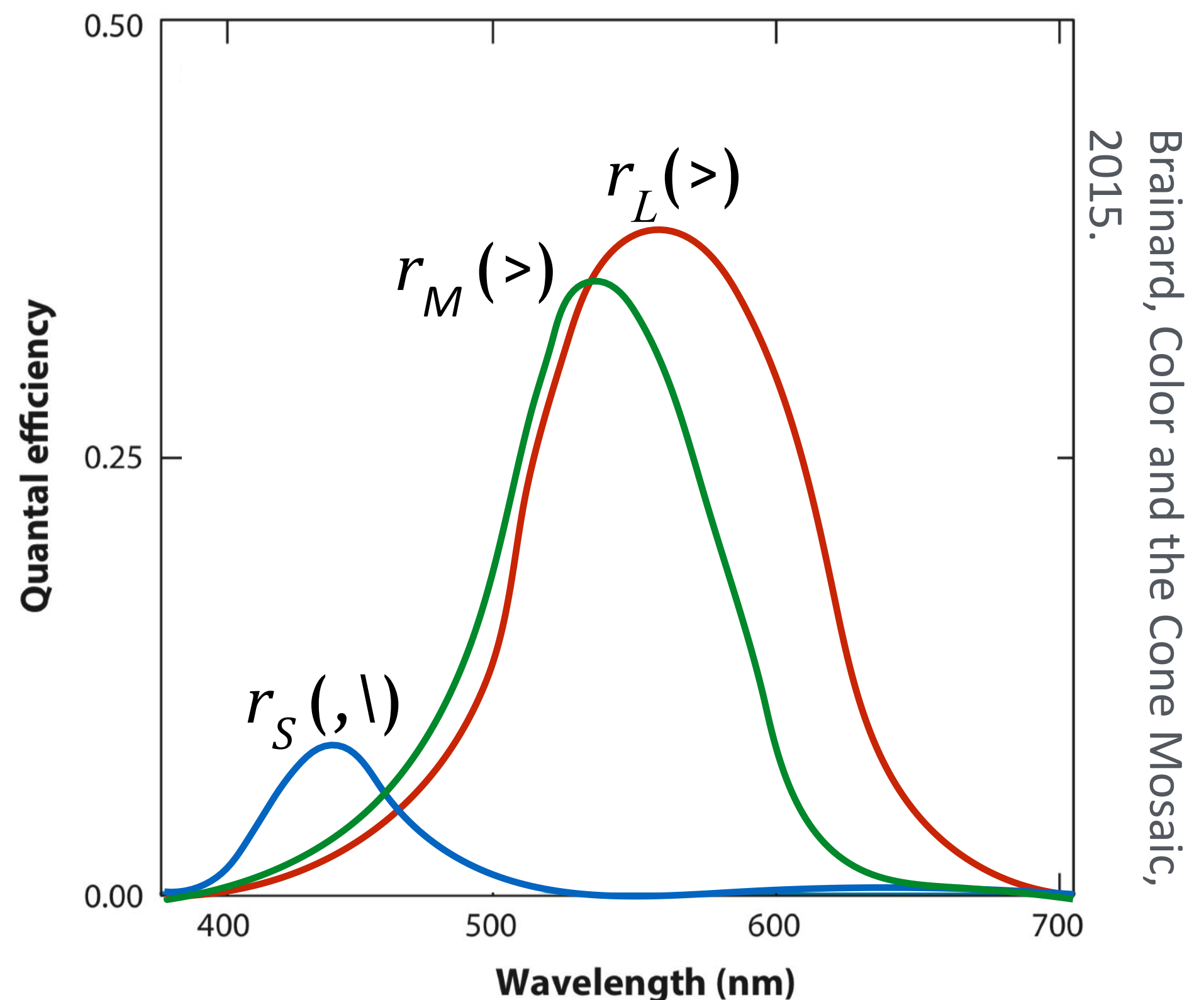
Spectral Response of Human Cone Cells

Instead of one detector as before, now we have three detectors (S, M, L cone cells), each with a different spectral response curve

$$S = \int r_S(\lambda) s(\lambda) d\lambda$$

$$M = \int r_M(\lambda) s(\lambda) d\lambda$$

$$L = \int r_L(\lambda) s(\lambda) d\lambda$$



Spectral Response of Human Cone Cells

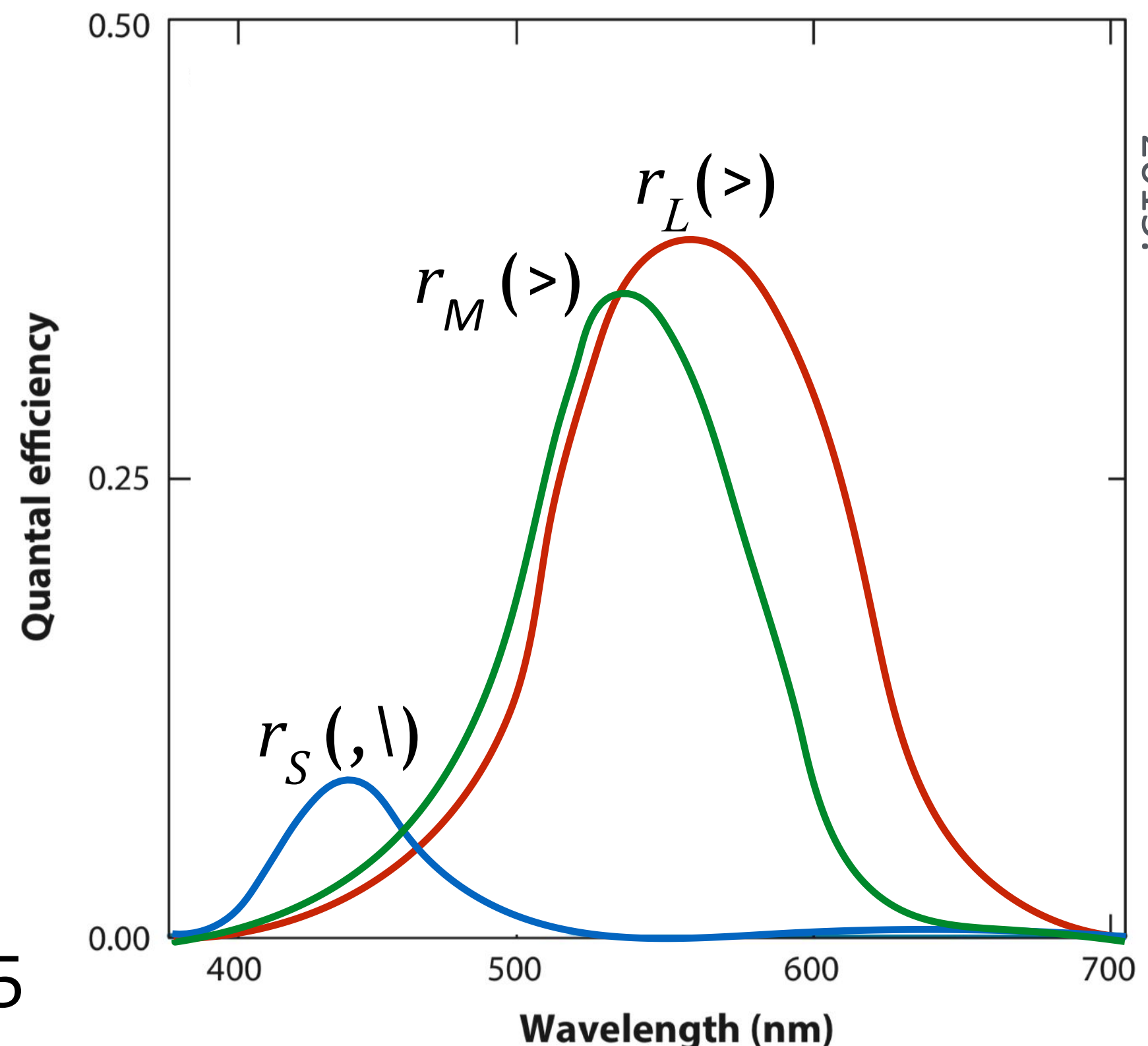
Instead of one detector as before, now we have three detectors (S, M, L cone cells), each with a different spectral response curve

Written as vector dot products:

$$\begin{aligned} S &= r_S \cdot s \\ M &= r_M \cdot s \\ L &= r_L \cdot s \end{aligned}$$

Matrix formulation:

$$\begin{bmatrix} S \\ M \\ L \end{bmatrix} = \begin{bmatrix} r_S \\ r_M \\ r_L \end{bmatrix} \cdot s$$



Brainard, Color and the Cone Mosaic, 2015.

Dimensionality Reduction From ∞ to 3

At each position on the human retina:

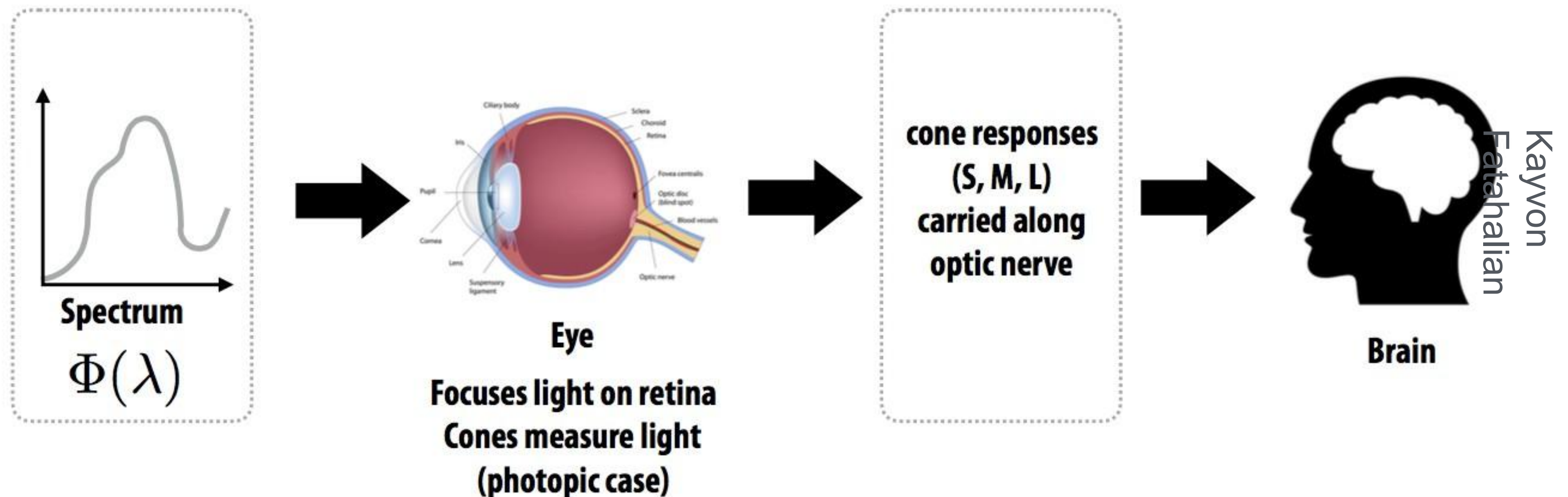
- **SPD is a function of wavelength (∞ - dimensional signal)**
- **3 types of cones near that position produce three scalar values (3 - dimensional signal)**

What about 2D images?

- **The dimensionality reduction described above is happening at every 2D position in our visual field**

The Human Visual System

- Human eye does not measure and brain does not receive information about each wavelength of light
- Rather, the eye measures three response values only (S, M, L) at each position in visual field, and this is only spectral info available to brain



Metamerism

Metamers

Metameters are two different spectra (∞ -dim) that project to the same (S,M,L) (3-dim) response.

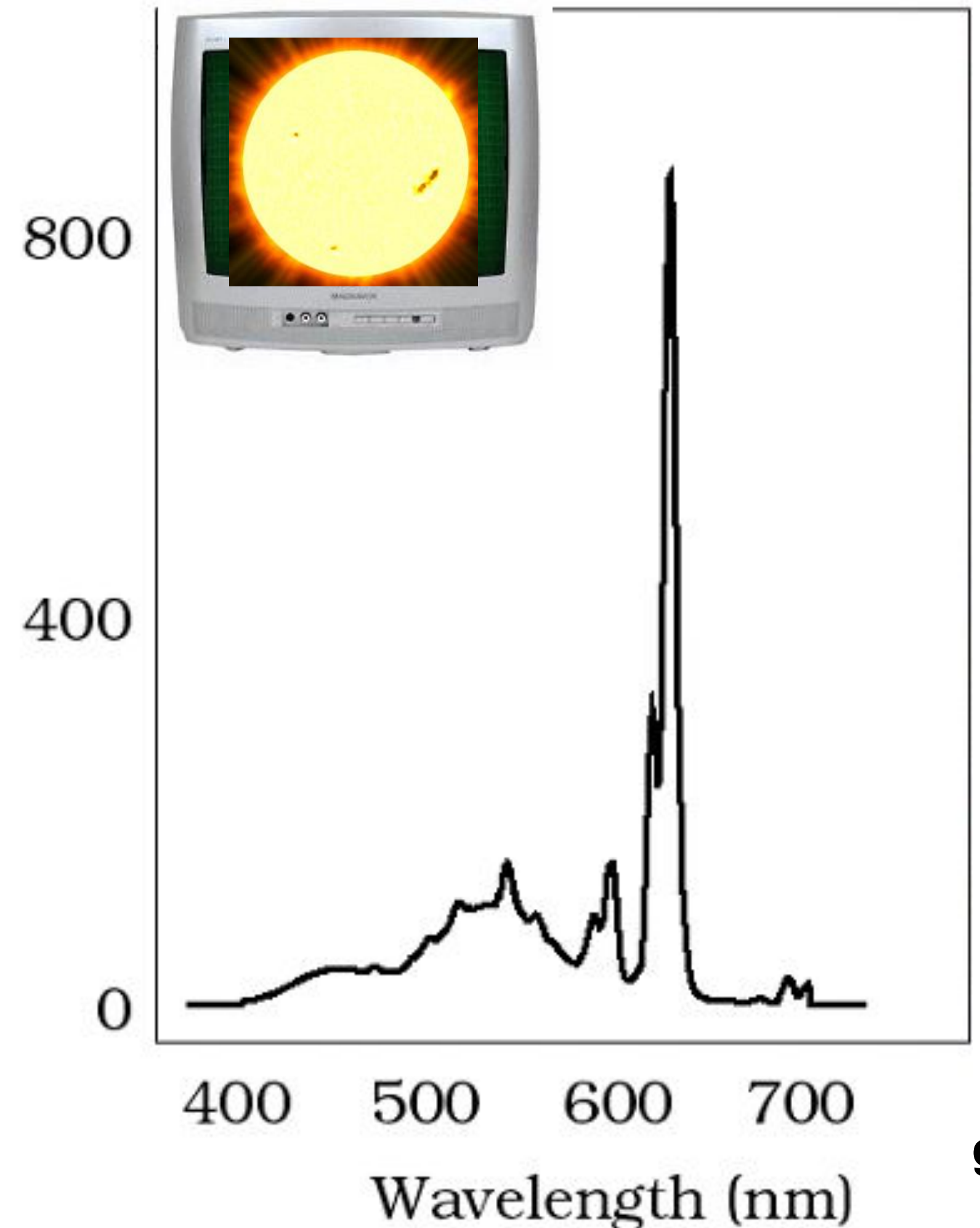
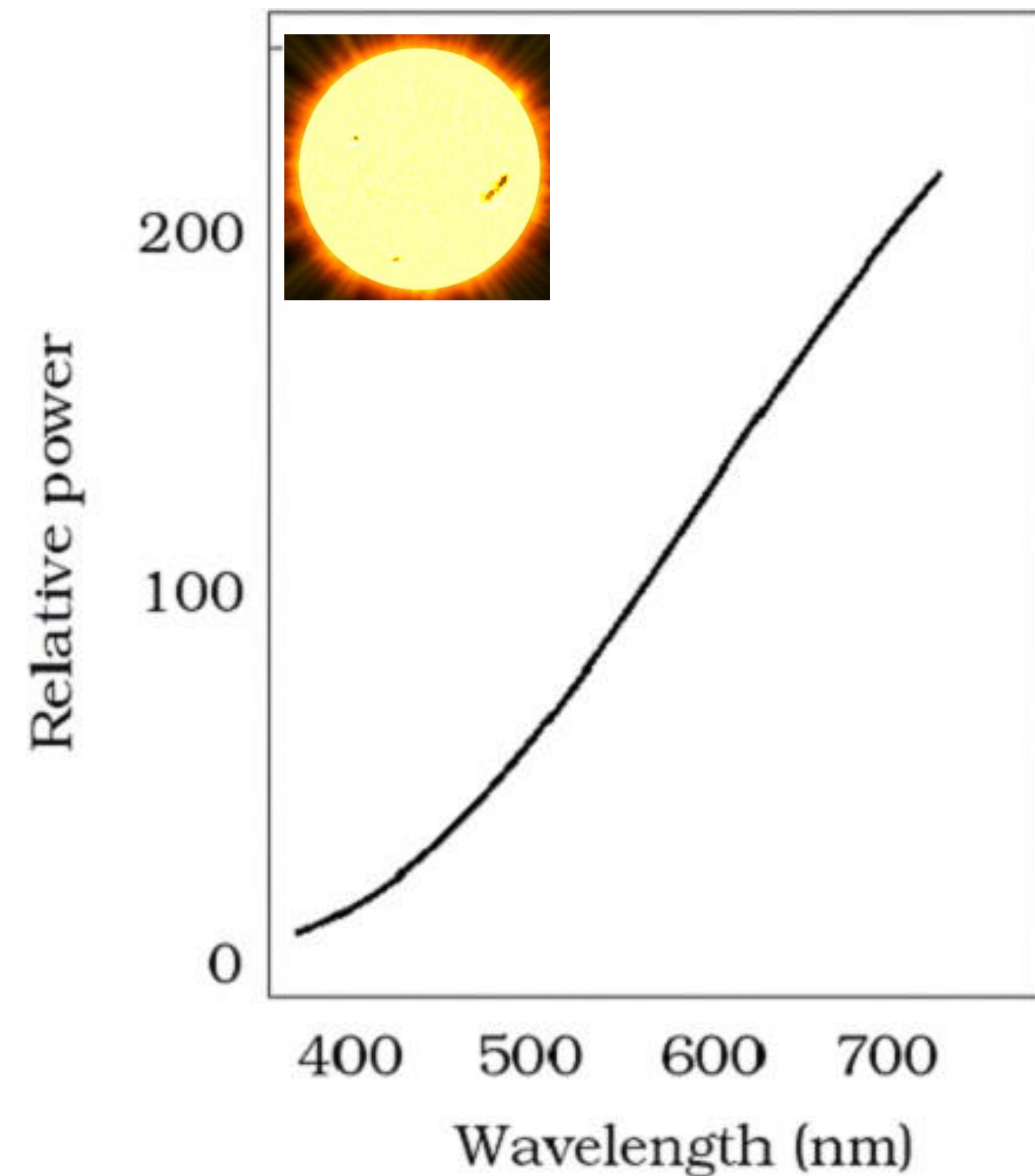
- **These will appear to have the same color to a human**

The existence of metamers is critical to color reproduction

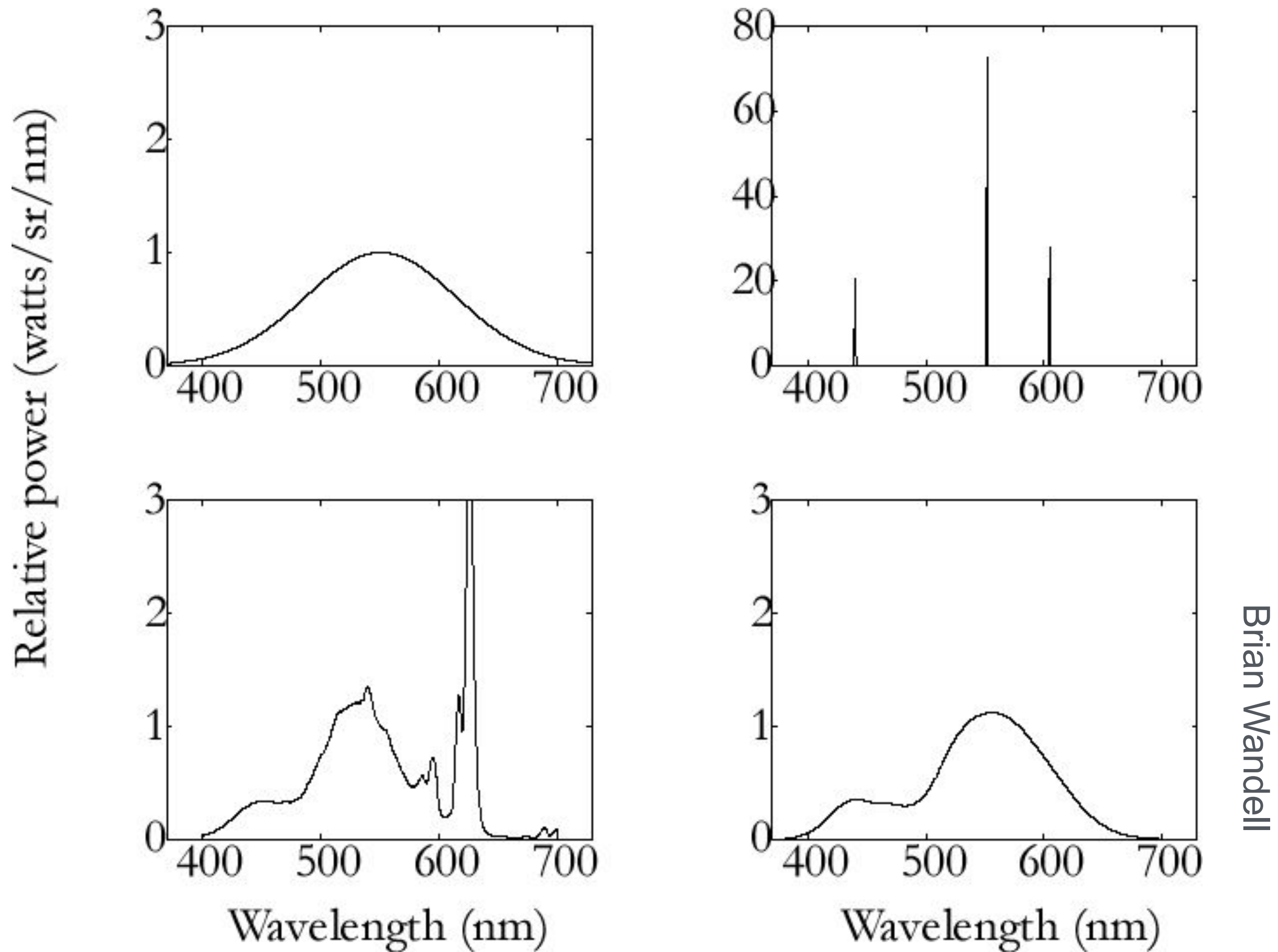
- **Don't have to reproduce the full spectrum of a real world scene**
- **Example: A metamer can reproduce the perceived color of a real-world scene on a display with pixels of only three colors**

Metamerism

Color matching is an important illusion that is understood quantitatively

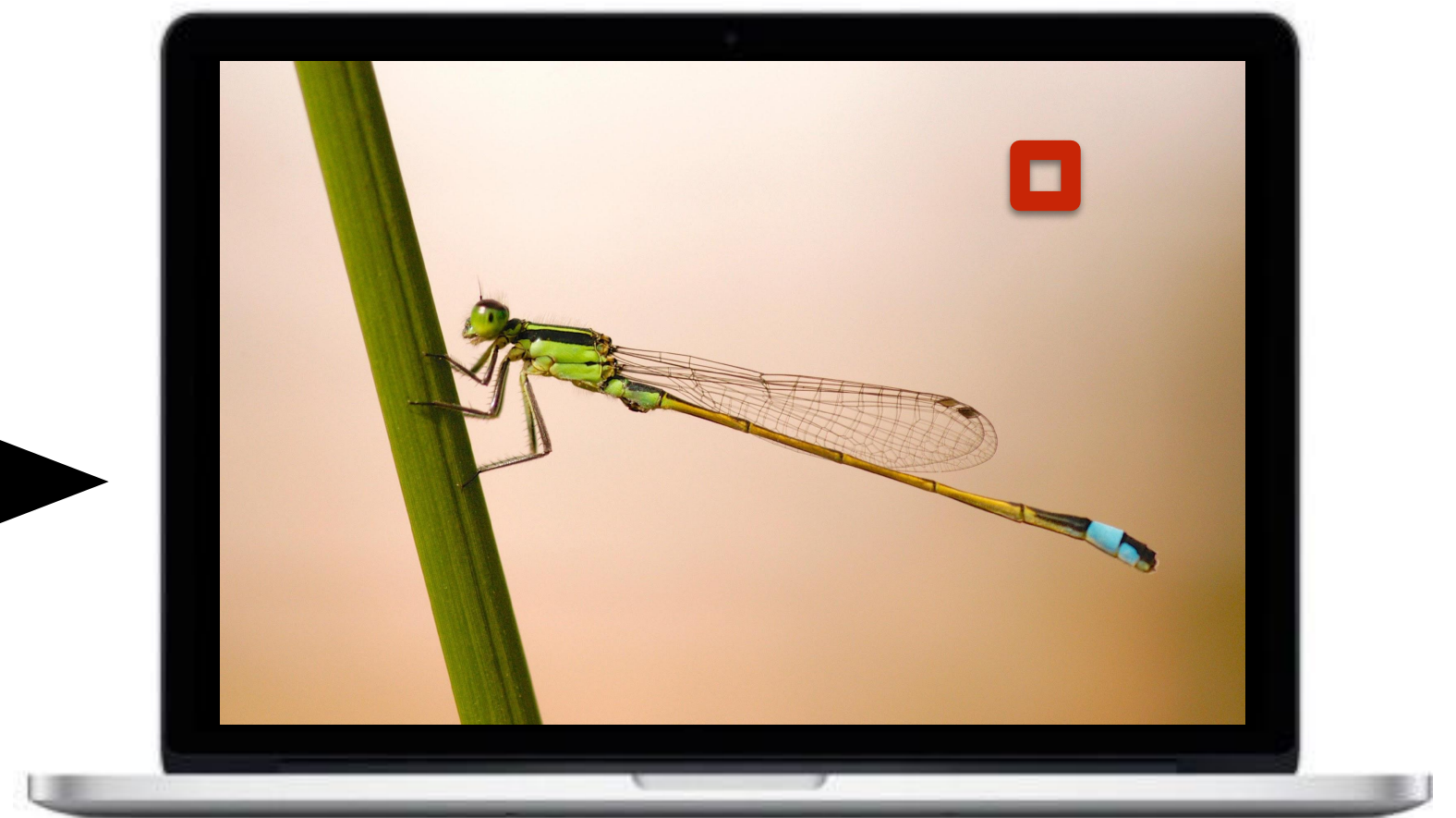
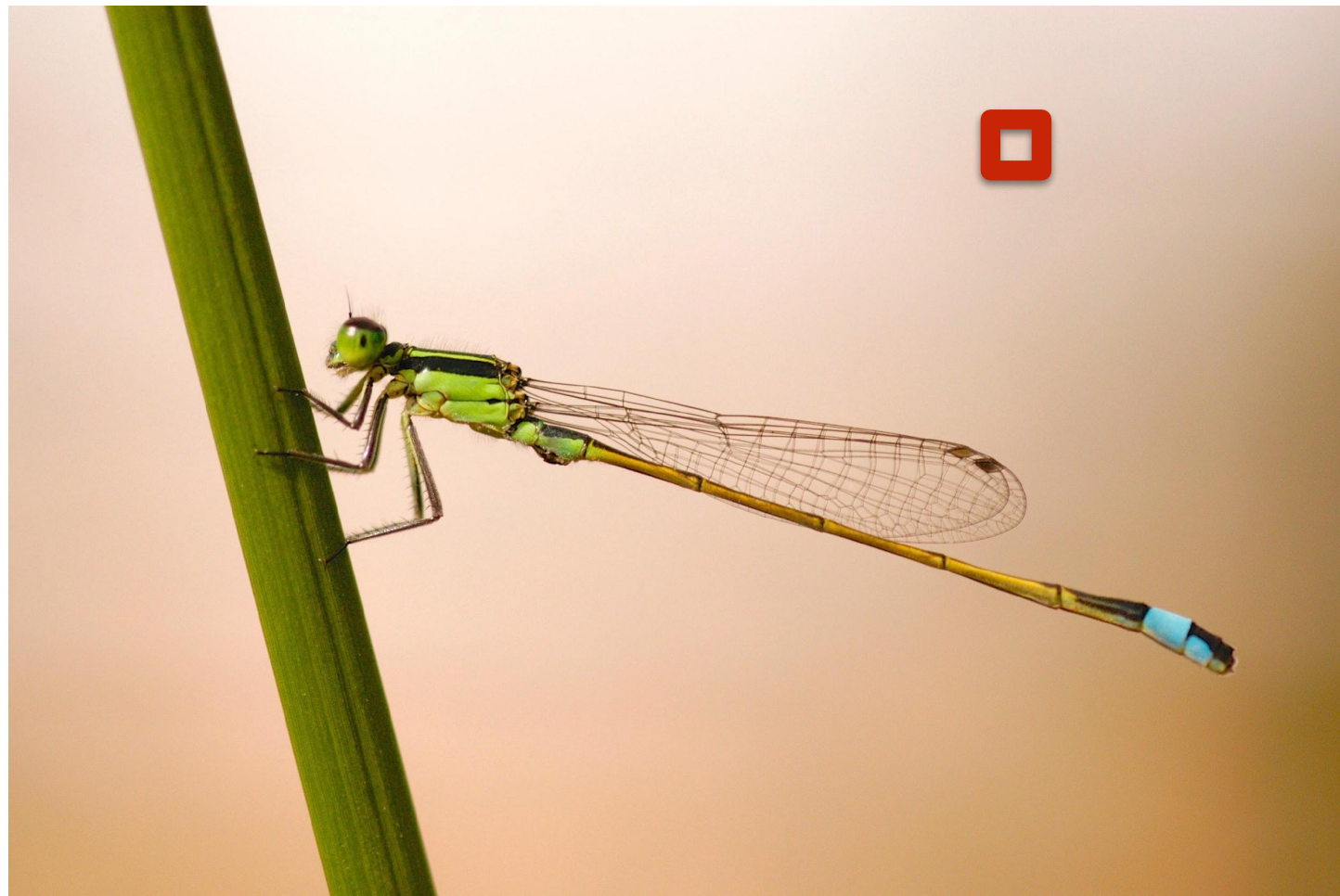


Metamerism is a Big Effect



Color Reproduction

Color Reproduction Problem



Target real spectrum
 $s(\lambda)$

Display outputs spectrum
 $R s_R(\lambda) + G s_G(\lambda) + B s_B(\lambda)$

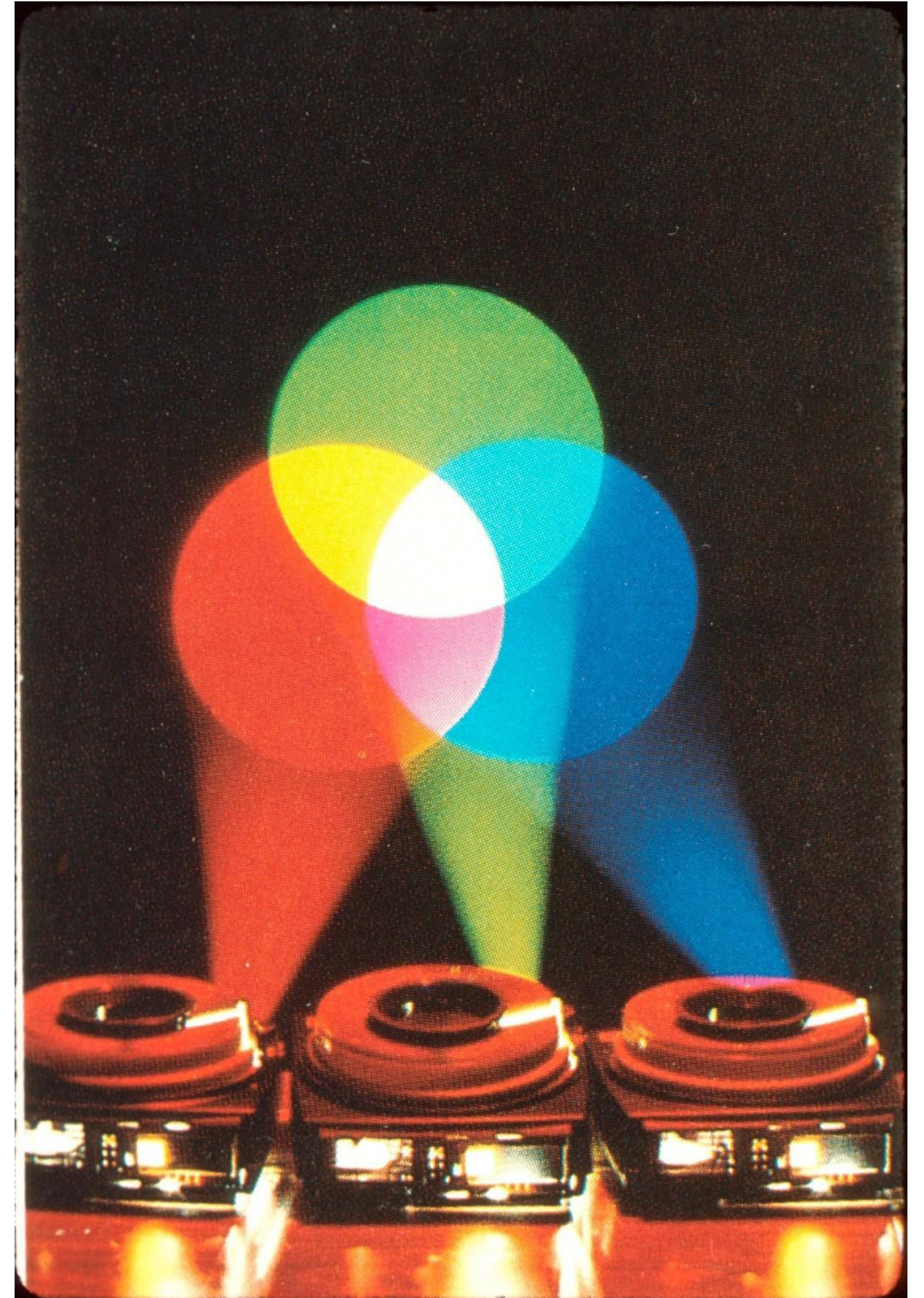
Goal: at each pixel, choose R, G, B values for display so that the output color matches the appearance of the target color in the real world.

Additive Color

- Given a set of primary lights, each with its own spectral distribution (e.g. R,G,B display pixels):

$$s_R(>), s_G(>), s_B(>)$$

- We can adjust the brightness of these lights and add them together to produce a linear subspace of spectral distribution: $R s_R(>) + G s_G(>) + B s_B(>)$
- The color is now described by the scalar values:

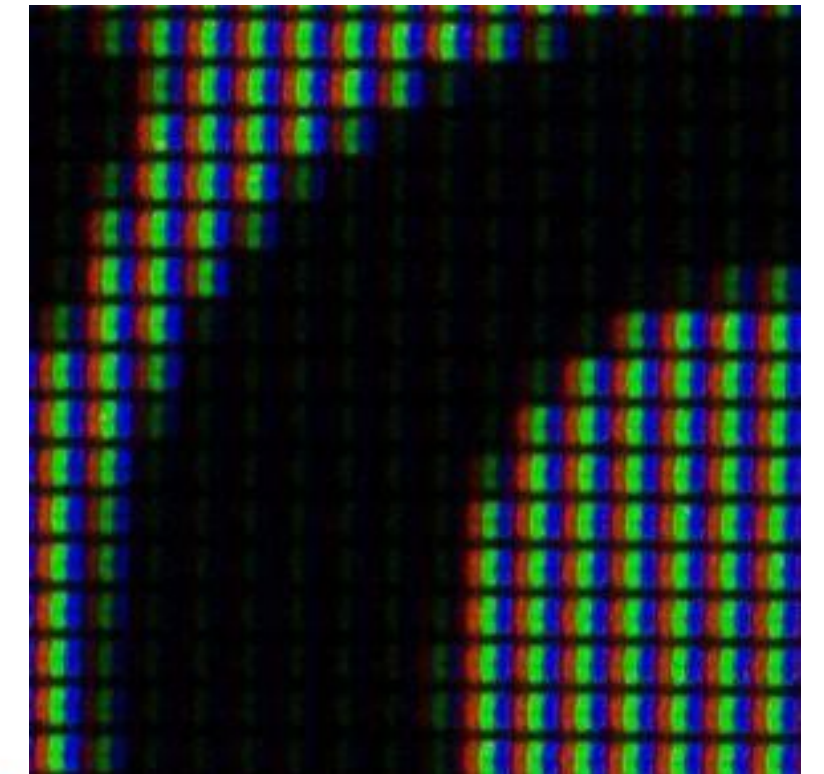
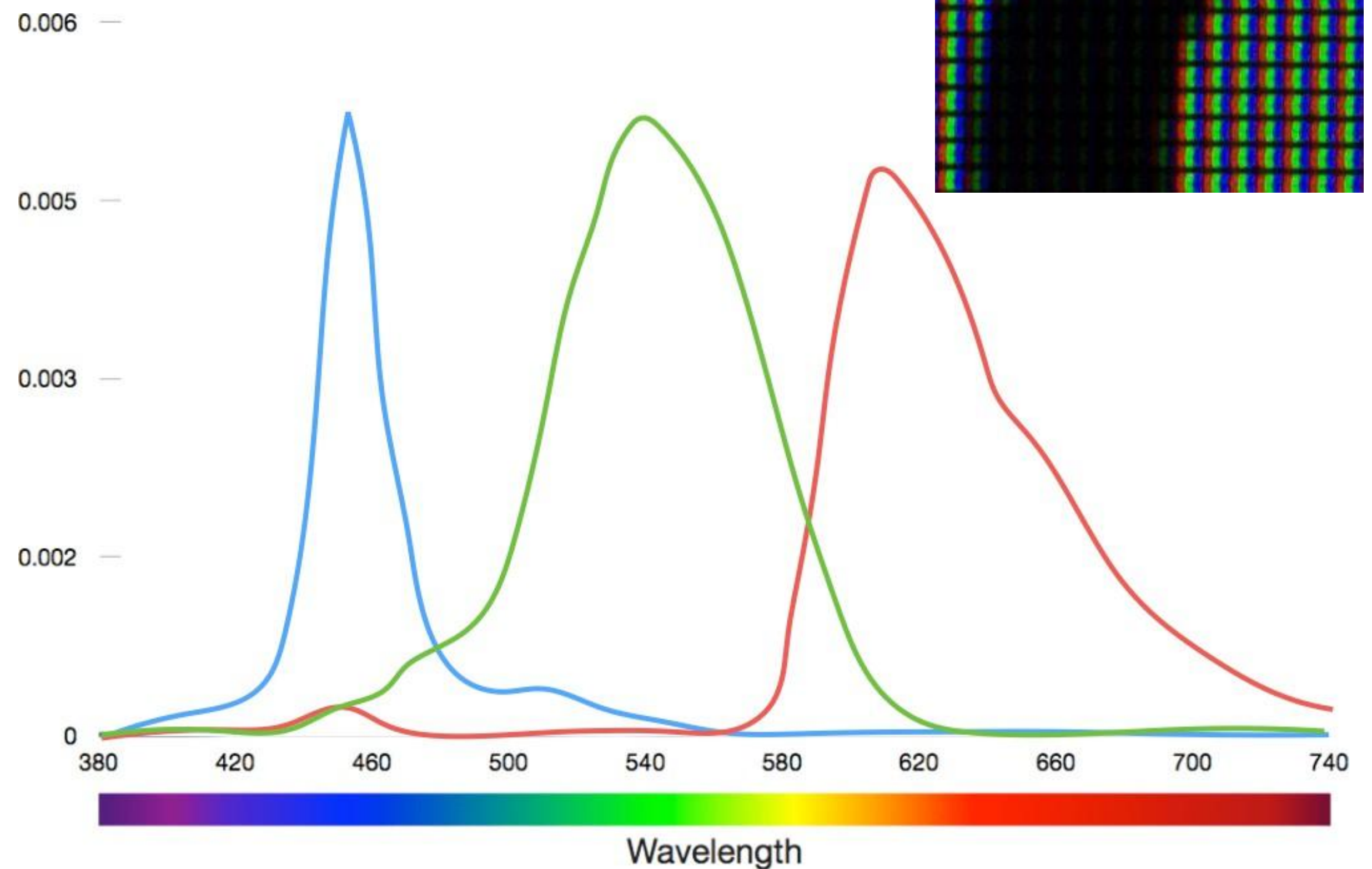


Example RGB Emission Spectra ("Color Primaries") for Phone Display

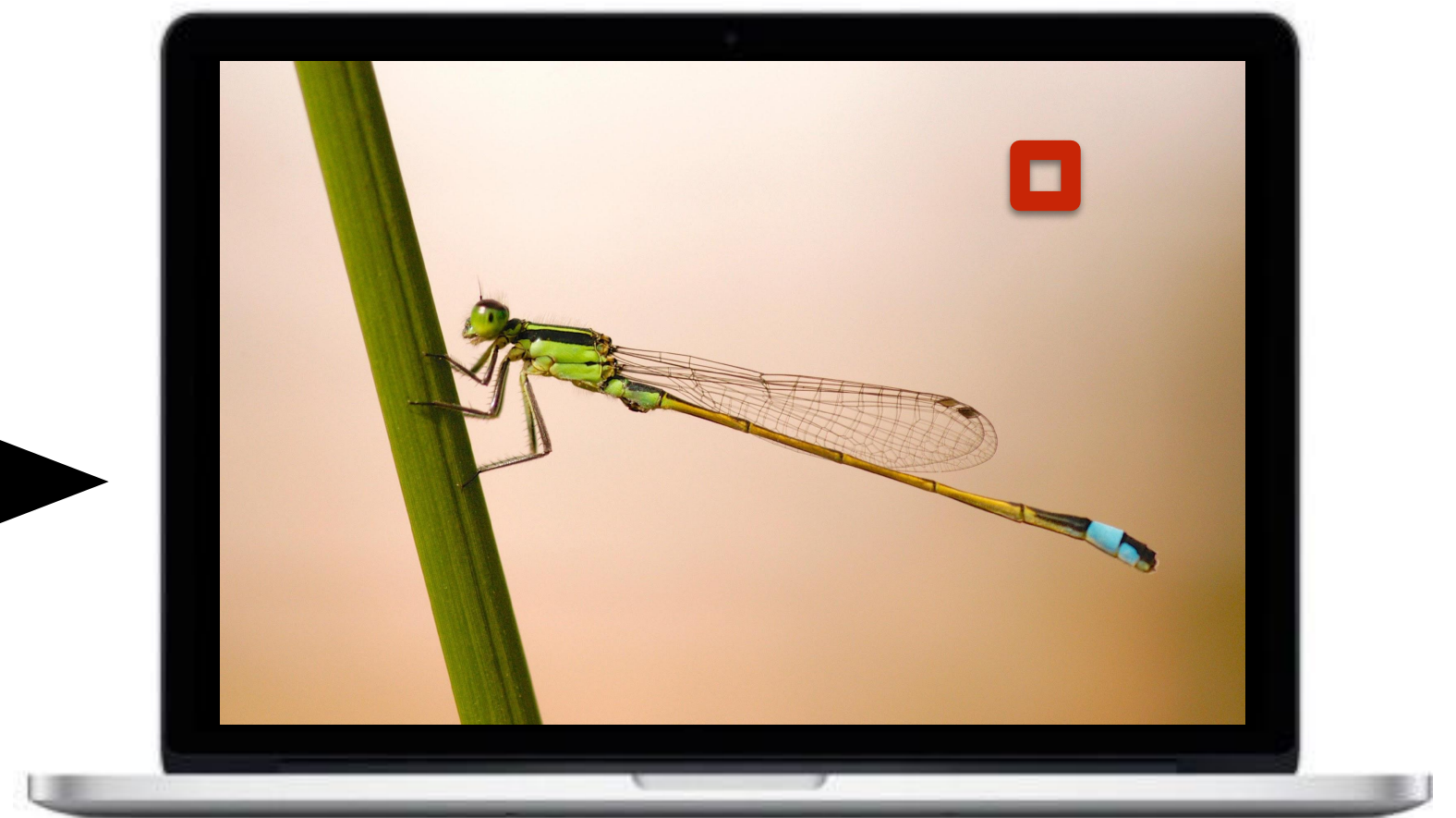
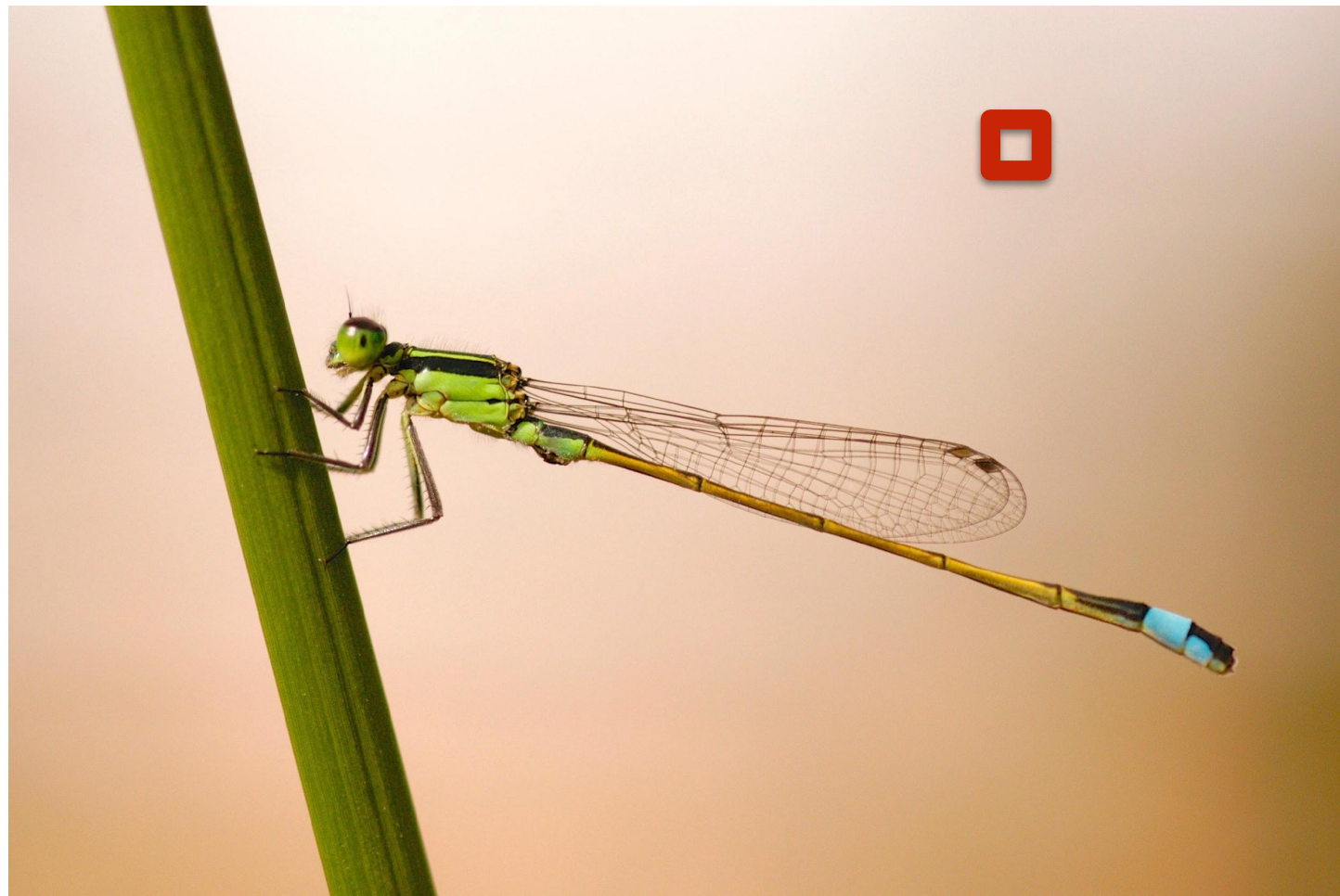


RGB pixel spectra (iPhone 5)

Credit: Yurek, <https://dot-color.com/tag/color-2/page/2/>



Color Reproduction Problem



Target real spectrum
 $s(\lambda)$

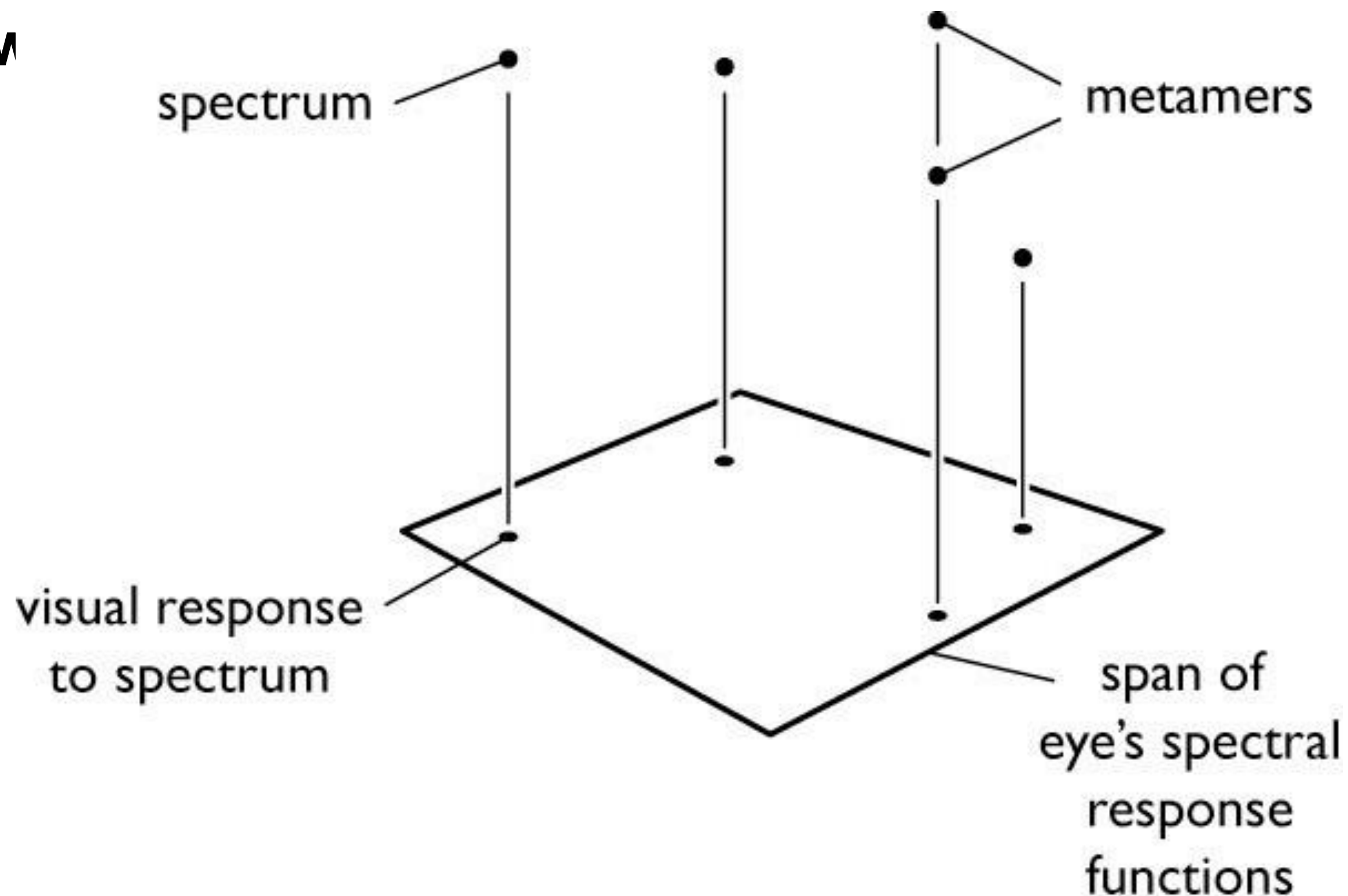
Display outputs spectrum
 $R s_R(\lambda) + G s_G(\lambda) + B s_B(\lambda)$

Goal: at each pixel, choose R, G, B values for display so that the output color matches the appearance of the target color in the real world.

Pseudo-Geometric Interpretation

We are projecting a high dimensional vector (wavelength spectrum function) onto a low-dimensional subspace (SML visual response)

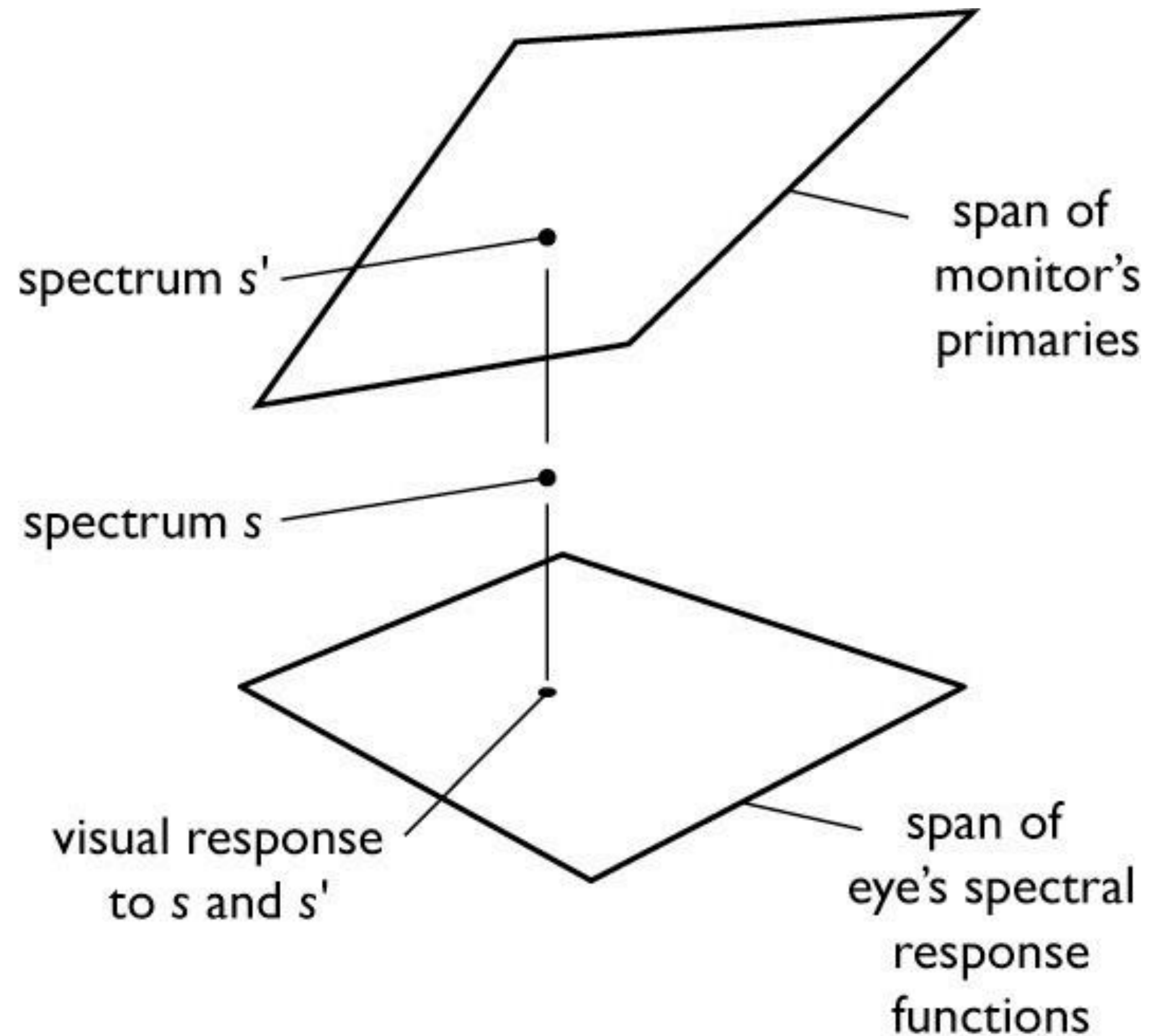
- Differences that are perpendicular to the basis vectors of the low



Slide credit: Steve Marschner

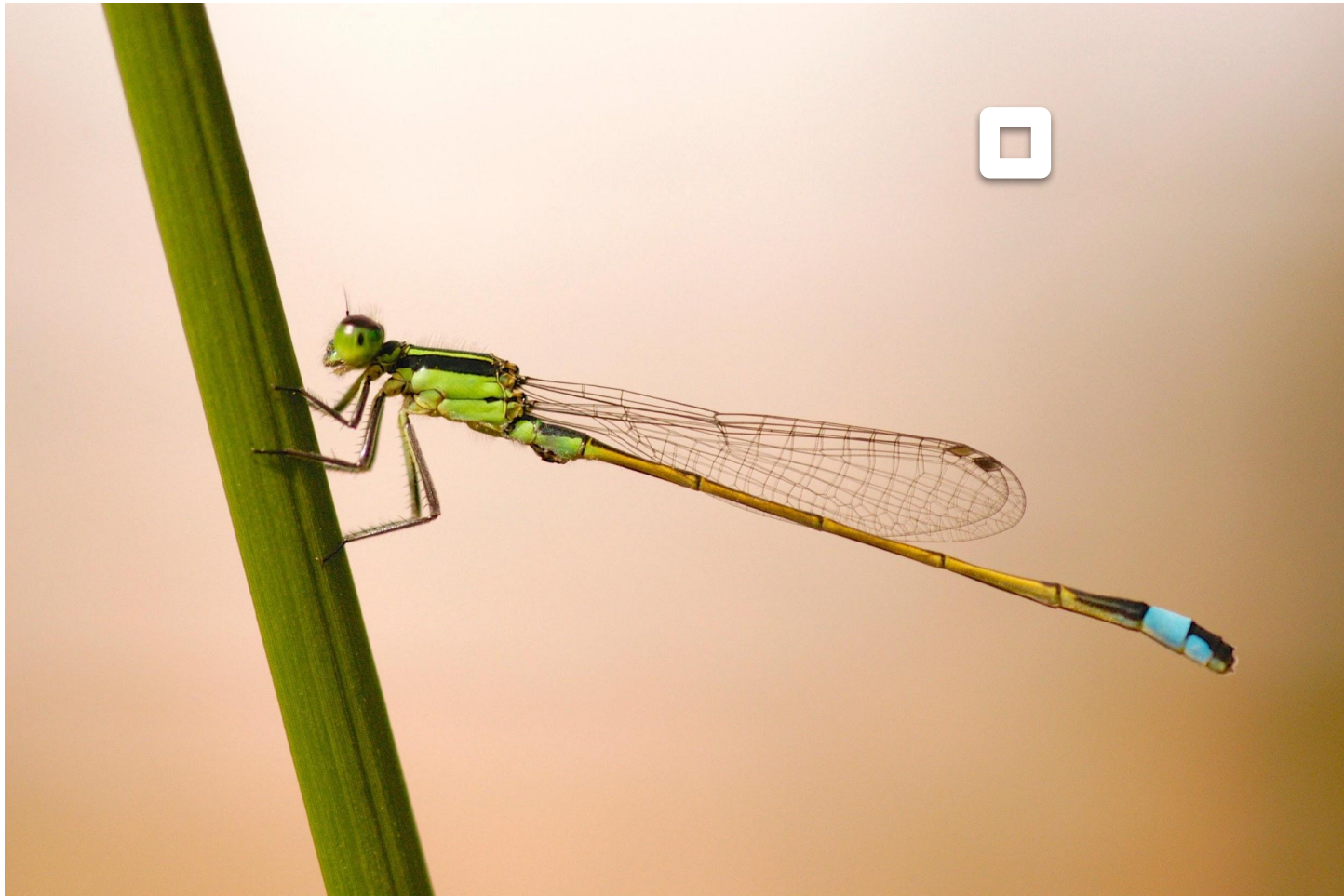
Pseudo-Geometric Interpretation of Color Reproduction

- The display can only produce a low-dimensional subspace of all possible spectra (linear combinations of display primaries)
- In color reproduction, for a given spectrum s (high dimensional), we want to choose a spectrum s' in the display's low-dimensional subspace, such that s' and s project to the same response in the low-dimensional subspace of the eye's SML response

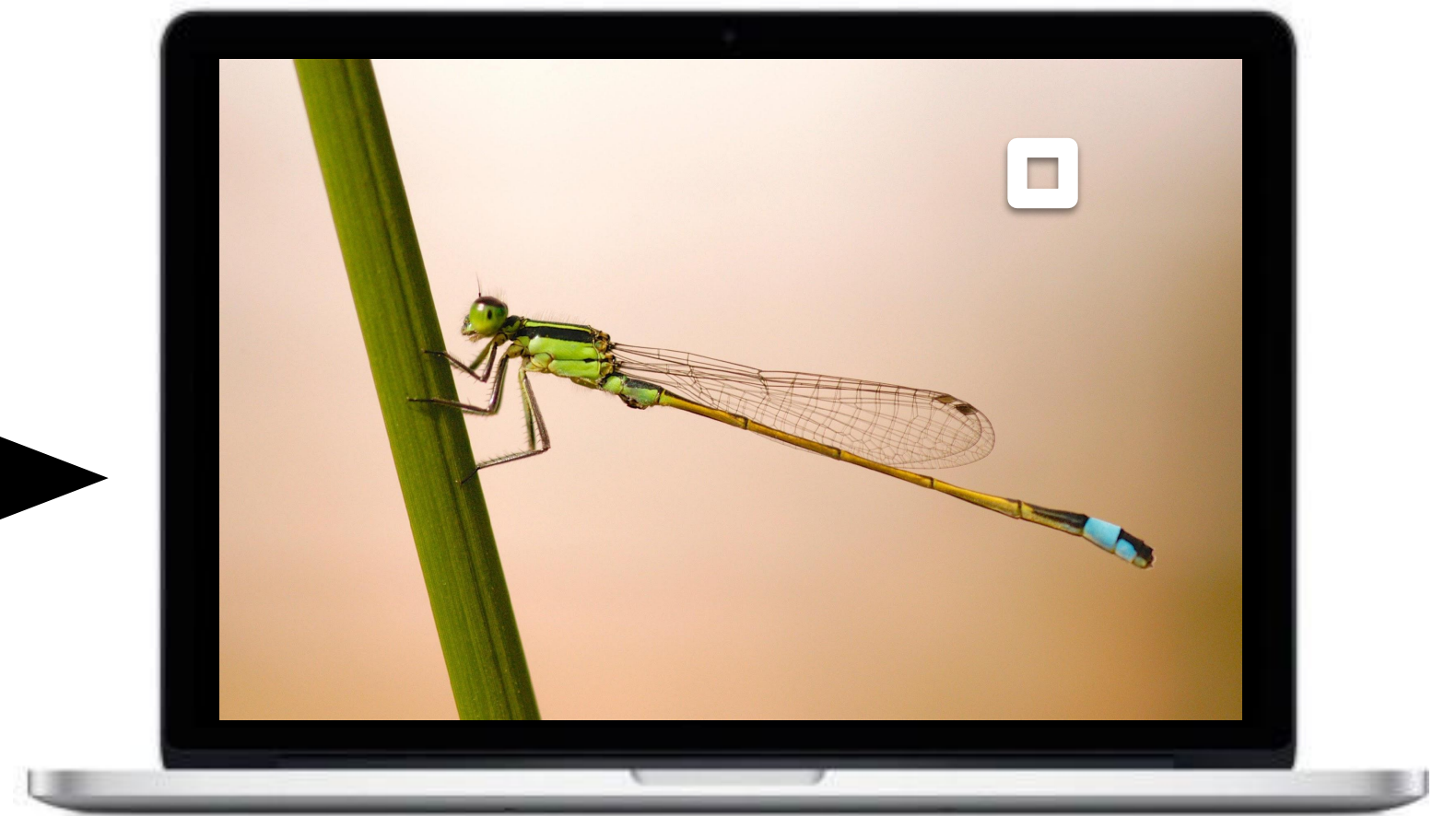


Slide credit: Steve Marschner

Color Reproduction as Linear Algebra



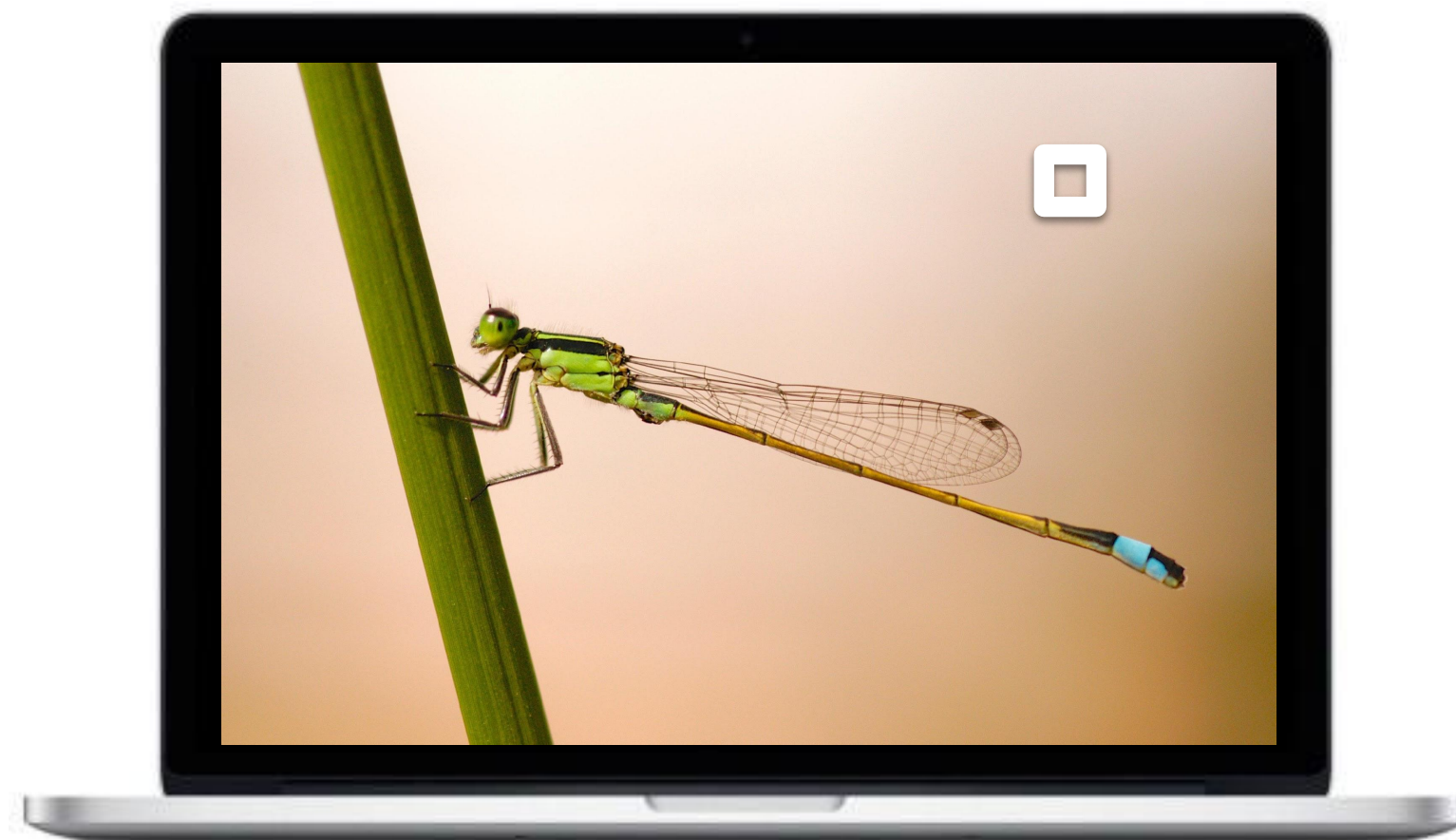
Input spectrum s



What R, G, B values?

Color Reproduction as Linear Algebra

Spectrum produced by display given values R,G,B:



Color Reproduction as Linear Algebra

What color do we perceive when we look at the display?

We want this displayed spectrum to be a metamer for the real-world target spectrum.

Color Reproduction as Linear Algebra

Color perceived for display spectra with values R, G, B

Color perceived for real scene spectra, s

How do we reproduce the color of s ? Set these lines equal and solve for R, G, B as a function of s !

Color Reproduction as Linear Algebra

Color Reproduction as Linear Algebra

Color Reproduction as Linear Algebra

Color Matching Functions

Recall the color matching functions from the matching experiment

Color Reproduction Issue: No Negative Light

R,G,B values must be positive

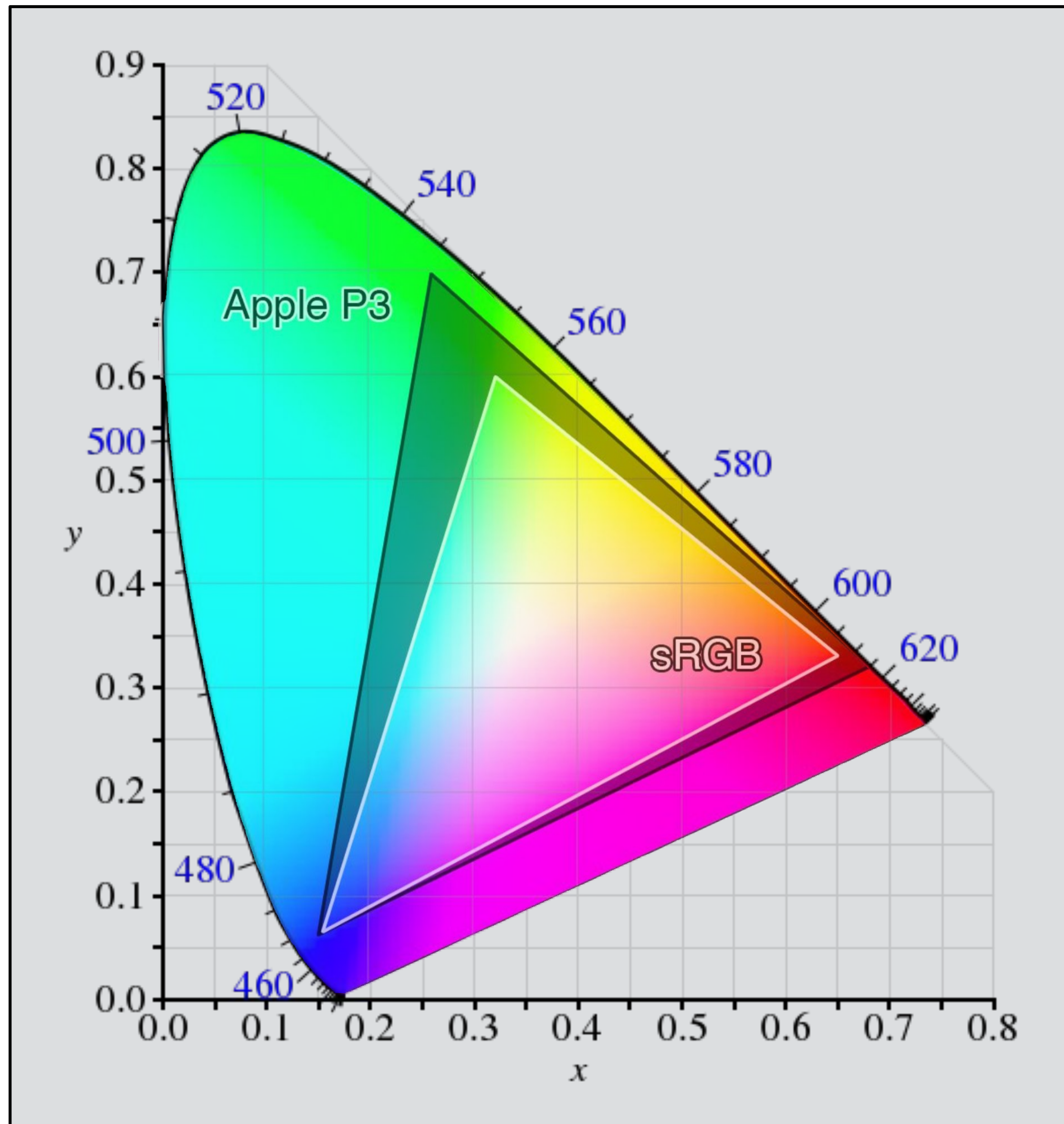
- Display primaries can't emit negative light
- But solution formulas can certainly produce negative R,G,B values

What do negative R,G,B values mean?

- Display can't physically reproduce the desired color
- Desired color is outside the display's color gamut

Color Gamut

Example: Color Gamut for sRGB and Apple P3



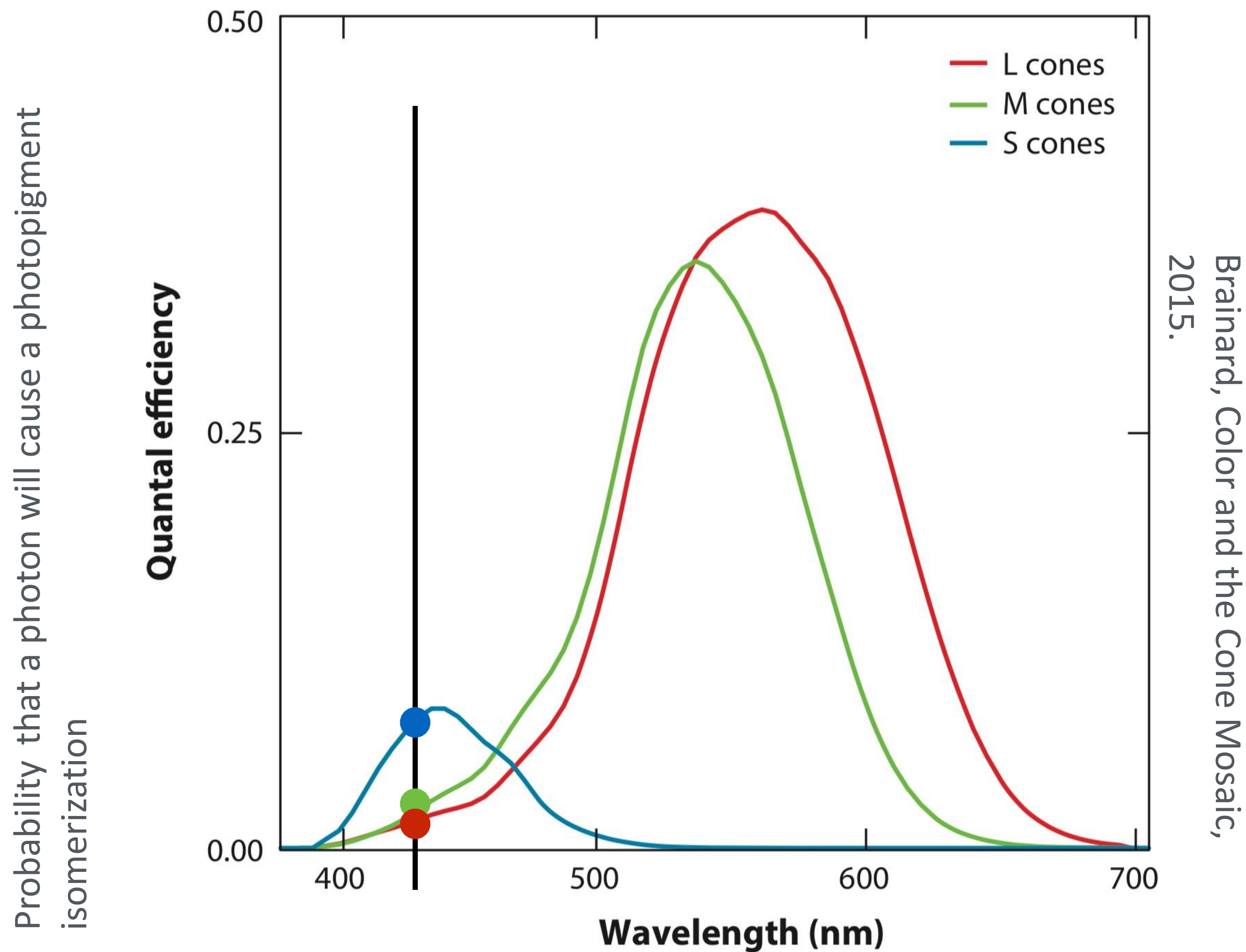
Comparing sRGB and Wide Gamut P3 Color Spaces



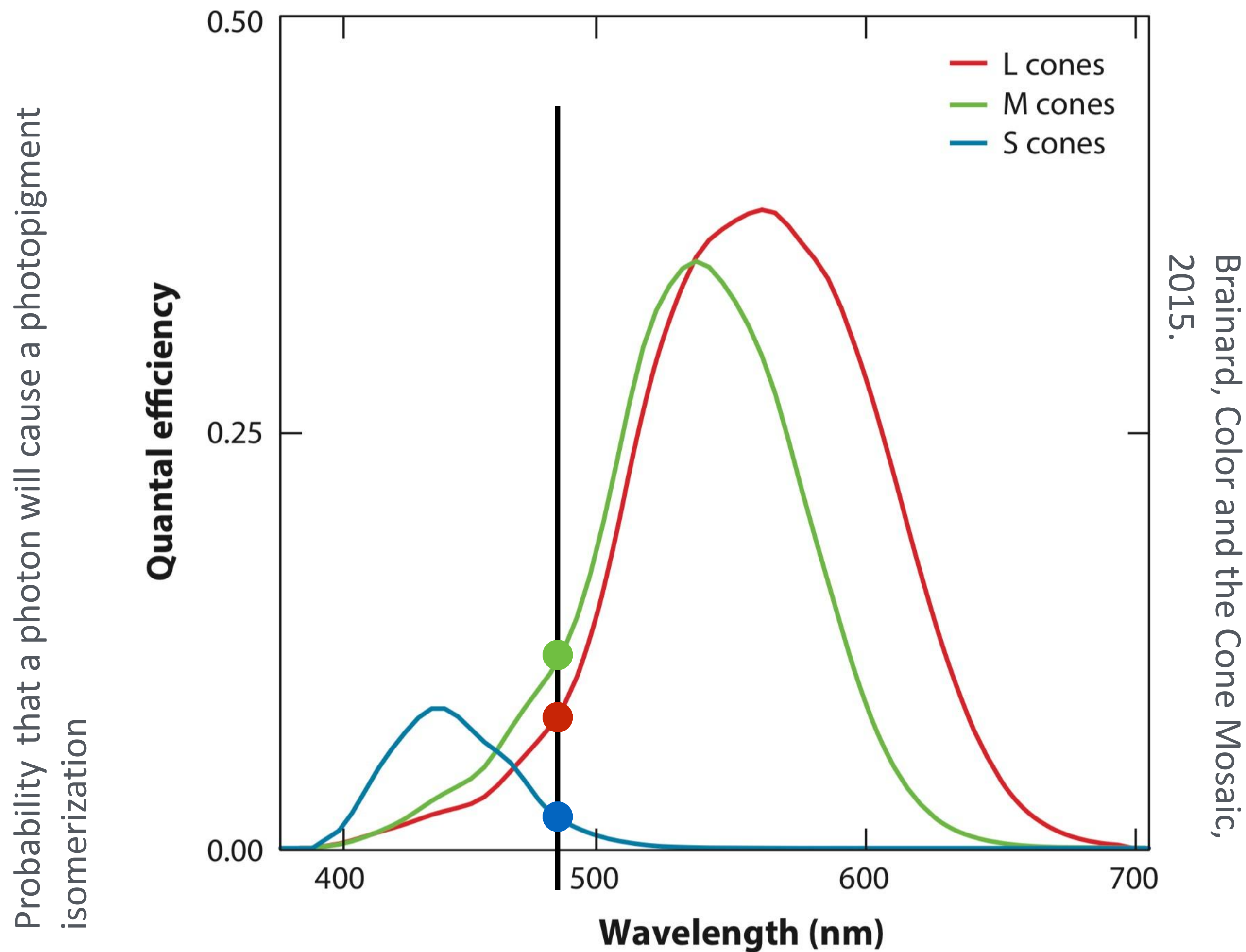
Interactive Color Space Comparison:

- Needs a wide-gamut physical display
- I can see differences clearly on my MacBook Pro, less so on LG display
- <https://webkit.org/blog-files/color-gamut/comparison.html>

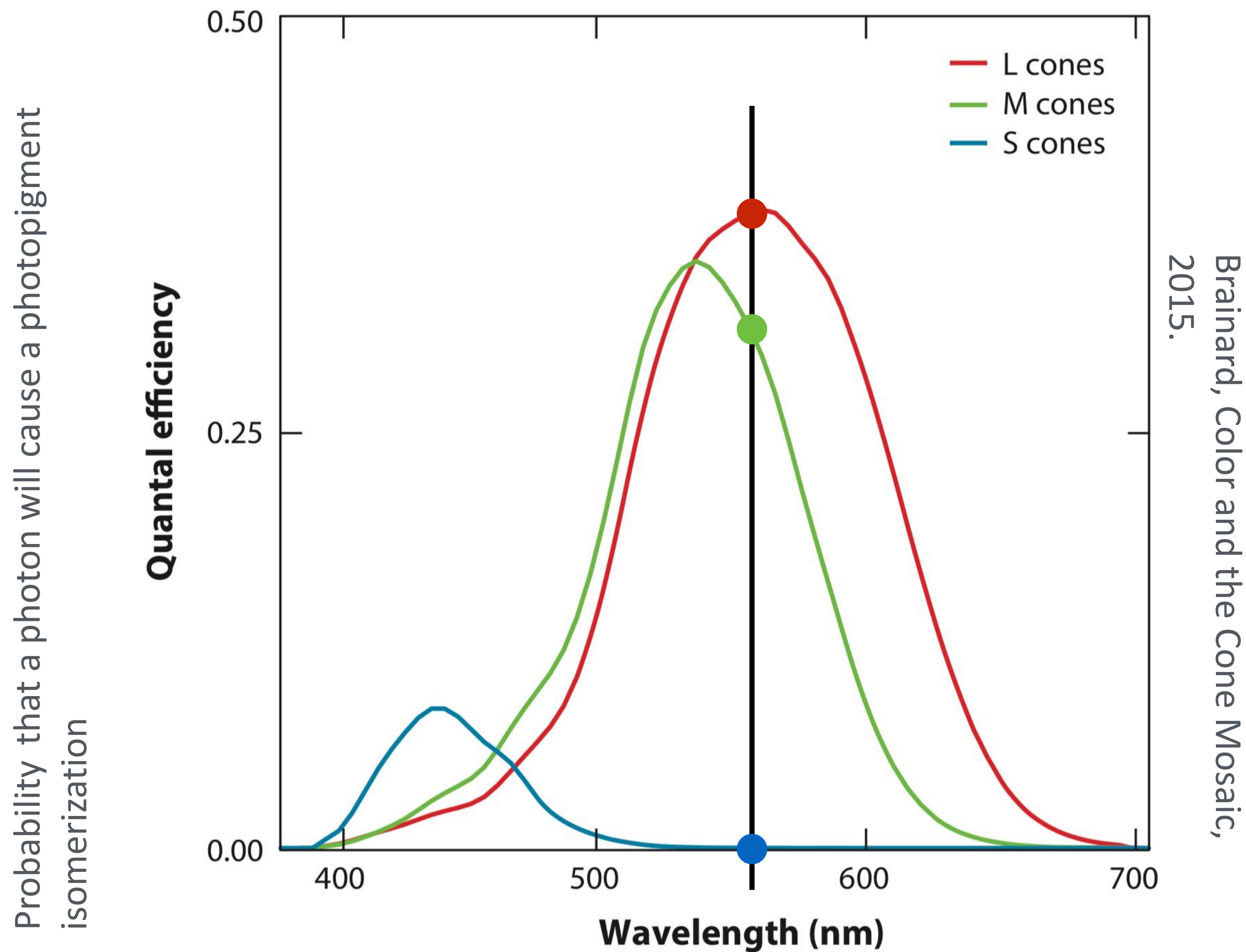
LMS Response Values for Each Wavelength



LMS Response Values for Each Wavelength



LMS Response Values for Each Wavelength

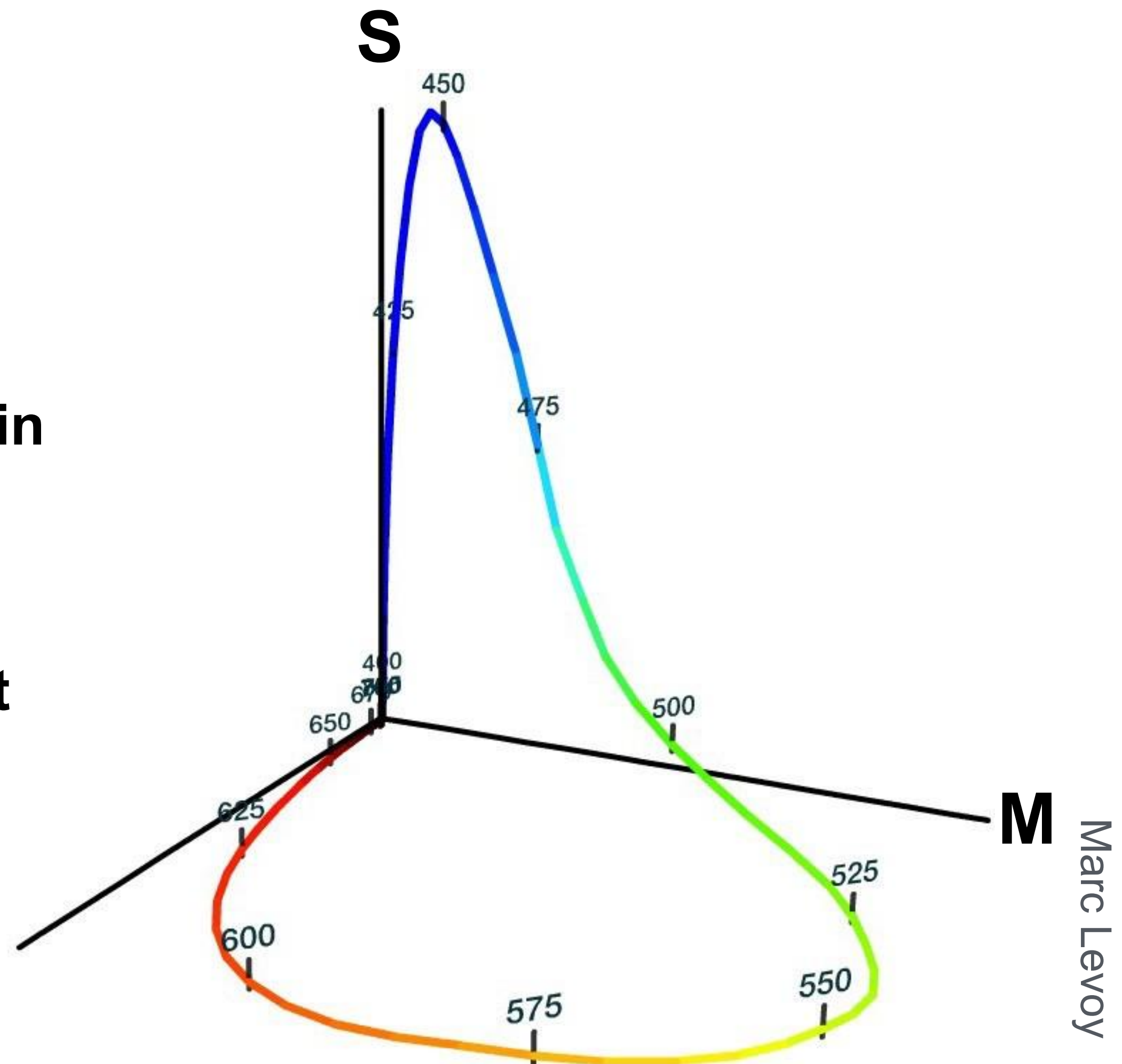


LMS Responses Plotted as 3D Color Space

Visualization of "spectral locus" of human cone cells' response to monochromatic light (light with energy in a single wavelength) as points in 3D space.

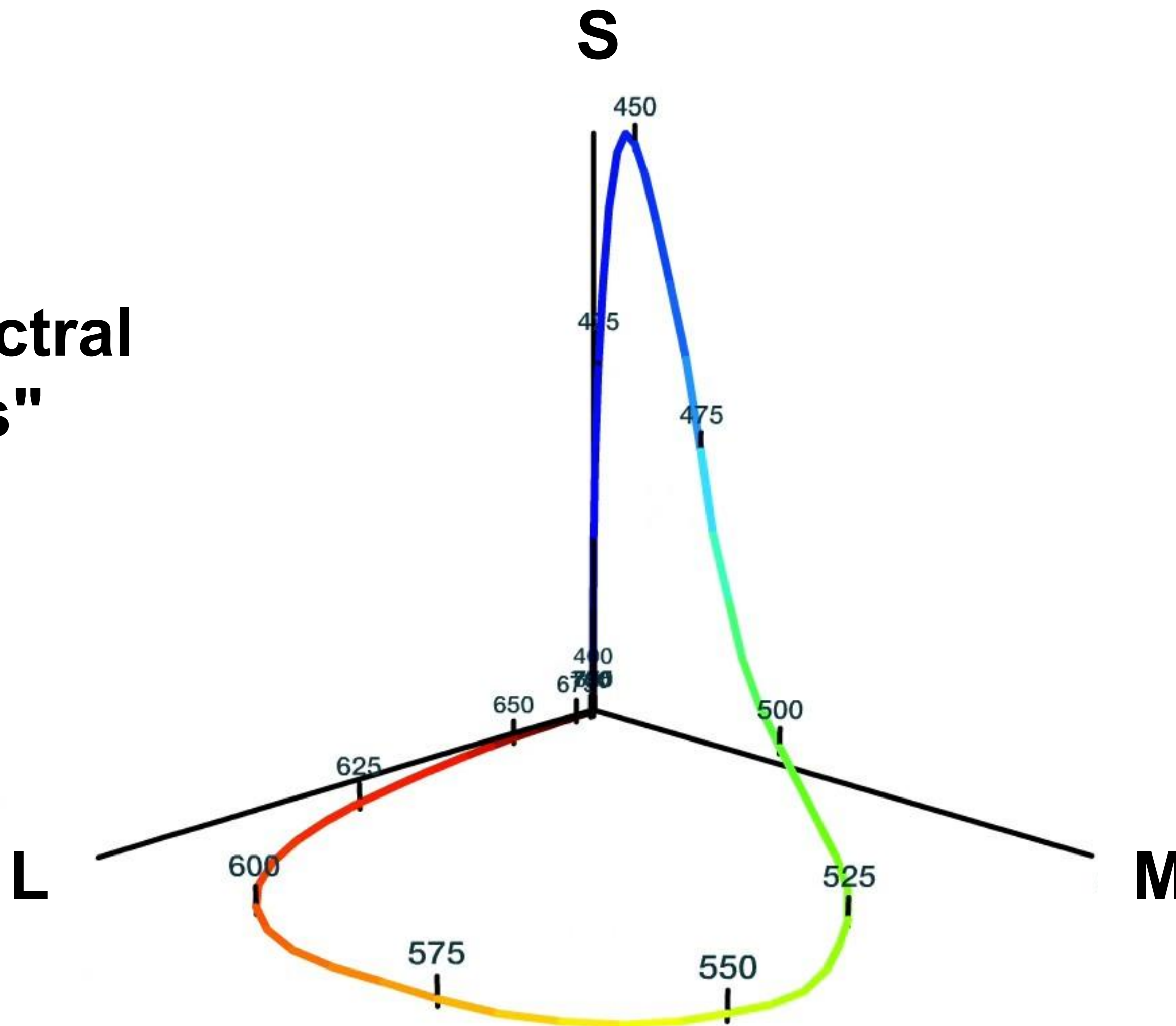
This is a plot of the S, M, L response functions as a point in 3D space.

Space of all possible
of points on this
responses are positive linear
combinations



LMS Responses Plotted as 3D Color Space

"Spectral locus"

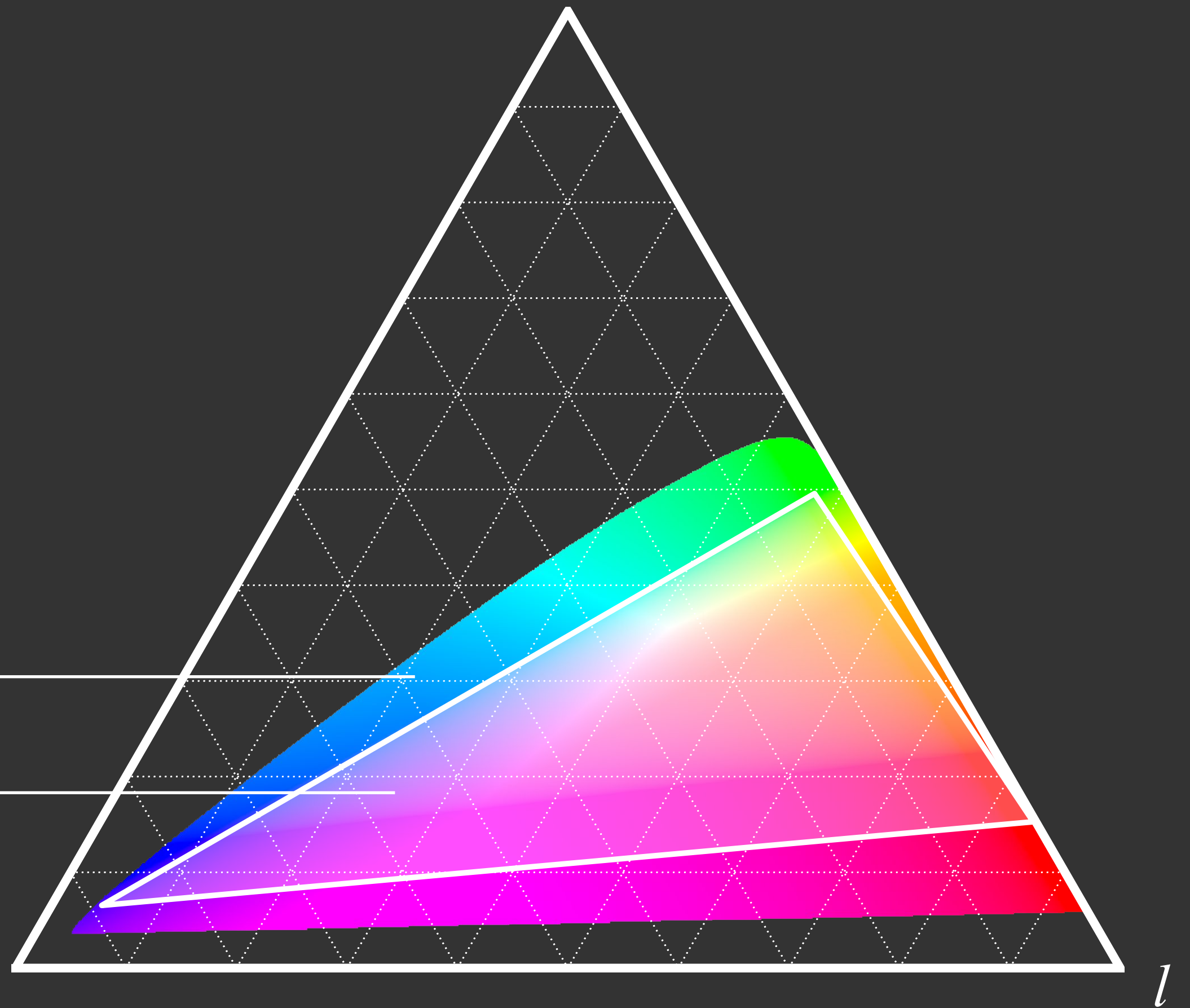


Color Gamut on Chromaticity Diagram (Maxwellian)

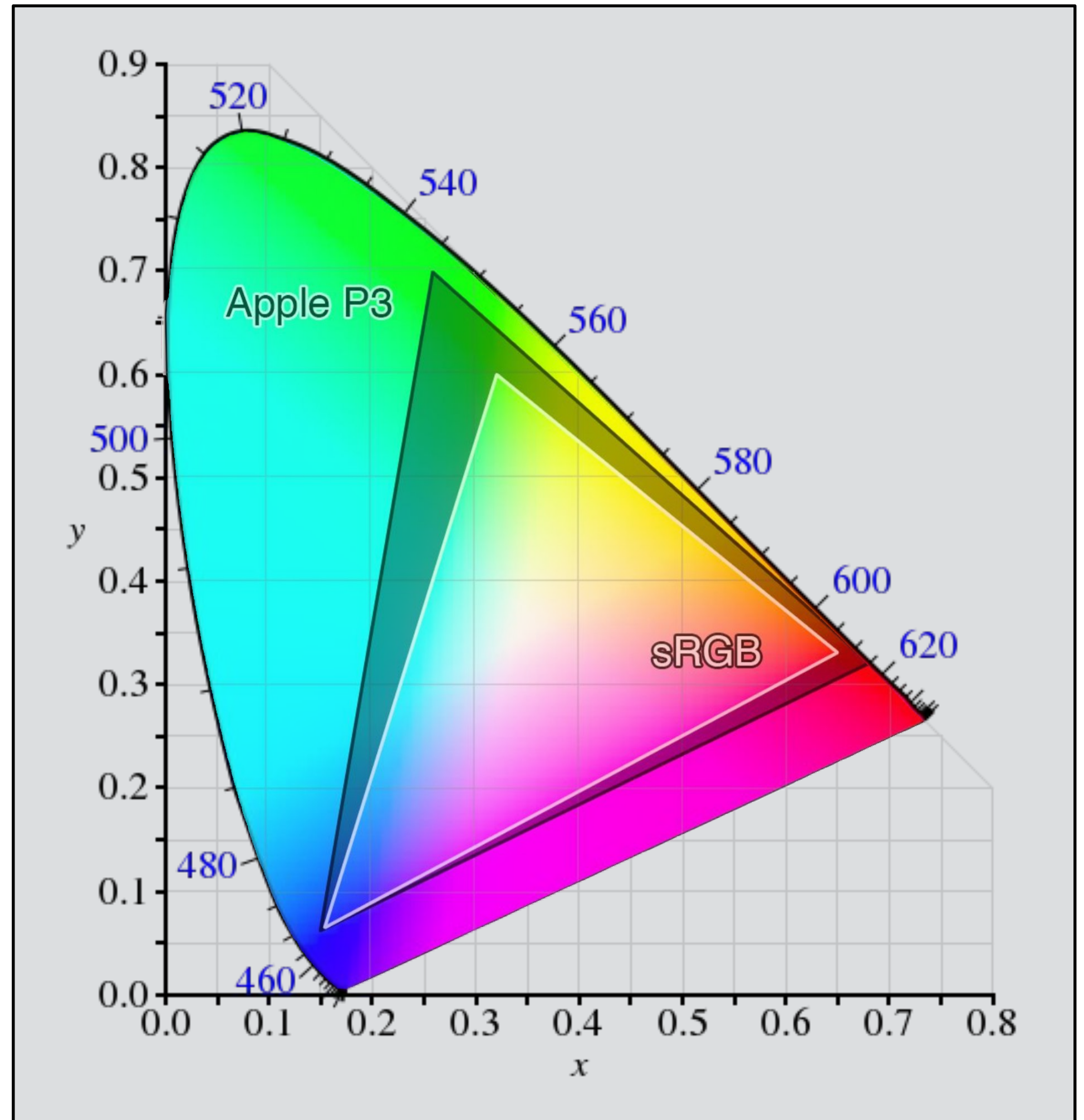
$$(l, m, s) = \frac{(L, M, S)}{L + M + S}$$

Human Gamut

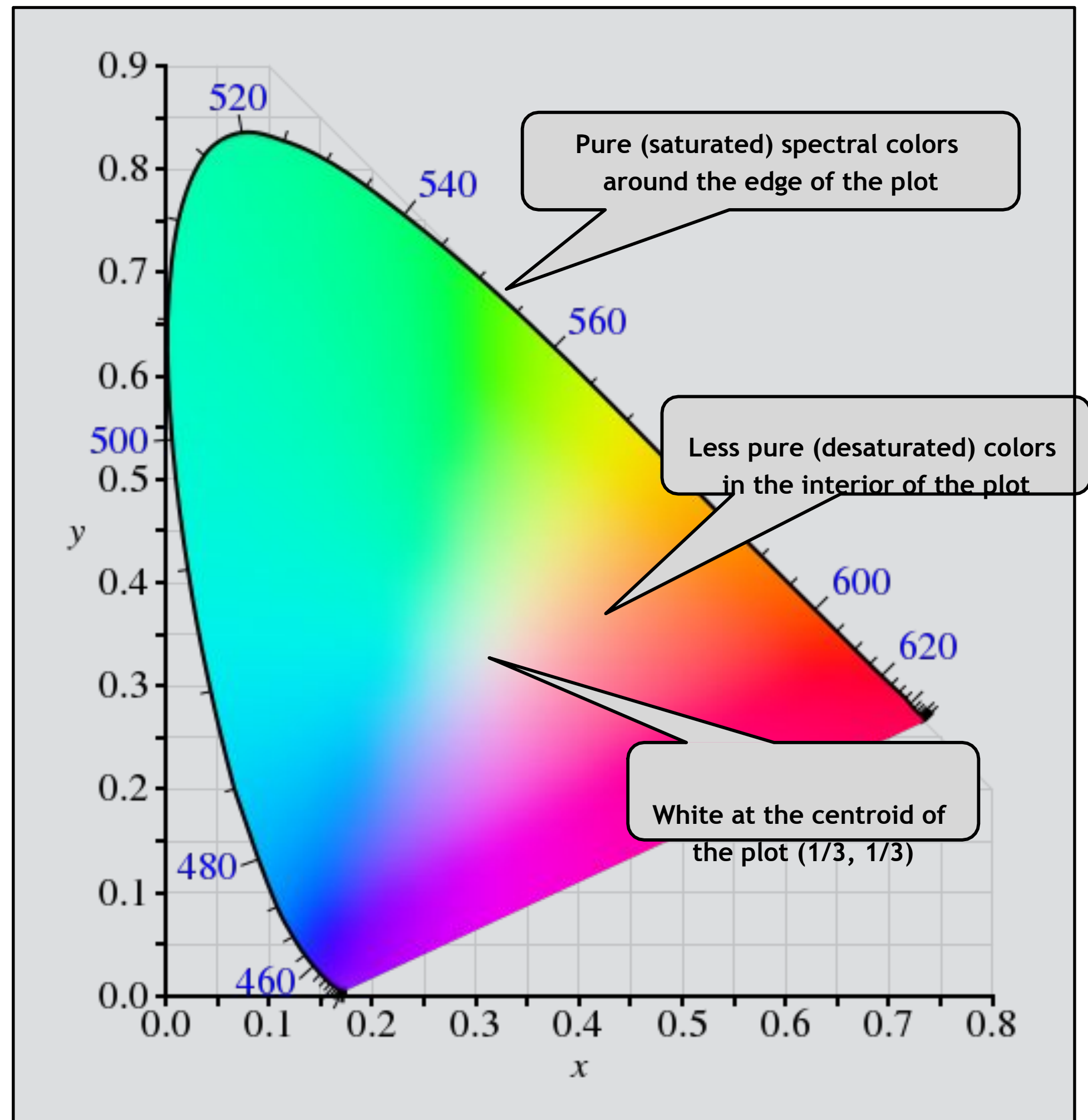
RGB Display
Gamut



Color Gamut on Chromaticity Diagram (CIE 1931 xy)



Color Gamut on Chromaticity Diagram (CIE 1931 xy)



Color Representation

Color Spaces

Need three numbers to specify a color

- But what three numbers?
- A color space is an answer to this question
- Same color has different coordinates in different color spaces. E.g. RGB, XYZ, Lab, HSV, ...

Common example: display color space

- Define a color by what R, G, B scalar values will produce it on your display
 - As before, $s(\lambda) = r(\lambda)R + g(\lambda)G + b(\lambda)B$ for some spectra r, g, b
- Device dependent (depends on primary spectra, gamma, ...)
 - Therefore if I choose R,G,B by looking at my display and send it to you, you may not see the same color

• Also leaves out some colors (limited gamut), e.g. vivid yellow

CS184/284A

Ren Ng

- Because in file formats R, G, B usually constrained to be non-negative

Standard Color Spaces

Standardized RGB (sRGB)

- makes a particular monitor RGB standard
- other color devices simulate that monitor by calibration
- sRGB is usable as an interchange space; still widely used today, though other standards common now
- gamut is still limited

The Historical “Standard” Color Space: CIE XYZ

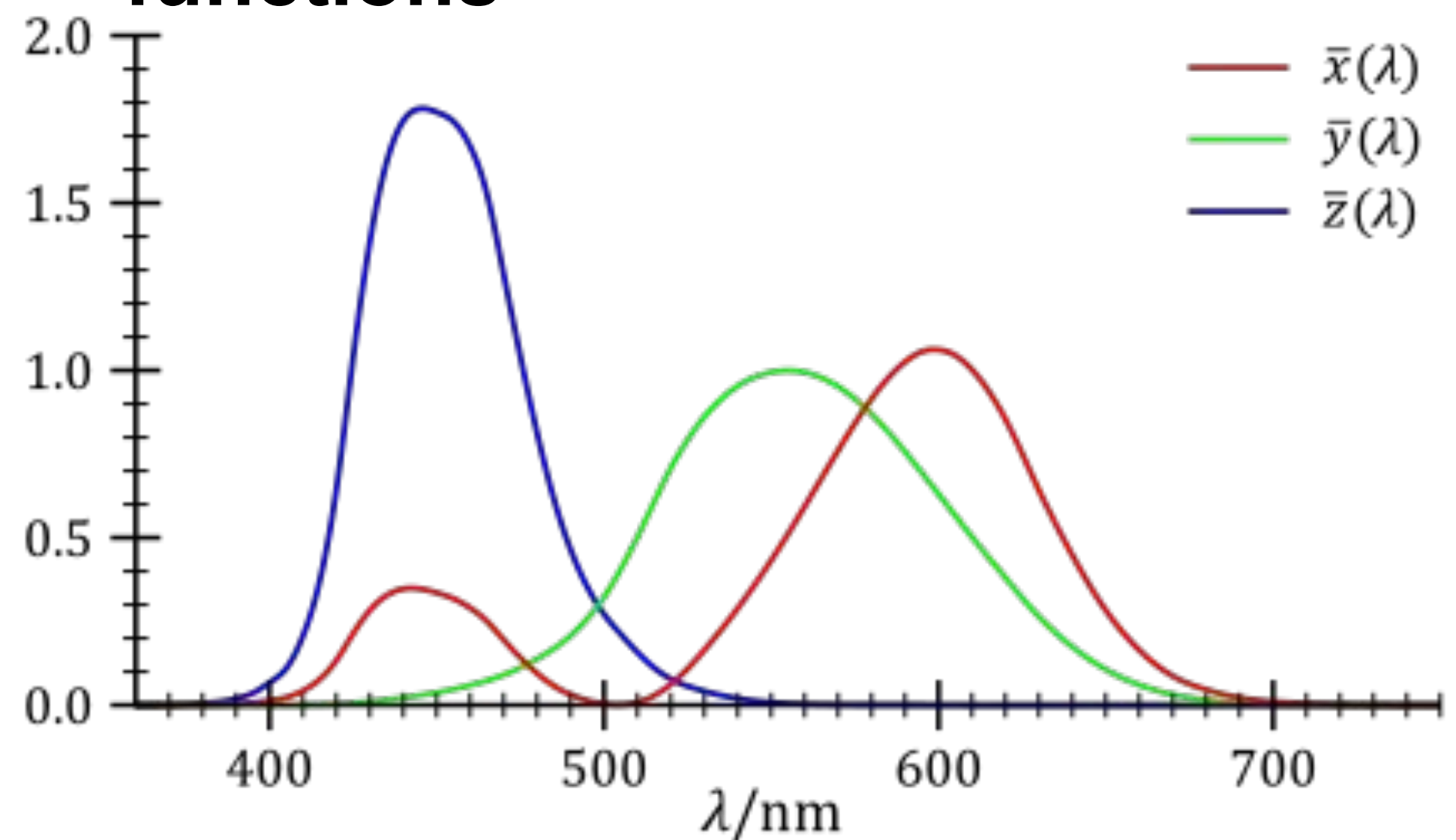
Imaginary set of
standard color primaries
X, Y, Z

Designed such that

- X, Y, Z span all observable colors
- Matching functions are strictly positive
- Y is luminance (brightness absent color)

Imaginary because can
only be realized with
primaries that are negative

CIE XYZ color matching
functions

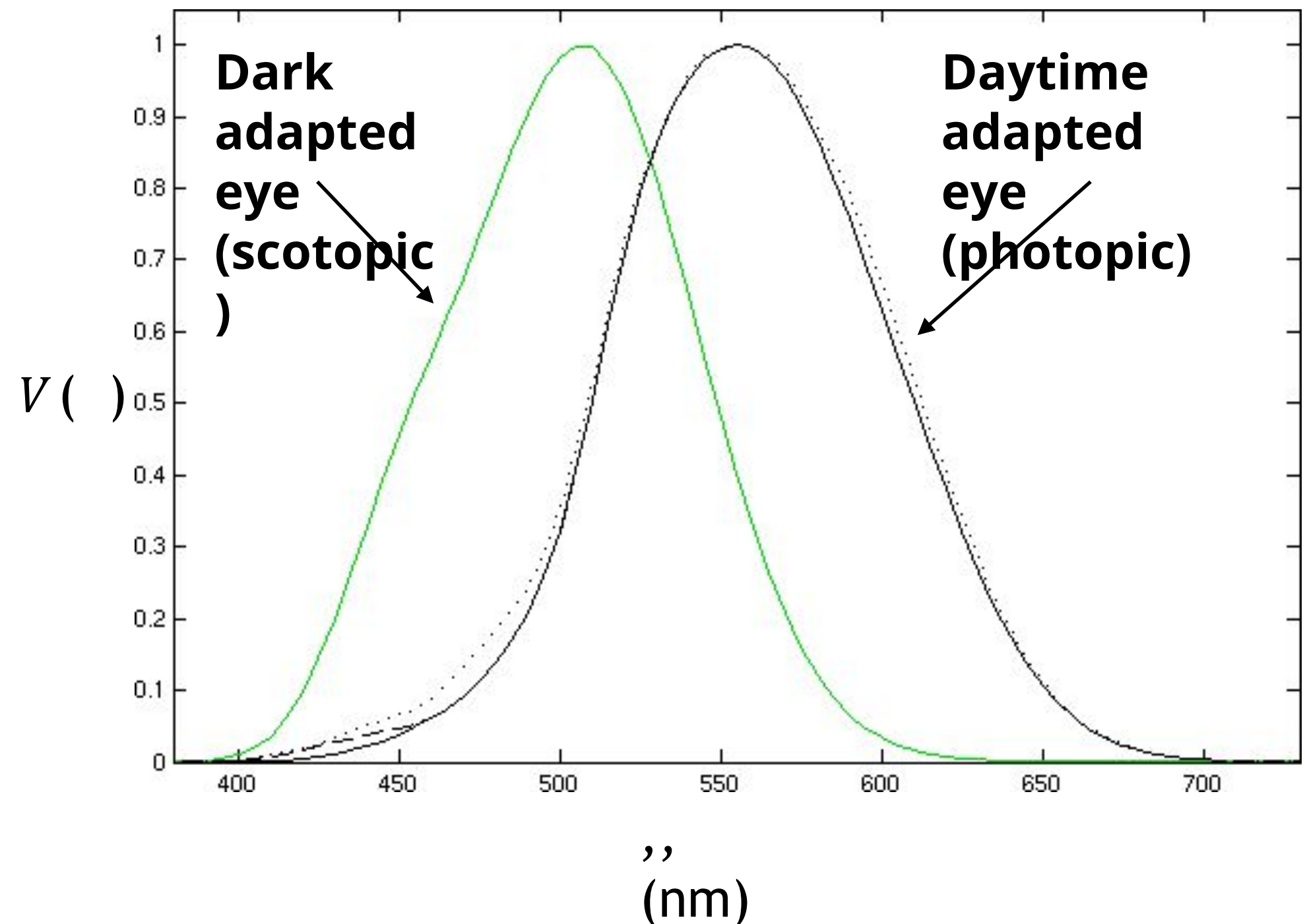


Luminance (Lightness)

Integral of radiance scaled
by the visual luminous
efficiency

$$Y = \int J(\lambda) V(\lambda) d\lambda$$

Luminous efficiency $V(\lambda)$ is
a measure of how bright a
light at a given wavelength is
perceived by a human



<https://upload.wikimedia.org/wikipedia/commons/a/a0/Luminosity.png>

Separating Luminance, Chromaticity

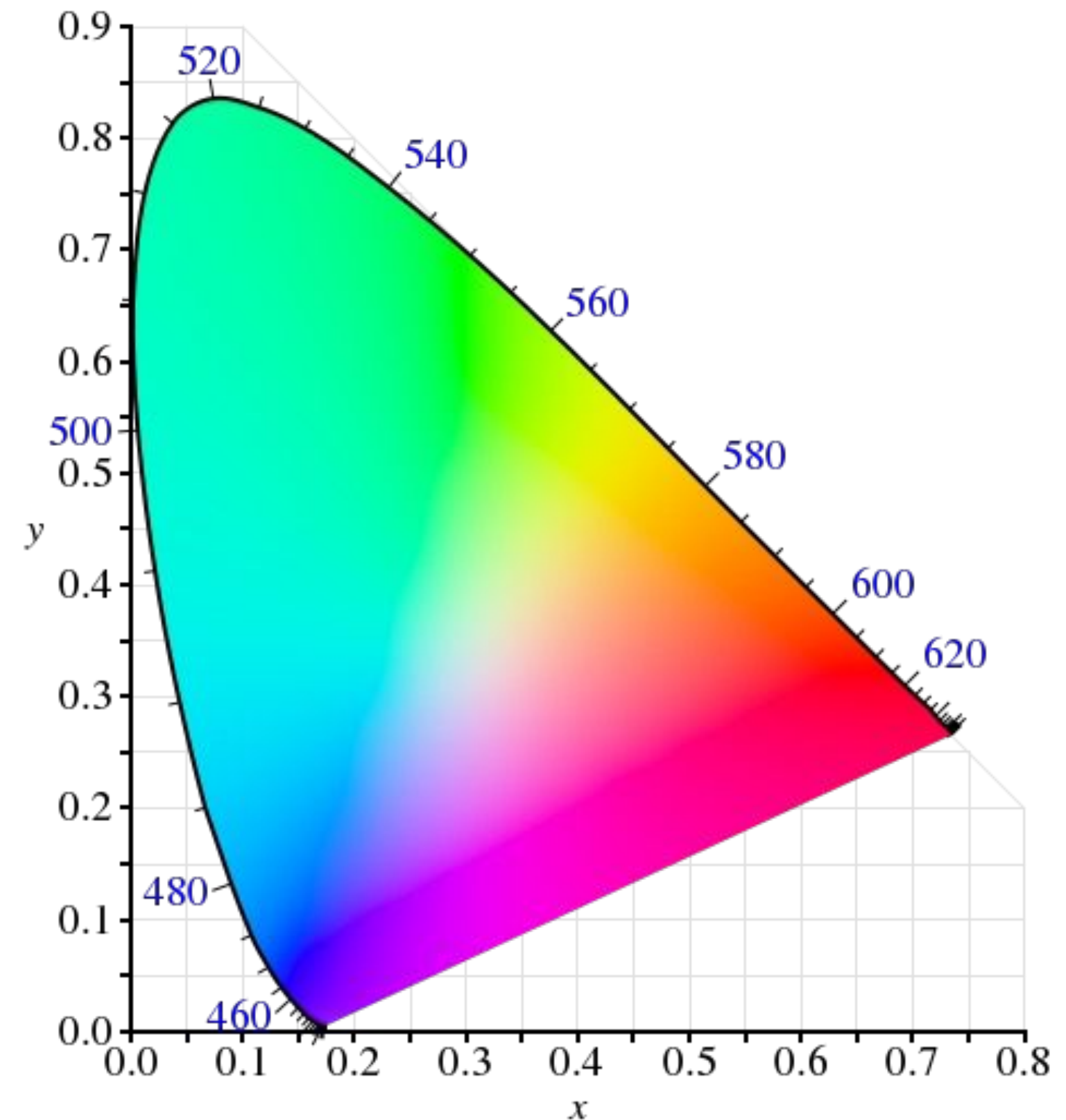
Luminance: Y

Chromaticity: x, y, z , defined as

$$x = \frac{X}{X + Y + Z}$$

$$y = \frac{Y}{X + Y + Z}$$

$$z = \frac{Z}{X + Y + Z}$$

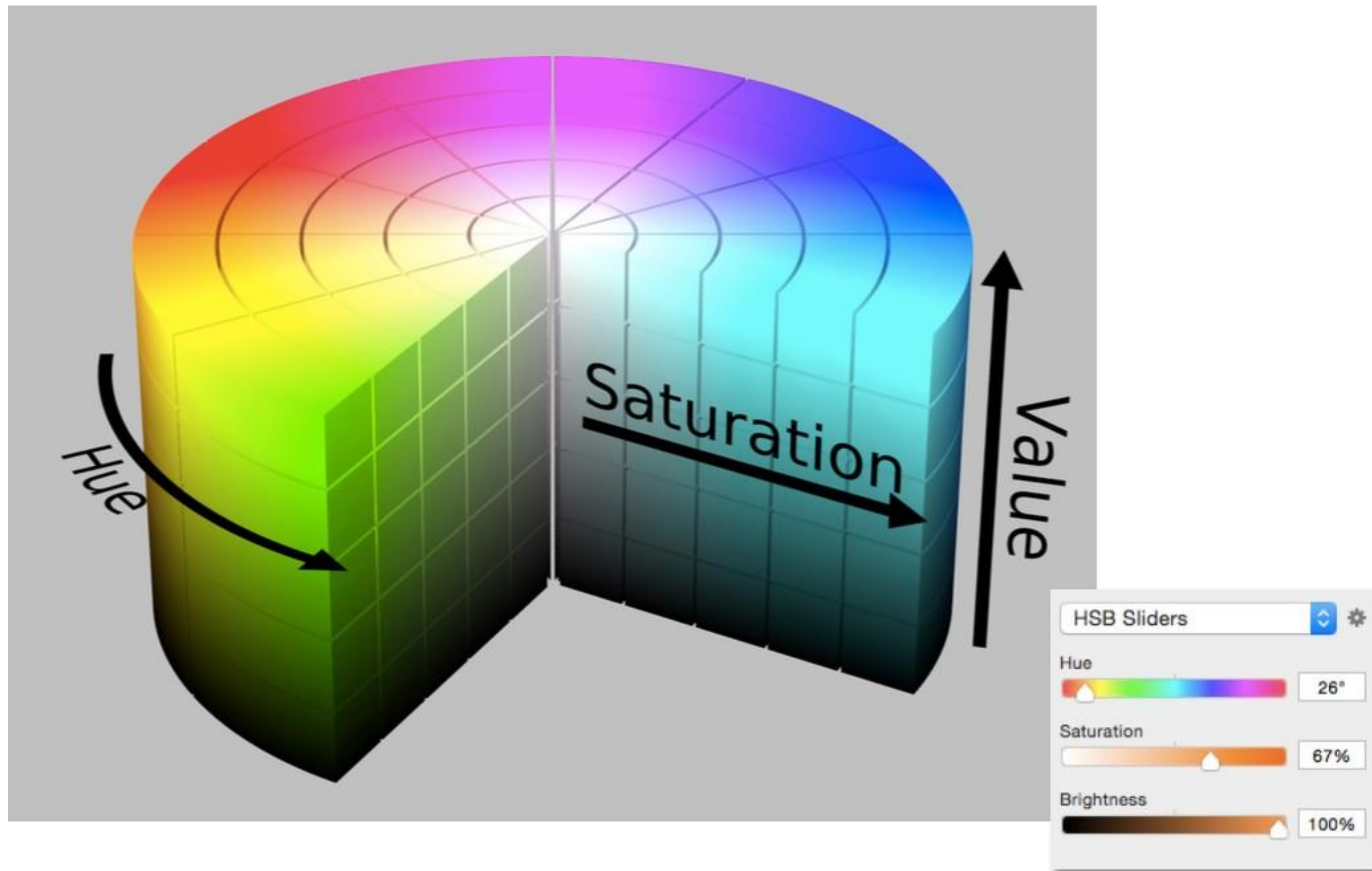


- since $x + y + z = 1$, we only need to record two of the three
- usually choose x and y , leading to (x, y, Y) coords

Perceptually Organized Color Spaces

HSV Color Space (Hue-Saturation-Value)

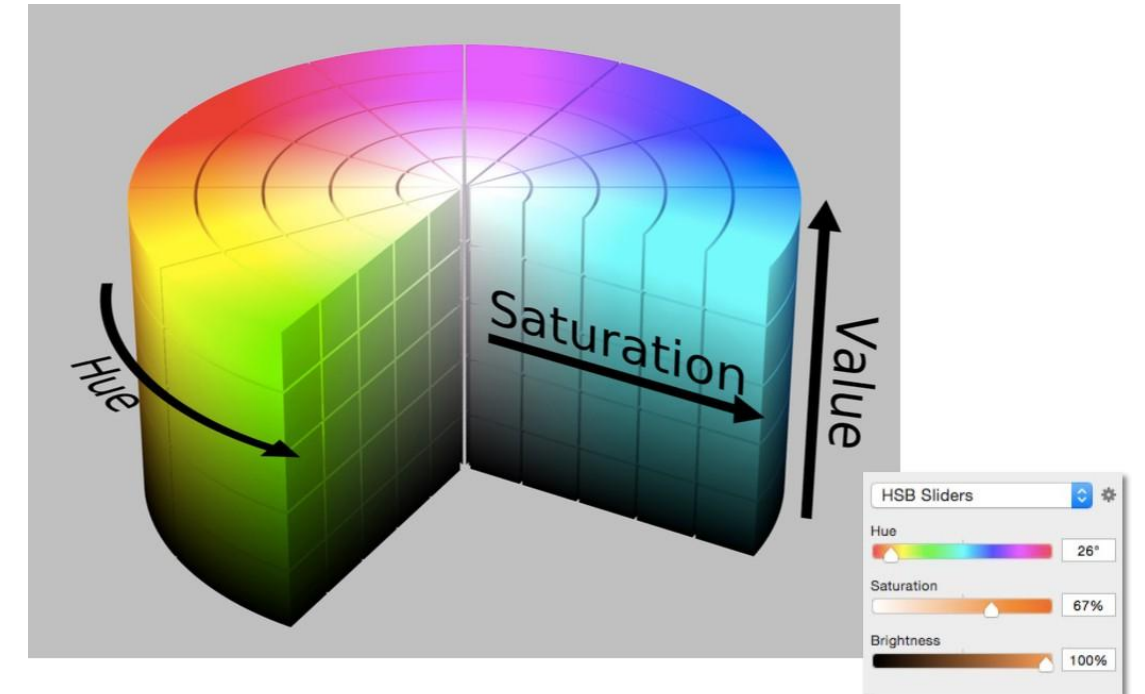
Axes correspond to artistic characteristics of color



HSV Color Space (Hue-Saturation-Value)

Perceptual dimensions of
color Hue

- the “kind” of color, regardless of attributes
 - colorimetric correlate: dominant wavelength
 - artist’s correlate: the chosen pigment
- color Saturation
- the “colorfulness”
 - colorimetric correlate: purity
 - artist’s correlate: fraction of paint from the colored tube
- Lightness (or value)
- the overall amount of light
 - colorimetric correlate: luminance
 - artist’s correlate: tints are lighter, shades are darker



CIELAB (AKA $L^*a^*b^*$)

A perceptually-organized color space that acts as a simple and useful color appearance model

Features

- **Chromatic adaptation (white balance)**
- **Predicts color appearance**
 - **Opponent color encoding**
 - **Formulas for hue, chroma, lightness**
- **Perceptual uniformity (non-linear warping)**

CIELAB Definition

**CIEXYZ -->
CIELAB**

$$\begin{aligned}L^* &= 116 f\left(\frac{Y}{Y_n}\right) - 16 \\a^* &= 500 \left(f\left(\frac{X}{X_n}\right) - f\left(\frac{Y}{Y_n}\right) \right) \\b^* &= 200 \left(f\left(\frac{Y}{Y_n}\right) - f\left(\frac{Z}{Z_n}\right) \right)\end{aligned}$$

where

$$f(t) = \begin{cases} \sqrt[3]{t} & \text{if } t > \delta^3 \\ \frac{t}{3\delta^2} + \frac{4}{29} & \text{otherwise} \end{cases}$$
$$\delta = \frac{6}{29}$$

X_n , Y_n and Z_n are the CIEXYZ coordinates of the reference white point

**CIELAB -->
CIEXYZ**

$$\begin{aligned}X &= X_n f^{-1} \left(\frac{L^* + 16}{116} + \frac{a^*}{500} \right) \\Y &= Y_n f^{-1} \left(\frac{L^* + 16}{116} \right) \\Z &= Z_n f^{-1} \left(\frac{L^* + 16}{116} - \frac{b^*}{200} \right)\end{aligned}$$

where

$$f^{-1}(t) = \begin{cases} t^3 & \text{if } t > \delta \\ 3\delta^2 \left(t - \frac{4}{29} \right) & \text{otherwise} \end{cases}$$

and where $\delta = 6/29$.

CIELAB Has Chromatic Adaptation (Reference White)

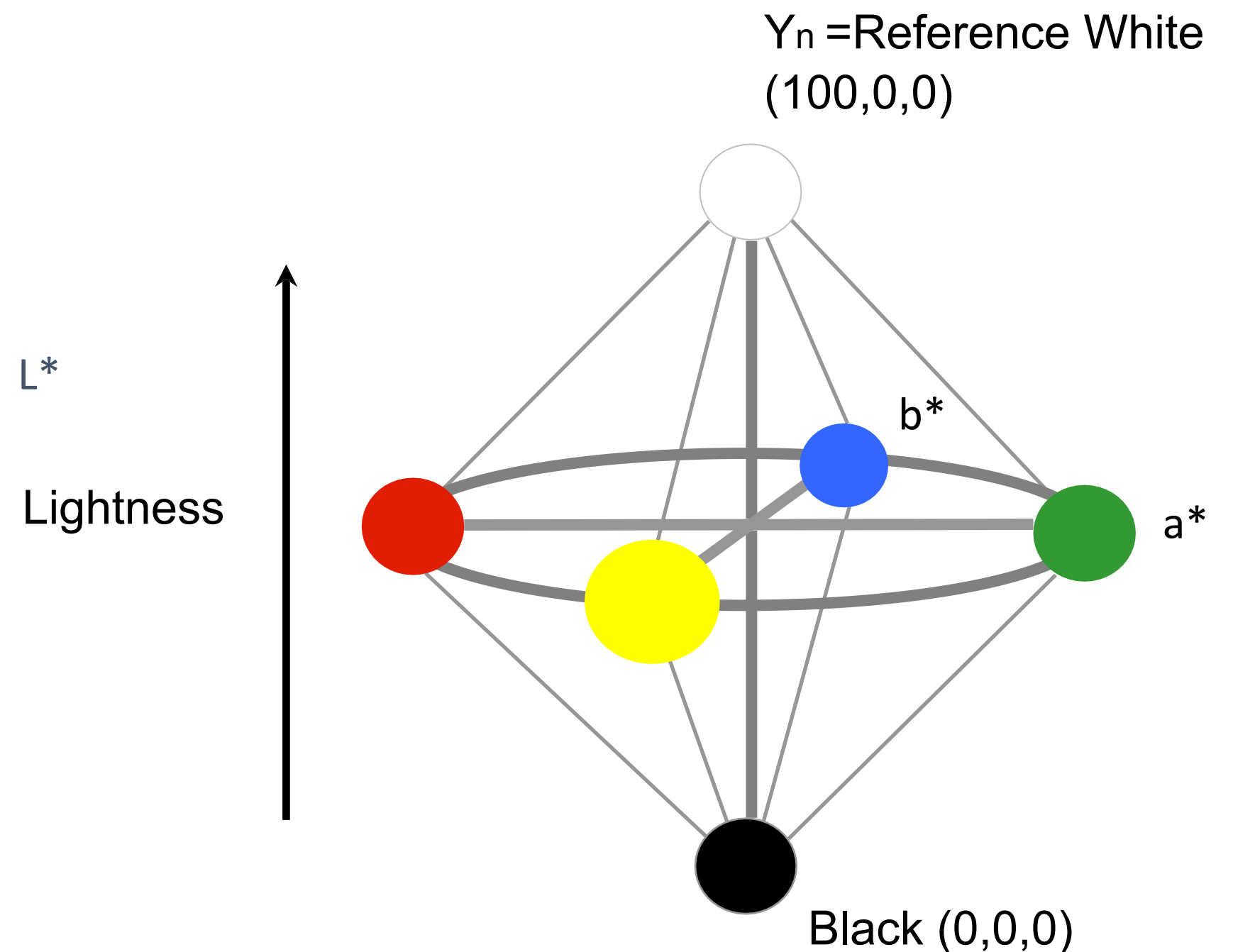
CIEXYZ -->
CIELAB

$$L^* = 116 f\left(\frac{Y}{Y_n}\right) - 16$$
$$a^* = 500 \left(f\left(\frac{X}{X_n}\right) - f\left(\frac{Y}{Y_n}\right) \right)$$
$$b^* = 200 \left(f\left(\frac{Y}{Y_n}\right) - f\left(\frac{Z}{Z_n}\right) \right)$$

where

$$f(t) = \begin{cases} \sqrt[3]{t} & \text{if } t > \delta^3 \\ \frac{t}{3\delta^2} + \frac{4}{29} & \text{otherwise} \end{cases}$$
$$\delta = \frac{6}{29}$$

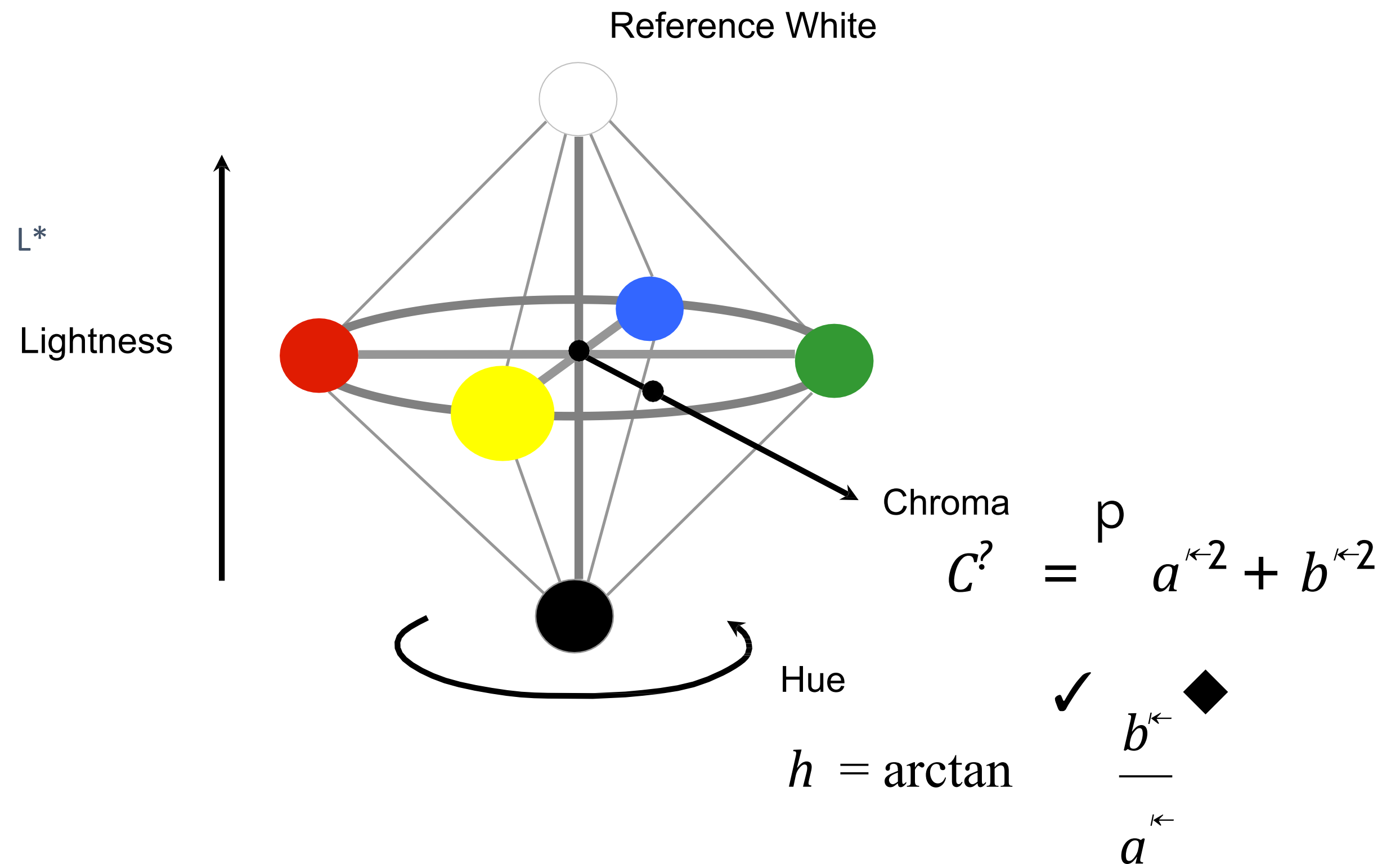
X_n , Y_n and Z_n are the CIEXYZ coordinates of the reference white point



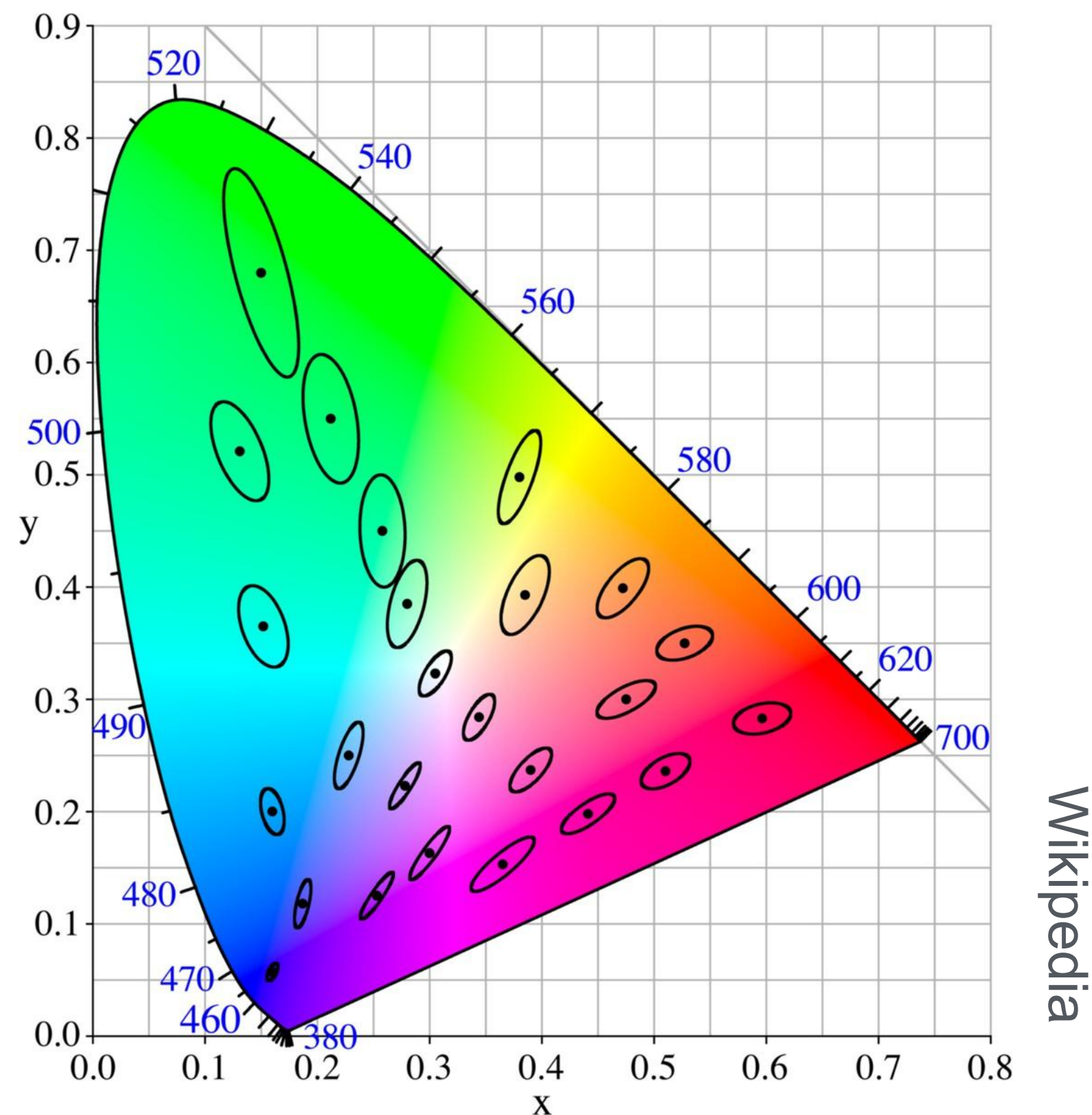
CIELAB As a Color Appearance Model

Hue,
lightness,
saturation

Not L^* , a^* , b^*

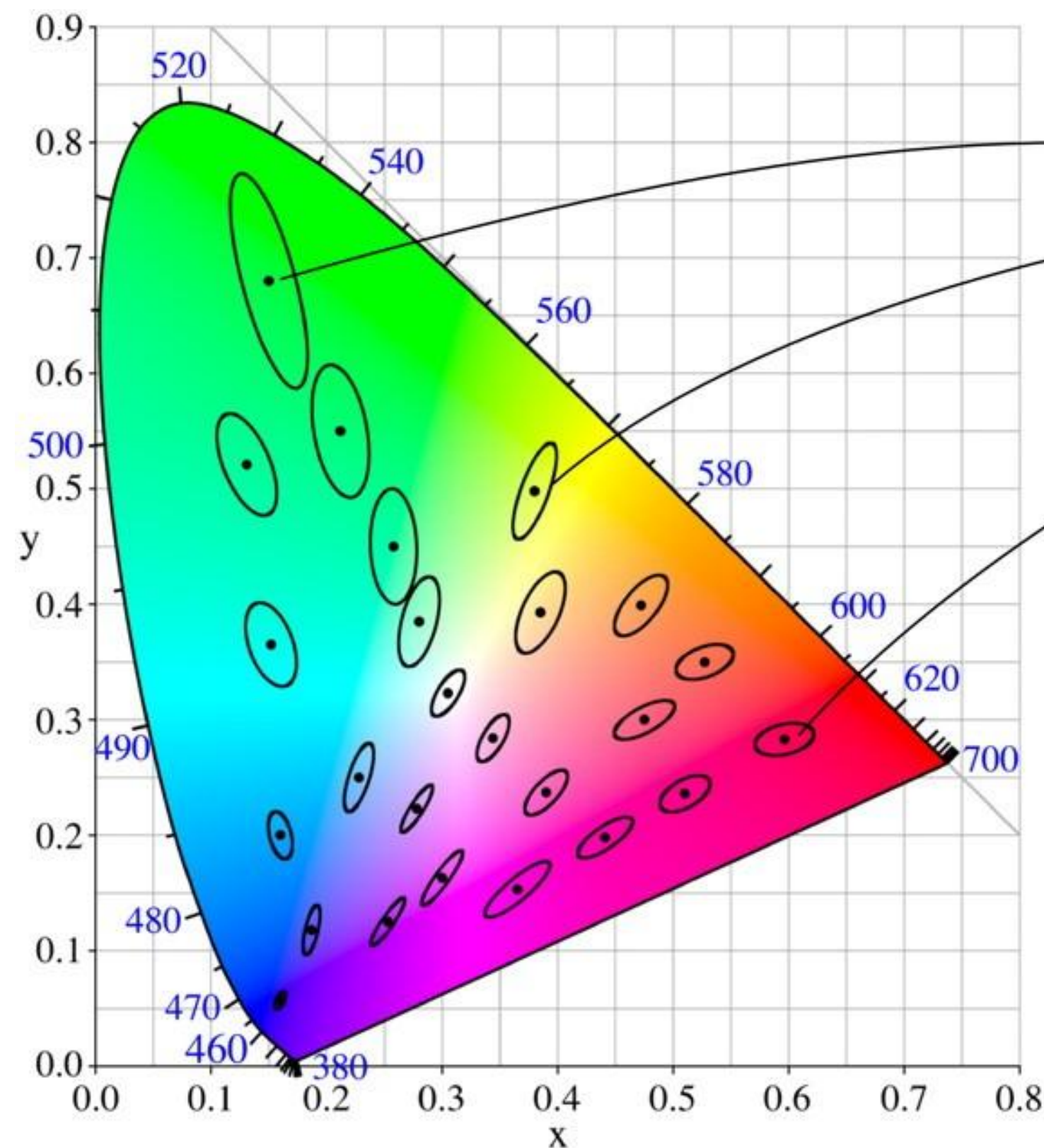


CIEXYZ is Not Perceptually Uniform

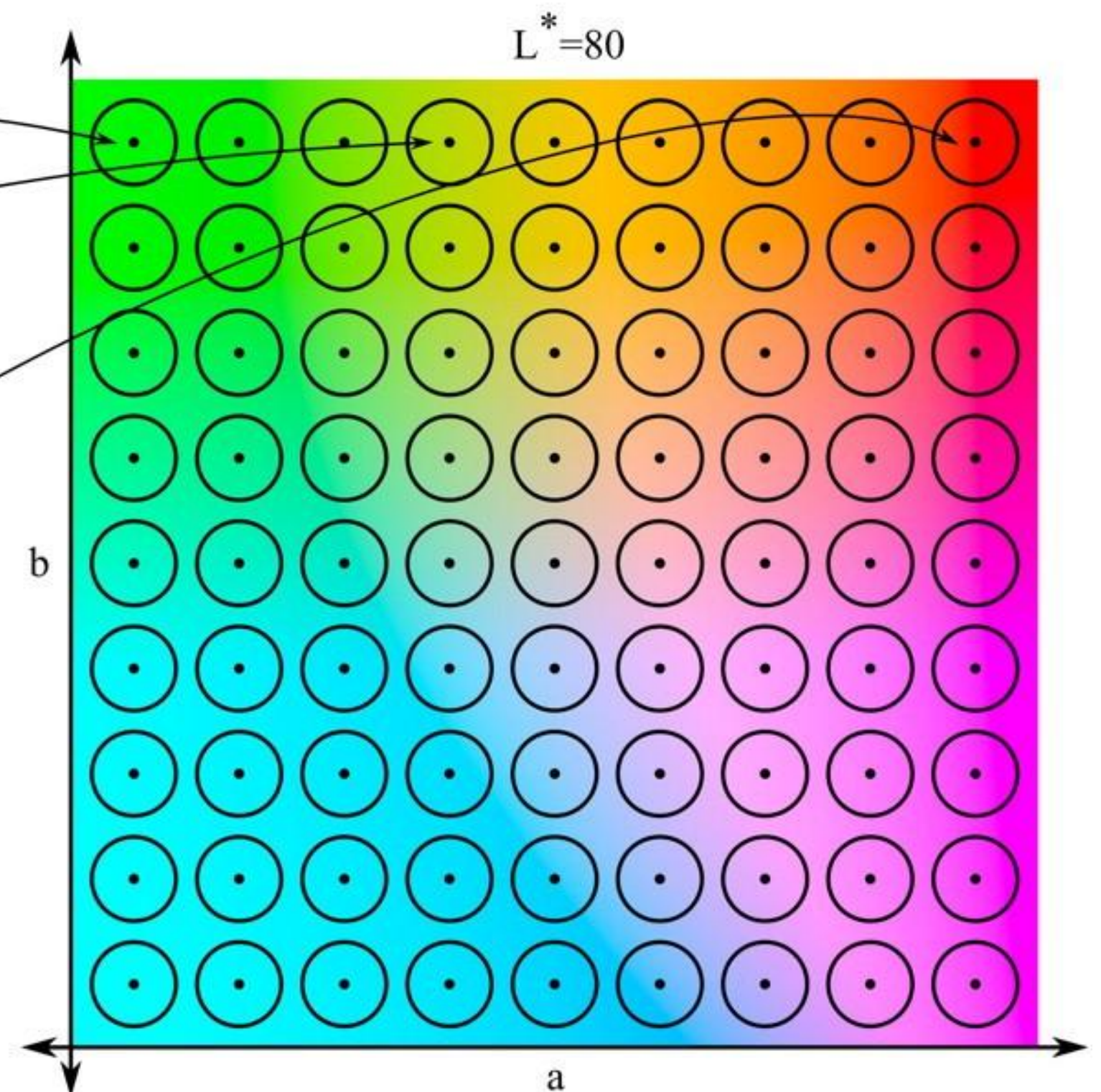


- In the xy chromaticity diagram at left, MacAdam ellipses show regions of perceptually equivalent color (ellipses enlarged 10x)

CIELAB Aims for Perceptual Uniformity



CIE 1931



CIELAB (CIE 1976 L^*, a^*, b^*)

From Henrich et al. 2011

<https://iovs.arvojournals.org/article.aspx?articleid=2187751>

Perceptual Normalization Function Applies to L^* , a^* , b^*

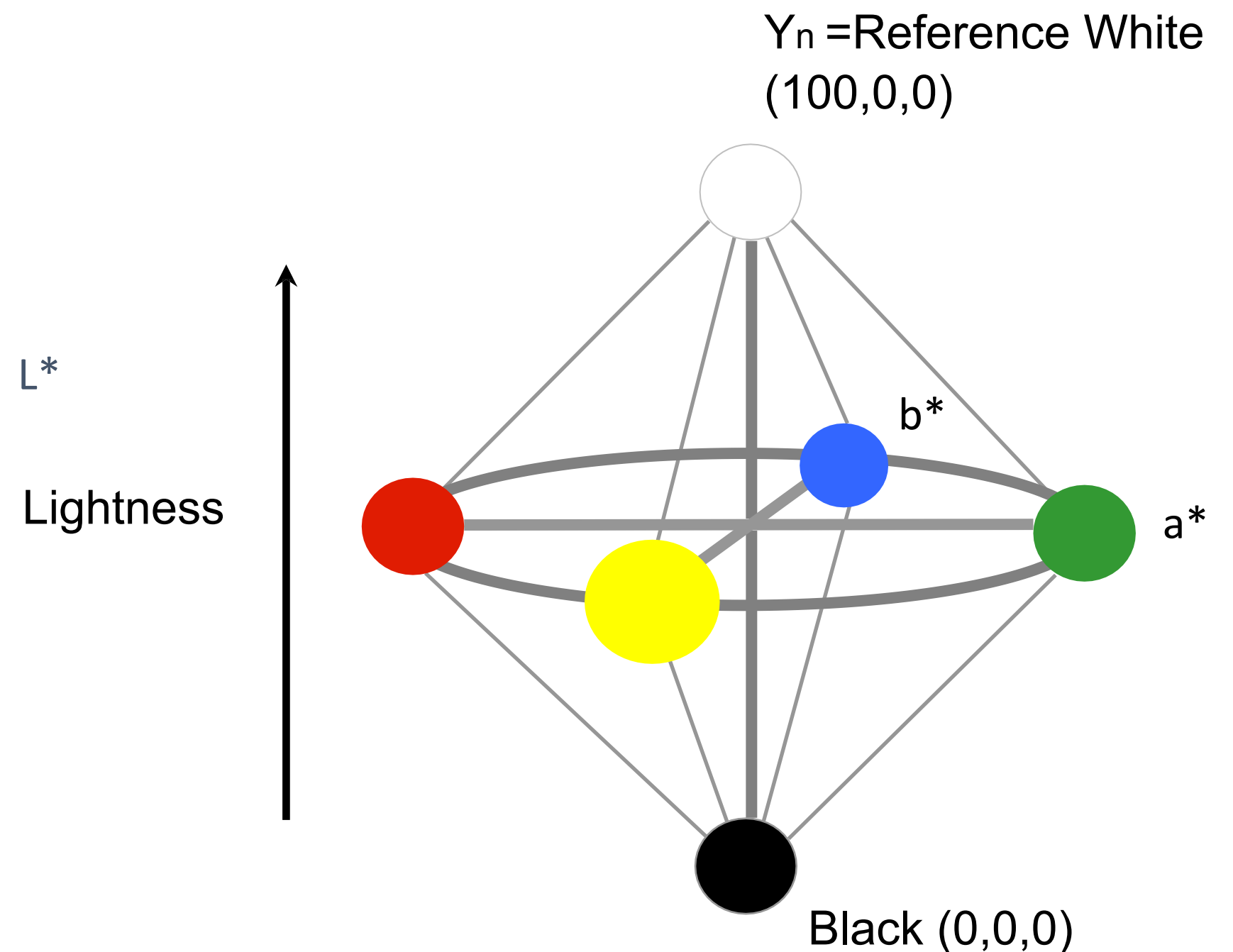
CIEXYZ -->
CIELAB

$$L^* = 116 f\left(\frac{Y}{Y_n}\right) - 16$$
$$a^* = 500 \left(f\left(\frac{X}{X_n}\right) - f\left(\frac{Y}{Y_n}\right) \right)$$
$$b^* = 200 \left(f\left(\frac{Y}{Y_n}\right) - f\left(\frac{Z}{Z_n}\right) \right)$$

where

$$f(t) = \begin{cases} \sqrt[3]{t} & \text{if } t > \delta^3 \\ \frac{t}{3\delta^2} + \frac{4}{29} & \text{otherwise} \end{cases}$$
$$\delta = \frac{6}{29}$$

X_n , Y_n and Z_n are the CIEXYZ coordinates of the reference white point



CIELAB Gives a Recommended Color Difference Metric

Other color spaces we looked at (RGB, CIEXYZ, HSV) are not perceptually uniform and are not recommended for color difference calculations

- E.g. a pair of colors that look similar to a human observer may have R,G,B coordinates further apart than another pair of colors that look quite different
- Try converting colors to CIELAB coordinates for applications that need to quantify differences in color appearance

Distance between (L^*, a^*, b^*) coordinates for two colors is a recommended color difference metric that is approximately perceptually uniform

$$\Delta E_{ab}^* = \sqrt{(L_2^* - L_1^*)^2 + (a_2^* - a_1^*)^2 + (b_2^* - b_1^*)^2}$$

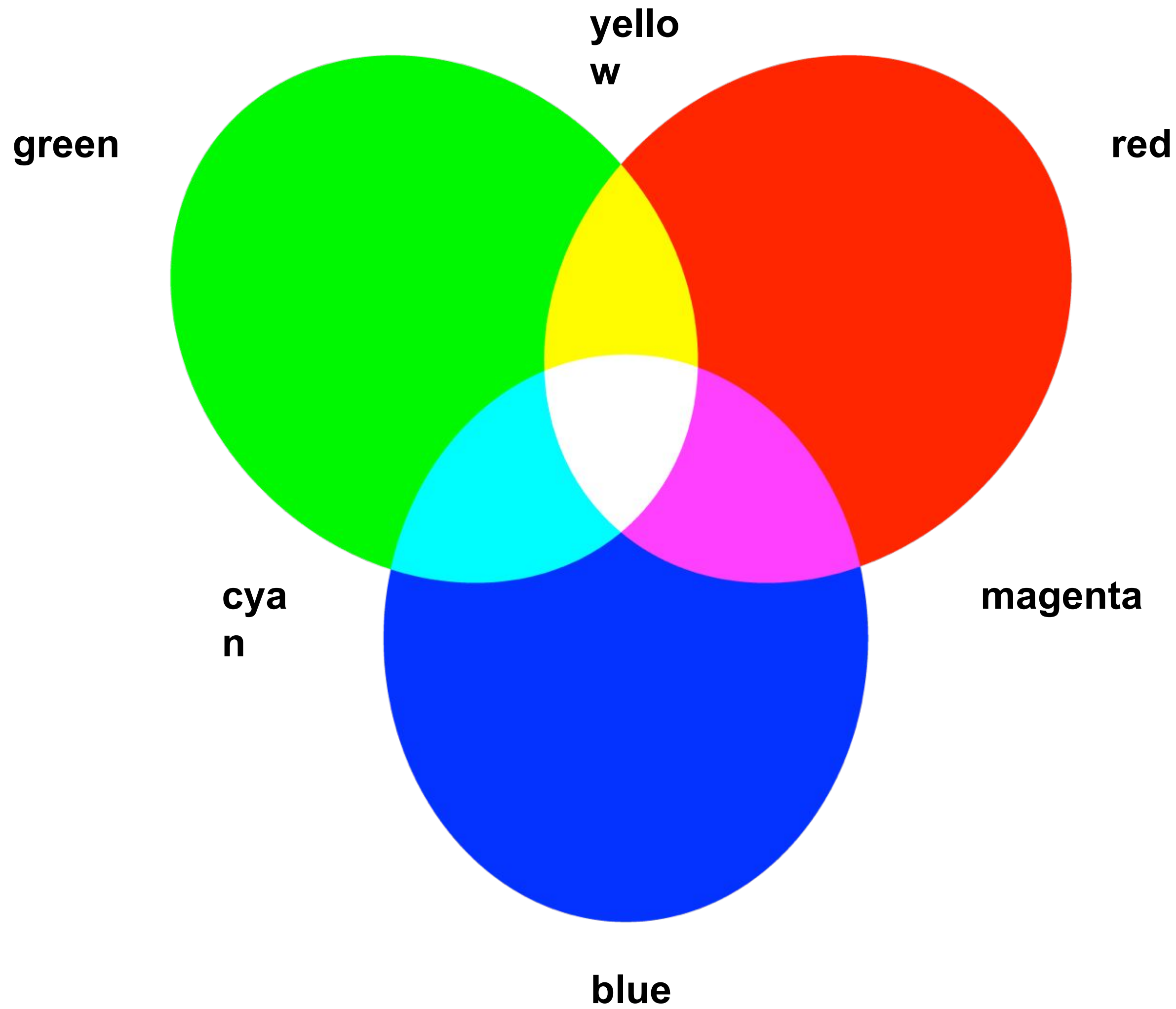
- Caveat: ΔE_{ab}^* is not perfect (e.g. large differences, and differences between highly saturated colors are inaccurate). CIEDE2000 is a more complex/accurate metric based on color appearance models

Additive vs Subtractive Color

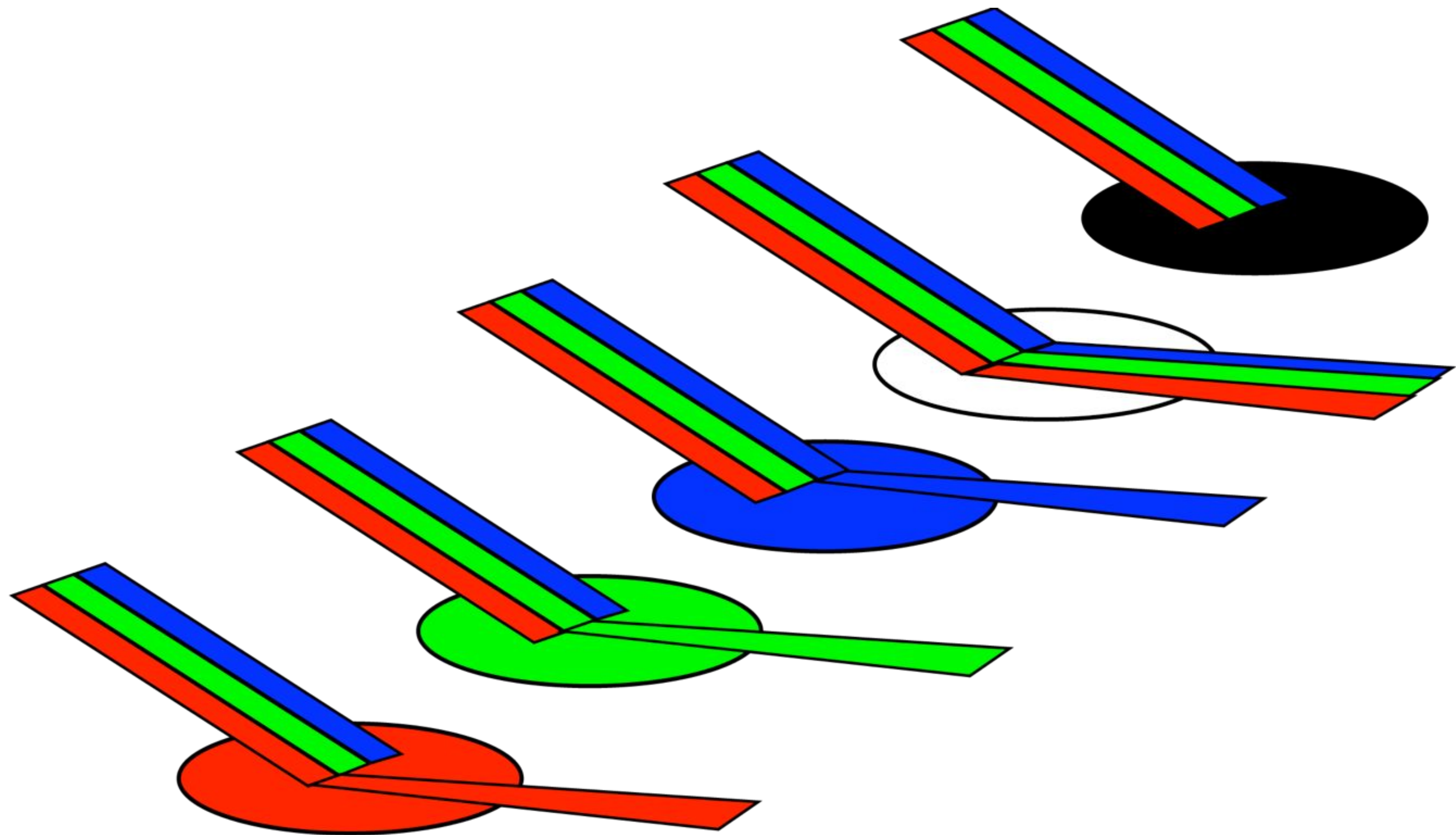
or

Beam Colors vs Object Colors

Additive Color

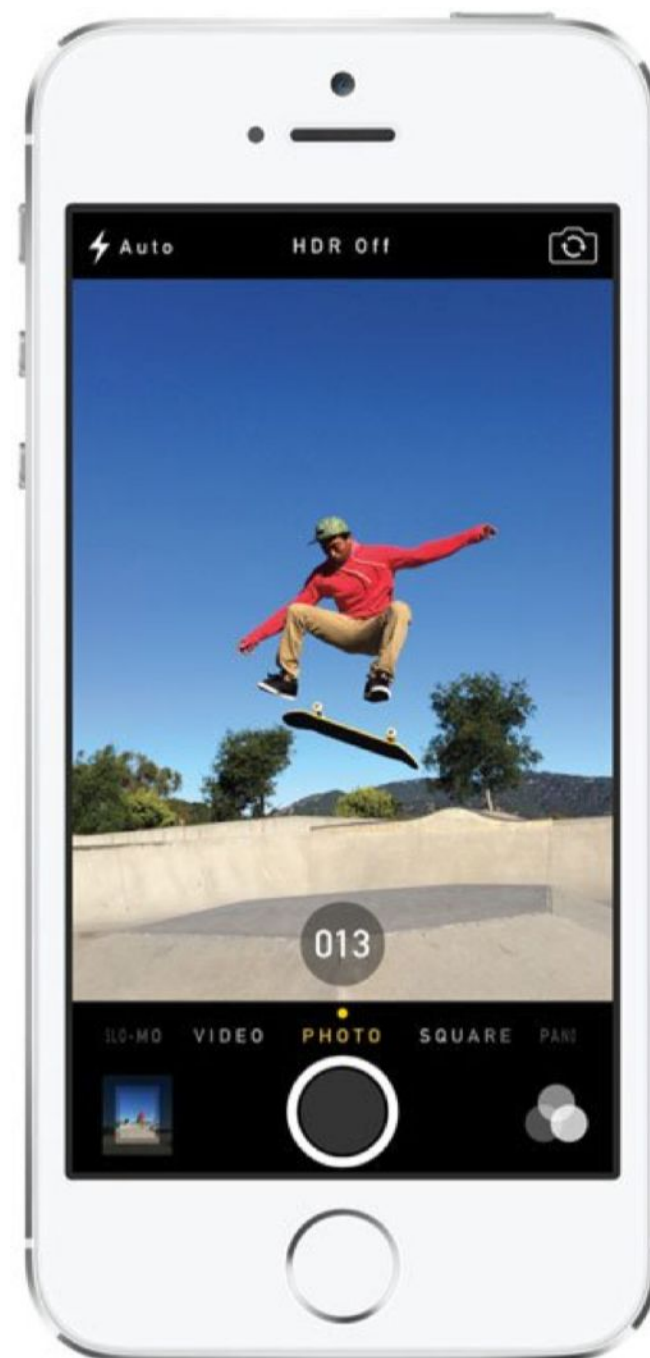
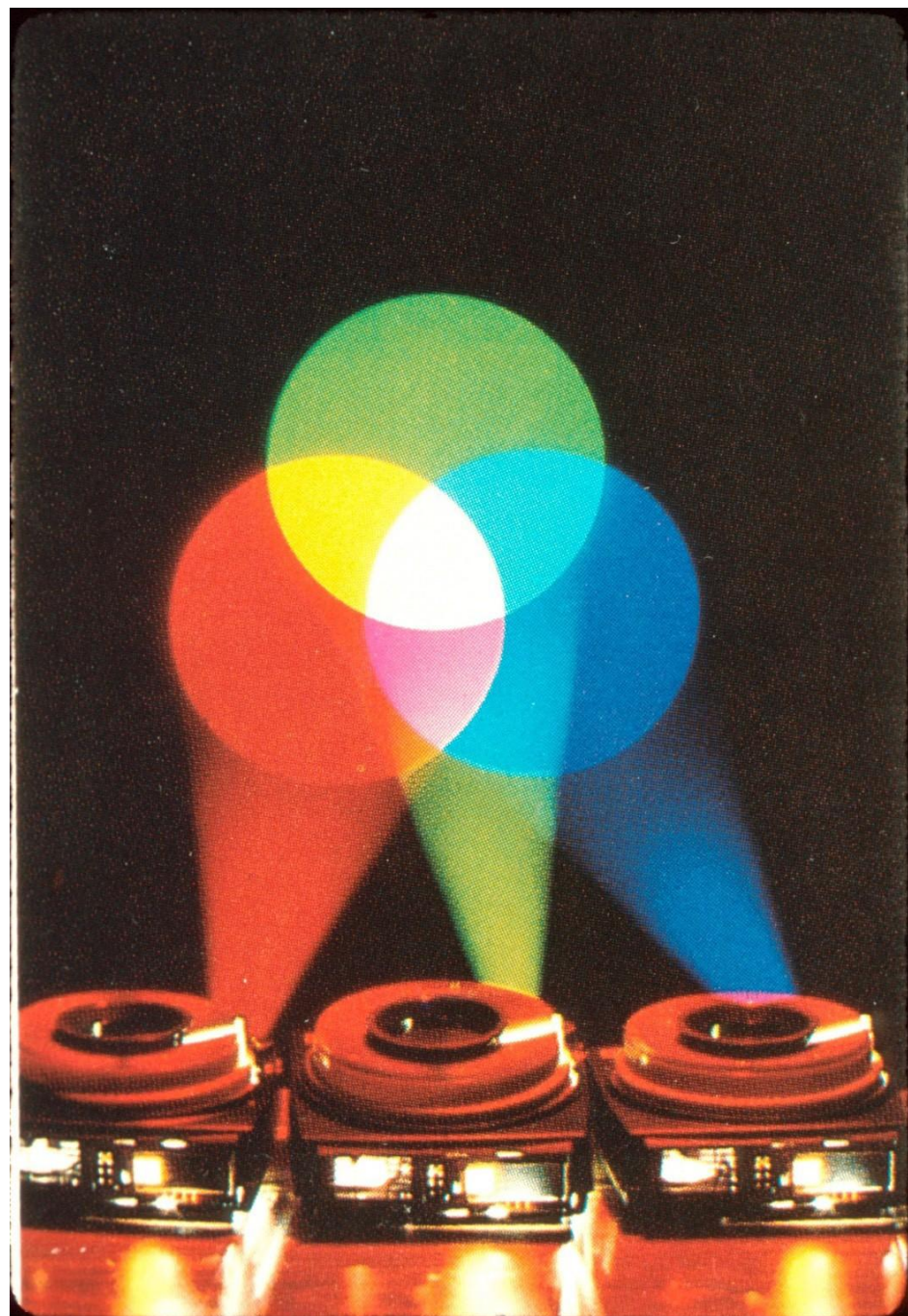


Subtractive (Actually Multiplicative) Color



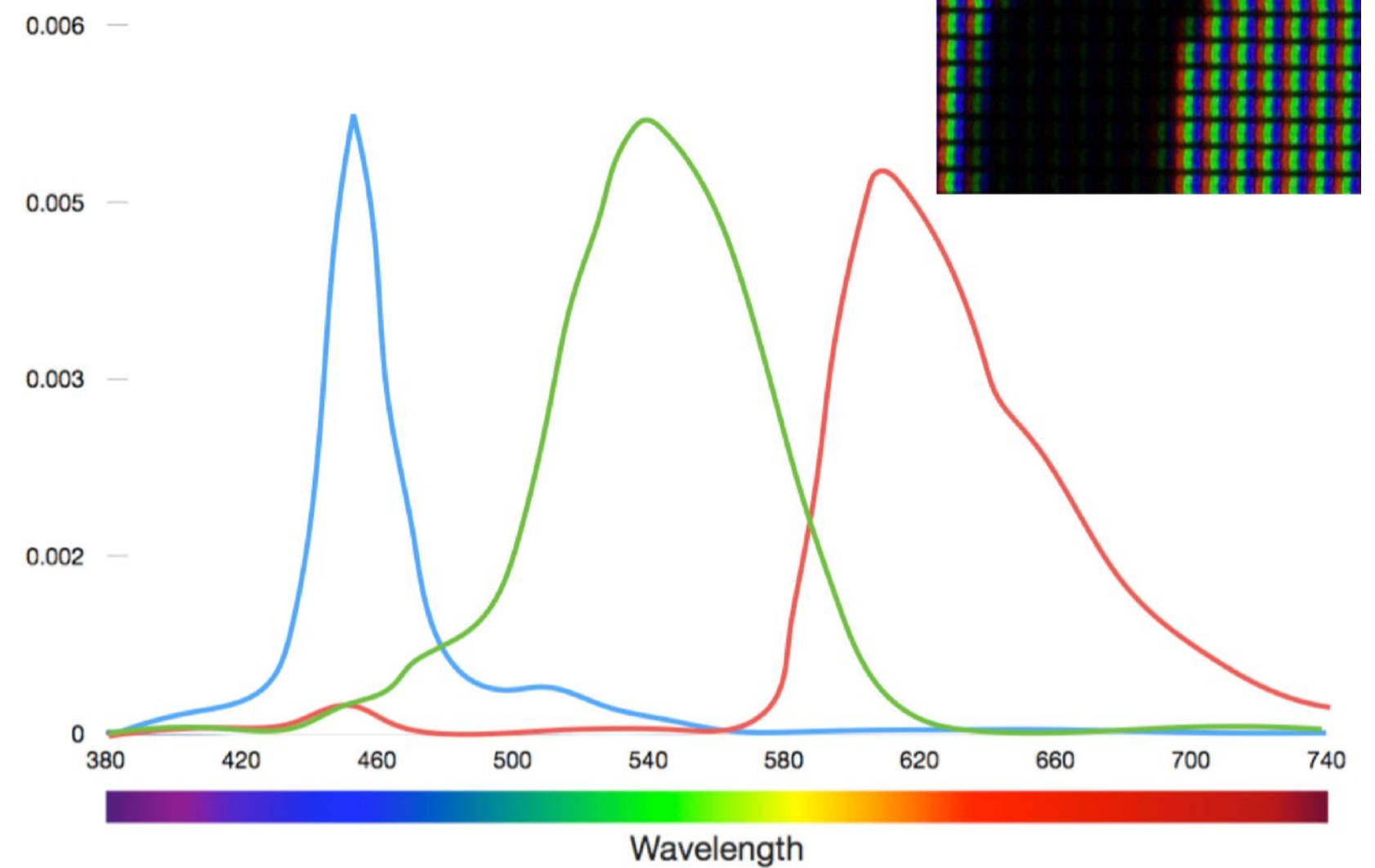
Shining white light on various colored pigments

Beam Colors and Additive Color



RGB pixel spectra (iPhone 5)

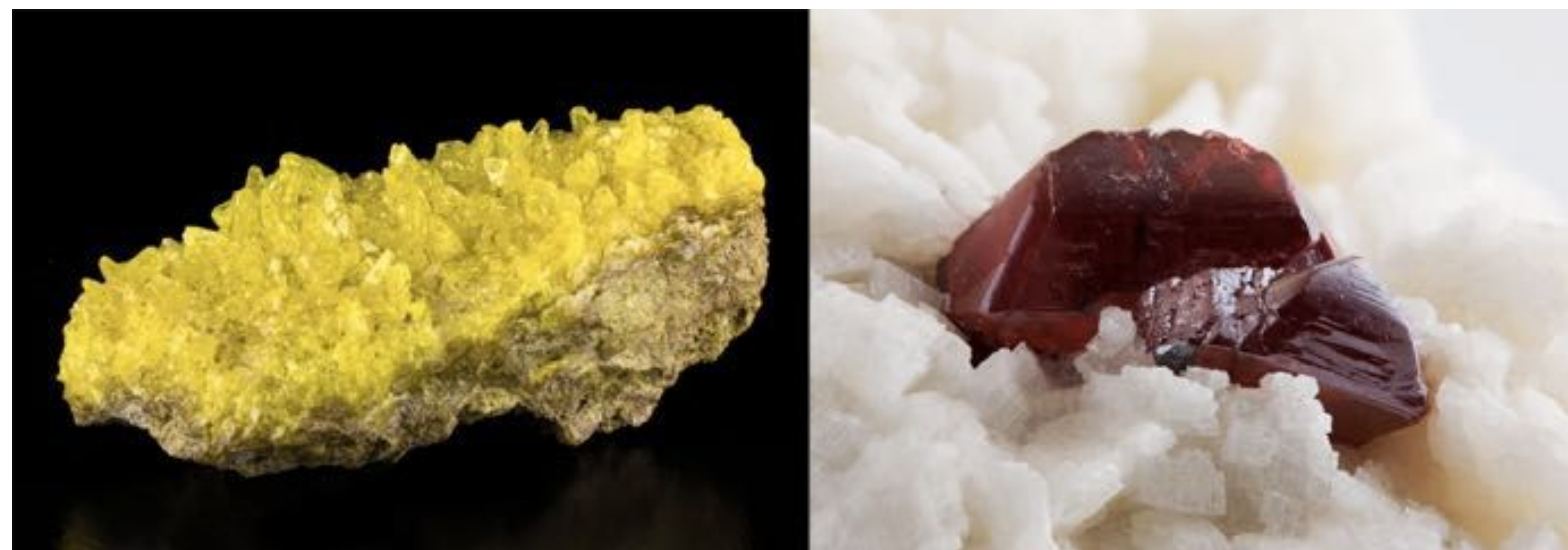
Credit: Yurek, <https://dot-color.com/tag/color-2/page/2/>



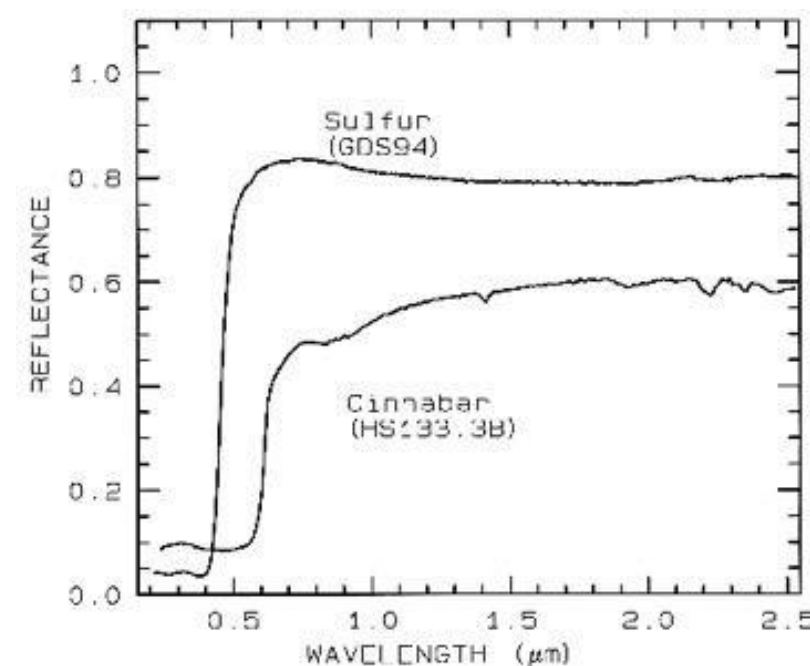
Object Colors - Multiplicative Color



The “Seven Sisters”, Sussex. Such white chalk cliffs are the primordial objects.



Sulphur crystals (the element, bright yellow) and cinnabar (a deep red mer- cury(II) sulphide) on Dolomite.



Reflection (range 0–100%) spectra of sulphur and cinnabar. The wavelength range involves the infrared, the visual range is about 0.4– 0.75μm. Notice that these spectra are roughly of an all-or-none type. There are no signs of anything special at some “yellow or red wavelength” as many naive persons are wont to think.

Things to Remember

Physics of Light

- Spectral power distribution (SPD)
- Superposition
(linearity) Tristimulus
theory of color
- Spectral response of human cone cells (S, M, L)
- Metamers - different SPDs with the same perceived color
- Color reproduction mathematics
- Color matching experiment, per-wavelength matching
functions Color spaces

Acknowledgments

Many thanks and credit for slides to Steve Marschner, Kayvon Fatahalian, Brian Wandell, Marc Levoy, Katherine Breeden, Austin Roorda, James O'Brien, Maureen Stone, Atsunobu Kotani.

Credit to

Michael S. Brown, "Understanding the In-Camera Image Processing Pipeline for Computer Vision", IEEE Computer Vision and Pattern Recognition - Tutorial, June 26, 2016.

Mark D. Fairchild, "Color appearance, color order, & other color systems," ISCC-AIC Munsell Centennial Color Symposium, Boston (2018).

calvin and hobbes

by WATSON

WOW, HONEY, YOU'RE MISSING A BEAUTIFUL SUNSET OUT HERE!



I'LL COUNT TO 10, AND THEN...
POW!



DAD, HOW COME OLD PHOTOGRAPHS ARE ALWAYS BLACK AND WHITE? DIDN'T THEY HAVE COLOR FILM BACK THEN?



SURE THEY DID. IN FACT, THOSE OLD PHOTOGRAPHS ARE IN COLOR. IT'S JUST THE ~~WORLD~~ WORLD WAS BLACK AND WHITE THEN.



REALLY?

YEP. THE WORLD DIDN'T TURN COLOR UNTIL SOMETIME IN THE 1930s, AND IT WAS PRETTY GRAINY COLOR FOR A WHILE, TOO.



THAT'S REALLY WEIRD.

WELL, TRUTH IS STRANGER THAN FICTION.



BUT THEN WHY ARE OLD PAINTINGS IN COLOR? IF THE WORLD WAS BLACK AND WHITE, WOULDN'T ARTISTS HAVE PAINTED IT THAT WAY?

NOT NECESSARILY. A LOT OF GREAT ARTISTS WERE INSANE.



BUT...BUT HOW COULD THEY HAVE PAINTED IN COLOR ANYWAY? WOULDN'T THEIR PAINTS HAVE BEEN SHADES OF GRAY BACK THEN?

OF COURSE, BUT THEY TURNED COLORS LIKE EVERYTHING ELSE DID IN THE '30s.



SO WHY DIDN'T OLD BLACK AND WHITE PHOTOS TURN COLOR TOO?

BECAUSE THEY WERE COLOR PICTURES OF BLACK AND WHITE. REMEMBER?



THE WORLD IS A COMPLICATED PLACE, HOBBS.

WHenever it seems that way, I take a nap in a tree and wait for dinner.

